Assume selt water weighs 10 kilonewtons per cubic meter.

A cylindrical tank with a radius of 3 m and a height of 10 m holds 8 m of salt water. Show that the work required to pump out the salt water to the top of the tank is 4320 to N-m (kJ).

$$A = \pi R^{2}$$

$$= 9\pi$$

$$dV = Ady$$

$$= 9\pi dy$$

$$dF = \rho dV$$

$$= 10 dV$$

$$= 90\pi dy$$

$$dW = h dF$$

$$= (10-y) dF$$

$$= 90\pi (10-y) dy$$

$$9W = \int_{8}^{8} dW$$

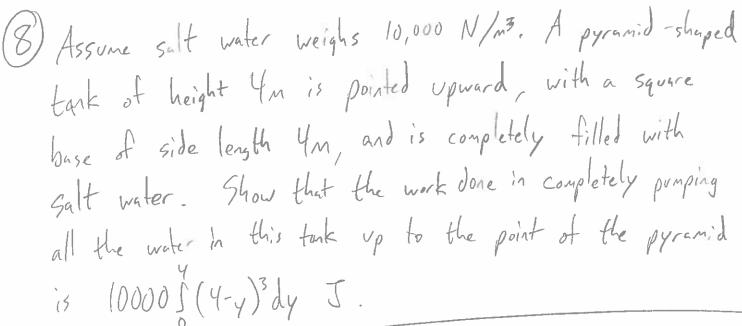
$$= 90\pi \int_{0}^{8} (10-y) dy$$

$$= 90\pi \left[ 10y - \frac{1}{2}y^{2} \right]_{0}^{8}$$

$$= 90\pi \left[ 80 - 32 \right]$$

$$= 40\pi \left( 48 \right)$$

$$= 4320\pi$$





$$A = s^{2}$$

$$= (4-y)^{2}$$

$$dV = Ady$$

$$= (4-y)^{2} dy$$

$$dF = \rho dV$$

$$= (0000 (4-y)^{2} dy$$

$$dW = h dF$$

$$= 10000 (4-y)^{3} dy$$

$$W = \int_{y=a}^{y=b} dW$$

$$= 10000 \int_{0}^{y} (4-y)^{3} dy$$

$$= 10000 \int_{0}^{y} u^{3} du$$

$$= 10000 \int_{0}^{y} u^{3} du$$

$$= 10000 \int_{0}^{y} u^{4} du$$

$$= 10000 \int_{0}^{y} u^{4} du$$

$$= 10000 \int_{0}^{y} u^{4} du$$

Assure that a cubic inch of Juicy Juice meighs

Doz. Suppose a perfectly spherical coconut-shaped cup

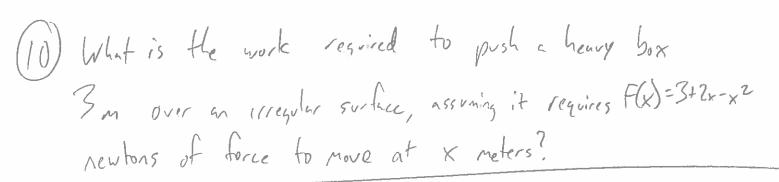
With radius R inches is completely filled with Juicy

Juice Th. Show that drinking the entire beverage using
a straw which extends S inches above the top of

the container requires 43 DTR R3 (R+S)

in-oz of work.

 $\frac{1}{R} = \frac{1}{R} = \frac{1}$  $=\pi\left(R^2-y^2\right)$  $dV = \pi \left(R^2 - y^2\right) dy$  $dF = D_{\pi}(R^2 - y^2) dy$  $W = D_{\pi} \int_{0}^{R} \left( R^{3} + R^{2} S - R^{2} y - R y^{2} - S y^{2} + y^{3} \right) dy$  $dW = D_{\pi}(R^2 - y^2)(R+5-y)dy$  $= D_{\pi} \left[ R^{3} y + R^{2} S_{y} - \frac{1}{2} R^{2} y^{2} - \frac{1}{3} R y^{3} - \frac{1}{3} S_{y}^{3} + \frac{1}{4} y^{3} \right]_{R} - W = \int_{-R}^{\infty} D_{\pi} \left( R^{2} - y^{2} \right) \left( R^{4} S - y \right) dy$  $=2D_{\pi}\left(R^{3}y+R^{2}S_{y}-\frac{1}{3}R_{y}^{3}-\frac{1}{3}S_{y}^{3}\right)$ =20-[R4+R35-3R4-35R3] = 4/3 DTR3 (R+S) []



$$W = \int_{0}^{3} F(x)dx = \int_{0}^{3} (3+2x-x^{2})dx = \left[3x+x^{2}-\frac{1}{3}x^{3}\right]_{0}^{3}$$

$$= \left[9+9-9\right] - \left[0+0-0\right] = \left[9\right] N-m \text{ or } J$$

11) What integral gives the work in ft-lbs required to pull up a hanging 30-16 15-ft chain?

$$F(x) = 2\frac{80 \text{ lbs}}{4} (15 - x \text{ ft})$$

$$= 30 - 2x \text{ lbs}$$

What integral gives the work in kN-m required to pump out all saltwater to the top of a cubical tank with sile length 4m, if it is initially balf-full? Assume that salt water weighs 10 kN per cubic meter.

A = (4)2 dV = Ady = 16dydF=pdV=10(16dy) =160 dy dw = hdF = (4-y)(160 dy) = 160(4-y)dyW= 5/160(4-4)dy