## MA 126 — Spring 2017 — Prof. Clontz — Readiness Quizzes

- Which of these is a definition of  $a^x$  for all positive numbers a and all real numbers x? (2017-01-11, 1.1, practice)
  - A.  $\ln(x \cdot e^a)$
  - B. a multiplied by itself x times
  - C. the unique function for which  $\frac{d}{dx}[a^x] = a^x$
  - D.  $\exp(x \ln a)$
- Which of these statements is false? (2017-01-11, 1.1, practice)
  - A.  $\ln(abc) = \ln(a) + \ln(b) + \ln(c)$
  - B.  $\frac{d}{dx}[\ln x] = \frac{1}{|x|}$  for all nonzero numbers x
  - C.  $y = \exp(x)$  if and only if  $x = \ln(y)$
  - D.  $e^x = \exp(x)$

- 1. The Substitution Rule is the opposite of which derivative rule? (2017-01-19, 2.1)
  - A. Chain Rule
  - B. Product Rule
  - C. Quotient Rule
  - D. Power Rule
- 2. What is incorrect about the following attempt at using the Substitution Rule?

$$\int_0^1 (3-2x)^5 dx = \int_0^1 u^5 \left(-\frac{1}{2}du\right)$$

(2017-01-19, 2.1)

- A. dx should have been replaced with  $+\frac{1}{2} du$ .
- B. u shouldn't be raised to the 5th power.
- C. dx should have been replaced with -2 du.
- D. The bounds are incorrect.

3. Which of these formulas would be most useful in finding  $\int \sin^4 \theta \cos^2 \theta \, d\theta$ ? (2017-01-25, 2.2)

A. 
$$\sin^2(\theta) = \frac{1}{2} + \frac{1}{2}\sin(2\theta)$$

B. 
$$\cos^2(\theta) = \frac{1}{2} + \frac{1}{2}\cos(2\theta)$$

C. 
$$\cos^2(\theta) = 1 - \sin^2(\theta)$$

D. 
$$\sin^2(\theta) = 1 - \cos^2(\theta)$$

4. Which of these formulas would be most useful in finding  $\int \sec^4(\theta) d\theta$ ? (2017-01-25, 2.2)

A. 
$$\sec^2(\theta) = 1 + \tan^2(\theta)$$

B. 
$$\sec^2(\theta) = 1 - \tan^2(\theta)$$

C. 
$$\tan^2(\theta) = 1 + \sec^2(\theta)$$

D. 
$$\tan^2(\theta) = 1 - \sec^2(\theta)$$

- 5. Which of these substitutions would be most useful in finding  $\int \frac{1}{25x^2+9} dx$ ? (2017-01-27, 2.3)
  - A. Let  $25x^2 + 9 = 25\sec^2\theta + 25$ .
  - B. Let  $25x^2 + 9 = 9\sin^2\theta + 9$ .
  - C. Let  $25x^2 + 9 = 9\tan^2\theta + 9$ .
  - D. Let  $25x^2 + 9 = 25\cos^2\theta + 25$ .
- 6. Which of these substitutions would be most useful in finding  $\int \frac{1}{x\sqrt{4-16x^2}} dx$ ? (2017-01-27, 2.3)
  - A. Let  $4 16x^2 = 16 16\cos^2\theta$ .
  - B. Let  $4 16x^2 = 4 4\sin^2\theta$ .
  - C. Let  $4 16x^2 = 4 + 4\tan^2\theta$ .
  - D. Let  $4 16x^2 = 16 + 16\sec^2\theta$ .
- 7. Which of these substitutions would be most useful in finding  $\int_3^5 \frac{1}{\sqrt{x^2-9}} dx$ ? (2017-01-27, 2.3)
  - A. Let  $x^2 9 = 9\sin^2\theta + 9$ .
  - B. Let  $x^2 9 = \tan^2 \theta 1$ .
  - C. Let  $x^2 9 = \cos^2 \theta + 1$ .
  - D. Let  $x^2 9 = 9\sec^2\theta 9$ .

8. Which of these sums is the first step in expanding  $\frac{4x^2+16x+17}{(x+2)^2(x^2+1)^2}$  into partial fractions? (2017-02-01, 2.4)

A. 
$$\frac{A}{x+2} + \frac{Bx}{x+2} + \frac{C}{(x^2+1)^2}$$

B. 
$$\frac{A}{x+2} + \frac{Bx}{(x+2)^2} + \frac{Cx+D}{(x^2+1)^2}$$

C. 
$$\frac{A}{x+2} + \frac{B}{(x+2)^2} + \frac{Cx+D}{x^2+1} + \frac{Ex+F}{(x^2+1)^2}$$

D. 
$$\frac{Ax+B}{(x+2)^2} + \frac{Cx+D}{(x^2+1)^2}$$

- 9. Why must  $\frac{3+5x^5}{(x+1)(x+3)^2}$  first be simplifed using long polynomial division before using the method of partial fractions? (2017-02-01, 2.4)
  - A. It is a rational function of x.
  - B. The degree of its numerator is odd, while the degree of its demoninator is even.
  - C. The degree of its numerator is greater than or equal to the degree of its denominator.
  - D. It is an irrational function of x.

- 10. Which of these techniques is most appropriate as the first step to find  $\int z^2 \sin(z^3) dz$ ? (2017-02-09, 2.6)
  - A. Integration by Substitution
  - B. Integration by Parts
  - C. Method of Partial Fractions
  - D. Trigonometric Identities
- 11. Which of these techniques is most appropriate as the first step to find  $\int \frac{t^2+3t+1}{t^3+t} dt$ ? (2017-02-09, 2.6)
  - A. Method of Partial Fractions
  - B. Trigonometric Substitution
  - C. Trigonometric Identities
  - D. Integration by Substitution

- 12. Which of these integrals represents the area bounded by the curves  $x=y^2$  and x=4? (2017-02-13, 3.1)
  - A.  $\int_0^4 ((\sqrt{x}) (-\sqrt{x})) dx$
  - B.  $\int_0^2 ((x^2) (4)) dx$
  - C.  $\int_2^4 ((x^2) (-x^2)) dx$
  - D.  $\int_{2}^{0} ((x^{2}) (\sqrt{x})) dx$

Answer the following questions about the solid of revolution obtained by rotating the triangle with vertices (1, 1), (2, 2), (2, 3) around the line y = -1.

- 13. Which of these curves should be used to find the outer radius R(x)? (2017-02-16, 3.3)
  - A.  $y = \frac{1}{2}x$
  - B. y = 2x 1
  - C. y = -2x + 2
  - D.  $y = -\frac{1}{2}x + 1$
- 14. What formula should be used for R(x)? (2017-02-16, 3.3)
  - A. R(x) = 2x
  - B. R(x) = 1 2x
  - C.  $R(x) = 2 \frac{1}{2}x$
  - D.  $R(x) = \frac{1}{2}x 1$
- 15. What are the correct bounds for the washer method integral? (2017-02-16, 3.3)
  - A.  $\pi \int_{-1}^{3} ([R(x)]^2 [r(x)]^2) dx$
  - B.  $\pi \int_2^3 ([R(x)]^2 [r(x)]^2) dx$
  - C.  $\pi \int_{1}^{2} ([R(x)]^{2} [r(x)]^{2}) dx$
  - D.  $\pi \int_0^2 ([R(x)]^2 [r(x)]^2) dx$

- 16. In the work integral  $\int_a^b F(x) dx$ , the function F(x) represents... (2017-02-24, 3.5)
  - A. Friction
  - B. Speed
  - C. Force
  - D. Mass
- 17. When computing the work done in pumping water out of a container, the video suggests using which formula?  $(2017-02-24,\ 3.5)$ 
  - A.  $\int_{y=c}^{y=d} dW$
  - B.  $\int_a^b F(x) dx$
  - C.  $\int_a^b \frac{W(x)}{x} dx$
  - D.  $\int_{y=c}^{y=d} y F(y) \, dy$