

MATH 2242-090 — Spring 2016 — Dr. Clontz — Quiz 4
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Name: Solomon

- Each quiz question is labeled with its worth toward your total quiz grade for the semester.
- On multiple choice problems, you do not need to show your work. No partial credit will be given.
- On full response problems, show all of your work and give a complete solution. When in doubt, don't skip any steps. Partial credit will be given at the discretion of the professor.
- This quiz is open notes and open book.
- This quiz is due at the end of class. Quizzes submitted over one minute late will be penalized by 50%.

1. (10 points) Give an approximate value of  $f(1.1, -2.1)$  given the following information about  $f$ :

$$f(1, -2) = 3 \quad \frac{\partial f}{\partial x}(1, -2) = 1 \quad \frac{\partial f}{\partial y}(1, -2) = -2$$

$$\frac{\partial^2 f}{\partial x^2}(1, -2) = 0 \quad \frac{\partial^2 f}{\partial y^2}(1, -2) = 3 \quad \frac{\partial^2 f}{\partial x \partial y}(1, -2) = 1$$

$$\begin{aligned} f(1.1, -2.1) &\approx f(1, -2) + \frac{\partial f}{\partial x}(1, -2)(1.1 - 1) \\ &\quad + \frac{\partial f}{\partial y}(1, -2)(-2.1 - 2) + \frac{1}{2} \frac{\partial^2 f}{\partial x^2}(1, -2)(1.1 - 1)^2 \\ &\quad + \frac{1}{2} \frac{\partial^2 f}{\partial y^2}(1, -2)(-2.1 - 2)^2 + \frac{\partial^2 f}{\partial x \partial y}(1, -2)(1.1 - 1)(-2.1 - 2) \\ &= 3 + 1(0.1) + (-2)(-0.1) + \frac{1}{2}(0)(0.1)^2 \\ &\quad + \frac{1}{2}(3)(-0.1)^2 + 1(0.1)(-0.1) \\ &= 3 + 0.1 + 0.2 + 0.015 - 0.01 \\ &= \boxed{3.305} \end{aligned}$$