

MATH 2242-090 — Spring 2016 — Dr. Clontz — Quiz 11
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Name: Solutions

- Each quiz question is labeled with its worth toward your total quiz grade for the semester.
- On multiple choice problems, you do not need to show your work. No partial credit will be given.
- On full response problems, show all of your work and give a complete solution. When in doubt, don't skip any steps. Partial credit will be given at the discretion of the professor.
- This quiz is open notes and open book.
- This quiz is due at the end of class. Quizzes submitted over one minute late will be penalized by 50%.

1. (10 points) Evaluate $\int_C 3xy^2 dx + xy dy$ where C is the counter-clockwise oriented boundary of the rectangle $[0, 2] \times [1, 3]$. (Hint: Partial credit will not be given if you attempt to evaluate this directly; try to use a technique from Chapter 8.)

$$\begin{aligned}
 &= \iint_{R} \left(\frac{\partial F_2}{\partial x} - \frac{\partial F_1}{\partial y} \right) dx dy \\
 &= \iint_{R} y - 6xy \, dx dy \\
 &= \int_1^3 \left[xy - 3x^2 y \right]_0^2 dy \\
 &= \int_1^3 -10y \, dy \\
 &= \left[-5y^2 \right]_1^3 = \boxed{-40}
 \end{aligned}$$

2. (10 points) Evaluate $\int_C (3x+y, 4y+x) \cdot ds$ where C is parameterized by $\mathbf{r}(t) = (2^t, \sin(\pi t))$ for $0 \leq t \leq 1$. (Hint: Partial credit will not be given if you attempt to evaluate this directly; try to use a technique from Chapter 8.)

$$\begin{aligned}
 f_x &= 3+y & f_y &= 4y+x \\
 f &= 3x+xy+C & f &= 2y^2+xy+C
 \end{aligned}$$

$$f = 3x + xy + 2y^2$$

$$\begin{aligned}
 &= \left[3x + xy + 2y^2 \right]_{C(0)}^{C(1)} \\
 &= \left[3x + xy + 2y^2 \right]_{(1,0)}^{(2,0)} \\
 &= (6+0+0) - (3+0+0) = \boxed{3}
 \end{aligned}$$