Modelling structured trial-by-trial variability in evidence accumulation

Steven Miletić et al.

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Introduction

In this tutorial, we will demonstrate how to design dynamic evidence accumulation models and fit them to data using hierarchical Bayesian methods. We will utilize the *EMC2* package, assuming some prior knowledge of its functionalities (for reference, see the *EMC2* tutorial). Specifically, we will fit models to dataset 1 from Miletic et al. (2025), which corresponds to the 'choice, short [CS]' condition from Wagenmakers et al. (2004). In this experiment, participants were presented with a single digit and required to determine whether the digit was even or odd.

First, let's load the required packages and data:

```
rm(list = ls())
# TMP -- install the right branch
# remotes::install_github("ampl-psych/EMC2@RL", dependencies=TRUE, Ncpus=8);.rs.restartR()
# END TMP
library(EMC2)
set.seed(1) # for reproducability

# This is some code that contains plotting functions used later on in this tutorial
source('./plotting_utils.R')

# Load in the data
load("datasets/dataset_1.RData")

# Inspect the data
print(head(dat))
```

```
    subjects
    S
    R
    rt

    1
    1
    even even 0.542

    2
    1
    even even 0.426

    3
    1
    even even 0.501

    4
    1
    even even 0.403

    5
    1
    odd odd 0.497

    6
    1
    even even 0.518
```

Here, subjects refers to subject number, S to the presented stimulus (even/odd), R the response (even/odd), and rt the response time in seconds.

Baseline models

We begin by setting up the 'static' baseline models without structured trial-by-trial variability. For a comprehensive tutorial on specifying designs in *EMC2*, please refer to the *EMC2* tutorial [ref]. We will set up two baseline models: first using a racing diffusion model (RDM), and then using a diffusion decision model (DDM). In the RDM, we model drift rates with a mean-difference parametrization. The mapped_pars() function is useful for tracking how parameter vectors are mapped onto each design cell:

```
Sampled Parameters:
[1] "B"
            "v"
                     "v_1Md" "t0"
Design Matrices:
$B
В
1
$v
    1M v v_1Md
 TRUE 1 0.5
FALSE 1 -0.5
$t0
t0
 1
$A
Α
 1
$s
 s
 1
```

mapped_pars(design_RDM)

```
$v
    1M
TRUE : exp(v + 0.5 * v_1Md)
FALSE : exp(v - 0.5 * v_1Md)
```

In the DDM, we need to remember to flip the sign of the drift rate for one of the two stimulus types (in this case, even):

```
Smat <- matrix(c(-1,1), nrow = 2,dimnames=list(NULL,"dif"))</pre>
design_DDM <- design(model=DDM,</pre>
                  data=dat,
                  contrasts=list(S=Smat),
                  formula=list(Z ~ 1, v ~ S, a~1, t0 ~ 1))
Sampled Parameters:
[1] "Z"
             "v"
                      "v_Sdif" "a"
                                         "t0"
Design Matrices:
$Z
Z
1
$v
    S v v_Sdif
even 1 -1
           1
 odd 1
$a
a
 1
$t0
t0
 1
$s
 s
1
$st0
st0
   1
$sv
 sv
 1
$SZ
SZ
 1
mapped_pars(design_DDM)
$v
 S
```

even : v - v_Sdif
odd : v + v_Sdif

Trend specification

Both the descriptive trends and the formal mechanisms of dynamics work through trend objects in *EMC2*. In this object, you specify (1) the covariate of interest (e.g., time on task), (2) a kernel to apply to the covariate (e.g., linear, power, exponential, polynomial, or delta rule), and (3) which decision parameter is informed by the resulting covariate, and (4) the functional form of the mapping between the resulting covariate and the decision parameters, referred to as the 'base'. The trend_help() function gives an overview of the options:

trend_help()

```
Available kernels:
  lin_decr: Decreasing linear kernel: k = -c
  lin_incr: Increasing linear kernel: k = c
  exp_decr: Decreasing exponential kernel: k = exp(-d_ed * c)
  exp_incr: Increasing exponential kernel: k = 1 - exp(-d_ei * c)
  pow_decr: Decreasing power kernel: k = (1 + c)^(-d_pd)
  pow_incr: Increasing power kernel: k = 1 - (1 + c)^(-d_pi)
  poly2: Quadratic polynomial: k = d1 * c + d2 * c^2
  poly3: Cubic polynomial: k = d1 * c + d2 * c^2 + d3 * c^3
  poly4: Quartic polynomial: k = d1 * c + d2 * c^2 + d3 * c^3 + d4 * c^4
  delta: Standard delta rule kernel: k = q[i].
         Updates q[i] = q[i-1] + alpha * (c[i-1] - q[i-1]).
         Parameters: q0 (initial value), alpha (learning rate).
  delta2: Dual kernel delta rule: k = q[i].
          Combines fast and slow learning rates
          and switches between them based on dSwitch.
          Parameters: q0 (initial value), alphaFast (fast learning rate),
          propSlow (alphaSlow = propSlow * alphaFast), dSwitch (switch threshold).
  deltab: Threshold learning delta rule kernel: k = q_[FM,i].
          Updates q[i] = q[i-1] + alpha * (B[i]/c[i-1] - q[i-1]).
          Parameters: q0 (initial value), alpha (learning rate).
Available base types:
  lin: Linear base: parameter + w * k
  exp_lin: Exponential linear base: exp(parameter) + exp(w) * k
  centered: Centered mapping: parameter + w*(k - 0.5)
  add: Additive base: parameter + k
  identity: Identity base: k
Trend options:
  premap: Trend is applied before parameter mapping. This means the trend parameters
          are mapped first, then used to transform cognitive model parameters before
          their mapping.
  pretransform: Trend is applied after parameter mapping but before transformations.
                Cognitive model parameters are mapped first, then trend is applied,
                followed by transformations.
  posttransform: Trend is applied after both mapping and transformations.
                 Cognitive model parameters are mapped and transformed first,
                 then trend is applied.
```

The last section, 'trend options', warrants some extra attention. In EMC2, the user can define parameters using model formula language, as we did above when defining the designs. EMC2 uses these to create a design matrix by mapping the relevant factors to each design cell. In the case of the RDM, once mapped,

in each design cell, only the v, B, t0, s, (and optionally A) parameters per accumulator remain. However, in many applications, the parameter of interest is defined as a between-accumulator difference (e.g., v_1Md in the RDM example above), or a between-condition difference (e.g., the effect of speed-accuracy trade-off cues on thresholds). These parameters only exist pre-mapping, and thus, the trend should be applied prior to mapping by setting premap to TRUE.

There is an important caveat here. By default, *EMC2* estimates parameters with a lower bound (e.g., non-decision time, thresholds, RDM's drift rates) on the log scale, and parameters with both a lower and upper bound on the probit scale. Parameters are *mapped* on the scale on which they are estimated, and *then* transformed. This also implies that if a trend is applied prior to mapping, the resulting parameters might later be transformed, leading to a potentially unwanted non-linear effect of the covariate on the parameter.

Let's clarify with an example. Let's try to impose a linear trend on thresholds in case of the RDM:

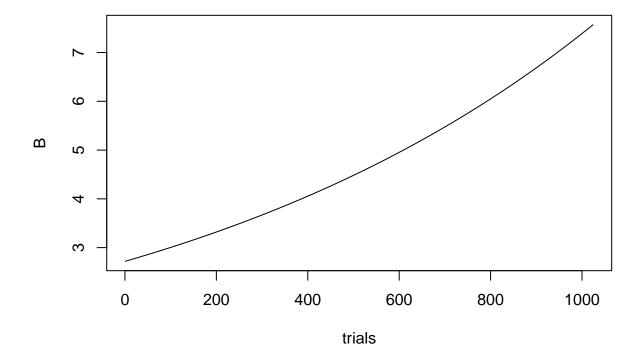
```
# Add a 'trials' column specifying trial number
dat <- EMC2:::add_trials(dat)</pre>
# Rescale the effect of this covariate to a larger parameter range to help sampling
dat$trials2 <- dat$trials/1000</pre>
lin_trend <- make_trend(cov_names='trials2',</pre>
                         kernels = 'lin_incr',
                         par_names='B',
                         bases='lin',
                         premap=TRUE)
design_RDM_lin_B <- design(model=RDM,</pre>
                          contrast=list(lM=ADmat),
                          covariates='trials2',
                                                  # specify relevant covariate columns
                          matchfun=function(d) d$S==d$1R,
                          formula=list(B ~ 1, v ~ 1M, t0 ~ 1),
                                                # add trend
                          trend=lin_trend)
```

```
Sampled Parameters:
[1] "B"
            υv။
                     "v 1Md" "t0"
                                      "B.w"
Design Matrices:
$B
В
1
    1M v v_1Md
  TRUE 1 0.5
FALSE 1 -0.5
$t0
 t0
  1
$B.w
B.w
   1
$A
```

```
A
1
$s
s
```

Note that we are now sampling one extra parameter compared to before, B.w, which is the weight of the influence of trial number on thresholds. In $B_t = B_0 + B.w * trial$. Let's define a set of parameters and look at the resulting trial-by-trial thresholds:

Threshold for odd



Clearly, this is not a linear increase. This happens because the threshold is sampled on the log scale, so an exponential transform is applied after mapping the parameter vector to the design cells. Since the linear trend was applied prior to mapping, this linear effect becomes non-linear. mapped_pars() can be used to clarify:

```
mapped_pars(design_RDM_lin_B)
```

```
intercept : exp(B_t)
Trends:
B_t = B + B.w * trials2

$v
     1M
TRUE : exp(v + 0.5 * v_1Md)
FALSE : exp(v - 0.5 * v_1Md)
```

One option to prevent this from happening is to apply the trend after mapping and transformation, as follows:

```
Sampled Parameters:
[1] "B"
            "v"
                    "v_1Md" "t0"
                                     "B.w"
Design Matrices:
$B
В
1
$v
    lM v v_lMd
 TRUE 1 0.5
FALSE 1 -0.5
$t0
t0
  1
$B.w
B.w
   1
$A
 Α
1
$s
 s
 1
```

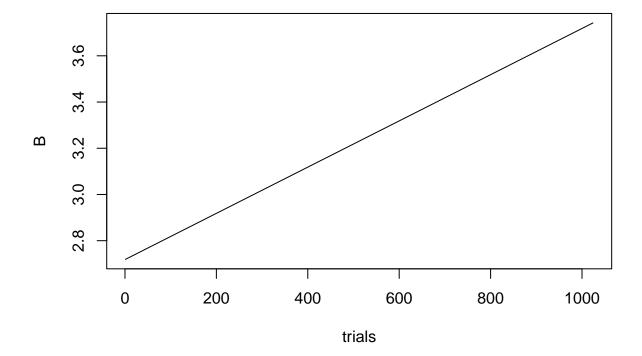
```
# note how the trend is added after the transformation
mapped_pars(design_RDM_lin_B2)
```

\$В

```
intercept : exp(B) + B_t
Trends:
B_t = B.w * trials2

$v
     1M
TRUE : exp(v + 0.5 * v_1Md)
FALSE : exp(v - 0.5 * v_1Md)
```

Threshold for odd

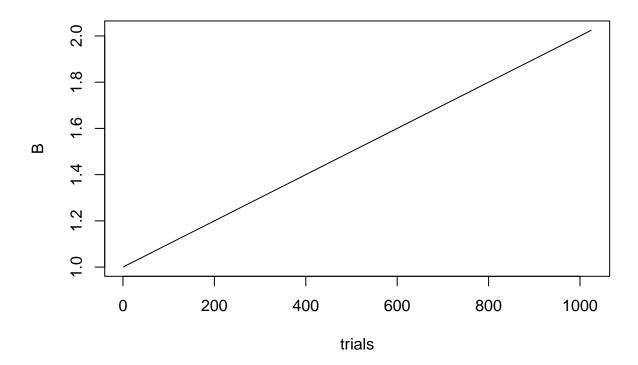


However, posttransform implies postmap, and many parameters of interest are defined only prior to mapping. So applying trends to those premap parameter types is not possible in combination with posttransform. Instead, the user can tell EMC2 to estimate parameters on their natural scales by turning off transformations of the relevant parameters. For example:

```
lin_trend3 <- make_trend(cov_names='trials2',</pre>
                         kernels = 'lin_incr',
                         par_names='B',
                         bases='lin',
                         premap=TRUE) # back to premap
design_RDM_lin_B3 <- design(model=RDM,</pre>
                          data=dat,
                          contrast=list(lM=ADmat),
                          covariates='trials2',
                          matchfun=function(d) d$S==d$lR,
             # here, we tell EMC2 to sample the threshold on the natural scale
                          transform=list(func=c('B'='identity')),
                          formula=list(B ~ 1, v ~ 1M, t0 ~ 1),
                          trend=lin_trend3)
                                               # add trend
Sampled Parameters:
            "v"
                    "v 1Md" "t0"
[1] "B"
                                    "B.w"
Design Matrices:
$В
В
1
$v
    lM v v_lMd
 TRUE 1 0.5
FALSE 1 -0.5
$t0
t0
 1
$B.w
B.w
   1
$A
 Α
1
$s
 s
 1
# note how the transformation is no longer applied at all
mapped_pars(design_RDM_lin_B3)
$B
 intercept : B_t
Trends:
B_t = B + B.w * trials2
```

```
$v
    1M
    TRUE : exp(v + 0.5 * v_1Md)
    FALSE : exp(v - 0.5 * v_1Md)
```

Threshold for odd

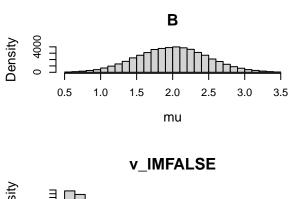


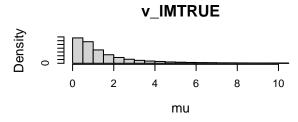
This leads to the expected effect. As a cautionary note, keep in mind that the default priors in EMC2 are Gaussian distributions centered on 0 with unit variance. Since many cognitive model parameters cannot be negative, a N(0,1) prior is poorly chosen for those parameters that do not have support on the real line. For estimation and sampling, this usually has little influence in practice, but it may be important when estimating Bayes Factors.

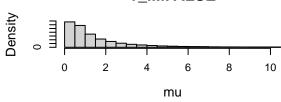
With all that in mind, we can now start sampling our first model. We set a N(2,0.5) prior on the threshold B to reduce the prior density on negative thresholds. This is a somewhat subjective choice based on earlier experience, so it reflects my (but perhaps not your) prior belief. The rest of the priors are left to their default N(0,1) – on the scale on which they are sampled.

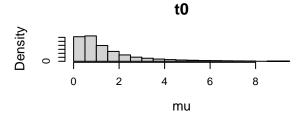
```
prior_linB <- prior(design_RDM_lin_B3, mu_mean=c(B=2, B.w=0), mu_sd=c(B=0.5,B.w=0.1))
emc <- make_emc(dat, design=design_RDM_lin_B3, prior_list = prior_linB)</pre>
```

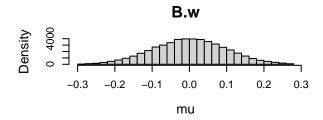
plot(emc, prior=TRUE)











check(emc)

Iterations:

preburn burn adapt sample 1000 [1,] 0 0 0 [2,] 0 0 0 1000 [3,] 0 0 0 1000

mu

 B
 v
 v_1Md
 t0
 B.w

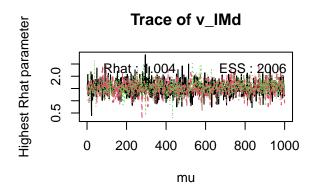
 Rhat
 1.001
 1.002
 1.004
 1.001
 1.001

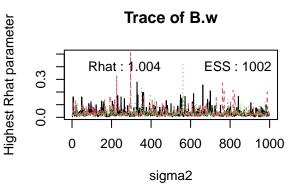
 ESS
 2094.000
 1943.000
 2006.000
 2070.000
 2038.000

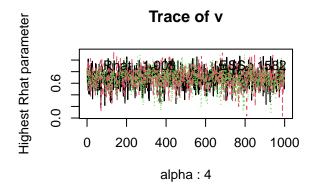
sigma2
B v v_1Md t0 B.w
Rhat 1 1.002 1.002 1 1.004
ESS 2078 1682.000 1657.000 1270 1002.000

alpha highest Rhat : 4
B v v_lMd t0 B.w

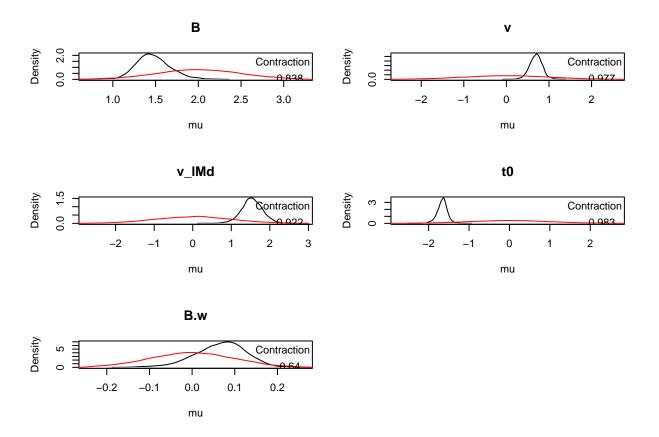
Rhat 1.001 1.008 1.003 1 1.002 ESS 2063.000 1582.000 1570.000 2401 2339.000







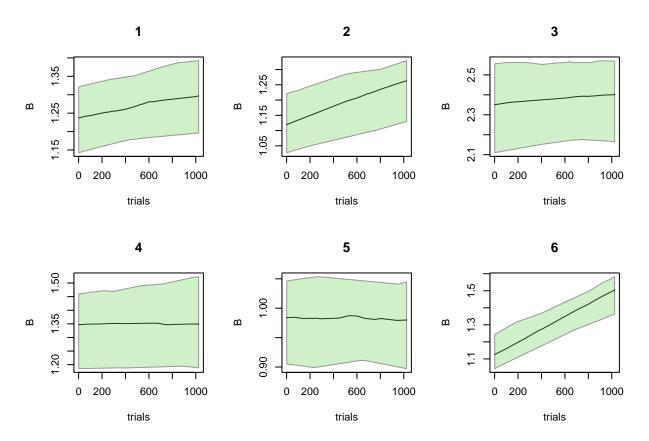
plot_pars(emc)



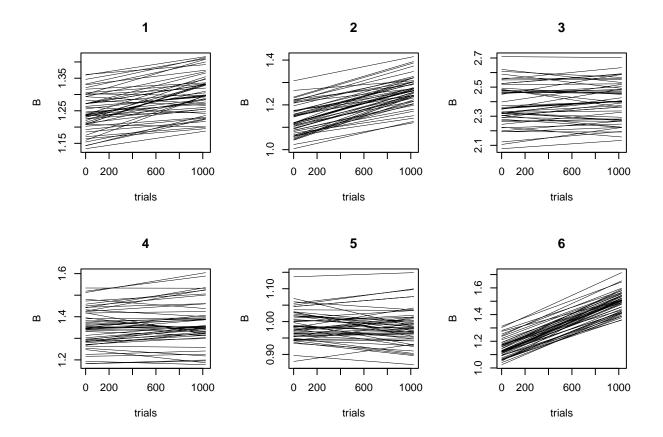
credint(emc)

```
$mu
       2.5%
                50%
                     97.5%
В
       1.122
             1.459
                     1.913
      0.389
             0.696
                    1.001
v_1Md
      0.978 1.536 2.088
      -1.951 -1.656 -1.428
t0
B.w
      -0.062 0.070 0.171
```

On a group-level, we find a small (not credible) positive B.w- on average, in this dataset, thresholds appear to increase by ~ 0.070 over the course of 1000 trials. We can now generate posterior predictives, and while doing that, ask EMC2 to return the mapped and transformed parameters, which will allow us to visualize the fitted thresholds over trials:



Here, the green shaded area indicated the 95% credible interval of the posterior on the threshold for each trial. We can also plot the individual thresholds of each posterior predictive separately as lines:



Exponential and power laws

Practice effects tend to be large initially and then gradually decay. Asymptotic functions like exponential or power functions can be used to model such effects. EMC2 offers increasing and decreasing kernels in both cases. To demonstrate these functional forms:

```
Sampled Parameters:
[1] "B" "v" "v_1Md" "t0" "B.w" "B.d_ei"

Design Matrices:
$B
B
```

```
1
$v
   lM v v_lMd
 TRUE 1 0.5
FALSE 1 -0.5
$t0
t0
 1
$B.w
B.w
  1
$B.d_ei
B.d_ei
     1
$A
Α
1
$s
 s
design_exp_decr <- design(model=RDM,</pre>
                          contrast=list(1M=ADmat),
                          covariates='trials2',
                          matchfun=function(d) d$S==d$1R,
                          transform=list(func=c('B'='identity')),
                          formula=list(B ~ 1, v ~ 1M, t0 ~ 1),
                          trend=trend_exp_decr)
Sampled Parameters:
[1] "B"
            "v"
                      "v_lMd" "t0"
                                    "B.w"
                                                 "B.d_ed"
Design Matrices:
$B
В
1
$v
    lM v v_lMd
 TRUE 1 0.5
FALSE 1 -0.5
$t0
t0
  1
```

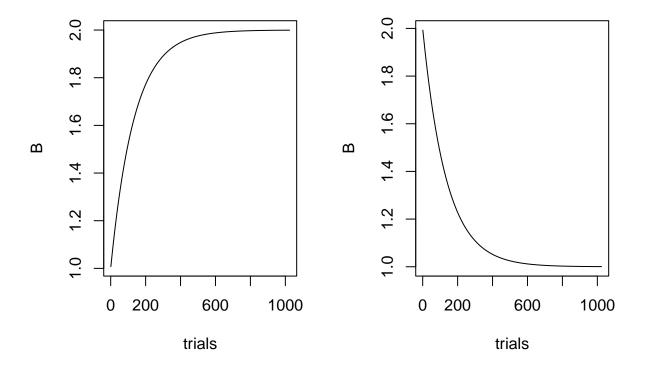
```
B.w
  1
$B.d_ed
B.d_ed
$A
Α
1
$s
 s
 1
emc_incr <- make_emc(dat, design_exp_incr)</pre>
emc_decr <- make_emc(dat, design_exp_decr)</pre>
p_vector_incr <- c('B'=1, 'v'=1, 'v_lMd'=1, 't0'=0.1, 'B.w'=1, 'B.d_ei'=2)</pre>
p_vector_decr <- c('B'=1, 'v'=1, 'v_lMd'=1, 't0'=0.1, 'B.w'=1, 'B.d_ed'=2)</pre>
par(mfrow=c(1,2))
plot_trend(p_vector_incr, emc=emc_incr,
```

par_name='B', subject=1, lR_filter='odd')

par_name='B', subject=1, lR_filter='odd')

plot_trend(p_vector_decr, emc=emc_decr,

\$B.w



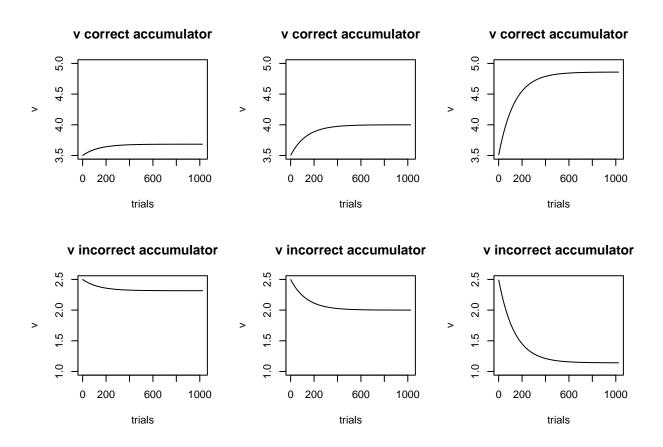
Note that the interpretation of the exponent (B.e_ei or B.e_ed) depends on the direction: In the increasing case, it corresponds to the asymptote; in the decreasing case, to the intercept.

Advanced note: Enforcing a direction

Having both increasing and decreasing kernels may appear redundant, since the direction of the effect can also be flipped by the w parameter in the lin base. However, having both increasing and decreasing kernels facilitates enforcing a directional effect. For example, one might hypothesize that v_lMd increases sharply over the first few trials due to practice effects, and then stabilizes. An increase could be implemented with exp_incr, but if the sampler converges on negative values of w of the base, the resulting trend is actually decreasing rather than increasing.

We can force the sampler to sample only increasing trends by restricting the range of w. This can be done by sampling w on the log-scale, and transforming it to the natural scale. Note that transformations applied to parameters relating to the trends are always applied prior to estimating the trend.

```
Sampled Parameters:
[1] "B"
                               "v_lMd"
                                            "t0"
                                                          "v lMd.w"
[6] "v_lMd.d_ei"
Design Matrices:
В
 1
$v
    lM v v_lMd
 TRUE 1 0.5
FALSE 1 -0.5
$t0
 t0
 1
$v_lMd.w
v_lMd.w
       1
$v_1Md.d_ei
v_lMd.d_ei
          1
$A
 Α
 1
$s
 S
 1
mapped_pars(design_exp_incr)
$v
  lM
TRUE : v + 0.5 * v_1Md_t
FALSE : v - 0.5 * v_1Md_t
 Trends:
 v_1Md_t = v_1Md + exp(v_1Md.w) * (1 - exp(-exp(v_1Md.d_ei) * trials2))
emc_incr <- make_emc(dat, design_exp_incr)</pre>
p_vector1 <- c('B'=1, 'v'=3, 'v_lMd'=1, 't0'=0.1, 'v_lMd.w'=-1, 'v_lMd.d_ei'=2)</pre>
p_vector2 <- c('B'=1, 'v'=3, 'v_lMd'=1, 't0'=0.1, 'v_lMd.w'=0, 'v_lMd.d_ei'=2)</pre>
p_vector3 <- c('B'=1, 'v'=3, 'v_lMd'=1, 't0'=0.1, 'v_lMd.w'=1, 'v_lMd.d_ei'=2)</pre>
par(mfcol=c(2,3))
plot_trend(p_vector1, emc=emc_incr, par_name='v',
            subject=1, lM_filter=TRUE, main='v correct accumulator', ylim=c(3.5,5))
plot_trend(p_vector1, emc=emc_incr, par_name='v',
            subject=1, lM_filter=FALSE, main='v incorrect accumulator', ylim=c(1, 2.5))
```



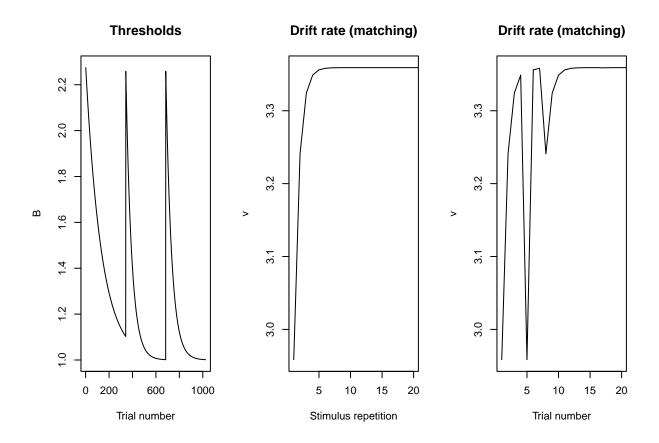
In this set-up, no matter the value of $v_1Md.w$ the between-accumulator difference in drift rates increases over time. Using the same logic, we can also enforce a decrease by using exp_decr as a kernel and applying an exponential transform to w.

So far, we only inspected time on task as defined by trial number. Other options include time on task within block (e.g., short breaks between trials could cause an increased threshold for the first few trials in each block), or the number of times a stimulus type has been shown. Furthermore, the parameters describing the trend could differ between blocks and stimulus types. To test such hypotheses, we can allow the trend parameters themselves to vary with experimental factors, as defined in formula in design(). The example data does not have stimulus type recorded, and all trials were run in a single block, but for demonstrative purposes we can simulate such effects:

```
# simulate block number (assume 3 blocks)
dat$block <- as.factor(as.numeric(cut(dat$trials, breaks=3)))
for(subject in unique(dat$subjects)) {
  dat[dat$subjects==subject,'trial_in_block'] <- ave(</pre>
```

```
seq_along(dat[dat$subjects==subject,'block']),
    dat[dat$subjects==subject,'block'], FUN = seq_along)/1000
}
# simulate presented digit
dat$stimulus_repetition <- ave(seq_along(dat$S),</pre>
                                 dat$S, FUN = seq_along)
 # combine two trends
trends <- make_trend(par_names=c('B', 'v_1Md'),</pre>
                      cov_names=c('trial_in_block', 'stimulus_repetition'),
                      kernels = c('exp_decr', 'exp_incr'),
                      bases = c('lin', 'lin'), )
design_multitrend <- design(model=RDM,</pre>
                          data=dat,
                          contrast=list(lM=ADmat),
                          covariates=c('trial_in_block', 'stimulus_repetition'),
                          matchfun=function(d) d$S==d$lR,
                          transform=list(func=c('v_lMd.w'='exp',
                                                 'B.w'='exp',
                                                 'v'='identity',
                                                 'B'='identity')),
                          formula=list(B ~ 1, v ~ lM, t0 ~ 1, `B.d_ed`~block),
                          trend=trends)
 Sampled Parameters:
 [1] "B"
                                      "v_lMd"
                                                       "t0"
 [5] "B.d_ed"
                      "B.d_ed_block2" "B.d_ed_block3" "B.w"
 [9] "v_1Md.w"
                     "v_lMd.d_ei"
Design Matrices:
$B
В
1
$v
    lM v v lMd
 TRUE 1 0.5
FALSE 1 -0.5
$t0
t0
 1
$B.d_ed
block B.d_ed B.d_ed_block2 B.d_ed_block3
     1
            1
     2
                                         0
            1
                          1
            1
                                         1
$B.w
B.w
   1
$v_lMd.w
```

```
emc_multitrend <- make_emc(dat, design_multitrend)</pre>
# thresholds
p_vector <- c('B'=1, 'v'=1, 'v_1Md'=2, 't0'=0.1,</pre>
              'B.d_ed'=2, 'B.d_ed_block2'=1, 'B.d_ed_block3'=1, 'B.w'=.25,
              'v_1Md.w'=1, 'v_1Md.d_ei'=.2)
par(mfcol=c(1,3))
plot_trend(p_vector, emc=emc_multitrend, par_name='B',
           subject=1, lR_filter='odd', main='Thresholds',
           xlab='Trial number')
plot_trend(p_vector, emc=emc_multitrend, par_name='v',
           subject=1, lM_filter=TRUE, main='Drift rate (matching)',
           on_x_axis='stimulus_repetition',
           xlab='Stimulus repetition', xlim=c(1,20))
plot_trend(p_vector, emc=emc_multitrend, par_name='v',
           subject=1, lM_filter=TRUE, main='Drift rate (matching)',
           xlab='Trial number', xlim=c(1,20))
```



mapped_pars(design_multitrend)

```
$B
intercept : B_t
Trends:
B_t = B + \exp(B.w) * \exp(-\exp(B.d_ed) * trial_in_block)
$v
 lM
TRUE
       : v + 0.5 * v_1Md_t
FALSE : v - 0.5 * v_1Md_t
v_1Md_t = v_1Md + exp(v_1Md.w) * (1 - exp(-exp(v_1Md.d_ei) * stimulus_repetition))
$B.d_ed
 block
 1
        : exp(B.d_ed)
        : exp(B.d_ed + B.d_ed_block2)
        : exp(B.d_ed + B.d_ed_block3)
```

The left panel illustrate how the thresholds decrease within each block (at different rates), but then reset to the same asymptote after every break. The middle panel shows the drift rate for the correct accumulator as a function of how often a stimulus has been presented. Note that, when plotted against trial number (right panel), this leads to strong variability in rates across trials.

Polynomials

add, identity

When a researcher has no strong prior assumptions about the shape of the trend but wishes to capture gradual changes, it is possible to fit a set of basis functions, such as polynomials. EMC2 currently includes second-, third-, and fourth-order polynomials as available kernels. This approach follows the logic of a Taylor expansion: any function can be approximated with increasing accuracy by summing polynomials of increasing order. However, the increased accuracy comes at a cost of increased sampling uncertainty, since more parameters need to be estimated. As such, it may be possible to estimate only a few polynomials.

```
trend_help(kernel='poly4')

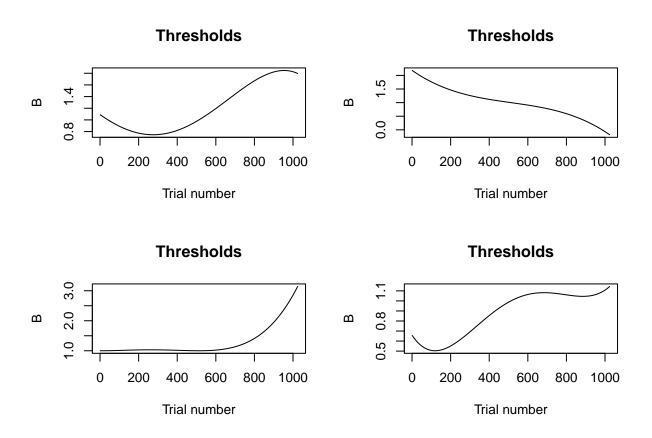
Description:
Quartic polynomial: k = d1 * c + d2 * c^2 + d3 * c^3 + d4 * c^4

Default transformations (in order):
list(d1 = "identity", d2 = "identity", d3 = "identity", d4 = "identity")

Available bases, first is the default:
```

Note that the kernel parameters (d1, d2, d3, d4) already weigh the contributions of the individual polynomial terms. As such, this kernel should not be combined with a linear base (base = 'lin'), but instead with an additive base (base = 'add'). Additionally, we should center the Taylor expansion around the mean of the covariate. The following demonstrates the flexibility of a 4th order polynomial with a few randomly chosen parameter sets:

```
$t0
t0
  1
$B.d1
B.d1
    1
$B.d2
B.d2
   1
$B.d3
B.d3
    1
$B.d4
B.d4
   1
$A
Α
1
$s
 s
mapped_pars(design_poly)
$B
intercept : B_t
Trends:
B_t = B + (B.d1 * tctrd + B.d2 * tctrd^2 + B.d3 * tctrd^3 + B.d4 * tctrd^4)
$v
  lM
       : \exp(v + 0.5 * v_1Md)
FALSE : exp(v - 0.5 * v_1Md)
emc_poly <- make_emc(dat, design_poly)</pre>
p_vector1 <- c('B'=1, 'v'=1, 'v_lMd'=2, 't0'=0.1,</pre>
               'B.d1'=2, 'B.d2'=3, 'B.d3'=-5, 'B.d4'=-5)
p_vector2 <- c('B'=1, 'v'=1, 'v_1Md'=2, 't0'=0.1,</pre>
               'B.d1'=-1, 'B.d2'=0, 'B.d3'=-5, 'B.d4'=0)
p_vector3 <- c('B'=1, 'v'=1, 'v_1Md'=2, 't0'=0.1,</pre>
               'B.d1'=0, 'B.d2'=2, 'B.d3'=8, 'B.d4'=8)
p_vector4 <- c('B'=1, 'v'=1, 'v_1Md'=2, 't0'=0.1,</pre>
               'B.d1'=1, 'B.d2'=-3, 'B.d3'=-2, 'B.d4'=10)
```



Mechanisms of dynamics: Stimulus memory

Models with formal mechanisms of dynamics rely on delta rules. To implement delta rules, we follow the same general logic as above—the delta rule is implemented as a kernel in make_trend. Let's implement the stimulus memory mechanism proposed by Miletic et al. (2025). Here, the decision maker keeps track of the probability that a stimulus is even (or odd). The covariate in this case is the stimulus, which we can recode as 1 (even) and -1 (odd). With the delta rule:

$$Q_{SM,t+1} = Q_{SM,t} + \alpha_{SM} \cdot (S_t - Q_{SM,t}), \quad S \in \{-1,1\}$$

The delta rule introduces two extra parameters: a learning rate α_{SM} , and a value for Q at the start of the experiment $Q_{SM,0}$. The latter is hard to estimate, and we tend to fix it to a constant—for this rule, a constant of 0 implies equal beliefs in both stimuli.

For now, let us assume that stimulus memory influences the relative thresholds: the even threshold increases, and the odd threshold decreases (by the same amount). To achieve this, we need to parameterize thresholds with the same mean-difference parameterization as we used for drift rates. That is,

$$B_{odd} = B_{mean} + B_{lRd}$$
$$B_{even} = B_{mean} - B_{lRd}$$

The B_{lRd} term is the parameter influenced by the updated covariate—however, since we do not necessarily expect an across-trial mean difference between thresholds, we set B_{lRd} as a constant to 0.

Using a linear base, we then allow the threshold difference to vary on a trial-by-trial basis with

$$B_{lRd,t} = B_{lRd} + w_{SM} \cdot Q_{SM,t}$$

Note the extra parameter here: w_{SM} .

```
dat$Stim1 <- ifelse(dat$S=='even', 1, -1)</pre>
SM_trend <- make_trend(cov_names=c('Stim1'),</pre>
                         kernels = 'delta',
                         par_names='B_lRd',
                         bases='lin',
                         premap=TRUE,
                         filter_lR=TRUE)
        # see advanced notes for an explanation filter_lR
design_RDM_SM <- design(model=RDM,</pre>
                          data=dat,
                          contrast=list(lM=ADmat, lR=ADmat),
                          covariates='Stim1',
                          matchfun=function(d) d$S==d$lR,
                          formula=list(B ~ 1R, v ~ 1M, t0 ~ 1),
                          trend=SM_trend,
                           constants=c('B_1Rd'=0, 'B_1Rd.q0'=0))
```

```
Sampled Parameters:
[1] "B"
                                  "v_lMd"
                                                "t0"
                                                               "B_lRd.w"
[6] "B_lRd.alpha"
Design Matrices:
$B
   1R B B_1Rd
 even 1 - 0.5
  odd 1
          0.5
$v
    1M v v_1Md
 TRUE 1
           0.5
FALSE 1 -0.5
$t0
```

```
t0
1
$B_1Rd.w
B_1Rd.q0
B_1Rd.q0
1
$B_1Rd.alpha
B_1Rd.alpha
1
$A
A
1
```

We can now apply a similar prior to B as above, and fit the model. Note that data compression is turned off automatically, since the delta rule needs to be applied to the covariate on each trial individually.

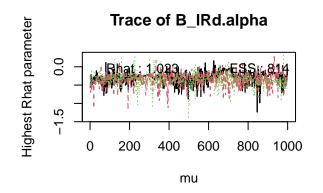
```
prior_SMB <- prior(design_RDM_SM, mu_mean=c(B=2), mu_sd=c(B=0.5))
emc <- make_emc(dat, design=design_RDM_SM, prior_list = prior_SMB, compress=FALSE)</pre>
```

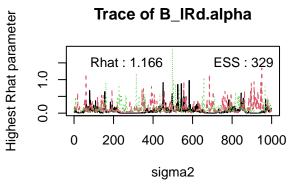
check(emc)

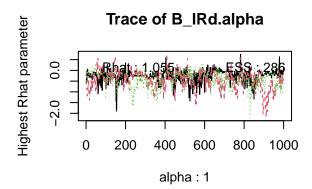
Iterations:

preburn burn adapt sample

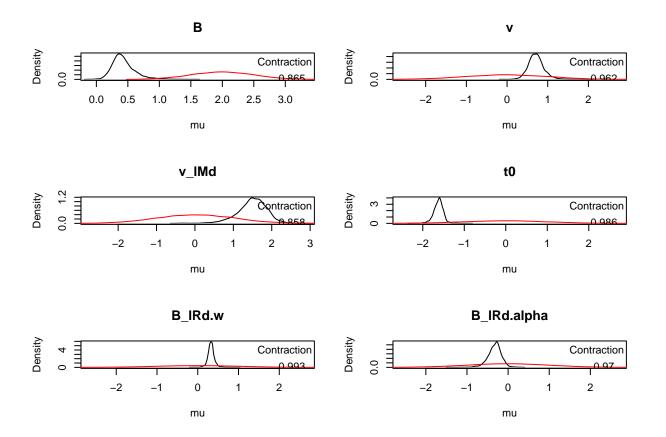
```
[1,]
                           1000
           0
                 0
                       0
[2,]
           0
                 0
                       0
                           1000
[3,]
           0
                       0
                           1000
mu
            В
                                        tO B_lRd.w B_lRd.alpha
                           v_lMd
                      ٧
Rhat
        1.006
                  1.004
                           1.005
                                                          1.023
     1220.000 1747.000 1668.000 1664.000 962.000
ESS
                                                        814.000
sigma2
           В
                     V
                          v_lMd
                                       tO B_1Rd.w B_1Rd.alpha
Rhat
       1.005
                1.007
                          1.005
                                    1.004
                                            1.028
                                                         1.166
ESS
    942.000 1265.000 1401.000 1553.000 795.000
                                                       329.000
alpha highest Rhat : 1
            В
                         v_lMd
                                      tO B_lRd.w B_lRd.alpha
                     V
Rhat
        1.004
                1.023
                         1.019
                                   1.003
                                           1.052
                                                        1.055
ESS 1543.000 806.000 812.000 1863.000 247.000
                                                      286.000
```







plot_pars(emc)



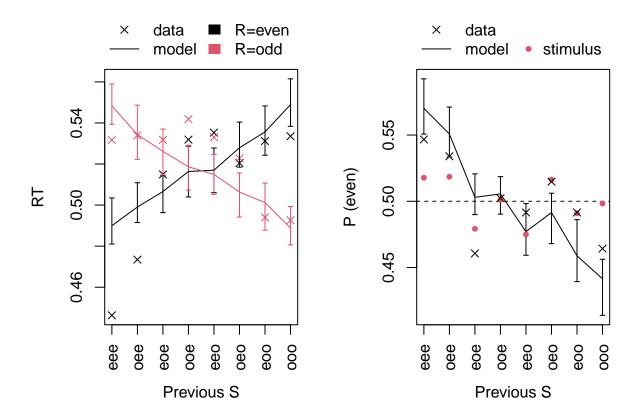
We find excellent convergence properties. Note that learning rates are by default sampled on the probit scale, so if we want to know the mean learning rate, we need to map and transform the parameters first:

```
credint(emc, map=TRUE)
```

\$mu 2.5% 50% 97.5% B 1Reven 1.162 1.495 2.445 B_1Rodd 1.162 1.495 2.445 v_lMTRUE 3.420 4.333 5.250 v_lMFALSE 0.499 0.947 2.226 t0 0.151 0.199 0.241 0.153 0.325 0.495 $B_1Rd.w$ B_1Rd.alpha 0.237 0.377 0.489

Hence, we find a group-wise mean learning rate of ~ 0.38 , and the threshold of the odd accumulator is 0.323 lower than the threshold for the even accumulator if the participant has a Q_{SM} -value of 1.

We can now check whether the SM mechanism can explain stimulus-history effects by plotting the RTs (by choice) and the probability of choosing left as a function of the previous three presented stimuli. First, generate posterior predictives:



The left panel of this plot shows the mean RT as a function of the three previous trials' stimuli (ooo = odd, odd, odd; ooe = odd, odd, even; etc. Note that the right-most letter in the string indicates the most recent trial). The data show a cross-over pattern, such that if the previous three stimuli were odd, 'odd' responses are faster than 'even' responses; and vice versa. The model tends to capture this cross-over pattern fairly well, with some misfits mostly due to an apparent asymmetry in the cross-over in the data.

The right panel shows the probability of choosing even (black) and the probability of the stimulus being even (red) as a function of local trial history. The black crosses demonstrates that participants are more likely (~.55) to choose 'even' if the previous three trials were 'even'. The red circles are important as a quality check. If the stimuli are generated truly randomly, the red circles should be approximately at 0.5 in all cases. However, some experiments use pseudorandomization, which can lead to negative correlations in local stimulus histories. This can confound any stimulus history effects present in the human data. True stimulus history effects are those that are larger than the ones present in the data, e.g., visible as black crosses deviating stronger from 0.5 compared to red circles.

Advanced note: filter_lR

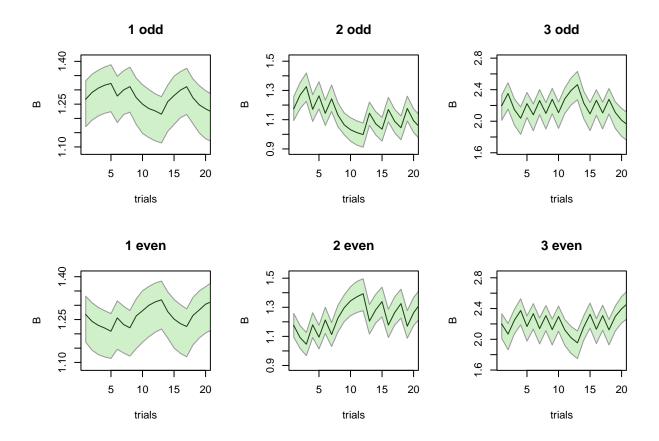
Under the hood, EMC2 works with data-augmented design matrices (dadms). A dadm contains one row per accumulator per trial – so for race models applied to two-alternative forced choice tasks, this will typically result in two rows per trial. We can inspect the dadm for the first subject in the emc object to see that the covariate Stim1 is indeed the same across accumulators in each trial:

head(emc[[1]]\$data[[1]])

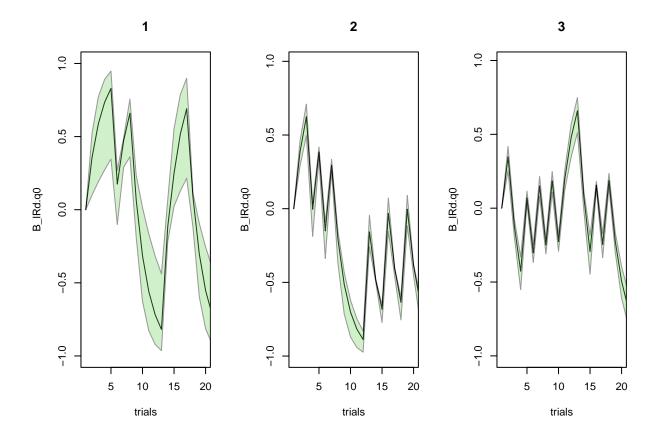
```
subjects
                         rt trials trials2 block trial_in_block
                                      0.001
1
         1 even even 0.54
                                  1
2
                                      0.001
                                                 1
                                                              0.001
         1 even even 0.54
                                  1
3
         1 even even 0.42
                                  2
                                      0.002
                                                 1
                                                              0.002
4
         1 even even 0.42
                                  2
                                      0.002
                                                 1
                                                              0.002
         1 even even 0.50
5
                                  3
                                      0.003
                                                 1
                                                              0.003
                                      0.003
                                                              0.003
6
         1 even even 0.50
                                  3
                                                 1
  stimulus_repetition
                          tctrd Stim1
                                          1R
                                                lM winner Stim1_lRfiltered
1
                      1 - 0.5115
                                     1 even
                                              TRUE
                                                      TRUE
2
                      1 -0.5115
                                        odd FALSE
                                                     FALSE
                                                                           NA
                                     1
3
                      2 - 0.5105
                                       even
                                              TRUE
                                                      TRUE
                                                                            1
4
                      2 -0.5105
                                                                           NA
                                        odd FALSE
                                                     FALSE
                                     1
5
                      3 - 0.5095
                                              TRUE
                                                      TRUE
                                                                            1
                                       even
6
                      3 -0.5095
                                        odd FALSE
                                                    FALSE
                                                                           NA
```

The delta rule is applied to the covariate as it is specified in the dadm. Since, in the examples in this tutorial, the covariate is the same for both accumulators, blindly applying a delta rule to the covariate in the dadm would lead to two updates every trial: One for the first accumulator, and then another one for the second accumulator. The Q-values would then also differ between accumulators. The correct behavior is to update only once every trial (i.e., for the first accumulator), and then feed forward the updated Q-value to every second (and third, fourth, ...) accumulator. This can be done by setting the covariate for every second, third, fourth, etc accumulator to NA, since NA-values are ignored when updating. filter_1R=TRUE does this: it creates a new column covariate_1Rfiltered, and applies the delta rule to that column, feeding forward updated Q-values when encountering an NA-value. In many applications when using dynamic EAMs, this is likely the intended behavior. However, there are two exceptions: 1) The DDM only has one accumulator per trial, so no filtering has to be done (or can be done); and 2) when using RL-EAMs, applied to instrumental learning tasks, the covariate can differ between the two accumulators (feedback can be given to one specific option, for example). In such cases, more advanced handling of the covariate is required, and filter_1R should not be TRUE.

As before, we can plot the trial-wise parameters with plot_trend(). Let's zoom in on the even and odd thresholds of the first three subject for the first 20 trials:



Alternatively, we can plot the evolution of the Q-values themselves. Note that predict() was run with another argument: return_covariates, which returns the updated covariates as an attribute. We can use this as follows:



Repetition/alternation memory

The stimulus-memory mechanism accounts for what Jones et al. (2014) termed first-degree recency effects: They depend on stimulus identity (e.g., 'odd' or 'even'). There are also second-degree recency effects, which depend on sequential properties - i.e., whether stimuli are repetitions or alternations of those stimuli before. It is easy to implement such a mechanism with a delta rule as well. If we code the stimuli as $S_t \in -1, 1$, then the multiplication $S_{t-1}S_t$ indicates if trial t repeats (outcome 1) or alternates (outcome -1) trial t-1. Let's hypothesize that participants keep track of the repetition rate using a repetition memory (RM). That could make use of the delta rule:

$$Q_{RM,t+1} = Q_{RM,t} + \alpha_{RM} \cdot (S_{t-1}S_t - Q_{RM,t}), \quad S \in \{-1,1\}$$

 Q_{RM} is a latent representation for the belief that the stimulus will repeat itself. We could hypothesize that, if participants believe that the stimulus is repeating, the threshold corresponding the choice option that repeats the previous stimulus is lower compared to the one that alternates - and vice versa. To implement this, we need to parametrise the thresholds as repeat/alternate:

$$B_{repeat} = B_{mean} + B_{lR2d}$$
$$B_{alternate} = B_{mean} - B_{lR2d}$$

Like before, we are making use of an advantage-difference parametrisation for the thresholds here, but the difference B_{lR2d} parameter here codes accumulators by whether they repeat or alternate the previous stimuli. This B_{lR2d} term is the parameter influenced by the updated covariate. Since we do not necessarily expect an across-trial mean difference between thresholds, we set B_{lR2d} itself as a constant to 0.

Using a linear base, we then allow the threshold difference to vary on a trial-by-trial basis with

$$B_{lR2d,t} = B_{lR2d} + w_{RM} \cdot Q_{RM,t}$$

Again introducing a weighting parameter: w_{RM} .

Let's implement this step by step. First, let's add $S_{t-1}S_t$ to the data, as dat\$Stim2. This will be our new covariate. It should affect B_1R2d with a linear basis. Contrary to 1R, the 1R2 factor is not automatically created by EMC2, so we must pass a function to design that creates it for us..

```
dat$Stim1 <- ifelse(dat$S=='even', 1, -1)</pre>
dat\$Stim2 \leftarrow dat\$Stim1*Hmisc::Lag(dat\$Stim1,1) # S_{t-1}S_{t}
RM_trend <- make_trend(cov_names=c('Stim2'),</pre>
                         kernels = 'delta',
                         par names='B 1R2d',
                         bases='lin',
                         premap=TRUE,
                         filter_1R=TRUE)
ADmat <- matrix(c(-.5,.5), ncol=1, dimnames=list(NULL,'d'))
make_1R2 <- function(x) {</pre>
  # note that we need to use lag 2, since the dadm has one row per accumulator
 1R2 <- as.numeric(x$1R)==as.numeric(Hmisc::Lag(x$S,2))</pre>
  # The first trial has no repeat/alternate.
  # However, since we set B_lR2d.q0, we can set lR2 for this trial
  # arbitrarily TRUE or FALSE -- B_lR2d_{1} is always 0.
  1R2[is.na(1R2)] <- TRUE</pre>
  factor(lR2, levels=c(1,0), labels=c('rep', 'alt'))
}
design_RDM_RM <- design(model=RDM,</pre>
                          contrast=list(lM=ADmat, lR=ADmat, lR2=ADmat),
                          covariates='Stim2',
                          functions=list(1R2=make_1R2),
                          matchfun=function(d) d$S==d$1R,
                          formula=list(B ~ 1R2, v ~ 1M, t0 ~ 1),
                          trend=RM_trend,
                          constants=c('B_1R2d'=0, 'B_1R2d.q0'=0))
```

```
Sampled Parameters:
[1] "B"
                                   "v_lMd"
                                                   "t0"
                                                                   "B 1R2d.w"
[6] "B_1R2d.alpha"
Design Matrices:
$B
1R2 B B_1R2d
rep 1
         -0.5
alt 1
          0.5
$17
    lM v v_lMd
 TRUE 1 0.5
FALSE 1 -0.5
$t0
 t0
```

```
1

$B_1R2d.w

B_1R2d.w

1

$B_1R2d.q0

B_1R2d.q0

1

$B_1R2d.alpha

B_1R2d.alpha

1

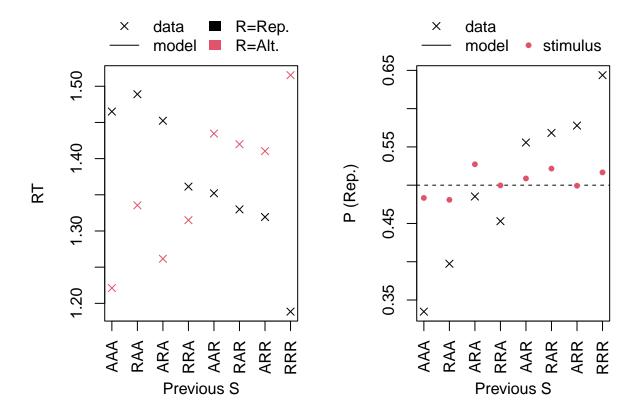
$A

A

1
```

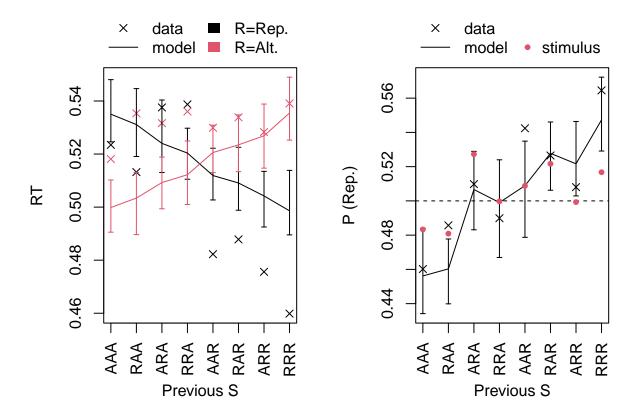
Before fitting, we might want to simulate some data to test whether simulated data indeed demonstrates second-degree recency effects.

```
p_vector <- sampled_pars(design_RDM_RM)
p_vector[1:6] <- c(log(2), log(1), .5, log(.15), 2, qnorm(0.1))
simDat <- make_data(p_vector, design_RDM_RM, data=dat)
# the plot_history_effects()-function takes an additional argument:
# degree, which can be 1 for first-degree or 2 for second-degree
# effects
plot_history_effects(dat=simDat, degree=2)</pre>
```

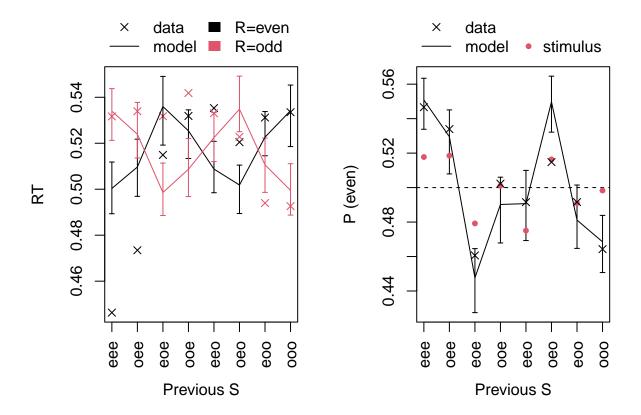


Which generates the expected pattern: if the previous trials were repeats, the model predicts participants are more likely to repeat on the current trial. Furthermore, a 'repeat' response would be faster than an 'alternate' response. Now let's fit the model to see the strength of these effects in real data:

```
plot_history_effects(dat, pp, degree=2)
```



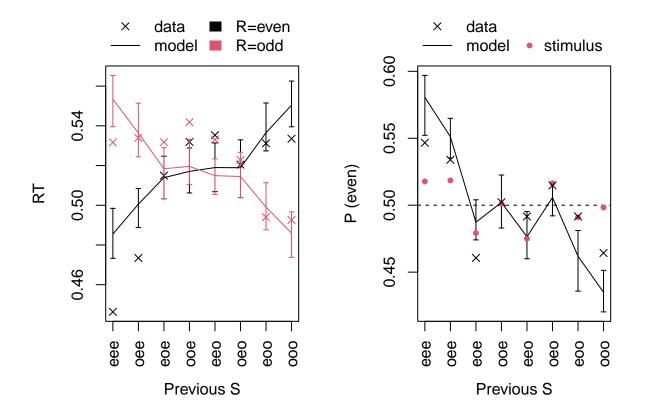
plot_history_effects(dat, pp, degree=1)



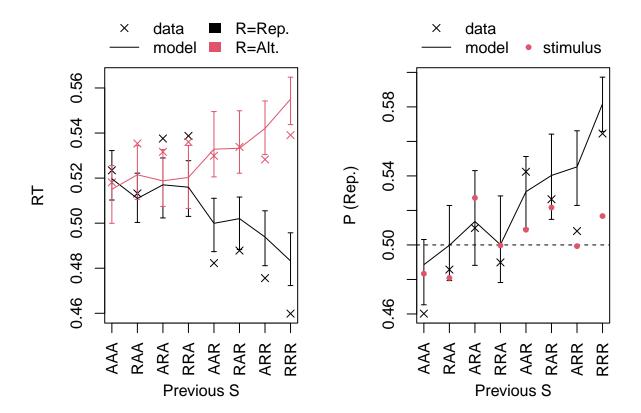
The second-degree recency effects are fitted well, but the first-degree effects now seem off. Perhaps a combination would work best.

```
dat$Stim1 <- ifelse(dat$S=='even', 1, -1)</pre>
dat$Stim2 <- dat$Stim1*Hmisc::Lag(dat$Stim1,1)</pre>
SM_RM_trend <- make_trend(cov_names=c('Stim1', 'Stim2'),</pre>
                         kernels = c('delta', 'delta'),
                         par_names=c('B_1Rd', 'B_1R2d'),
                         bases=c('lin', 'lin'),
                          premap=TRUE,
                          filter_lR=TRUE)
design_RDM_RM <- design(model=RDM,</pre>
                          data=dat,
                          contrast=list(lM=ADmat, lR=ADmat, lR2=ADmat),
                          covariates=c('Stim1', 'Stim2'),
                          functions=list(1R2=function(x) {
                             1R2 <- as.numeric(x$1R) == as.numeric(Hmisc::Lag(x$S,2))</pre>
                             1R2[is.na(1R2)] <- TRUE</pre>
                            factor(1R2, levels=c(1,0), labels=c('rep', 'alt'))
                          matchfun=function(d) d$S==d$lR,
                          formula=list(B ~ 1R2+1R, v ~ 1M, t0 ~ 1),
                          trend=SM_RM_trend,
                           constants=c('B_1R2d'=0, 'B_1R2d.q0'=0,
                                        'B_1Rd'=0, 'B_1Rd.q0'=0))
```

plot_history_effects(dat, pp, degree=1)



plot_history_effects(dat, pp, degree=2)



While the alternation effects are relatively small in this dataset, formal model comparison suggests that the inclusion of the RM mechanism sufficiently improves the quality of fit to warrant the additional model complexity:

```
emc_SMB <- get(load('./samples/ds1_SMB.RData'))
emc_SMB_RMB <- get(load('./samples/ds1_SMB_RMB.RData'))
compare(list('SM'=emc_SMB, 'SM+RM'=emc_SMB_RMB), BayesFactor=FALSE)</pre>
```

```
DIC wDIC BPIC wBPIC EffectiveN meanD Dmean minD SM -6995 0 -6895 0 100 -7096 -7121 -7196 SM+RM -7085 1 -6995 1 90 -7175 -7194 -7265
```

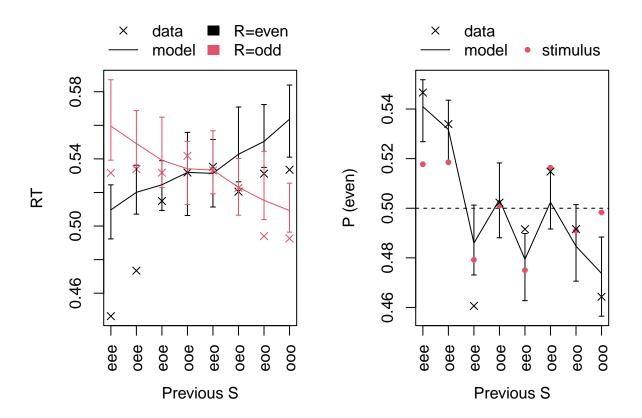
Stimulus memory: DDM and drift rate effects

The examples above mimick Miletic et al. (2025) by using an RDM and assuming that stimulus memory causes a threshold (start point) bias. EMC2 is flexibly designed to implement your own hypotheses. For example, we can propose a DDM instead and hypothesize that drift rates rather than start points are biased. This can be implemented as follows:

However, this does not appear to fit as well qualitatively and loses quantitative model comparisons:

```
pp_ddm <- predict(emc, n_cores=10)
save(pp_ddm, file='./samples/ds1_SMv_DDM_pps.RData')</pre>
```

```
plot_history_effects(dat, pp_ddm)
```



```
#compare(sList=list(rdm=get(load('./samples/ds1_SMB.RData')),
# ddm=get(load('./samples/ds1_SMv_DDM.RData'))))
```

Mechanisms of dynamics: Accuracy memory

Accuracy memory follows the same logic as above, with a different covariate (errors) and a different parameter (urgency, v). Errors are the inverse of accuracy; they are 0 when the response matches the stimulus, and 1 otherwise. Unlike the presented stimulus, accuracy/error is not a static property of the experimental design but depends on the observed behavior. This also means that, when simulating behavior, accuracy needs to be re-calculated based on the newly simulated data.

For this reason, it is useful to have *EMC2* calculate accuracy with a function rather than specifying it in the dataframe (in which case it would be treated as a static experimental factor and assumed fixed across simulations). The same function is applied when generating posterior predictives, so the accuracy is correctly determined in that phase.

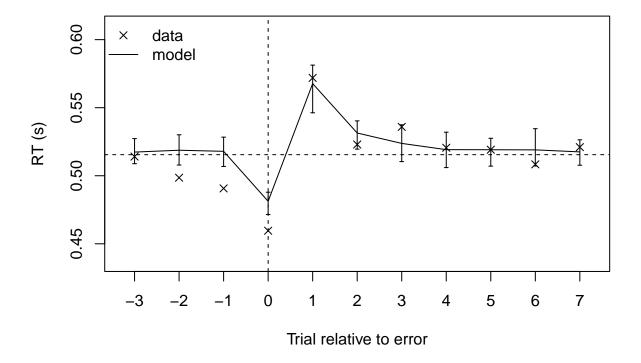
```
AM_trend <- make_trend(cov_names='error',
                        kernels = 'delta',
                        par_names='v',
                        bases='lin',
                        premap=TRUE,
                        filter 1R=TRUE)
design RDM AM <- design(model=RDM,</pre>
                         contrast=list(lM=ADmat, lR=ADmat),
                         functions=list(error=function(x) x$S!=x$R),
                         covariates='error',
                         matchfun=function(d) d$S==d$1R,
                         formula=list(B ~ 1, v ~ lM, t0 ~ 1, s~lM),
                         trend=AM trend,
                         constants=c('v.q0'=0, 's'=1))
# note that 1) we allow within-trial noise s to vary with accumulator
# match (correct/incorrect), which will allow us to capture the
# relative speed of errors.
# note that 2) in this case, we are not estimating v on the natural scale:
mapped_pars(design_RDM_AM)
# This is because the AM mechanism can push drift rates on individual trials
# to negative values when applied on the natural scale.
# Since the RDM has no known analytic likelihood for negative drift rates,
# this can lead to difficulties sampling. Hence, the effect of errors on
# urgency as we implement it here, is not strictly linear -- it is linear on
# the log-scale, and then exponentiated.
# The cognitive interpretation is similar.
emc <- make emc(dat, design=design RDM AM, compress=FALSE)
emc <- fit(emc, cores per chain=6, cores for chains=3,
                fileName='./samples/ds1_AM.RData')
credint(emc)
```

Accuracy memory can help explain error-related effects, like post-error slowing. To visualize, we can generate posterior predictives and then use a convenience function to plot mean RT as a function of trial number relative to an error. Note that, since the covariate in this case depends on observed behavior, we need to simulate data and determine the covariate one trial at a time. EMC2 detects whether the covariate is rt, R, or the output of one of the functions provided to design. If it is, it automatically simulates data trial-by-trial. As vectorisation is not possible in this case, this way of simulating data is slower.

```
emc <- get(load('./samples/ds1_AM.RData'))

pp <- predict(emc, n_cores=10, conditional_on_data=FALSE)
save(pp, file='./samples/ds1_AM_pps.RData')</pre>
```

```
plot_error_effects(dat, pp)
```

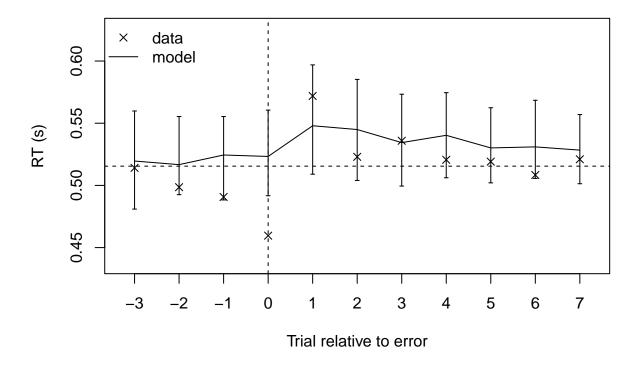


Like in the case of stimulus memory, the accuracy memory mechanism can be adjusted to other EAMs like the DDM, and it can affect other parameters. The DDM does not have an urgency mechanism, but we could, for example, allow AM to affect thresholds. This trend can be specified as post-transform since the thresholds are the same across all design cells. So in this case, we can sample thresholds on the log scale, then transform to the natural scale, and then apply the trend.

However, this again does not appear to fit as well qualitatively, and loses model comparisons:

```
emc <- get(load('./samples/ds1_AMa_DDM.RData'))
pp_ddm <- predict(emc, n_cores=10, conditional_on_data=FALSE)
save(pp_ddm, file='./samples/ds1_AMa_DDM_pps.RData')</pre>
```

```
plot_error_effects(dat, pp_ddm)
```



```
# and loses model comparisons again
#compare(sList=list(rdm=get(load('./samples/ds1_AM.RData')),
# ddm=get(load('./samples/ds1_AMa_DDM.RData'))))
```

Special case: Fluency memory

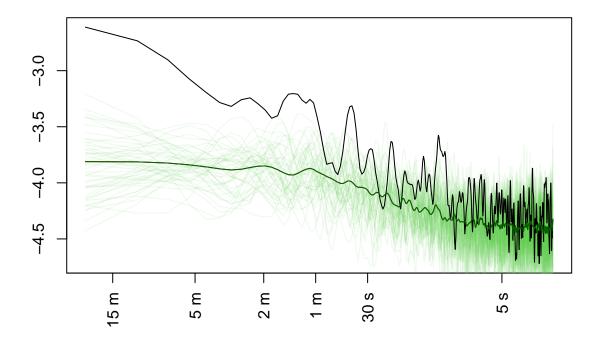
Fluency memory is a formalization of the idea that participants adjust their behavior according to perceived difficulty. To estimate perceived difficulty, we rely on a few simplifying assumptions: participants can quantify (1) their thresholds, and (2) their response time. In race models, the ratio of threshold over response time constitutes a measure of mean speed, which can be used as a proxy for difficulty. After all, we expect processing efficiency to be lower for difficult trials than for easy trials. Formally, $Q_{FM,t+1} = \frac{1}{2} \left(\frac{$

 $Q_{FM,t} + \alpha_{FM}(b_t/rt_t - Q_{FM,t})$. Contrary to stimulus and accuracy memory, fluency memory is a very specific effect, and its implementation is not very flexible. It can only work for race models; it must influence thresholds; and the thresholds should be estimated on the natural scale. EMC2 implements it as a separate kernel deltab with covariate rt:

```
trend_FM=make_trend(kernel='deltab',
                     base='lin',
                     cov names ='rt'.
                     par_names='B', premap = TRUE, filter_lR=TRUE)
design_FM <- design(model=RDM,</pre>
                  data=dat.
                  contrast=list(lM=ADmat),
                  matchfun=function(d) d$S==d$lR,
                  formula=list(B ~ 1, v ~ 1M, t0 ~ 1, s~1M),
                  transform=list(func=c(B='identity'),
                                                                  # should also update prior in this case
                                 lower=c(B.alpha=0.05)),
                  constants=c('B.q0'=3, 's'=log(1)),
                                                                  # Why 3? When fitting a static RDM, the
                  trend=trend FM)
prior_FM <- prior(design_FM, mu_mean=c('B'=2), mu_sd=c('B'=0.5))</pre>
emc <- make_emc(dat, design=design_FM, compress=FALSE, prior_list=prior_FM)</pre>
emc <- fit(emc, cores_per_chain=6, cores_for_chains=3,</pre>
                fileName='samples/ds1_FM.RData')
check(emc)
pp <- predict(emc, n_cores=10, conditional_on_data=FALSE)</pre>
save(pp, file='./samples/ds1_FM_pps.RData')
```

Fluency memory provides an explanation for the slower fluctuations in the observed response times. One useful way to visualize these is by creating a power spectrum of the RT data. We provide a convenience function that does this for the data and the posterior predictives of the estimated model:

```
# convenience function to plot the spectrum
plotSpectrum(dat=dat, pp=pp, trial_duration=1.265) # mean trial duration of this task was 1.265 s, wh
```



which demonstrates that fluency can account for the fluctuations that are moderate to fast, but not the slowest fluctuations.