431 Class 25

thomase love. github. io/431

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Today's Agenda

- What exactly is R doing if you ignore missing values when fitting models?
 - What does type.convert() do?
 - na.omit vs. na.exclude vs. na.delete
- Use multiple imputation to deal with missing data in fitting a linear regression with 1m using the mice package.

(MICE = Multiple Imputation through Chained Equations)

My Setup

```
My R project for Class 25 is located in the following folder...
"unique_stuff_to_me/2021-431/431-classes/class25"
library(here)
here() starts at C:/Users/Thomas/Dropbox/2021-431/431-classes,
library(magrittr); library(knitr)
library(janitor); library(naniar)
library(mice)
  # mice = multiple imputation through chained equations
library(broom)
library(tidyverse)
theme set(theme bw())
```

What happens if you fit a regression model without doing anything at all about missing data?

What happens if you ignore NAs?

Let's open a small, simulated data set with 100 subjects and some missing values.

```
sim1 <- read_csv(here("data", "c12_sim1.csv")) %>%
    type.convert(as.is = FALSE, na.strings = "NA")
head(sim1)
```

What does type.convert() actually do?

Tries to convert each column (individually) to either logical, integer, numeric, complex or (if a character vector) to factor.

- The first type (from that list) that can accept all non-missing values is chosen.
- If all of the values are missing, the column is converted to logical.
- Columns containing just F, T, FALSE, TRUE or NA values are made into logical.
- Use the na.strings parameter to add missing strings (default = "NA")
- as.is = FALSE converts characters to factors. as.is = TRUE will become the default soon, so you should specify.

Our sim1 data

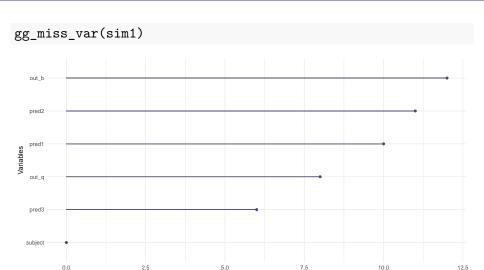
Variable	Description
subject	Subject identifier
$\mathtt{out}\mathtt{_q}$	Quantitative outcome
out_b	Binary outcome with levels Yes, No
pred1	Predictor 1 (quantitative)
pred2	Predictor 2 (also quantitative)
pred3	Predictor 3 (categories are Low, Middle, High)

• Clean up the factors?

Cleaning up subject and pred3

```
pred3 No Yes NA_
Low 10 12 4
Middle 12 17 4
High 16 15 4
<NA> 4 2 0
```

How much missingness do we have?



Missing

How much missingness do we have?

```
miss_var_summary(sim1)
# A tibble: 6 x 3
 variable n_miss pct_miss
 <chr>
          <int> <dbl>
             12
                     12
1 out b
2 pred2 11
                   11
3 pred1
         10
                     10
4 out_q
5 pred3
                      6
6 subject
                      0
n_miss(sim1)
```

[1] 47

How much missingness do we have?

```
prop_complete_case(sim1)
[1] 0.65
miss_case_table(sim1)
  A tibble: 4 \times 3
  n_miss_in_case n_cases pct_cases
                              <dbl>
           <int>
                  <int>
                      65
                                 65
                      25
                                 25
```

3

Suppose we run a linear regression

without dealing with the missing data, so that we run:

How can we tell how many observations will be used?

What happens when we run a regression model?

```
mod1 <- lm(out_q ~ pred1 + pred2 + pred3, data = sim1)
anova(mod1)</pre>
```

Analysis of Variance Table

• How many observations were used to fit this model?

Summary of our linear model

```
summary(mod1)
Call:
lm(formula = out_g ~ pred1 + pred2 + pred3, data = sim1)
Residuals:
   Min 1Q Median 3Q Max
-39.164 -13.900 2.419 15.541 34.156
Coefficients:
          Estimate Std. Error t value Pr(>|t|)
(Intercept) 105.2070 18.6185 5.651 3.82e-07 ***
pred1 -0.8361 1.3010 -0.643 0.523
pred2 0.2611 0.4614 0.566 0.573
pred3Middle -1.3498 5.6802 -0.238 0.813
pred3High -2.7443 5.5427 -0.495 0.622
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 18.74 on 65 degrees of freedom
 (30 observations deleted due to missingness)
Multiple R-squared: 0.01843, Adjusted R-squared: -0.04198
F-statistic: 0.3051 on 4 and 65 DF, p-value: 0.8736
```

Another way to see this

logLik AIC BIC deviance df.residual nobs
<dbl> <dbl> <dbl> <int> <int><</pre>

1 -302. 616. 629. 22822.

65 70

How could we have known this would be 70, in advance?

```
sim1 %>% select(out_q, pred1, pred2, pred3) %>%
    miss_case_table()

# A tibble: 3 x 3
    n_miss_in_case n_cases pct_cases
```

70

25

<int> <int> <dbl>

25

70

0

3

Which observations were not used?

summary(mod1)\$na.action

```
3 4 5 6 13 16 19 26 27 29 30 34 39 48 51 56 62 66 67 68 3 4 5 6 13 16 19 26 27 29 30 34 39 48 51 56 62 66 67 68 72 75 81 83 86 89 93 94 96 97 72 75 81 83 86 89 93 94 96 97 attr(,"class")
```

 A potentially more useful na.action setting in lm is na.exclude which pads out predicted values and residuals with NAs instead of omitting the 30 observations listed above.

Predictions from mod1 with na.omit and na.exclude

101.8528 103.0287

NΑ

NΑ

NΑ

NΑ

Multiple Imputation: Potential and Pitfalls

Sterne et al. 2009 BMJ

Multiple imputation for missing data in epidemiological and clinical research: potential and pitfalls

In this article, we review the reasons why missing data may lead to bias and loss of information in epidemiological and clinical research. We discuss the circumstances in which multiple imputation may help by reducing bias or increasing precision, as well as describing potential pitfalls in its application. Finally, we describe the recent use and reporting of analyses using multiple imputation in general medical journals, and suggest guidelines for the conduct and reporting of such analyses.

https://www.bmj.com/content/338/bmj.b2393

Note: The next 7 slides are derived from Sterne et al.

An Example from Sterne et al.

Consider, for example, a study investigating the association of systolic blood pressure with the risk of subsequent coronary heart disease, in which data on systolic blood pressure are missing for some people.

The probability that systolic blood pressure is missing is likely to:

- decrease with age (doctors are more likely to measure it in older people),
- decrease with increasing body mass index, and
- decrease with history of smoking (doctors are more likely to measure it in people with heart disease risk factors or comorbidities).

If we assume that data are missing at random and that we have systolic blood pressure data on a representative sample of individuals within strata of age, smoking, body mass index, and coronary heart disease, then we can use multiple imputation to estimate the overall association between systolic blood pressure and coronary heart disease.

Missing Data Mechanisms

- Missing completely at random There are no systematic differences between the missing values and the observed values.
 - For example, blood pressure measurements may be missing because of breakdown of an automatic sphygmomanometer.
- Missing at random Any systematic difference between the missing and observed values can be explained by other observed data.
 - For example, missing BP measurements may be lower than measured BPs but only because younger people more often have a missing BP.
- Missing not at random Even after the observed data are taken into account, systematic differences remain between the missing values and the observed values.
 - For example, people with high BP may be more likely to have headaches that cause them to miss clinic appointments.

"Missing at random" is an **assumption** that justifies the analysis, and is not a property of the data.

Trouble: Data missing not at random

Sometimes, it is impossible to account for systematic differences between missing and observed values using the available data.

- In such (MNAR) cases, multiple imputation may give misleading results.
 - Those results can be either more or less misleading than a complete case analysis.
- For example, consider a study investigating predictors of depression.
 - If individuals are more likely to miss appointments because they are depressed on the day of the appointment, then it may be impossible to make the MAR assumption plausible, even if a large number of variables is included in the imputation model.

Where complete cases and multiple imputation analyses give different results, the analyst should attempt to understand why, and this should be reported in publications.

What if the data are MCAR?

If we assume data are MAR, then unbiased and statistically more powerful analyses (compared with analyses based on complete cases) can generally be done by including individuals with incomplete data.

There are circumstances in which analyses of **complete cases** will not lead to bias.

- Missing data in predictor variables do not cause bias in analyses of complete cases if the reasons for the missing data are unrelated to the outcome.
 - In such cases, imputing missing data may lessen the loss of precision and power resulting from exclusion of individuals with incomplete predictor variables but are not required in order to avoid bias.

Stages of Multiple Imputation (1 of 2)

Multiple imputation ... aims to allow for the uncertainty about the missing data by creating several different plausible imputed data sets and appropriately combining results obtained from each of them.

The first stage is to create multiple copies of the dataset, with the missing values replaced by imputed values.

 The imputation procedure must fully account for all uncertainty in predicting the missing values by injecting appropriate variability into the multiple imputed values; we can never know the true values of the missing data.

Note that single Imputation of missing values usually causes standard errors to be too small, since it fails to account for the fact that we are uncertain about the missing values.

Stages of Multiple Imputation (2 of 2)

The second stage is to use standard statistical methods to fit the model of interest to each of the imputed datasets.

- Estimated associations in each of the imputed datasets will differ because of the variation introduced in the imputation of the missing values, and they are only useful when averaged together to give overall estimated associations.
- Standard errors are calculated using Rubin's rules, which take account
 of the variability in results between the imputed datasets, reflecting the
 uncertainty associated with the missing values.
- Valid inferences are obtained because we are averaging over the distribution of the missing data given the observed data.

Comparing Two Linear Models including Multiple Imputation

Framingham data

```
fram_raw <- read_csv(here("data/framingham.csv")) %>%
    clean_names()

dim(fram_raw)

[1] 4238    17
n_miss(fram_raw)
```

• See https://www.framinghamheartstudy.org/ for more details.

[1] 645

fram_sub Tibble for Today

```
fram sub <- fram raw %>%
    mutate(educ = fct recode(factor(education),
                          "Some HS" = "1".
                          "HS grad" = "2",
                          "Some Coll" = "3",
                          "Coll grad" = "4")) %>%
    mutate(obese = as.numeric(bmi >= 30)) %>%
    rename(smoker = "current_smoker",
           sbp = "sys bp") %>%
    mutate(subj id = as.character(subj id)) %>%
    select(sbp, educ, smoker, obese, glucose, subj id)
```

Data Descriptions (variables we'll use today)

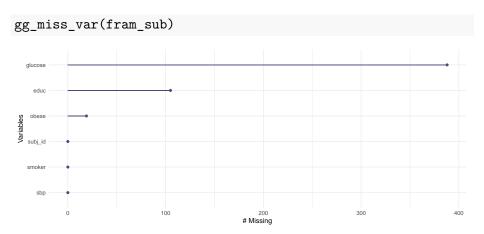
The variables describe n=4238 adult subjects who were examined at baseline and then followed for ten years to see if they developed incident coronary heart disease during that time.

Variable	Description
educ	four-level factor: educational attainment
smoker	1 = current smoker at time of examination, else 0
sbp	systolic blood pressure (mm Hg)
obese	1 if subject's bmi is 30 or higher, else 0
glucose	blood glucose level in mg/dl

Today's Goal

Use linear regression to predict sbp using two different models, in each case accounting for missingness via multiple imputation, where the predictors of interest are glucose, obese, educ, and smoker.

Which variables are missing data?



Track missingness with shadow

```
fram sub sh <- bind shadow(fram sub)</pre>
head(fram sub sh)
# A tibble: 6 x 12
  sbp educ smoker obese glucose subj_id sbp_NA educ_NA
 77 1 !NA !NA
  106 Coll gr~
                0
2 121 HS grad 0
                    0 76 2 !NA !NA
3 128. Some HS 1
                    O 70 3 !NA !NA
           1 0
4
  150 Some Co~
                        103 4 !NA !NA
5 130 Some Co~
                    0
                     85 5 !NA !NA
6
  180
                         99 6 !NA
                                      ! NA
     HS grad
# ... with 4 more variables: smoker NA <fct>,
#
  obese_NA <fct>, glucose_NA <fct>, subj id NA <fct>
```

Our Two Models

Model 2: predict sbp using glucose and obese.

Model 4: predict sbp using glucose, obese, educ, and smoker.

Model 2 (CC): Two-predictor model for sbp

Suppose we ignore the missingness and just run the model on the data with complete information on sbp, glucose and obese.

```
m2_cc <- fram_sub_sh %$% lm(sbp ~ glucose + obese)

tidy(m2_cc, conf.int = TRUE) %>% select(-statistic) %>%
    kable(digits = 3)
```

term	estimate	std.error	p.value	conf.low	conf.high
(Intercept)	121.671	1.244	0	119.232	124.110
glucose	0.111	0.015	0	0.082	0.139
obese	13.532	1.045	0	11.484	15.580

Edited Summary of Model 2 (CC)

```
summary(m2_cc) ## we'll just look at the bottom
```

```
Residual standard error: 21.42 on 3833 degrees of freedom
(402 observations deleted due to missingness)
Multiple R-squared: 0.05857, Adjusted R-squared: 0.05808
F-statistic: 119.2 on 2 and 3833 DF, p-value: < 2.2e-16
```

```
glance(m2_cc) %>%
    select(nobs, r.squared, adj.r.squared, AIC, BIC) %>%
    kable(digits = c(0, 4, 4, 0, 0))
```

nobs	r.squared	adj.r.squared	AIC	BIC
3836	0.0586	0.0581	34401	34426

Model 4 (CC): Four-predictor model for sbp

```
m4_cc <- fram_sub_sh %$%
    lm(sbp ~ glucose + obese + smoker + educ)

tidy(m4_cc, conf.int = TRUE) %>% select(-statistic) %>%
    kable(digits = 3)
```

term	estimate	std.error	p.value	conf.low	conf.high
(Intercept)	127.107	1.388	0	124.385	129.829
glucose	0.106	0.015	0	0.078	0.135
obese	12.304	1.066	0	10.213	14.395
smoker	-4.704	0.699	0	-6.075	-3.332
educHS grad	-3.698	0.833	0	-5.332	-2.065
educSome Coll	-4.724	1.010	0	-6.704	-2.744
educColl grad	-5.954	1.158	0	-8.225	-3.683

Edited Summary of Model 4 (CC)

```
summary(m4_cc) ## we'll just look at the bottom
```

```
Residual standard error: 21.2 on 3733 degrees of freedom
(498 observations deleted due to missingness)
Multiple R-squared: 0.08257, Adjusted R-squared: 0.0811
F-statistic: 56 on 6 and 3733 DF, p-value: < 2.2e-16
```

```
glance(m4_cc) %>%
    select(nobs, r.squared, adj.r.squared, AIC, BIC) %>%
    kable(digits = c(0, 4, 4, 0, 0))
```

nobs	r.squared	adj.r.squared	AIC	BIC
3740	0.0826	0.0811	33466	33516

Variables used in our models 2 and 4

```
miss_var_summary(fram_sub)
# A tibble: 6 x 3
```

• Are we missing data on our outcome for these models?

Create multiple imputations for this subset

```
How many subjects have complete / missing data that affect this model?

pct_complete_case(fram_sub)

[1] 88.24917

pct_miss_case(fram_sub)

[1] 11.75083
```

Let's create 15 imputed data sets.

```
set.seed(431431)
fram_mice24 <- mice(fram_sub, m = 15, printFlag = FALSE)</pre>
```

Warning: Number of logged events: 1

 Using printFlag = FALSE eliminates a lot of unnecessary (and not particularly informative) output here.

Summary Information about Imputation Process

```
summary(fram_mice24)
```

```
Class: mids
Number of multiple imputations:
Imputation methods:
          educ
                   smoker
                                         glucose
      gda
                                 obese
                                                   subj_id
       "" "polyreg"
                          11 11
                                 "mmmg"
                                           "mmg"
PredictorMatrix:
       sbp educ smoker obese glucose subj id
sbp
              1
educ
smoker 1 1
obese 1 1
glucose 1 1
subj_id
Number of logged events:
  it im dep
             \mathtt{meth}
                        out
```

Options within mice for imputation approaches

Default methods include:

- pmm predictive mean matching (default choice for quantitative variables)
- logreg logistic regression (default for binary categorical variables)
- polyreg polytomous logistic regression (for nominal multi-categorical variables)
- polr proportional odds logistic regression (for ordinal categories)

but there are cart methods and many others available, too.

What should we include in an imputation model?

- If things you are imputing are not Normally distributed, this can pose special challenges, and either a transformation or choosing an imputation method which is robust to these concerns is helpful.
- Include the outcome when imputing predictors. It causes you to conclude the relationship is weaker than it actually is, if you don't.
- The MAR assumption may only be reasonable when a certain variable is included in the model.
 - As a result, it's usually a good idea to include as wide a range of variables in imputation models as possible. The concerns we'd have about parsimony in outcome models don't apply here.

Store one (or more) of the imputed data sets

```
This will store the fifth imputed data set in imp_5.
```

```
imp_5 <- complete(fram_mice24, 5) %>% tibble()
dim(imp_5)
```

```
[1] 4238 6
n_miss(imp_5)
```

[1] 0

Run Model 2 on each imputed data frame

```
m2_mods <- with(fram_mice24, lm(sbp ~ glucose + obese))</pre>
```

```
summary(m2_mods)
 A tibble: 45 x 6
           estimate std.error statistic p.value
                                           nobs
  term
           <db1> <db1> <db1>
                                     <db1> <int>
  <chr>
                    1.15 106. 0
1 (Intercept) 122.
                                           4238
2 glucose 0.104 0.0134 7.74 1.27e-14
                                           4238
        13.3
                     0.984 13.5 5.93e-41
3 obese
                                           4238
4 (Intercept) 121.
                                           4238
                     1.19 102.
                                   0
                                           4238
5 alucose 0.112
                     0.0139 8.03 1.23e-15
        13.4
6 obese
                     0.986 13.6 4.48e-41
                                          4238
7 (Intercept) 121.
                                           4238
                     1.15 105.
                                  0
8 alucose 0.120
                     0.0135 8.93 6.49e-19
                                           <u>4</u>238
        13.1
9 obese
                     0.986 13.3 1.89e-39
                                           4238
10 (Intercept) 121.
                     1.20
                             101.
                                   0
                                           4238
  .. with 35 more rows
```

• 3 coefficients in each model, times 15 imputations = 45 rows.

More detailed regression results?

Consider working with the analysis done on the 4th imputed data set (of the 15 created). . .

```
m2_a4 <- m2_mods$analyses[[4]]
tidy(m2_a4) %>% kable(digits = 3)
```

term	estimate	std.error	statistic	p.value
(Intercept)	121.052	1.200	100.861	0
glucose	0.117	0.014	8.322	0
obese	13.243	0.985	13.441	0

Pool Results across the 15 imputations

```
m2_pool <- pool(m2_mods)</pre>
summary(m2 pool, conf.int = TRUE, conf.level = 0.95)
        term estimate std.error statistic
                                                    df
  (Intercept) 121.1962463 1.28910584 94.015745 408.3743
     glucose 0.1153255 0.01529575 7.539707 332.3981
3
       obese 13.2902350 0.99510223 13.355648 3704.3661
      p.value
                     2.5 % 97.5 %
1 0.000000e+00 118.66213491 123.7303577
2 4.527489e-13 0.08523679 0.1454141
3 0.000000e+00 11.33923297 15.2412370
```

Model 2 (Complete Cases vs. Multiple Imputation)

```
tidy(m2_cc, conf.int = TRUE) %>% kable(digits = 3)
```

term	estimate	std.error	statistic	p.value	conf.low	conf.high
(Intercept)	121.671	1.244	97.792	0	119.232	124.110
glucose	0.111	0.015	7.577	0	0.082	0.139
obese	13.532	1.045	12.954	0	11.484	15.580

```
summary(m2_pool, conf.int = TRUE, conf.level = 0.95) %>%
select(-df) %>% kable(digits = 2)
```

term	estimate	std.error	statistic	p.value	2.5 %	97.5 %
(Intercept)	121.20	1.29	94.02	0	118.66	123.73
glucose	0.12	0.02	7.54	0	0.09	0.15
obese	13.29	1.00	13.36	0	11.34	15.24

More Details on Multiple Imputation Modeling

m2_pool

Definitions of all of these terms are available in the mipo help file.

- riv = relative increase in variance attributable to nonresponse
- fmi = fraction of missing information due to nonresponse

Model 4 run on each imputed data frame

```
summary(m4_mods)
 A tibble: 105 x 6
        estimate std.error statistic p.value
  term
                                                nobs
                 <db1> <db1> <db1> <db1> <int>
  <chr>
1 (Intercept) 128.
                        1.27 100. 0
                                                4238
2 glucose
             0.0969
                        0.0133
                                   7.28 3.93e-13
                                                4238
3 obese
               11.8
                        0.985 12.0 1.57e-32
                                                4238
4 smoker
                        0.656
                                  -6.80 1.23e-11
                                                <u>4</u>238
5 educHS grad
                        0.780
                                  -4.72 2.40e- 6
                                                4238
6 educSome Coll
                                                <u>4</u>238
                        0.947
                                  -5.61 2.13e- 8
7 educColl grad -6.16
                        1.09
                                  -5.65 1.71e- 8
                                                4238
8 (Intercept)
              127.
                        1.31
                                  97.2 0
                                                <u>4</u>238
                        0.0138 7.57 4.70e-14
9 alucose 0.104
                                                4238
10 obese
                         0.986
                                                4238
               11.8
                                  12.0 1.12e-32
 ... with 95 more rows
```

Pool Results across the five imputations

```
m4_pool <- pool(m4_mods)
summary(m4_pool, conf.int = TRUE, conf.level = 0.95) %>%
select(-df) %>% kable(digits = 2)
```

term	estimate	std.error	statistic	p.value	2.5 %	97.5 %
(Intercept)	126.91	1.41	90.25	0	124.14	129.67
glucose	0.11	0.02	7.16	0	0.08	0.14
obese	11.77	1.00	11.82	0	9.82	13.73
smoker	-4.43	0.66	-6.75	0	-5.72	-3.15
educHS grad	-3.66	0.79	-4.62	0	-5.21	-2.11
educSome Coll	-5.25	0.96	-5.47	0	-7.13	-3.37
educColl grad	-6.13	1.10	-5.58	0	-8.28	-3.97

Complete Cases Result (Model 4)

tidy(m4_cc, conf.int = TRUE) %>% select(-statistic) %>%
 kable(digits = 3)

term	estimate	std.error	p.value	conf.low	conf.high
(Intercept)	127.107	1.388	0	124.385	129.829
glucose	0.106	0.015	0	0.078	0.135
obese	12.304	1.066	0	10.213	14.395
smoker	-4.704	0.699	0	-6.075	-3.332
educHS grad	-3.698	0.833	0	-5.332	-2.065
educSome Coll	-4.724	1.010	0	-6.704	-2.744
educColl grad	-5.954	1.158	0	-8.225	-3.683

Multiple Imputation Result (Model 4)

```
summary(m4_pool, conf.int = TRUE) %>%
select(-statistic, -df) %>% kable(digits = 3)
```

term	estimate	std.error	p.value	2.5 %	97.5 %
(Intercept)	126.905	1.406	0	124.143	129.668
glucose	0.107	0.015	0	0.078	0.137
obese	11.774	0.996	0	9.820	13.728
smoker	-4.435	0.657	0	-5.723	-3.147
educHS grad	-3.660	0.792	0	-5.214	-2.106
educSome Coll	-5.251	0.960	0	-7.133	-3.369
educColl grad	-6.126	1.097	0	-8.276	-3.975

More Details on Multiple Imputation Modeling

m4_pool

```
m4_pool
Class: mipo
               m = 15
                                                                     t dfcom
                      estimate
                                       ubar
    (Intercept) 15 126.9054997 1.6777883057 2.806862e-01 1.9771868946
                                                                        4231
                                                                              521.7802
        alucose 15
                     0.1074957 0.0001848288 3.778876e-05 0.0002251368
                                                                        4231
                                                                              387.9514
                                                                        4231 3628.0260
          obese 15 11.7738693 0.9713228490 2.028081e-02 0.9929557100
                                                                        4231 4184.1354
         smoker 15 -4.4347370 0.4295295322 1.829583e-03 0.4314810871
    educHS grad 15 -3.6597613 0.6073110889 1.939744e-02 0.6280016922
                                                                        4231 3105.0759
 educSome Coll 15 -5.2509672 0.8952687033 2.432866e-02 0.9212192783
                                                                        4231 3333.3562
 educColl grad 15
                    -6.1257072 1.1823783257 1.974515e-02 1.2034398227
                                                                        4231 3808.7663
                   lambda
1 0.178448370 0.151426549 0.154660564
2 0.218083002 0.179037883 0.183237700
3 0.022271546 0.021786330 0.022325139
 0.004543471 0.004522921 0.004998414
5 0.034069200 0.032946732 0.033569016
6 0.028986353 0.028169813 0.028752383
 0.017812824 0.017501080 0.018016589
```

Estimate R²

```
pool.r.squared(m2_mods)

est lo 95 hi 95 fmi
R^2 0.05944041 0.04607775 0.07426549 NaN

pool.r.squared(m4_mods)
```

est lo 95 hi 95 fmi R^2 0.08146963 0.06617182 0.09805258 NaN

• Can also calculated adjusted R^2 by using pool.r.squared(m2_mods, adjusted = TRUE). See next slide.

Estimates of adjusted R^2

Tests of Nested Fits after imputation

The models must be nested (same outcome, one set of predictors is a subset of the other) for this to be appropriate.

Comparing Model 4 to Model 2 fits

We'll use the Wald test after a linear regression fit.

D1(fit4, fit2)

Could also use a likelihood ratio test.

D3(fit4, fit2)

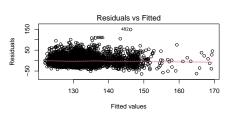
```
test statistic df1 df2 dfcom p.value riv
1 ~~ 2 24.76194 4 276830.7 4231 0 0.01339975
```

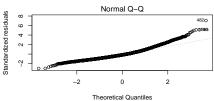
Residual Plots for mod4 with 6th imputed data set

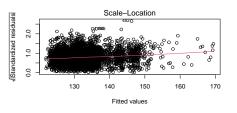
```
par(mfrow = c(2,2))
plot(m4_mods$analyses[[6]])
par(mfrow = c(1,1))
```

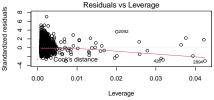
See the next slide for the results.

Residual Plots for mod4 using imputation 6

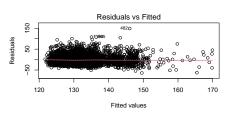


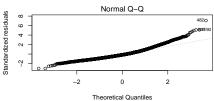


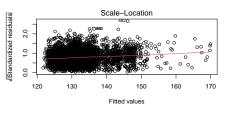


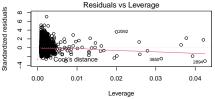


Residual Plots for mod4 using imputation 7









Guidelines for Reporting

Guidelines for reporting, I (Sterne et al.)

How should we report on analyses potentially affected by missing data?

- Report the number of missing values for each variable of interest, or the number of cases with complete data for each important component of the analysis. Give reasons for missing values if possible, and indicate how many individuals were excluded because of missing data when reporting the flow of participants through the study. If possible, describe reasons for missing data in terms of other variables (rather than just reporting a universal reason such as treatment failure.)
- Clarify whether there are important differences between individuals with complete and incomplete data, for example, by providing a table comparing the distributions of key exposure and outcome variables in these different groups
- Describe the type of analysis used to account for missing data (eg, multiple imputation), and the assumptions that were made (eg, missing at random)

Guidelines for reporting, II (Sterne et al.)

How should we report on analyses that involve multiple imputation?

- Provide details of the imputation modeling (software used, key settings, number of imputed datasets, variables included in imputation procedure, etc.)
- If a large fraction of the data is imputed, compare observed and imputed values.
- Where possible, provide results from analyses restricted to complete cases, for comparison with results based on multiple imputation. If there are important differences between the results, suggest explanations.
- It is also desirable to investigate the robustness of key inferences to possible departures from the missing at random assumption, by assuming a range of missing not at random mechanisms in sensitivity analyses.