432 Class 09 Slides

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Today's Agenda

- Data from the Heart and Estrogen/Progestin Study
- Using ols to fit linear regression models in the presence of missing values
- Using aregImpute to facilitate principled multiple imputation when fitting regressions
- Developing detailed regression results under a variety of imputation plans

Setup

```
library(magrittr); library(janitor)
library(here); library(knitr)
library(naniar); library(simputation)
library(rms)
library(tidyverse)
```

Today's Data

Heart and Estrogen/Progestin Study (HERS)

- Clinical trial of hormone therapy for the prevention of recurrent heart attacks and deaths among 2763 post-menopausal women with existing coronary heart disease (see Hulley et al 1998 and many subsequent references, including Vittinghoff, Chapter 4.)
- We're excluding the women in the trial with a diabetes diagnosis.

The Codebook (n = 2032)

Variable	Description
subject	subject code
HT	factor: hormone therapy or placebo
diabetes	yes or no (all are no in our sample)
ldl	LDL cholesterol in mg/dl
age	age in years
smoking	yes or no
drinkany	yes or no
sbp	systolic BP in mm Hg
physact	5-level factor, details next slide
bmi	body-mass index in kg/m^2

Goal Predict 1dl using age, smoking, drinkany, sbp, physact and bmi, across both HT levels but restricted to women without diabetes.

The physact variable

hers1 %>% count(physact)

Comparison is to activity levels for these women just before menopause.

Any missing data?

```
miss_var_summary(hers1)
 A tibble: 10 x 3
   variable n_miss pct_miss
   <chr> <int>
                     <dbl>
                7 0.344
 1 ldl
                2 0.0984
 2 drinkany
                2 0.0984
 3 bmi
 4 subject
 5 ht
 6 age
 7 smoking
 8 sbp
                    0
```

9 physact

10 diabetes

0

Single Imputation for drinkany, bmi and 1dl

Since drinkany is a factor, we have to do some extra work to impute.

```
set.seed(432092)
hers2 <- hers1 %>%
    mutate(drinkany n =
               ifelse(drinkany == "yes", 1, 0)) %>%
    impute pmm(drinkany n ~ age + smoking) %>%
    mutate(drinkany =
               ifelse(drinkany_n == 1, "yes", "no")) %>%
    impute rlm(bmi ~ age + smoking + sbp) %>%
    impute_rlm(ldl ~ age + smoking + sbp + bmi)
```

Now, check missingness...

miss_var_summary(hers2)

```
# A tibble: 11 x 3
  variable n_miss pct_miss
  <chr> <int>
                       <dbl>
 1 subject
2 ldl
3 ht
4 age
 5 smoking
 6 drinkany
  sbp
 8 physact
  bmi
10 diabetes
11 drinkany_n
```

Multiple Imputation using aregImpute from Hmisc

Model to predict all missing values of any variables, using additive regression bootstrapping and predictive mean matching.

Steps are:

- aregImpute draws a sample with replacement from the observations where the target variable is observed, not missing.
- ② It then fits a flexible additive model to predict this target variable while finding the optimum transformation of it.
- It then uses this fitted flexible model to predict the target variable in all of the original observations.
- Finally, it imputes each missing value of the target variable with the observed value whose predicted transformed value is closest to the predicted transformed value of the missing value.

Fitting a Multiple Imputation Model

Iteration 1 Iteration 2 Iteration 3 Iteration 4 Iteration 5 It

Multiple Imputation using aregImpute from Hmisc

aregImpute requires specifications of all variables, and several other details:

- n.impute = number of imputations, we'll run 20
- nk = number of knots to describe level of complexity, with our choice
 nk = c(0, 3:5) we'll fit both linear models and models with
 restricted cubic splines with 3, 4, and 5 knots
- tlinear = FALSE allows the target variable to have a non-linear transformation when nk is 3 or more
- B = 10 specifies 10 bootstrap samples will be used
- data specifies the source of the variables

aregImpute Imputation Results (1 of 4)

```
fit3
```

Multiple Imputation using Bootstrap and PMM

```
aregImpute(formula = ~ldl + age + smoking + drinkany + sbp +
physact + bmi, data = hers1, n.impute = 20, nk = c(0, 3:5),
tlinear = FALSE, B = 10)
```

```
n: 2032 p: 7 Imputations: 20 nk: 0
```

Number of NAs:

```
ldl age smoking drinkany sbp physact bmi 7 0 0 2 0 0 2
```

fit3 Imputation Results (2 of 4)

```
R-squares for Predicting Non-Missing Values for Each
Variable Using Last Imputations of Predictors
ldl drinkany bmi
0.041 0.014 0.109
```

fit3 Imputation Results (3 of 4)

Resampling results for determining the complexity of imputation models

Variable being imputed: Idl

Bootstrap bias-corrected summaries:

Statistic	nk = 0	nk = 3	nk = 4	nk = 5
R^2	0.0139	0.0149	0.00776	0.0124
mean absolute error	28.3594	42.9139	44.09937	39.8266
median abs. error	22.8301	35.5441	38.85302	32.6386

10-fold cross-validated:

Statistic	nk = 0	nk = 3	nk = 4	nk = 5
R^2	0.0214	0.0180	0.01517	0.0191
mean absolute error	145.7176	43.5007	45.02428	44.2456
median abs. error	141.4238	36.4102	38.88053	37.3141

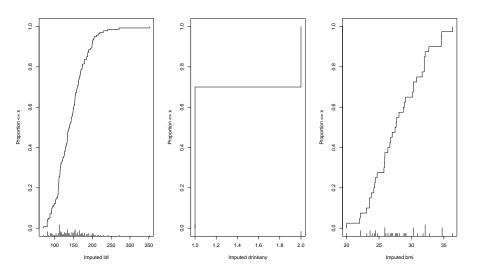
fit3 Imputation Results (4 of 4)

```
Variable being imputed: drinkany  nk=0 \quad nk=3 \quad nk=4 \quad nk=5 \\ Bootstrap \quad R^2 \qquad 0.0163 \quad 0.0113 \quad 0.0102 \quad 0.00986 \\ 10-fold \quad cv \quad R^2 \qquad 0.0205 \quad 0.0249 \quad 0.0163 \quad 0.01358 \\ Bootstrap \quad mean \mid error \mid \quad 0.4470 \quad 0.4568 \quad 0.4558 \quad 0.46624 \\ 10-fold \quad cv \quad mean \mid error \mid \quad 0.4450 \quad 0.4454 \quad 0.4476 \quad 0.44676 \\ Bootstrap \quad median \mid error \mid \quad 0.0000 \quad 0.0000 \quad 0.0000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.1000 \quad 0.00000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0500 \quad 0.0000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0000 \quad 0.0000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0000 \quad 0.0000 \quad 0.0000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0000 \quad 0.0000 \quad 0.0000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0000 \quad 0.0000 \quad 0.0000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0000 \quad 0.0000 \quad 0.0000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0000 \quad 0.0000 \quad 0.0000 \\ 10-fold \quad cv \quad median \mid error \mid \quad 0.0000 \quad 0.0000 \quad 0.0000 \quad 0.0000
```

Variable being imputed: bmi

nk=0	nk=3	nk=4	nk=5
0.0845	0.0932	0.0946	0.0847
0.0864	0.0903	0.0968	0.0899
3.7829	4.8119	4.9226	5.1775
27.6776	4.8359	4.9390	5.1136
2.9955	3.9704	3.9371	4.2634
27.0143	3.9894	3.9431	4.1876
	0.0845 0.0864 3.7829 27.6776 2.9955	0.0845 0.0932 0.0864 0.0903 3.7829 4.8119 27.6776 4.8359 2.9955 3.9704	nk=0 nk=3 nk=4 0.0845 0.0932 0.0946 0.0864 0.0903 0.0968 3.7829 4.8119 4.9226 27.6776 4.8359 4.9390 2.9955 3.9704 3.9371 27.0143 3.9894 3.9431

A plot of the imputed values... (results)



A plot of the imputed values... (code)

```
par(mfrow = c(1,3))
plot(fit3)
par(mfrow = c(1,1))
```

- For ldl, we imputed most of the 7 missing subjects in most of the 20 imputation runs to values within a range of around 120 through 200, but occasionally, we imputed values that were substantially lower than 100.
- For drinkany we imputed about 70% no and 30% yes.
- For bmi, we imputed values ranging from about 23 to 27 in many cases, and up near 40 in other cases.
- This method never imputes a value for a variable that doesn't already exist in the data.

Kitchen Sink Model (Main Effects only)

```
Factor d.f. Partial SS MS F P
                9330.911 9330.911 6.93 0.0085
age
smoking
       1
               8199.755 8199.755 6.09 0.0137
        1 6444.424 6444.424 4.79 0.0288
drinkany
       1 9274.287 9274.287 6.89 0.0087
sbp
        4 10874.528 2718.632 2.02 0.0891
physact
           1 15876.957 15876.957 11.80 0.0006
hmi
REGRESSION
           9
               60077.708 6675.301 4.96 < .0001
ERROR
         2022 2721037.890 1345.716
```

Analysis of Variance

Response: 1d1

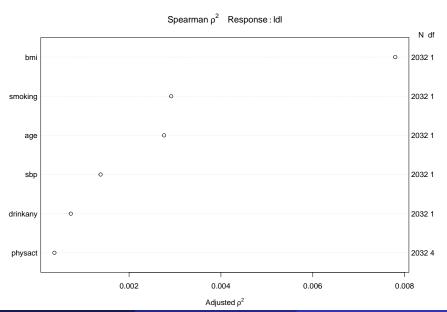
Spearman ρ^2 **Plot**

How should we prioritize the degrees of freedom we spend on non-linearity?

Plot's on the next page.

• Note the use of the simple imputation hers2 data here. Why?

Spearman ρ^2 **Plot** Result



Spending Degrees of Freedom

We're spending 9 degrees of freedom in our kitchen sink model. (We can verify this with anova or the plot.)

- Each quantitative main effect costs 1 df to estimate
- Each binary categorical variable also costs 1 df
- Multi-categorical variables with L levels cost L-1 df to estimate

Suppose we're willing to spend up to a total of ${\bf 14}$ degrees of freedom (i.e. a combined 5 more on interaction terms and other ways to capture non-linearity.)

What should we choose?

What did we see in the Spearman ρ^2 Plot?

Group 1 (largest adjusted ρ^2)

• bmi, a quantitative predictor, is furthest to the right

Group 2 (next largest)

- smoking, a binary predictor, is next, followed closely by
- age, a quantitative predictor

Other predictors (rest of the group)

- sbp, quantitative
- drinkany, binary
- physact, multi-categorical (5 levels)

Impact of Adding Non-Linear Terms on Spent DF

What happens when we add a non-linear term?

- Adding a polynomial of degree D costs D degrees of freedom.
 - So a polynomial of degree 2 (quadratic) costs 2 df, or 1 more than the main effect alone.
- Adding a restricted cubic spline with K knots costs K-1 df.
 - So adding a spline with 4 knots uses 3 df, or 2 more than the main effect.
 - We restrict ourselves to considering splines with 3, 4, or 5 knots.
- Adding an interaction (product term) depends on the main effects of the predictors we are interacting
 - If the product term's predictors have df1 and df2 degrees of freedom, product term adds df1 \times df2 degrees of freedom.
 - An interaction of a binary and quantitative variable adds $1 \times 1 = 1$ additional degree of freedom to the main effects model.
 - When we use a quantitative variable in a spline and interaction, we'll do the interaction on the main effect, not the spline.

Model we'll fit with ols

Fitting a model to predict 1d1 using

- bmi with a restricted cubic spline, 5 knots
- age with a quadratic polynomial
- sbp as a linear term
- drinkany indicator
- physact factor
- smoking indicator and its interaction with the main effect of bmi

We can fit this to the data

- restricted to complete cases (hers1, effectively)
- after simple imputation (hers2)
- after our multiple imputation (fit3)

Using only the Complete Cases

Fitting the model to the complete cases

where %ia% identifies the linear interaction alone.

m1 results (screen 1/2)

m1

```
Frequencies of Missing Values Due to Each Variable
                                                  smokina
    1d1
            bmi
                     age
                             sbp drinkany physact
                      0
                               0
Linear Regression Model
ols(formula = ldl \sim rcs(bmi, 5) + pol(age, 2) + sbp + drinkany +
    physact + smoking + smoking %ia% bmi, data = hers1, x = TRUE,
    y = TRUE)
                Model Likelihood
                                  Discrimination
                      Ratio Test
                                         Indexes
        2021
               LR chi2 52.61
Obs
                                  R2
                                     0.026
sigma36.7430 d.f.
                             14
                                   R2 adi 0.019
d.f.
        2006
               Pr(> chi2) 0.0000
                                   a
                                         6.629
Residuals
     Min
           10
                   Median
                               3Q
                                      Max
 -113.440 -24.519 -3.778
                           20.940 197.087
```

m1 results (screen 2/2)

m 1

```
Coef S.E. t
                                                 Pr(>|t|)
                           121.6057 68.2000 1.78 0.0747
Intercept
bmi
                             1.5687 1.0107 1.55 0.1208
bmi'
                            -8.6685 9.1577 -0.95 0.3440
bmi''
                            40.5712 37.4468 1.08 0.2787
bmi'''
                           -55.8872 44.5946 -1.25 0.2103
                            -0.5791 1.9657 -0.29 0.7683
age
age^2
                             0.0018 0.0149 0.12 0.9024
sbp
                             0.1221
                                     0.0453 2.69 0.0072
drinkany=yes
                            -3.7427 1.6629 -2.25 0.0245
physact=much less active -4.5660 3.8904 -1.17 0.2407
physact=much more active
                            -0.3291 2.7521 -0.12 0.9048
physact=somewhat less active
                            -0.0160 2.5270 -0.01 0.9950
physact=somewhat more active
                           3.7731 2.0293 1.86 0.0631
smoking=yes
                            -7.0832 12.0586 -0.59 0.5570
smoking=yes * bmi
                             0.4961
                                     0.4391 1.13 0.2587
```

Fit Model after Single Imputation

Fitting the model after simple imputation

where, again, %ia% identifies the linear interaction alone.

m2 results (screen 1/2)

m2

```
Linear Regression Model
 ols(formula = 1d1 \sim rcs(bmi, 5) + pol(age, 2) + sbp + drinkany +
    physact + smoking + smoking %ia% bmi. data = hers2. x = TRUE.
    y = TRUE
                Model Likelihood
                                  Discrimination
                                        Indexes
                     Ratio Test
Obs
       2032
              LR chi2 53.14
                                  R2
                                          0.026
sigma36.6503 d.f.
                                  R2 adj 0.019
                            14
 d.f. 2017
               Pr(> chi2) 0.0000
                                          6.631
                                  g
 Residuals
          10 Median
     Min
                              30
                                     Max
 -113.379 -24.326
                  -3.835 20.832 197.097
```

m2 results (screen 2/2)

m2

```
Coef S.E. t
                                                  Pr(>|t|)
                            120.2662 67.6113 1.78 0.0754
Intercept
bmi
                              1.5508 1.0071 1.54 0.1237
bmi'
                             -8.4486 9.0978 -0.93 0.3532
bmi''
                             39.6413 37.1378 1.07 0.2859
bmi'''
                            -54.8924 44.2677 -1.24 0.2151
                             -0.5249 1.9490 -0.27 0.7877
age
age^2
                              0.0014 0.0148
                                             0.10 0.9233
sbp
                              0.1209 0.0451 2.68 0.0074
drinkany=yes
                             -3.7023 1.6544 -2.24 0.0253
physact=much less active
                             -4.7408 3.8621 -1.23 0.2198
physact=much more active
                             -0.2635 2.7391 -0.10 0.9234
physact=somewhat less active 0.0130 2.5101
                                             0.01 0.9959
physact=somewhat more active 3.8031 2.0193 1.88 0.0598
smoking=yes
                             -6.8961 12.0196 -0.57 0.5662
smoking=yes * bmi
                              0.4892
                                      0.4375 1.12 0.2636
```

ANOVA results for m2 from ols

anova(m2)

```
Analysis of Variance
                                             Response: 1d1
Factor
                                             d.f. Partial SS
                                                                MS
     (Factor+Higher Order Factors)
                                                 5 2.758824e+04 5517.64861 4.11 0.0010
 All Interactions
                                                 1 1.679813e+03 1679.81344 1.25 0.2636
 Nonlinear
                                                  9.735452e+03 3245.15068 2.42 0.0647
                                                    .175762e+03 4587.88077
age
Nonlinear
                                                 1 1.244351e+01
                                                                  12.44351 0.01 0.9233
sbp
                                                 1 9.657476e+03 9657.47569 7.19 0.0074
drinkany
                                                 1 6.726918e+03 6726.91809 5.01 0.0253
                                                4 9.709992e+03 2427.49791 1.81 0.1247
physact
smoking (Factor+Higher Order Factors)
                                                 2 1.085405e+04 5427.02463 4.04 0.0177
 All Interactions
                                                 1 1.679813e+03 1679.81344 1.25 0.2636
smoking * bmi (Factor+Higher Order Factors)
                                                 1 1.679813e+03 1679.81344 1.25 0.2636
TOTAL NONLINEAR
                                                 4 9.738807e+03 2434.70175 1.81 0.1237
TOTAL NONLINEAR + INTERACTION
                                                    .171134e+04 2342.26845 1.74 0.1214
REGRESSION
                                               14 7.178905e+04 5127.78931 3.82 <.0001
ERROR
                                             2017 2.709327e+06 1343.24569
```

Validation of summary statistics

set.seed(432); validate(m2)

```
index.orig
                    training
                                  test optimism index.corrected
R-square
             0.0258
                      0.0307
                                0.0182
                                        0.0125
                                                       0.0133 40
MSE
          1333.3300 1323.5182 1343.7711 -20.2529
                                                    1353.5829 40
             6.6306 7.1676
                                5.8338
                                        1.3338
                                                       5.2968 40
             0.0000
                      0.0000
                               26.5316 -26.5316
                                                      26.5316 40
Intercept
Slope
            1.0000 1.0000
                                0.8174
                                        0.1826
                                                       0.8174 40
```

summary(m2) results

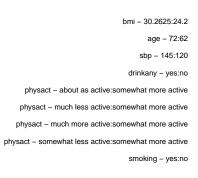
summary(m2)

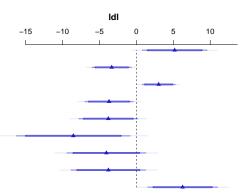
```
Effects
                                  Response : 1d1
Factor
                                                            Hiah
                                                                                            Lower 0.95 Upper 0.95
bmi
                                                                     6.0625
                                                                                               0.82921
                                                                                                         9.54330
                                                                                             -5.97890
age
                                                             72.000 10.0000 -3.3412 1.3450
                                                                                                        -0.70357
                                                      120.0 145.000 25.0000
sbp
                                                                              3.0218 1.1270
                                                                                              0.81165
                                                                                                         5 23190
drinkany - yes:no
                                                        1.0
                                                              2.000
                                                                          NA -3.7023 1.6544
                                                                                             -6.94690
                                                                                                        -0.45779
physact - about as active:somewhat more active
                                                              1.000
                                                                                             -7.76310
                                                        5.0
                                                                                                         0.15695
physact - much less active:somewhat more active
                                                              2.000
                                                                          NA -8.5439 3.9035 -16.19900
                                                                                                        -0.88862
physact - much more active:somewhat more active
                                                        5.0
                                                              3.000
                                                                                             -9.38630
                                                                                                         1.25310
physact - somewhat less active:somewhat more active
                                                        5.0
                                                              4.000
                                                                          NA -3.7901 2.5633
                                                                                             -8.81720
                                                                                                         1.23690
smoking - yes:no
                                                              2.000
                                                                              6.2635 2.4009
                                                                                                        10.97200
                                                        1.0
                                                                                               1.55500
Adiusted to: bmi=26.9 smokina=no
```

• Of course, these should really be plotted...

Effect Size Plot for m2

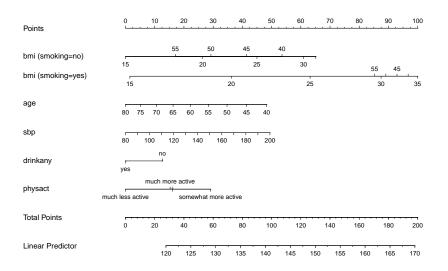
plot(summary(m2))





Adjusted to:bmi=26.9 smoking=no

Nomogram for m2



Making Predictions for an Individual

Suppose now that we want to use R to get a prediction for a new individual subject with bmi = 30, age = 50, smoking = yes and physact = about as active, drinkany= yes and sbp of 150.

```
$linear.predictors $lower $upper
160.9399 88.48615 233.3936
```

Making Predictions for a Long-Run Mean

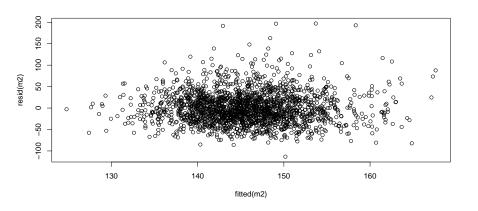
The other kind of prediction we might wish to make is for the mean of a series of subjects whose bmi = 30, age = 50, smoking = yes and physact = about as active, drinkany= yes and sbp of 150.

```
$linear.predictors $lower $upper
160.9399 151.8119 170.0679
```

Of course, the confidence interval will always be narrower than the prediction interval given the same predictor values.

Residuals vs. Fitted Values?

```
plot(resid(m2) ~ fitted(m2))
```



Influential Points?

```
which.influence(m2, cutoff = 0.4)
$Intercept
[1] 1135
$age
[1] 1135
$smoking
[1] 132
$`smoking * bmi`
[1] 132
```

Using Multiple Imputation

Fitting the Model using Multiple Imputation

What do we have now?

• An imputation model fit3

• A prediction model (from m1 or m2)

Now we put them together with the fit.mult.impute function...

Linear Regression & Imputation Model

- When you run this without the pr = FALSE it generates considerable output related to the imputations, which we won't use today.
- Let's look at the rest of the output this yields. . .

m3imp results (screen 1/2)

m3imp

```
Linear Regression Model
fit.mult.impute(formula = ldl ~ rcs(bmi, 5) + pol(age, 2) + sbp +
    drinkany + physact + smoking + smoking %ia% bmi, fitter = ols.
    xtrans = fit3, data = hers1, pr = FALSE)
               Model Likelihood
                                 Discrimination
                     Ratio Test
                                       Indexes
Obs
       2032 LR chi2 52.74
                                         0.026
                                 R2
sigma36.7331 d.f. 14
                                 R2 adi 0.019
 d.f. 2017
              Pr(> chi2) 0.0000
                                   6.621
                                 а
Residuals
             10 Median
     Min
                              30
                                     Max
 -113.345 -24.510 -3.803
                          20.777 197.295
```

m3imp results (screen 2/2)

m3imp

```
Coef
                                     S.E.
                                                  Pr(>|t|)
                            119.8951 67.8409 1.77 0.0773
Intercept
bmi
                              1.5436 1.0097 1.53 0.1265
bmi'
                             -8.3664 9.1409 -0.92 0.3602
bmi''
                             39.2149 37.3458 1.05 0.2938
bmi'''
                            -54.2873 44.5323 -1.22 0.2230
                             -0.5002 1.9555 -0.26 0.7981
age
                              0.0012 0.0148 0.08 0.9351
age^2
sbp
                              0.1198 0.0454 2.64 0.0083
drinkany=yes
                             -3.7196 1.6613 -2.24 0.0253
physact=much less active
                        -4.7109 3.8716 -1.22 0.2238
physact=much more active
                         -0.2328 2.7512 -0.08 0.9326
physact=somewhat less active -0.0417 2.5246 -0.02 0.9868
physact=somewhat more active 3.8197 2.0286 1.88 0.0599
smoking=yes
                             -6.8967 12.0503 -0.57 0.5672
smoking=yes * bmi
                              0.4866
                                      0.4389 1.11 0.2677
```

ANOVA results for m3imp

anova(m3imp)

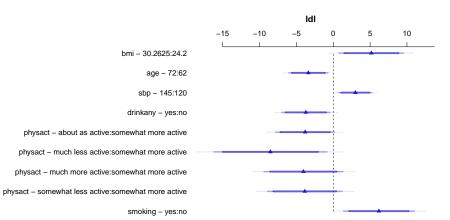
```
Analysis of Variance
                                             Response: 1d1
Factor
                                             d.f. Partial SS
     (Factor+Higher Order Factors)
                                                5 2.728300e+04 5456.600791 4.04 0.0012
 All Interactions
                                                1 1.658459e+03 1658.458931 1.23 0.2677
 3 9.585703e+03 3195.234412 2.37 0.0690
                                                2 9.320445e+03 4660.222299 3.45 0.0318
age
 1 8.950493e+00
                                                                  8.950493 0.01 0.9351
sbp
                                                1 9.407603e+03 9407.602954 6.97 0.0083
drinkanv
                                                1 6.763854e+03 6763.853503 5.01 0.0253
physact
                                                4 9.698175e+03 2424.543639 1.80 0.1268
        (Factor+Higher Order Factors)
smokina
                                                2 1.031090e+04 5155.452328 3.82 0.0221
 All Interactions
                                                1 1.658459e+03 1658.458931 1.23 0.2677
              (Factor+Higher Order Factors)
smoking * bmi
                                                1 1.658459e+03 1658.458931 1.23 0.2677
TOTAL NONLINEAR
                                                    .587178e+03 2396.794504 1.78 0.1309
TOTAL NONLINEAR + INTERACTION
                                                    152744e+04 2305.487432 1.71 0.1293
REGRESSTON
                                               14 7.030149e+04 5021.535034 3.72 <.0001
                                             2017 2.721574e+06 1349.317884
ERROR
```

Summary of Effect Estimates for m3imp

summary(m3imp)

```
Effects
                                  Response : 1d1
 Factor
                                                                            Effect S.E.
                                                                                           Lower 0.95 Upper 0.95
 bmi
                                                             30.263
                                                                    6.0625
                                                                             5.1643 2.2300
                                                                                             0.79099
                                                                                                        9.53750
 age
                                                             72.000 10.0000 -3.3824 1.3518
                                                                                            -6.03340
                                                                                                      -0.73144
 sbp
                                                      120.0 145.000 25.0000
                                                                            2.9955 1.1345
                                                                                             0.77068
                                                                                                        5.22040
drinkany - yes:no
                                                       1.0
                                                              2.000
                                                                         NA -3.7196 1.6613
                                                                                            -6.97780
                                                                                                      -0.46150
physact - about as active:somewhat more active
                                                       5.0
                                                             1.000
                                                                         NA -3.8197 2.0286
                                                                                            -7.79800
                                                                                                       0.15861
physact - much less active:somewhat more active
                                                       5.0
                                                             2.000
                                                                         NA -8.5306 3.9152 -16.20900
                                                                                                      -0.85228
physact - much more active:somewhat more active
                                                       5.0
                                                             3.000
                                                                         NA -4.0525 2.7260
                                                                                            -9.39850
                                                                                                       1.29350
physact - somewhat less active:somewhat more active
                                                       5.0
                                                             4.000
                                                                         NA -3.8614 2.5796
                                                                                            -8.92030
                                                                                                       1.19760
smoking - yes:no
                                                                            6.1923 2.4427
                                                       1.0
                                                             2.000
                                                                                             1.40190
                                                                                                      10.98300
Adjusted to: bmi=26.9 smoking=no
```

plot(summary(m3imp))

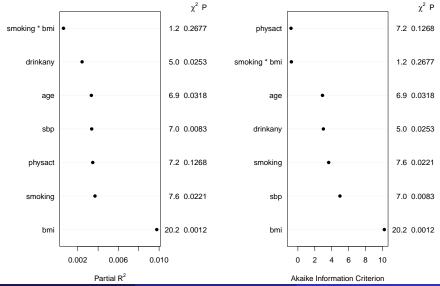


Adjusted to:bmi=26.9 smoking=no

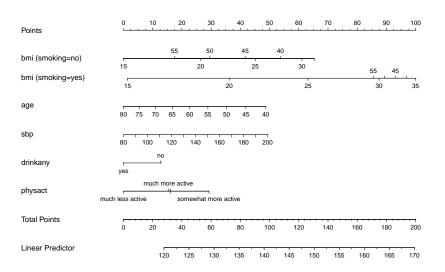
Evaluation via Partial R² and AIC (code)

```
par(mfrow = c(1,2))
plot(anova(m3imp), what="partial R2")
plot(anova(m3imp), what="aic")
par(mfrow = c(1,1))
```

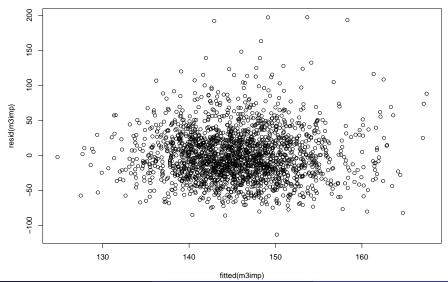
Evaluation via Partial R² and AIC (result)



plot(nomogram(m3imp))



plot(resid(m3imp) ~ fitted(m3imp))



Other Things | Might Need after aregImpute?

How can I estimate the AIC (and BIC) of a model fit with fit.mult.impute?

glance won't work with an ols fit, but we can just use...

```
AIC(m3imp)
```

d.f.

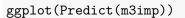
20425.29

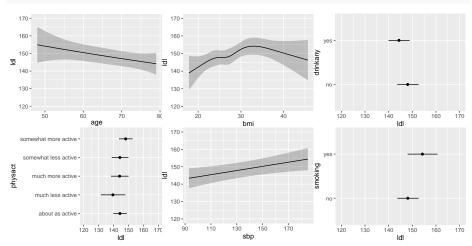
BIC(m3imp)

d.f.

20515.16

Can I run ggplot(Predict())?





Pull out one imputation from aregImpute?

• How can I pull a single one (say, the fifth) of the imputations from aregImpute out?

Remember that fit3 was our imputation model here, build on the hers1 data, which keeps its subject identifiers in the subject column.

We'll show the result on the next slide.

Our fifth_imp tibble

fifth_imp

```
# A tibble: 2,032 x 8
  subject ldl age smoking drinkany sbp physact bmi
    <int> <dbl> <int> <fct>
                              <int> <int> <fct>
                                                  <dbl>
          122.
                  70 no
                                      138 much mo~ 23.7
        2 242. 62 no
                                      118 much le~ 28.6
3
        4 116.
                  64 yes
                                      152 much le~ 24.4
        5
          151. 65 no
                                      175 somewha~ 21.9
5
        6 138. 68 no
                                      174 about a~ 29.0
6
        8 121.
                                      178 much mo~ 23.2
               69 no
        9
          133
                  61 no
                                      162 about a~ 30.3
8
       10 220
                  62 yes
                                  2
                                      111 somewha~ 45.7
       11 173.
               72 no
                                      122 about a~ 22.2
10
       12
          124.
               73 no
                                      158 somewha~ 25.3
# ... with 2,022 more rows
```

Create Residual Plots for this imputation?

We can look at this model with glance or tidy to see that it gives similar results to what we see across the multiple imputations.

```
broom::glance(model_for_resid_plots) %>%
  select(r.squared, AIC, BIC, nobs, df, df.residual) %>%
  kable(digits = 3)
```

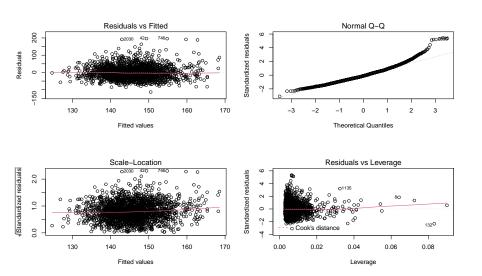
r.squared	AIC	BIC	nobs	df	df.residual
0.027	20451.36	20541.23	2032	14	2017

What else can we do?

We can plot residuals for the model fit to this single imputation, as shown on the next slide.

```
par(mfrow = c(2,2))
plot(model_for_resid_plots)
par(mfrow = c(1,1))
```

Residual Plots for Fifth Imputation



Next Step

Can we do all of this for a logistic regression model?