

432 Class 06 Slides

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Moving Forward

- Logistic Regression Models and the `smart3_sh` data

Setup

```
library(here); library(magrittr)
library(janitor); library(knitr)
library(patchwork); library(broom)
library(equatiomatic); library(simputation)
library(naniar)
library(rsample); library(yardstick)
library(tidyverse)

theme_set(theme_bw())
```

smart3 Variables, by Type

Variable	Type	Description
landline	Binary (1/0)	survey conducted by landline? (vs. cell)
healthplan	Binary (1/0)	subject has health insurance?
age_imp	Quantitative	age (imputed from groups - see Notes)
fruit_day	Quantitative	mean servings of fruit / day
drinks_wk	Quantitative	mean alcoholic drinks / week
bmi	Quantitative	body-mass index (in kg/m ²)
physhealth	Count (0-30)	of last 30 days, # in poor physical health
dm_status	Categorical	diabetes status (4 levels, <i>we'll collapse to 2</i>)
activity	Categorical	physical activity level (4 levels, <i>we'll re-level</i>)
smoker	Categorical	smoking status (4 levels, <i>we'll collapse to 3</i>)
genhealth	Categorical	self-reported overall health (5 levels)

The smart3 data (built last time)

```
smart3_sh <- readRDS(here("data", "smart3_sh.Rds"))
```

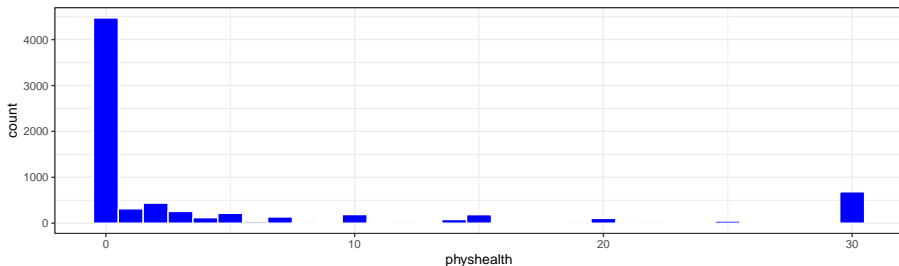
```
str(smart3_sh)
```

```
tibble [7,412 x 28] (S3: tbl_df/tbl/data.frame)
```

```
$ SEQNO      : chr [1:7412] "2017000001" "2017000002" "2017000003" ...
$ mmsa       : chr [1:7412] "Cincinnati" "Cincinnati" "Cincinnati" ...
$ mmsa_wt    : num [1:7412] 670 407 356 203 194 ...
$ landline   : int [1:7412] 1 1 1 1 1 1 1 1 1 1 ...
$ age_imp    : num [1:7412] 36 41 55 61 57 24 65 53 51 42 ...
$ healthplan : chr [1:7412] "1" "1" "1" "1" ...
$ dm_status  : Factor w/ 2 levels "Yes","No": 2 2 2 2 2 2 1 ...
$ fruit_day  : num [1:7412] 1.43 1 3 0.5 0.72 ...
$ drinks_wk : num [1:7412] 4.67 0 0 0 0.23 1.87 0 0 0.23 0 ...
$ activity   : Factor w/ 4 levels "Highly_Active",...: 2 2 1 ...
$ smoker     : Factor w/ 3 levels "Current","Former",...: 3 ...
$ physhealth : int [1:7412] 0 0 2 0 2 0 0 30 2 30 ...
```

Days (in last 30) of poor physical health

```
ggplot(smart3_sh, aes(x = physhealth)) +  
  geom_histogram(binwidth = 1,  
                 fill = "blue", col = "white")
```



```
smart3_sh %>% tabyl(physhealth > 0)
```

physhealth > 0	n	percent
FALSE	4472	0.6033459
TRUE	2940	0.3966541

Create day6 data: predicting $\Pr(\text{physhealth} > 0)$?

```
day6 <- smart3_sh %>%  
  mutate(sick = as.numeric(physhealth > 0),  
         id = as.character(  
           as.numeric(SEQNO)-2017000000)) %>%  
  select(id, sick, age = age_imp, dm_status, smoker,  
         bmi, physhealth)  
  
slice(day6, 17:19) # show rows 17-19
```

A tibble: 3 x 7

	id	sick	age	dm_status	smoker	bmi	physhealth
	<chr>	<dbl>	<dbl>	<fct>	<fct>	<dbl>	<int>
1	17	0	72	No	Former	31.4	0
2	18	1	82	No	Never	27.6	5
3	19	0	62	Yes	Current	27.5	0

Before fitting models, let's split our sample

```
set.seed(4322022)

day6_split <- initial_split(day6, prop = 0.7,
                             strata = smoker)

d6_train <- training(day6_split)
d6_test  <- testing(day6_split)
```

What does `strata = smoker` do?

Impact of strata = smoker in split

```
d6_train %>% tabyl(smoker)
```

smoker	n	percent
Current	933	0.1798728
Former	1443	0.2781955
Never	2811	0.5419318

```
d6_test %>% tabyl(smoker)
```

smoker	n	percent
Current	400	0.1797753
Former	619	0.2782022
Never	1206	0.5420225

The logistic regression model

$$\text{logit}(\text{event}) = \log \left(\frac{\text{Pr}(\text{event})}{1 - \text{Pr}(\text{event})} \right) = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \dots + \beta_k X_k$$

$$\text{odds}(\text{event}) = \frac{\text{Pr}(\text{event})}{1 - \text{Pr}(\text{event})}$$

$$\text{Pr}(\text{event}) = \frac{\text{odds}(\text{event})}{\text{odds}(\text{event}) + 1}$$

$$\text{Pr}(\text{event}) = \frac{\exp(\text{logit}(\text{event}))}{1 + \exp(\text{logit}(\text{event}))}$$

Model 1: predict sick from smoker and age

Fit the model with and without an interaction term?

```
mod1 <- glm(sick ~ age + smoker,  
            family = binomial(link = "logit"),  
            data = d6_train)
```

```
mod2 <- glm(sick ~ age * smoker,  
            family = binomial(link = "logit"),  
            data = d6_train)
```

- 1 Can we use the models to make predictions?
- 2 How should we interpret the model coefficients?
- 3 Can we compare the models based on in-sample performance?
- 4 How can we assess predictions using our test sample?

Model 1

```
extract_eq(mod1, wrap = TRUE, terms_per_line = 2,  
           operator_location = "start", use_coefs = TRUE,  
           coef_digits = 3)
```

$$\log \left[\frac{P(\widehat{\text{sick}} = 1)}{1 - P(\widehat{\text{sick}} = 1)} \right] = -0.322 + 0.005(\text{age}) \quad (1)$$
$$- 0.318(\text{smoker}_{\text{Former}}) - 0.51(\text{smoker}_{\text{Never}})$$

Likelihood Ratio Tests: Model 1

```
anova(mod1, test = "LRT")
```

Analysis of Deviance Table

Model: binomial, link: logit

Response: sick

Terms added sequentially (first to last)

	Df	Deviance	Resid. Df	Resid. Dev	Pr(>Chi)
NULL			5186	6964.6	
age	1	7.422	5185	6957.2	0.006442 **
smoker	2	45.045	5183	6912.1	1.654e-10 ***

Signif. codes:

0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Model 1

```
tidy(mod1, conf.int = TRUE, conf.level = 0.90) %>%  
  select(term, estimate, std.error, conf.low, conf.high, p.v  
  kable(dig = 3)
```

term	estimate	std.error	conf.low	conf.high	p.value
(Intercept)	-0.322	0.105	-0.494	-0.150	0.002
age	0.005	0.002	0.002	0.007	0.003
smokerFormer	-0.318	0.086	-0.460	-0.176	0.000
smokerNever	-0.510	0.077	-0.636	-0.384	0.000

Model 1 Predictions for subjects A-F

- $\text{logit}(\text{sick}) = -0.322 + 0.005 \text{ age} - 0.318 \text{ Former} - 0.510 \text{ Never}$

ID	age	smoker	logit(sick)	odds(sick)	Pr(sick)
A	33	Current	-0.157	0.8547	0.461
B	33	Former	-0.475	0.6219	0.383
C	33	Never	-0.667	0.5132	0.339
D	55	Current	-0.047	0.9541	0.488
E	55	Former	-0.365	0.6942	0.410
F	55	Never	-0.557	0.5729	0.364

Sample Calculation (for E):

- $\text{logit}(\text{sick}) = -0.322 + 0.005 (55) - 0.318 (1) - 0.510 (0) = -0.365$
- $\text{odds}(\text{sick}) = \exp(-0.365) = 0.6942$
- $\text{Prob}(\text{sick}) = 0.6942 / (1 + 0.6942) = 0.410$

Model 1 (coefficients exponentiated)

```
tidy(mod1, exponentiate = TRUE, conf.int = TRUE,  
      conf.level = 0.90) %>%  
  select(term, estimate,  
          lo90 = conf.low, hi90 = conf.high) %>%  
  kable(dig = 3)
```

term	estimate	lo90	hi90
(Intercept)	0.725	0.610	0.861
age	1.005	1.002	1.007
smokerFormer	0.728	0.631	0.839
smokerNever	0.601	0.529	0.681

- So what can we conclude about, for instance, the effect of Never smoking (as compared to Current smoking)?

Model 1 (coefficients exponentiated)

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tidy(mod1, exponentiate = TRUE, conf.int = TRUE,  
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- So what can we conclude about, for instance, the effect of Never smoking (as compared to Current smoking)?
- Suppose Chloe and Nancy are the same age, where Nancy never smoked and Chloe is a current smoker.

Model 1 (Chloe and Nancy)

term	estimate	lo90	hi90
(Intercept)	0.725	0.610	0.861
age	1.005	1.002	1.007
smokerFormer	0.728	0.631	0.839
smokerNever	0.601	0.529	0.681

- Chloe and Nancy are the same age; Nancy never smoked and Chloe smokes currently. What can we conclude about the relative odds for Nancy of a sick day as compared to Chloe?

Model 1 (Chloe and Nancy)

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(Intercept)	0.725	0.610	0.861
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smokerNever	0.601	0.529	0.681

- Chloe and Nancy are the same age; Nancy never smoked and Chloe smokes currently. What can we conclude about the relative odds for Nancy of a sick day as compared to Chloe?
- Nancy's odds of at least one sick day in the past 30 are 60.1% of Chloe's odds.

Model 1 (Chloe and Nancy)

term	estimate	lo90	hi90
(Intercept)	0.725	0.610	0.861
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- Chloe and Nancy are the same age; Nancy never smoked and Chloe smokes currently. What can we conclude about the relative odds for Nancy of a sick day as compared to Chloe?
- Nancy's odds of at least one sick day in the past 30 are 60.1% of Chloe's odds.
- 90% CI for this odds ratio is (0.529, 0.681).

Model 1 (Chloe and Nancy)

term	estimate	lo90	hi90
(Intercept)	0.725	0.610	0.861
age	1.005	1.002	1.007
smokerFormer	0.728	0.631	0.839
smokerNever	0.601	0.529	0.681

- Chloe and Nancy are the same age; Nancy never smoked and Chloe smokes currently. What can we conclude about the relative odds for Nancy of a sick day as compared to Chloe?
- Nancy's odds of at least one sick day in the past 30 are 60.1% of Chloe's odds.
- 90% CI for this odds ratio is (0.529, 0.681).
- Chloe's odds of a sick day are ($1/0.601 = 1.664$) times those of Nancy.

Does this match the predictions we made?

- Suppose both Chloe and Nancy are 33 years old.
- We saw that Nancy's odds(sick) should be 0.601 times Chloe's odds(sick) .

ID	age	smoker	logit(sick)	odds(sick)	Pr(sick)
Chloe	33	Current	-0.157	0.8547	0.461
Nancy	33	Never	-0.667	0.5132	0.339

- and we have $0.5132 / 0.8547 = 0.600$ for the ratio of Nancy's odds to Chloe's odds
- and Chloe's odds are $0.8547 / 0.5132 = 1.665$ times those of Nancy.
- These discrepancies are just due to rounding error in my table.

Model 1 results from glance

- We'll have some additional measures of fit quality, in time.
- Deviance = $-2(\log \text{Likelihood})$

```
glance(mod1) %>%  
  select(nobs, df.null, null.deviance,  
         deviance, df.residual) %>%  
  kable(dig = 1)
```

nobs	df.null	null.deviance	deviance	df.residual
5187	5186	6964.6	6912.1	5183

```
glance(mod1) %>%  
  select(nobs, logLik, AIC, BIC) %>%  
  kable(dig = 1)
```

nobs	logLik	AIC	BIC
5187	3456.1	6920.1	6946.4

Model 2

```
extract_eq(mod2, wrap = TRUE, terms_per_line = 1,  
           operator_location = "start", use_coefs = TRUE,  
           coef_digits = 3)
```

$$\log \left[\frac{P(\widehat{\text{sick}} = 1)}{1 - P(\widehat{\text{sick}} = 1)} \right] = -0.188$$
$$\begin{aligned} &+ 0.002(\text{age}) \\ &- 0.563(\text{smoker}_{\text{Former}}) \\ &- 0.642(\text{smoker}_{\text{Never}}) \\ &+ 0.004(\text{age} \times \text{smoker}_{\text{Former}}) \\ &+ 0.003(\text{age} \times \text{smoker}_{\text{Never}}) \end{aligned} \tag{2}$$

Likelihood Ratio Tests: Model 2

```
anova(mod2, test = "LRT")
```

Analysis of Deviance Table

Model: binomial, link: logit

Response: sick

Terms added sequentially (first to last)

	Df	Deviance	Resid. Df	Resid. Dev	Pr(>Chi)	
NULL			5186	6964.6		
age	1	7.422	5185	6957.2	0.006442	**
smoker	2	45.045	5183	6912.1	1.654e-10	***
age:smoker	2	0.733	5181	6911.4	0.693211	

Signif. codes:

Model 2

```
tidy(mod2, conf.int = TRUE, conf.level = 0.90) %>%  
  select(term, estimate, std.error, conf.low, conf.high, p.v  
  kable(dig = 3)
```

term	estimate	std.error	conf.low	conf.high	p.value
(Intercept)	-0.188	0.214	-0.542	0.164	0.380
age	0.002	0.004	-0.005	0.009	0.608
smokerFormer	-0.563	0.300	-1.057	-0.070	0.060
smokerNever	-0.642	0.245	-1.046	-0.238	0.009
age:smokerFormer	0.004	0.005	-0.004	0.013	0.392
age:smokerNever	0.003	0.004	-0.005	0.010	0.564

- $\text{logit}(\text{sick}) = -0.188 + 0.002 \text{ age} - 0.563 \text{ Former} - 0.642 \text{ Never} + 0.004 \text{ age*Former} + 0.003 \text{ age*Never}$

Model 2 predictions for subjects A-F

- $\text{logit}(\text{sick}) = -0.188 + 0.002 \text{ age} - 0.563 \text{ Former} - 0.642 \text{ Never} + 0.004 \text{ age*Former} + 0.003 \text{ age*Never}$

ID	age	smoker	logit(sick)	odds(sick)	Pr(sick)
A	33	Current	-0.122	0.8851	0.470
B	33	Former	-0.553	0.5752	0.365
C	33	Never	-0.665	0.5143	0.340
D	55	Current	-0.078	0.9250	0.481
E	55	Former	-0.421	0.6564	0.396
F	55	Never	-0.555	0.5741	0.365

- Subject E: $\text{logit}(\text{sick}) = -0.188 + 0.002 (55) - 0.563 (1) - 0.642 (0) + 0.004(55)(1) + 0.003(55)(0) = -0.421$
- $\text{odds}(\text{sick}) = \exp(-0.421) = 0.6564$ so
- $\text{Prob}(\text{sick}) = 0.6564 / (1 + 0.6564) = 0.396$ for subject E.

Model 2 (coefficients exponentiated)

```
tidy(mod2, exponentiate = TRUE, conf.int = TRUE,  
      conf.level = 0.90) %>%  
  select(term, estimate,  
          lo90 = conf.low, hi90 = conf.high) %>%  
  kable(dig = 3)
```

term	estimate	lo90	hi90
(Intercept)	0.828	0.582	1.178
age	1.002	0.995	1.009
smokerFormer	0.570	0.348	0.932
smokerNever	0.526	0.351	0.788
age:smokerFormer	1.004	0.996	1.013
age:smokerNever	1.003	0.995	1.010

Model 2 (Chloe and Nancy)

term	estimate	lo90	hi90
(Intercept)	0.828	0.582	1.178
age	1.002	0.995	1.009
smokerFormer	0.570	0.348	0.932
smokerNever	0.526	0.351	0.788
age:smokerFormer	1.004	0.996	1.013
age:smokerNever	1.003	0.995	1.010

- Chloe and Nancy are the same age; Nancy never smoked and Chloe smokes currently. What can we conclude about the relative odds for Nancy of a sick day as compared to Chloe?

Model 2 (Chloe and Nancy)

term	estimate	lo90	hi90
(Intercept)	0.828	0.582	1.178
age	1.002	0.995	1.009
smokerFormer	0.570	0.348	0.932
smokerNever	0.526	0.351	0.788
age:smokerFormer	1.004	0.996	1.013
age:smokerNever	1.003	0.995	1.010

- Chloe and Nancy are the same age; Nancy never smoked and Chloe smokes currently. What can we conclude about the relative odds for Nancy of a sick day as compared to Chloe?
- We cannot conclude anything **unless** we know what age Chloe and Nancy are, since the effect of smoking depends on age.

Model 2 (Chloe and Nancy)

If Chloe (current smoker) and Nancy (never smoker) are each 33, then ...

ID	age	smoker	logit(sick)	odds(sick)	Pr(sick)
Chloe	33	Current	-0.122	0.8851	0.470
Nancy	33	Never	-0.665	0.5143	0.340

- Chloe's odds of being sick are $0.8851/0.5143 = 1.72$ times that of Nancy, **if** they are each 33 years old.
- If Chloe and Nancy are each 55, then from the table below, Chloe's odds are $0.9250 / 0.5741 = 1.61$ times Nancy's odds of being sick.

ID	age	smoker	logit(sick)	odds(sick)	Pr(sick)
D	55	Current	-0.078	0.9250	0.481
F	55	Never	-0.555	0.5741	0.365

Comparing Model 1 to Model 2 with AIC and BIC

```
bind_rows(glance(mod1) %>% select(nobs, AIC, BIC),  
          glance(mod2) %>% select(nobs, AIC, BIC)) %>%  
  mutate(mod = c("m1 (no int.)", "m2 (interaction)")) %>%  
  kable(digits = 1)
```

nobs	AIC	BIC	mod
5187	6920.1	6946.4	m1 (no int.)
5187	6923.4	6962.7	m2 (interaction)

- Which model looks like it performs better in the training sample?

Comparison with Mallows' C_p statistic?

```
anova(mod1, mod2, test = "Cp")
```

Analysis of Deviance Table

Model 1: sick ~ age + smoker

Model 2: sick ~ age * smoker

	Resid. Df	Resid. Dev	Df	Deviance	Cp
1	5183	6912.1			6920.1
2	5181	6911.4	2	0.73284	6923.4

- Same as what we got from glance for AIC in this case.

Can we compare the models with a Test?

```
anova(mod1, mod2, test = "LRT")
```

Analysis of Deviance Table

Model 1: sick ~ age + smoker

Model 2: sick ~ age * smoker

	Resid. Df	Resid. Dev	Df	Deviance	Pr(>Chi)
1	5183	6912.1			
2	5181	6911.4	2	0.73284	0.6932

Could also consider:

- Rao's efficient score test (test = "Rao")
- Pearson's chi-square test (test = "Chisq")

Let's get predicted probabilities in training sample

```
m1_aug <- augment(mod1, type.predict = "response")  
m2_aug <- augment(mod2, type.predict = "response")
```

The predicted probabilities are in the `.fitted` column.

```
m1_aug %>% select(age, smoker, sick, .fitted) %>% slice(1)
```

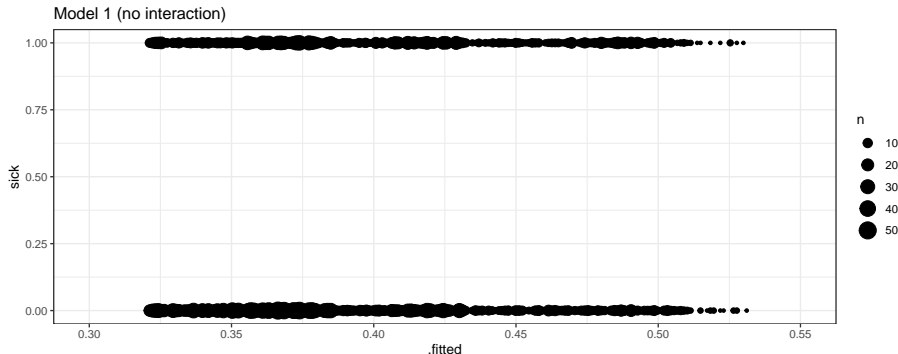
```
# A tibble: 1 x 4  
  age smoker    sick .fitted  
  <dbl> <fct>   <dbl>   <dbl>  
1    57 Current     1    0.486
```

```
m2_aug %>% select(age, smoker, sick, .fitted) %>% slice(1)
```

```
# A tibble: 1 x 4  
  age smoker    sick .fitted  
  <dbl> <fct>   <dbl>   <dbl>  
1    57 Current     1    0.482
```

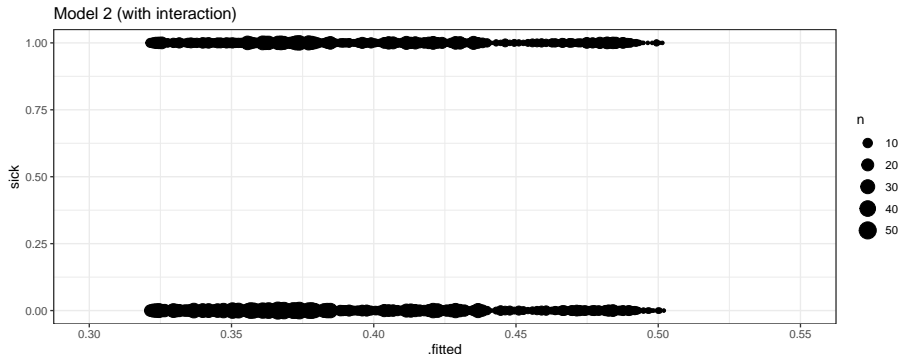
Observed (sick status) vs. Model 1 fitted $\Pr(\text{sick})$

```
ggplot(m1_aug, aes(x = .fitted, y = sick)) +  
  geom_count() + xlim(0.30, 0.55) +  
  labs(title = "Model 1 (no interaction)",  
       sub = "Training Data")
```



Observed (sick status) vs. Model 2 fitted $\Pr(\text{sick})$

```
ggplot(m2_aug, aes(x = .fitted, y = sick)) +  
  geom_count() + xlim(0.30, 0.55) +  
  labs(title = "Model 2 (with interaction)",  
       sub = "Training Data")
```



Making Classification Decisions

- Our outcome is `sick`, where `sick = 1` if `physact > 0`, otherwise `sick = 0`.
- We can establish a classification rule based on our model's predicted probabilities of `sick = 1`.
- 0.5 is a natural (but not inevitable) cut point.
 - if `.fitted` is below 0.50, we'll predict `sick = 0`
 - if `.fitted` is 0.50 or larger, we'll predict `sick = 1`.

```
m1_aug %>% table(.fitted >= 0.50, sick)
```

	sick	
	0	1
FALSE	3058	2005
TRUE	75	49

Standard Epidemiological Format

Confusion matrix for Model mod1 in the training sample.

```
confuse_m1 <- m1_aug %>%  
  mutate(sick_obs = factor(sick == "1"),  
         sick_pred = factor(.fitted >= 0.50),  
         sick_obs = fct_relevel(sick_obs, "TRUE"),  
         sick_pred = fct_relevel(sick_pred, "TRUE")) %$%  
  table(sick_pred, sick_obs)
```

```
confuse_m1
```

	sick_obs	
sick_pred	TRUE	FALSE
TRUE	49	75
FALSE	2005	3058

Terminology associated with the Confusion Matrix

```
confuse_m1
```

```
      sick_obs  
sick_pred TRUE FALSE  
   TRUE    49    75  
  FALSE 2005  3058
```

- Total Observations = $49 + 75 + 2005 + 3058 = 5187$
- Correct Predictions = $49 + 3058 = 3107$, or 59.9% accuracy
- Incorrect Predictions = $75 + 2005 = 2080$ (40.1%)
- Observed TRUE = $49 + 2005 = 2054$, or 39.6% prevalence
- Predicted TRUE = $49 + 75 = 124$, or 2.4% detection prevalence

Other Summaries from a Confusion Matrix

```
confuse_m1
```

```
      sick_obs  
sick_pred TRUE FALSE  
TRUE      49      75  
FALSE 2005  3058
```

- Sensitivity = $49 / (49 + 2005) = 2.4\%$ (also called Recall)
 - if the subject actually was sick, our model predicts that 2.4% of the time
- Specificity = $3058 / (3058 + 75) = 97.6\%$
 - if the subject was actually not sick, our model predicts that 97.6% of the time
- Positive Predictive Value (or Precision) = $49 / (49 + 75) = 39.5\%$
 - our predictions of sick were correct 39.5% of the time
- Negative Predictive Value = $3058 / (3058 + 2005) = 60.4\%$
 - our predictions of “not sick” were correct 60.4% of the time

Confusion Matrix for mod2 (training sample)

We can obtain a similar confusion matrix for model mod2 using the same (arbitrary) cutoff of `.fitted >= 0.5` to indicate sick.

```
confuse_m1
```

```
              sick_obs
sick_pred TRUE FALSE
      TRUE      49      75
      FALSE 2005   3058
```

```
confuse_m2
```

```
              sick_obs
sick_pred TRUE FALSE
      TRUE      2      3
      FALSE 2052   3130
```

Which of these confusion matrices looks better?

Get confusion matrix more easily?

Switch to a 0.45 cutoff...

```
m1_aug <- m1_aug %>%  
  mutate(obs = factor(sick),  
         pred = factor(ifelse(.fitted >= 0.45, 1, 0)))  
  
conf_mat(data = m1_aug, truth = obs, estimate = pred)
```

	Truth	
Prediction	0	1
0	2679	1642
1	454	412

Accuracy and Kappa Results for mod_1

```
metrics(data = m1_aug, truth = obs, estimate = pred) %>%  
  kable(digits = 6)
```

.metric	.estimator	.estimate
accuracy	binary	0.595913
kap	binary	0.061834

- Kappa = a correlation statistic from -1 to +1, with complete agreement +1 and complete disagreement -1.
- Kappa measures the inter-rater reliability of our predicted and true classifications.

Confusion Matrix for mod_2 with 0.45 cutoff

```
m2_aug <- m2_aug %>%  
  mutate(obs = factor(sick),  
         pred = factor(ifelse(.fitted >= 0.45, 1, 0)))  
  
conf_mat(data = m2_aug, truth = obs, estimate = pred)
```

	Truth	
Prediction	0	1
0	2582	1561
1	551	493

- $493 + 2582 = 3075$ accurate predictions (59.3% accuracy)
- Sensitivity = $493 / (493 + 1561) = 24.0\%$
 - for the people who were actually sick, we made correct predictions 24% of the time
- Specificity = $2582 / (2582 + 551) = 82.4\%$
 - for the people who weren't actually sick, we made correct predictions 82.4% of the time with this decision rule and model mod_2.

Holdout Sample?

```
mod1_aug_test <- augment(mod1, newdata = d6_test,  
                           type.predict = "response") %>%  
  mutate(obs = factor(sick),  
          pred = factor(ifelse(.fitted >= 0.45, 1, 0)))  
  
mod2_aug_test <- augment(mod2, newdata = d6_test,  
                           type.predict = "response") %>%  
  mutate(obs = factor(sick),  
          pred = factor(ifelse(.fitted >= 0.45, 1, 0)))
```

metrics for test sample, models 1 and 2

```
bind_cols(  
  metrics(data = mod1_aug_test,  
           truth = obs, estimate = pred) %>%  
    select(.metric, mod1 = .estimate),  
  metrics(data = mod2_aug_test,  
           truth = obs, estimate = pred) %>%  
    select(mod2 = .estimate)  
)
```

```
# A tibble: 2 x 3  
  .metric    mod1    mod2  
  <chr>      <dbl> <dbl>  
1 accuracy 0.609  0.604  
2 kap      0.0938 0.0979
```

What's Next?

Expanding our options with tidymodels and the Harrell-verse. . .

- Fitting linear and logistic regression models in new ways
- Evaluating the success of our models in new ways
- Incorporating imputation approaches more seamlessly

Please don't forget to submit your Project A proposal by Monday at 9 PM.