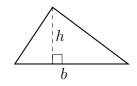
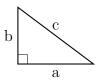


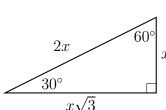
$$A = \ell w$$



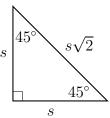
$$A = 1/2bh$$



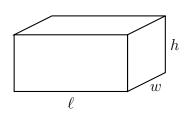
$$a^2 + b^2 = c^2$$







Special Right Triangles



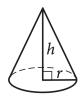
 $V = \ell w h$ 



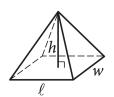
$$V = \pi r^2 h$$



$$V = \frac{4}{3}\pi r^3$$



$$V = \frac{1}{3}\pi r^2 h$$



$$V = \frac{1}{3} \ell wh$$

## Exponents/Roots/Logs

$$2^{-2} = \frac{1}{4}$$
  $2^{-1} = \frac{1}{2}$   $2^{0} = \frac{1}{1}$   $2^{1} = \frac{2}{1}$   $2^{2} = \frac{4}{1}$   $\sqrt{a} \times \sqrt{b} = \sqrt{ab}$ 

$$a = \sqrt[d]{b^c} \Rightarrow a = b^{c/d} \Rightarrow \sqrt[c]{d}a = b \Rightarrow \sqrt[c]{a^d} = b$$

$$i^0 = 1$$
  $i^1 = i$   $i^2 = -1$   $i^3 = -i$ 

$$\frac{x^a}{\frac{a}{a^b}} = x^{a-b} \qquad \qquad \mathbf{x}^a \times x^b = x^{a+b}$$

$$(x^a)^b = x^{ab} \qquad \qquad \ln(a)^r = r\ln(a)$$

$$\ln(a) - \ln(b) = \ln\left(\frac{a}{b}\right)$$
  $\ln(a) + \ln(b) = \ln(ab)$ 

$$ln(x) = log_e(x)$$
  $log_a b = c \Rightarrow a^c = b$ 

$$\log_x(x) = 1 \qquad \qquad \log_b(x) = \frac{\log_a(x)}{\log_a(b)}$$

# **Statistics**

Mean - average

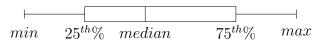
Median - middle value in a sorted list

Mode - most frequent

Range - difference between smallest and largest

Fundamental counting principle - multiply odds together to find the chances of two occurrences happening at once. Eg: the odds getting two heads is  $\frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$ .

## Box and whisker plot



# **Linear Equations**

Standard form: Ax+By=C

Slope-Intercept form: y=mx+b

Point-slope form:  $y-y_1 = m(x - x_1)$ 

Midpoint formula:  $M = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$ 

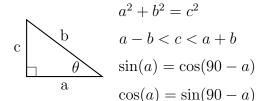
Distance formula:  $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ 

#### Matrices

determinants 
$$\begin{pmatrix} a & b \\ c & d \end{pmatrix} \Rightarrow ad - bc$$

# Trigonometry

# Basic properties of triangles



$$\sin(\theta) = \frac{a}{c}$$
  $\cos(\theta) = \frac{b}{c}$   $\tan(\theta) = \frac{a}{b}$ 

## Common values of trig functions

$\theta$	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$	$\pi$
$\sin \theta$	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1	0
$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0	-1
$\tan \theta$	0	$\frac{\sqrt{3}}{3}$	1	$\sqrt{3}$	$\infty$	0

## Law of sines

$$\frac{\sin(A)}{a} = \frac{\sin(B)}{b} = \frac{\sin(C)}{c}$$

#### Law of cosines

$$a^2 = b^2 + c^2 - 2bc\cos(A)$$

# Simplifying trig functions

$$\sin(a+b) = \sin(a)\cos(b) + \cos(a)\sin(b)$$

$$\cos(a+b) = \cos(a)\cos(b) - \sin(a)\sin(b)$$

$$\sin(a-b) = \sin(a)\cos(b) - \cos(a)\sin(b)$$

$$\cos(a-b) = \cos(a)\cos(b) + \sin(a)\sin(b)$$

# Trig functions with the unit circle

$$\sin(\theta) = \frac{y}{r}$$
  $\cos(\theta) = \frac{x}{r}$   $\tan(\theta) = \frac{y}{x}$   
 $\csc(\theta) = \frac{r}{y}$   $\sec(\theta) = \frac{r}{x}$   $\cot(\theta) = \frac{x}{y}$   
 $x^2 + y^2 = r^2$ 

### Reciprocal Identities

$$\cot \theta = \frac{1}{\tan \theta}$$
  $\sec \theta = \frac{1}{\cos \theta}$   $\csc \theta = \frac{1}{\sin \theta}$ 

# **Quotient Identities**

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$
  $\cot \theta = \frac{\cos \theta}{\sin \theta}$ 

# Pythagorean Identities

$$\sin^2 \theta + \cos^2 \theta = 1$$
  $\tan^2 \theta + 1 = \sec^2 \theta$   $1 + \cot^2 \theta = \csc^2 \theta$ 

#### Double Angle Formulas

$$\sin(2\theta) = 2\sin\theta\cos\theta$$
  $\cos(2\theta) = \cos^2\theta - \sin^2\theta$   
 $\cos(2\theta) = 1 - 2\sin^2\theta$   $\cos(2\theta) = 2\cos^2\theta - 1$ 

# Heron's Formula

$$\sqrt{s \cdot (s-a)(s-b)(s-c)}$$
$$s = \frac{a+b+c}{2}$$

### Calculating a triangle's area

$$area = \frac{1}{2}ab\sin(C^{\circ})$$

# Sector Arc Length

$$s = r\theta$$
 where  $\theta$  is in radians

# Sector Area

$$A = \frac{1}{2}\theta r^2$$

#### Calculus

#### Limits

If for every number  $\epsilon > 0$  there is a number  $\delta > 0$  such that if  $0 < |x - a| < \delta$  then  $|f(x) - L| < \epsilon$ .

### Power Rule

$$\frac{d}{dx}[ax^n] = (n \times a)x^{n-1}$$

## Quotient Rule

$$\frac{d}{dx} \left[ \frac{f(x)}{g(x)} \right] = \frac{g(x)f'(x) - f(x)g'(x)}{g(x) \times g(x)}$$

#### **Product Rule**

$$\frac{d}{dx}[f(x)g(x)] = f(x)g'(x) + f'(x)g(x) \qquad \qquad \frac{d}{dx}[f(g(x))] = f'(g(x)) \times g'(x)$$

#### Chain Rule

$$\frac{d}{dx}[f(g(x))] = f'(g(x)) \times g'(x)$$

# **Exponential Rule**

$$\frac{d}{dx}[x^{a+b}] = x^{a+b} \times ln(x)(a+b)'$$

 $\frac{d}{dx}(a^x) = a^x \ln a$ 

# Log Rule

$$\frac{d}{dx}[log_a x] = \frac{1}{x \times ln(a)} \times x'$$

### **Basic Derivatives**

$$\frac{d}{dx}(\sin x) = \cos x \qquad \frac{d}{dx}(-\sin x) = -\cos x \qquad \frac{d}{dx}(\cos x) = -\sin x \qquad \frac{d}{dx}(-\cos x) = \sin x$$

$$\frac{d}{dx}(\sinh x) = \cosh x \qquad \frac{d}{dx}(-\sinh x) = -\cosh x \qquad \frac{d}{dx}(\cosh x) = \sinh x \qquad \frac{d}{dx}(-\cosh x) = -\sinh x$$

$$\frac{d}{dx}(\tan x) = \sec^2 x \qquad \frac{d}{dx}(\cot x) = -\csc^2 x \qquad \frac{d}{dx}(\sec x) = \sec x \tan x \qquad \frac{d}{dx}(\csc x) = -\csc x \cot x$$

$$\frac{d}{dx}(\arcsin x) = \frac{1}{\sqrt{1-x^2}} \qquad \frac{d}{dx}(\arccos x) = \frac{-1}{\sqrt{1-x^2}} \qquad \frac{d}{dx}(\arctan x) = \frac{1}{1+x^2} \qquad f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$\frac{d}{dx}(e^{2x}) = 2e^x \qquad \frac{d}{dx}(a^x) = a^x \ln a \qquad \frac{d}{dx}(\ln x) = \frac{1}{x} \qquad \frac{d}{dx}(\log_b x) = \frac{1}{x \ln(b)}$$

$$\frac{d}{dx}(\cos x) = -\sin x$$

$$\frac{d}{dx}(\cosh x) = \sinh x$$

$$\frac{d}{dx}(\sec x) = \sec x \tan x$$

$$\frac{d}{dx}(\arctan x) = \frac{1}{1+x^2}$$

 $\frac{d}{dx}(\ln x) = \frac{1}{x}$ 

$$\frac{d}{dx}(-\cosh x) = -\sinh x$$

$$x \quad \frac{d}{dx}(\csc x) = -\csc x \cot x$$

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

$$\frac{d}{dx}(\log_b x) = \frac{1}{x \ln(b)}$$

# Position, velocity and acceleration

#### Position

### Velocity

$$\frac{unit}{time} \Rightarrow x'(t)$$

$$_{\mathrm{ex.}} \frac{\mathit{meters}}{\mathit{second}} \Rightarrow v(t)$$

#### Acceleration

$$\frac{unit}{time^2} \Rightarrow x''(t)$$

$$_{\mathrm{ex.}} \frac{\mathit{meters}}{\mathit{second}^2} \Rightarrow a(t)$$

# Rolle's Theorem

If f(x) is continuous on [a, b], differentiable on (a, b) and f(a) = f(b) = 0, then there exists a value for c on the interval (a, b) such that f'(c) = 0.

# Intermediate Value Theorem

If f(x) is continuous on [a, b]and c falls between f(a) and f(b), then there is at least one value of x in which f(x) = con the interval (a, b).

#### Mean Value Theorem

If f(x) is continuous on [a, b], differentiable on (a, b) and a < c < b, then there exists a value for c such that  $f'(c) = \frac{f(b) - f(a)}{b - a}$ 

#### Extreme Value Theorem

If f(x) is continuous on [a, b], then there exists both a minimum and a maximum on the interval [a, b].

# Rewriting Riemann Sums

$$\lim_{n \to \infty} \sum_{k=1}^{n} f(x_k) \Delta x = \int_{a}^{b} f(x) dx$$

# Trapezoidal Sums

$$\int_{a}^{b} f(x)dx \approx \frac{1}{2} \frac{b-a}{n} [y_0 + 2y_1 + 2y_2...2y_{n-1} + 2y_{n-1} + y_n]$$

# Right Riemann Sums

$$\frac{b-a}{n}[f(x_1) + f(x_2)...f(x_n)]$$

# Left Riemann Sums

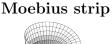
$$\frac{b-a}{n}[f(x_0) + f(x_1)...f(x_{n-1})]$$

# Midpoint Riemann Sums

$$\frac{b-a}{n}[f(x_{1/2}) + f(x_{3/2})...f(x_{n-1/2})]$$

# l'Hopital's Rule

If 
$$\frac{f(a)}{g(b)} = \frac{0}{0}$$
 or  $\frac{\infty}{\infty}$ , then  $\lim_{x \to a} \frac{f(x)}{g(x)} = \lim_{x \to a} \frac{f'(x)}{g'(x)}$ 



f(x)	+	-	+m	-m	rel min	rel max
f'(x)			+	-	+m	-m
f''(x)					+	-

#### Constants

 $\pi \approx 3.14159$ 

 $e \approx 2.71828$ 

 $\gamma \approx 0.57721$ 

 $\phi = \frac{1+\sqrt{5}}{2} \approx 1.61803$   $\hat{\phi} = \frac{1-\sqrt{5}}{2} \approx -.61803$ 

### Waves

### Sine and cosine

$$y = A\sin(Bx + C) + D$$

period:  $\frac{2\pi}{B}$ 

amplitude: |A|

domain:  $(-\infty, \infty)$  range: [D-|A|, D+|A|]

phase shift: Bx + C = 0, solve for x

horizontal line of rest: D

#### Cosecant and secant

$$y = A\csc(Bx + C) + D$$

period:  $\frac{2\pi}{B}$  $amplitude:\ none$ 

domain:  $\csc \neq 0$  range:  $(-\infty, D - |A|] \cup [D + |A|, \infty)$ 

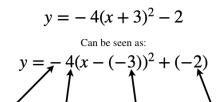
phase shift: Bx + C = 0, solve for x

horizontal line of rest: D

### **Parabolas**

Standard form:  $ax^2 + bx + c = 0$ Vertex form:  $y = a(x - h)^2 + k$ 

Discriminant: From standard form,  $b^2 - 4ac$ No real solutions when discriminant < 0One real solution when discriminant = 0Two real solutions when discriminant > 0



The negative sign causes an x-axis reflection.

The 4 causes a vertical scaling by a factor of

horizontal translation left

a vertical translation down 2 units

Quadratic Formula: 
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

### Units of Measurement

1	
meter, m	kilogram, kg
second, s	ampere, A
kelvin, K	mole, mol
mole, mol	hertz, Hz
newton, N	pascal, Pa
joule, J	watt, W
coulomb, C	volt, V
ohm, $\Omega$	henry, H
farad, F	tesla, T

### **Unit Prefixes**

Prefix	Symbol	Factor
giga	G	$10^{9}$
mega	M	$10^{6}$
kilo	k	$10^{3}$
centi	c	$10^{-2}$
milli	m	$10^{-3}$
micro	$\mu$	$10^{-6}$
nano	n	$10^{-9}$
pico	p	$10^{-12}$

## Pascal's Triangle

1 1 1 2 1 1 3 3 1 1 4 6 4 1 1 5 10 10 5 1 1 6 15 20 15 6 1 1 7 21 35 35 21 7 1 1 8 28 56 70 56 28 8 1 1 9 36 84 126 126 84 36 9 1 1 10 45 120 210 252 210 120 41 10 1 1 11 55 165 330 462 462 330 165 55 11 1 1 12 66 220 495 792 924 792 495 220 66 12 1