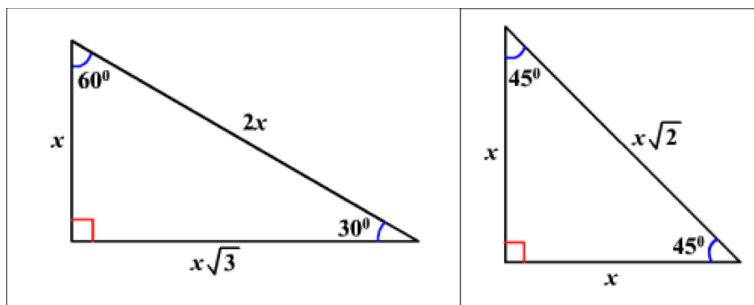


Special Right Triangles

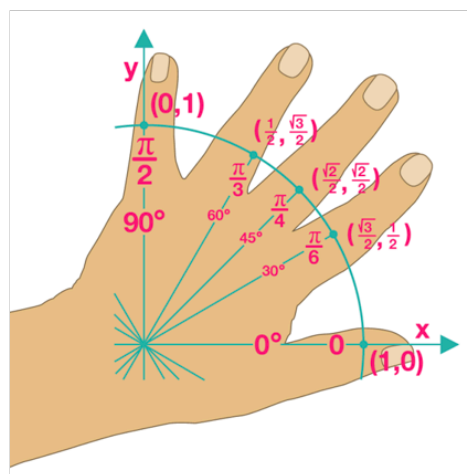
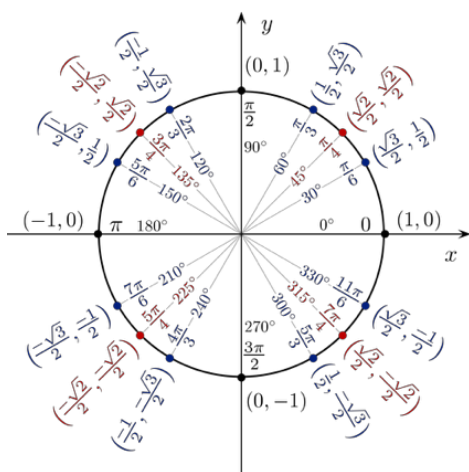


Converting between radians and degrees

$$\text{radians} = \left(\frac{\pi}{180^\circ}\right) \cdot \text{degrees}$$

$$\text{degrees} = \left(\frac{180^\circ}{\pi}\right) \cdot \text{radians}$$

The Unit Circle + hand trick



Definitions of sine, cosine, tangent and their reciprocals

$$\sin \theta = \frac{\textit{opposite}}{\textit{hypotenuse}} \qquad \csc \theta = \frac{\textit{hypotenuse}}{\textit{opposite}}$$

$$\cos \theta = \frac{\textit{adjacent}}{\textit{hypotenuse}} \qquad \sec \theta = \frac{\textit{hypotenuse}}{\textit{adjacent}}$$

$$\tan \theta = \frac{\textit{opposite}}{\textit{adjacent}} \qquad \cot \theta = \frac{\textit{adjacent}}{\textit{opposite}}$$

Using sine, cosine and tangent with the unit circle

$$\sin \theta = \frac{y}{r} \qquad \csc \theta = \frac{r}{y}$$

$$\cos \theta = \frac{x}{r} \qquad \sec \theta = \frac{r}{x}$$

$$\tan \theta = \frac{y}{x} \qquad \cot \theta = \frac{x}{y}$$

$$x^2 + y^2 = r^2$$

Simplifying trigonometric expressions (sine and cosine)

$$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$

$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

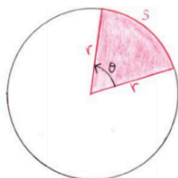
$$\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$$

$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

Arc length, sector area, and radius formulas

Arc Length of a Sector of a Circle

For a circle of radius r , the length of the arc, s , intercepted by a central angle of θ radians is given by $s = r\theta$.

**Area of a Sector of a Circle**

For a circle of radius r , and central angle of θ radians, the area, A , of a sector of a circle is given by $A = \frac{1}{2}\theta r^2$.



The formula for the area of a sector of a circle, $A = \frac{1}{2}\theta r^2$ is only valid if the angle θ is in radians. An angle given in degrees must first be converted to radians.

Trigonometric identities

Reciprocal Identities

$$\cot \theta = \frac{1}{\tan \theta} \quad \sec \theta = \frac{1}{\cos \theta} \quad \csc \theta = \frac{1}{\sin \theta}$$

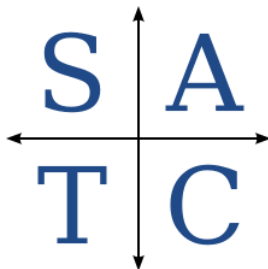
Quotient Identities

$$\tan \theta = \frac{\sin \theta}{\cos \theta} \quad \cot \theta = \frac{\cos \theta}{\sin \theta}$$

Pythagorean Identities

$$\sin^2 \theta + \cos^2 \theta = 1 \quad \tan^2 \theta + 1 = \sec^2 \theta \quad 1 + \cot^2 \theta = \csc^2 \theta$$

All Students Take Calculus



Double Angle Formulas

$$\sin(2\theta) = 2 \sin \theta \cos \theta \qquad \cos(2\theta) = \cos^2 \theta - \sin^2 \theta$$

$$\cos(2\theta) = 1 - 2 \sin^2 \theta \qquad \cos(2\theta) = 2 \cos^2 \theta - 1$$

Solving Generic Triangles

$$\text{Heron's Formula: } \sqrt{s \cdot (s - a)(s - b)(s - c)}, \quad s = \frac{a+b+c}{2}$$

$$\text{Two sides and an included angle: area} = \frac{1}{2}ab \sin(C)$$

$$\frac{\sin(a)}{A} = \frac{\sin(b)}{B}$$

Waves

Sine

$$Y = A \sin(Bx + C) + D$$

$$\text{Amp} \Rightarrow |A|$$

$$\text{Period} \Rightarrow \frac{2\pi}{B}$$

$$\text{Phase shift} \Rightarrow Bx + C = 0, \text{ solve for } x$$

$$\text{Horizontal line of rest} \Rightarrow D$$

$$\text{Range} \Rightarrow [D - |A|, D + |A|]$$

$$\text{Domain} \Rightarrow (-\infty, \infty)$$

Cosine

$$Y = A \cos(Bx + C) + D$$

$$\text{Amp} \Rightarrow |A|$$

$$\text{Period} \Rightarrow \frac{2\pi}{B}$$

$$\text{Phase shift} \Rightarrow Bx + C = 0, \text{ solve for } x$$

$$\text{Horizontal line of rest} \Rightarrow D$$

$$\text{Range} \Rightarrow [D - |A|, D + |A|]$$

$$\text{Domain} \Rightarrow (-\infty, \infty)$$

Secant

$$Y = A \sec(Bx + C) + D$$

$$\text{Amp} \Rightarrow \text{None}$$

$$\text{Period} \Rightarrow \frac{2\pi}{B}$$

$$\text{Phase shift} \Rightarrow Bx + C = 0, \text{ solve for } x$$

$$\text{Horizontal line of rest} \Rightarrow D$$

$$\text{Range} \Rightarrow (-\infty, D - |A|] \cup [D + |A|, \infty)$$

$$\text{Domain} \Rightarrow \cos \neq 0$$

(Happens when cosine crosses the HLR and is represented with a v.a.)

Cosecant

$$Y = A \csc(Bx + C) + D$$

$$\text{Amp} \Rightarrow \text{None}$$

$$\text{Period} \Rightarrow \frac{2\pi}{B}$$

$$\text{Phase shift} \Rightarrow Bx + C = 0, \text{ solve for } x$$

$$\text{Horizontal line of rest} \Rightarrow D$$

$$\text{Range} \Rightarrow (-\infty, D - |A|] \cup [D + |A|, \infty)$$

$$\text{Domain} \Rightarrow \sin \neq 0$$

(Happens when sine crosses the HLR and is represented with a v.a.)