Intro. to Computer Programming
Midterm 1

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Defining Functions

- **Via a file.** `myFunct.m` possibly with sub-functions:

```
function [out1, out2, ...] = myFunct(in1, in2, ...)
```

- **Via function handle.**

```
f = @(arg1, arg2, ...) expression(arg1, arg2, ...);
result = f(in1, in2, ...);
```

Useful Functions

- **Random integers.**

```
1   randi([minVal, maxVal], rows, cols);
```

- **Formatted output.**

```
1   fprintf(formatSpec, values);
```

Commonly used formats: `%d`, `%f`, `\n`, ...

Workspace

- Command.

```
1  save(filename, var1, var2, ..., formatSpec);
2  load(filename, formatSpec);
```

- What are the optional formats?
- What are the types of the stored data? What will happen if you reload the data?

File Reading and Writing

- Open and close a file.

```
fid = fopen(filename, permission);
fclose(fid);
```

- Reading from a file.

```
fscanf(fid, formatSpec, variables);
fgetl(fid);
fread(fid, sizeA, precision);
```

- Write to a file.

```
fprintf(fid, formatSpec, variables);
fwrite(fid, A, precision)
```

File Reading and Writing

Example

- Formatted I/O.

```
d = date();
fid = fopen('date.txt', 'r');
fprintf(fid, 'Today is %s.\n', d);
fclose(fid);
```

- Binary write/read.

```
A = magic(4);
fid = fopen('magic.txt', 'w');
fwrite(fid, A, 'int64');
fclose(fid);
```

Q: Once you have written these data to the files, how can you read the original data back from these output files?

Methodology

- Required to design a function f to solve a problem of size D_n.
- Assume we know how to solve of problem of size smaller than or equal to D_{n-1}. (How can we solve the problem of size D_n with solutions of problem of sizes $D_1, \ldots, D_{n-1}$?)
- Then to solve the current problem of size D_n,
  1. Call $f(D_{n-1})$ and possibly $f(D_{n-2}), f(D_{n-3}), \ldots$
  2. Solve problem of size D_n with the solutions to smaller-sized problems.

Methodology

In terms of programming,

- Identify base case: the smallest problem that we can solve without question.
- Design algorithm to solve the problem of size D_n with previous solutions. Get the solutions we need by calling the function inside itself.

Generate Permutations

Algorithm 1 Generate Permutations

Require: a set of characters S

Ensure: a set containing all permutations of the characters

1: **if** S is empty or contains only one character **then**
2: **return** S;
3: **end if**
4: **for all** character $c \in S$ **do**
5: call Generate Permutations with the remaining characters;
6: concatenate c with all returned permutations and set as P_c;
7: **end for**
8: merge all P_cs into a single set P;
9: **return** P;

Depth-First Search

Algorithm 2 Depth-First Search (DFS)

Require: graph G, with some nodes connected, a source node s
Ensure: visit all the nodes in the graph

```
1: visit s;
2: update G;
3: for all node v that can be reached from s do
4:     if node v has not been visited then
5:         call DFS with the current graph G and source node v;
6:     end if
7: end for
```

Factorization

Q: What is the problem in the following pseudocode?

Algorithm 3 Factorize Integers

Require: a positive integer n
Ensure: a set of primes P with $n = p_1 \times p_2 \times \cdots \times p_k$

```
if n is a prime or 1 then
    return {n};
end if
P ← {};
for all k ← 1, ..., ⌊√n⌋ do
    if n is divisible by k then
        add k into P;
        call Factorization with input n/k;
        merge the output from the previous call with P;
        return P;
    end if
end for
```

Factorization

Algorithm 4 Factorize Integers

Require: a positive integer n

Ensure: a set of primes P with $n = p_1 \times p_2 \times \cdots \times p_k$

1: **if** n is a prime or 1 **then**
2: **return** $\{n\}$;
3: **end if**
4: $P \leftarrow \{\}$;
5: **for all** $k \leftarrow 2, \ldots, \lfloor \sqrt{n} \rfloor$ **do**
6: **if** n is divisible by k **then**
7: add k into P;
8: call Factorization with input n/k;
9: merge the output from the previous call with P;
10: **return** P;
11: **end if**
12: **end for**

Remarks

- Slides with *relevant* notes are allowed in Part B. But do not write the whole project on your notes. :)
- Think about the questions on the last slide of each chapter.
- Do not expect to complete all the questions.
- Try to be more familiar with coding.
- If you encounter something that is unfamiliar to you, search in documentation.
- *Read through the exam paper before you start.*

Good luck for your Midterm 1!