

Offline Multi-Objective Optimization

Table 8. Average rank of different offline MOO methods on each type of task with 256 solutions and 100th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	Synthetic	MO-NAS	MORL	MOCO	Sci-Design	RE	Average Rank
$\mathcal{D}(\text{best})$	11.77 \pm 0.17	12.11 \pm 0.21	8.75 \pm 0.25	2.23 \pm 0.31	9.00 \pm 0.00	12.90 \pm 0.03	10.07 \pm 0.14
End-to-End	6.94 \pm 0.00	8.18 \pm 0.03	7.00 \pm 2.00	6.31 \pm 0.62	6.75 \pm 0.88	7.40 \pm 0.60	7.17 \pm 0.01
End-to-End + GradNorm	8.28 \pm 0.53	7.47 \pm 0.11	5.75 \pm 2.75	7.81 \pm 0.04	8.50 \pm 0.62	10.40 \pm 0.07	8.33 \pm 0.03
End-to-End + PcGrad	7.81 \pm 0.00	7.03 \pm 0.24	10.75 \pm 1.25	5.81 \pm 0.65	8.62 \pm 2.75	8.13 \pm 0.13	7.41 \pm 0.06
Multi-Head	6.44 \pm 0.44	5.24 \pm 0.29	6.00 \pm 2.00	8.38 \pm 0.08	9.38 \pm 0.50	8.20 \pm 0.47	6.95 \pm 0.33
Multi-Head + GradNorm	7.78 \pm 0.53	9.96 \pm 0.04	12.00 \pm 2.00	10.13 \pm 0.17	9.06 \pm 0.94	10.50 \pm 0.17	9.59 \pm 0.08
Multi-Head + PcGrad	8.61 \pm 0.20	6.84 \pm 0.58	9.75 \pm 3.25	8.12 \pm 0.19	9.25 \pm 0.62	8.37 \pm 0.17	7.99 \pm 0.26
Multiple Models	4.02 \pm 0.14	4.93 \pm 0.28	9.25 \pm 0.75	6.67 \pm 0.37	<u>5.50 \pm 0.88</u>	<u>4.40 \pm 0.07</u>	<u>5.01 \pm 0.02</u>
Multiple Models + COMs	9.81 \pm 0.31	6.47 \pm 0.37	5.50 \pm 3.00	5.69 \pm 0.54	8.12 \pm 1.75	10.40 \pm 0.47	8.06 \pm 0.34
Multiple Models + RoMA	8.98 \pm 0.02	4.92 \pm 0.03	6.50 \pm 0.50	7.81 \pm 0.35	7.88 \pm 1.25	6.20 \pm 0.07	7.00 \pm 0.02
Multiple Models + IOM	<u>6.08 \pm 0.39</u>	4.76 \pm 0.39	3.75 \pm 2.75	<u>3.58 \pm 0.04</u>	7.12 \pm 0.50	3.17 \pm 0.03	4.58 \pm 0.08
Multiple Models + ICT	9.17 \pm 0.33	11.68 \pm 0.42	4.75 \pm 0.25	9.46 \pm 0.46	8.38 \pm 0.50	8.30 \pm 0.30	9.46 \pm 0.17
Multiple Models + Tri-Mentoring	7.89 \pm 0.11	11.11 \pm 0.37	5.00 \pm 2.50	9.19 \pm 0.04	9.12 \pm 0.75	6.67 \pm 0.20	8.62 \pm 0.16
MOBO	8.72 \pm 0.34	7.03 \pm 0.66	10.25 \pm 0.25	14.38 \pm 0.12	4.69 \pm 0.31	5.82 \pm 0.18	8.57 \pm 0.36
MOBO-ParEGO	10.05 \pm 0.20	11.50 \pm 0.13	N/A	14.22 \pm 0.00	8.50 \pm 1.50	12.62 \pm 0.29	11.62 \pm 0.05
MOBO-JES	12.05 \pm 0.05	16.00 \pm 0.00	N/A	N/A	7.50 \pm 6.50	8.00 \pm 0.42	9.95 \pm 0.55

Table 9. Hypervolume results for synthetic functions with 256 solutions and 100th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	DTLZ1	DTLZ2	DTLZ3	DTLZ4	DTLZ5	DTLZ6	DTLZ7	OmniTest	VLMOP1	VLMOP2	VLMOP3	ZDT1	ZDT2	ZDT3	ZDT4	ZDT6
$\mathcal{D}(\text{best})$	10.52	9.43	9.71	10.76	9.06	8.20	8.32	3.87	2.28	1.64	45.14	4.04	4.70	5.12	5.46	4.76
End-to-End	10.12 \pm 0.02	10.65 \pm 0.00	10.65 \pm 0.00	10.70 \pm 0.05	10.65 \pm 0.00	10.65 \pm 0.00	10.70 \pm 0.01	4.35 \pm 0.00	<u>2.57 \pm 2.26</u>	4.24 \pm 0.01	<u>46.93 \pm 0.00</u>	2.69 \pm 0.00	3.21 \pm 0.00	5.50 \pm 0.04	3.12 \pm 0.09	4.92 \pm 0.00
End-to-End + GradNorm	10.65 \pm 0.00	10.65 \pm 0.00	10.65 \pm 0.00	10.76 \pm 0.00	10.54 \pm 0.09	10.64 \pm 0.00	10.71 \pm 0.00	3.76 \pm 0.03	<u>2.33 \pm 2.33</u>	2.79 \pm 1.34	42.23 \pm 0.98	4.77 \pm 0.01	5.63 \pm 0.02	5.27 \pm 0.03	3.23 \pm 0.03	3.81 \pm 1.02
End-to-End + PcGrad	<u>10.65 \pm 0.00</u>	10.65 \pm 0.00	10.65 \pm 0.00	10.70 \pm 0.05	9.02 \pm 0.10	9.45 \pm 0.15	10.52 \pm 0.00	4.35 \pm 0.00	2.57 \pm 2.26	4.14 \pm 0.07	46.79 \pm 0.06	4.84 \pm 0.01	<u>5.70 \pm 0.01</u>	5.45 \pm 0.00	3.12 \pm 0.01	2.04 \pm 0.22
Multi-Head	10.38 \pm 0.25	10.65 \pm 0.00	10.65 \pm 0.00	10.70 \pm 0.05	<u>10.65 \pm 0.00</u>	<u>10.65 \pm 0.00</u>	10.63 \pm 0.11	4.30 \pm 0.05	2.57 \pm 2.26	<u>4.26 \pm 0.00</u>	46.92 \pm 0.02	2.69 \pm 0.00	4.48 \pm 1.27	5.50 \pm 0.04	3.23 \pm 0.16	<u>4.91 \pm 0.00</u>
Multi-Head + GradNorm	10.65 \pm 0.00	10.65 \pm 0.00	10.65 \pm 0.00	10.76 \pm 0.00	9.29 \pm 0.86	10.62 \pm 0.02	10.61 \pm 0.10	4.34 \pm 0.00	0.00 \pm 0.00	4.13 \pm 0.03	46.64 \pm 0.22	4.83 \pm 0.00	5.68 \pm 0.05	5.26 \pm 0.04	3.39 \pm 0.00	4.87 \pm 0.00
Multi-Head + PcGrad	10.64 \pm 0.00	10.65 \pm 0.00	10.65 \pm 0.00	10.76 \pm 0.00	9.08 \pm 0.35	10.59 \pm 0.01	10.49 \pm 0.01	4.35 \pm 0.00	2.55 \pm 2.24	4.01 \pm 0.02	46.91 \pm 0.00	2.73 \pm 0.03	5.69 \pm 0.03	5.45 \pm 0.00	3.64 \pm 0.17	2.17 \pm 0.05
Multiple Models	10.65 \pm 0.00	10.65 \pm 0.00	10.65 \pm 0.00	10.76 \pm 0.00	10.65 \pm 0.00	10.65 \pm 0.00	10.73 \pm 0.00	4.35 \pm 0.00	2.57 \pm 2.26	4.28 \pm 0.00	46.94 \pm 0.00	4.75 \pm 0.00	5.58 \pm 0.00	5.80 \pm 0.01	4.14 \pm 0.20	4.91 \pm 0.00
Multiple Models + COMs	10.64 \pm 0.01	10.39 \pm 0.18	10.59 \pm 0.05	10.70 \pm 0.05	10.57 \pm 0.06	10.26 \pm 0.25	9.64 \pm 0.22	4.29 \pm 0.03	2.54 \pm 2.25	1.90 \pm 0.05	46.78 \pm 0.07	4.24 \pm 0.01	4.89 \pm 0.07	5.54 \pm 0.02	4.56 \pm 0.04	4.57 \pm 0.00
Multiple Models + RoMA	10.64 \pm 0.00	10.65 \pm 0.00	10.65 \pm 0.00	10.76 \pm 0.00	10.18 \pm 0.45	10.63 \pm 0.03	10.63 \pm 0.03	3.03 \pm 0.03	2.54 \pm 2.24	1.46 \pm 0.00	44.15 \pm 2.36	4.87 \pm 0.00	5.65 \pm 0.00	5.78 \pm 0.02	3.18 \pm 0.05	1.78 \pm 0.02
Multiple Models + IOM	10.65 \pm 0.00	10.61 \pm 0.02	10.62 \pm 0.02	10.76 \pm 0.00	10.63 \pm 0.01	10.50 \pm 0.11	<u>10.74 \pm 0.08</u>	4.34 \pm 0.00	2.55 \pm 2.24	3.77 \pm 0.01	46.92 \pm 0.00	4.66 \pm 0.01	5.74 \pm 0.01	5.61 \pm 0.01	4.65 \pm 0.19	4.89 \pm 0.02
Multiple Models + ICT	10.64 \pm 0.00	10.65 \pm 0.00	10.65 \pm 0.00	10.76 \pm 0.00	10.63 \pm 0.01	10.65 \pm 0.00	10.75 \pm 0.02	4.30 \pm 0.00	2.27 \pm 2.07	1.46 \pm 0.00	46.74 \pm 0.09	4.39 \pm 0.01	5.53 \pm 0.00	4.37 \pm 0.03	3.44 \pm 0.16	2.33 \pm 0.11
Multiple Models + Tri-Mentoring	10.64 \pm 0.00	10.65 \pm 0.00	10.65 \pm 0.00	10.76 \pm 0.00	10.59 \pm 0.04	10.65 \pm 0.00	10.67 \pm 0.01	3.97 \pm 0.00	4.83 \pm 0.00	1.46 \pm 0.00	46.82 \pm 0.02	4.52 \pm 0.02	5.55 \pm 0.01	5.62 \pm 0.09	3.47 \pm 0.04	2.36 \pm 0.28
MOBO	10.65 \pm 0.00	10.54 \pm 0.10	10.51 \pm 0.07	10.65 \pm 0.00	10.17 \pm 0.13	9.58 \pm 0.13	10.56 \pm 0.01	4.35 \pm 0.00	0.32 \pm 0.00	1.50 \pm 0.02	46.89 \pm 0.01	4.54 \pm 0.01	5.15 \pm 0.11	5.54 \pm 0.01	4.43 \pm 0.31	4.17 \pm 0.51
MOBO-ParEGO	10.63 \pm 0.00	9.73 \pm 0.20	9.80 \pm 0.19	10.76 \pm 0.00	9.03 \pm 0.24	9.16 \pm 0.10	10.25 \pm 0.05	4.33 \pm 0.00	0.28 \pm 0.00	2.93 \pm 0.06	46.93 \pm 0.00	4.32 \pm 0.02	5.12 \pm 0.17	5.20 \pm 0.01	<u>4.81 \pm 0.10</u>	3.31 \pm 0.03
MOBO-JES	10.61 \pm 0.00	/	/	/	/	/	9.36 \pm 0.08	3.87 \pm 0.00	N/A	1.46 \pm 0.00	46.88 \pm 0.00	3.97 \pm 0.09	4.44 \pm 0.07	5.17 \pm 0.02	4.43 \pm 0.08	3.09 \pm 0.02

Table 10. Hypervolume results for MO-NAS with 256 solutions and 100th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	C-10/MOP1	C-10/MOP2	C-10/MOP3	C-10/MOP4	C-10/MOP5	C-10/MOP6	C-10/MOP7	C-10/MOP8	C-10/MOP9	IN-1K/MOP1	IN-1K/MOP2	IN-1K/MOP3	IN-1K/MOP4	IN-1K/MOP5	IN-1K/MOP6	IN-1K/MOP7	IN-1K/MOP8	IN-1K/MOP9	NasBench201-Test
$\mathcal{D}(\text{best})$	4.78	10.49	9.78	21.15	40.51	92.43	358.27	4.55	10.59	4.97	5.00	11.21	16.63	17.26	44.43	4.69	11.42	21.50	9.24
End-to-End	4.84 \pm 0.00	10.49 \pm 0.02	10.84 \pm 0.01	26.25 \pm 0.07	50.20 \pm 0.03	<u>112.47 \pm 0.01</u>	523.26 \pm 0.11	4.56 \pm 0.07	10.50 \pm 0.15	4.85 \pm 0.07	4.70 \pm 0.02	10.88 \pm 0.10	17.07 \pm 0.03	<u>17.93 \pm 0.13</u>	45.89 \pm 0.16	5.17 \pm 0.02	11.15 \pm 0.18	23.35 \pm 0.30	10.30 \pm 0.03
End-to-End + GradNorm	4.84 \pm 0.00	10.54 \pm 0.01	10.86 \pm 0.01	26.46 \pm 0.04	50.64 \pm 0.00	<u>112.27 \pm 0.03</u>	525.63 \pm 0.10	4.56 \pm 0.08	10.48 \pm 0.23	5.21 \pm 0.00	5.04 \pm 0.02	10.87 \pm 0.05	16.93 \pm 0.07	17.80 \pm 0.09	45.40 \pm 0.12	4.96 \pm 0.05	10.73 \pm 0.08	22.55 \pm 0.13	9.94 \pm 0.01
End-to-End + PcGrad	4.84 \pm 0.00	10.50 \pm 0.01	10.81 \pm 0.00	26.30 \pm 0.04	50.54 \pm 0.08	112.15 \pm 0.01	526.46 \pm 0.12	4.58 \pm 0.04	11.10 \pm 0.04	5.27 \pm 0.04	5.20 \pm 0.03	11.11 \pm 0.03	16.82 \pm 0.01	17.63 \pm 0.01	44.47 \pm 0.04	5.03 \pm 0.07	11.20 \pm 0.20	23.43 \pm 0.24	10.45 \pm 0.09
Multi-Head	4.83 \pm 0.01	10.55 \pm 0.00	10.59 \pm 0.00	<u>26.59 \pm 0.01</u>	50.45 \pm 0.03	112.72 \pm 0.00	529.51 \pm 0.36	4.52 \pm 0.09	9.88 \pm 0.15	5.37 \pm 0.00	5.05 \pm 0.01	11.55 \pm 0.01	17.03 \pm 0.04	18.00 \pm 0.06	<u>46.01 \pm 0.10</u>	5.33 \pm 0.00	11.73 \pm 0.10	25.31 \pm 0.14	10.36 \pm 0.01
Multi-Head + GradNorm	4.85 \pm 0.00	10.57 \pm 0.02	10.23 \pm 0.00	24.49 \pm 0.06	50.24 \pm 0.00	111.16 \pm 0.09	525.72 \pm 0.21	3.90 \pm 0.05	9.43 \pm 0.13	5.05 \pm 0.01	4.41 \pm 0.09	10.07 \pm 0.07	17.03 \pm 0.19	17.74 \pm 0.08	45.25 \pm 0.18	4.97 \pm 0.01	8.61 \pm 0.05	20.78 \pm 0.20	10.35 \pm 0.00
Multi-Head + PcGrad	<u>4.85 \pm 0.00</u>	10.58 \pm 0.03	<u>10.36 \pm 0.01</u>	24.44 \pm 0.11	50.53 \pm 0.01	112.13 \pm 0.19	520.43 \pm 0.27	4.51 \pm 0.09	10.51 \pm 0.18	4.99 \pm 0.10	5.18 \pm 0.02	11.40 \pm 0.13	17.01 \pm 0.06	17.76 \pm 0.15	45.14 \pm 0.13	5.53 \pm 0.05	10.95 \pm 0.10	23.60 \pm 0.29	10.35 \pm 0.01
Multiple Models	4.82 \pm 0.00	10.54 \pm 0.00	10.83 \pm 0.01	26.62 \pm 0.02	50.20 \pm 0.02	111.91 \pm 0.03	525.80 \pm 0.28	4.75 \pm 0.04	11.17 \pm 0.06	<u>5.34 \pm 0.00</u>	<u>5.22 \pm 0.01</u>	11.57 \pm 0.01	17.19 \pm 0.04	17.82 \pm 0.00	46.02 \pm 0.04	5.64 \pm 0.11	11.77 \pm 0.03	24.92 \pm 0.24	10.34 \pm 0.02
Multiple Models + COMs	4.84 \pm 0.01	10.57 \pm 0.00	10.66 \pm 0.07	25.66 \pm 0.12	50.42 \pm 0.01	111.31 \pm 0.50	525.66 \pm 0.11	4.90 \pm 0.00	10.90 \pm 0.04	5.26 \pm 0.00	5.17 \pm 0.00	11.58 \pm 0.01	16.79 \pm 0.10	17.86 \pm 0.00	43.33 \pm 0.00	12.70 \pm 0.03	26.21 \pm 0.00	10.40 \pm 0.12	9.94 \pm 0.01
Multiple Models + COMs + PC	4.84 \pm 0.01	10.57 \pm 0.00	10.66 \pm 0.07	25.66 \pm 0.12	50.42 \pm 0.01	111.31 \pm 0.50	525.66 \pm 0.11	4.90 \pm 0.00	10.90 \pm 0.04	5.26 \pm 0.00	5.17 \pm 0.00	11.58 \pm 0.01	16.79 \pm 0.10	17.86 \pm 0.00	43.33 \pm 0.00	12.70 \pm 0.03	26.21 \pm 0.00	10.40 \pm 0.12	9.94 \pm 0.01
Multiple Models + ICM	4.83 \pm 0.01	10.43 \pm 0.03	10.73 \pm 0.00	26.04 \pm 0.20	50.52 \pm 0.01	112.47 \pm 0.04	<u>527.83 \pm 0.01</u>	4.88 \pm 0.05	11.59 \pm 0.02	5.28 \pm 0.01	5.21 \pm 0.02	11.62 \pm 0.01	16.97 \pm 0.07	17.81 \pm 0.07	45.51 \pm 0.01	4.79 \pm 0.00	12.18 \pm 0.00	26.56 \pm 0.00	10.54 \pm 0.50
Multiple Models + ICT	4.82 \pm 0.36	10.49 \pm 0.01	10.43 \pm 0.03	25.82 \pm 0.03	50.36 \pm 0.09	108.80 \pm 3.66	40.43 \pm 0.99	3.62 \pm 0.14	8.21 \pm 0.14	5.78 \pm 0.01	4.99 \pm 0.02	9.60 \pm 0.23	16.72 \pm 0.02	16.85 \pm 0.23	45.61 \pm 0.01	4.79 \pm 0.01	11.47 \pm 0.24	18.48 \pm 0.31	9.62 \pm 0.20
Multiple Models + PC + ICM	4.82 \pm 0.02	10.51 \pm 0.01	10.77 \pm 0.00	26.10 \pm 0.02	50.52 \pm 0.01	112.47 \pm 0.04	<u>527.83 \pm 0.01</u>	4.88 \pm 0.05	11.59 \pm 0.02	5.28 \pm 0.01	5.21 \pm 0.02	11.62 \pm 0.01	16.97 \pm 0.07	17.81 \pm 0.07	45.51 \pm 0.01	4.79 \pm 0.00	12.18 \pm 0.00	26.56 \pm 0.00	10.54 \pm 0.50
MOBO	4.82 \pm 0.02	<u>10.58 \pm 0.01</u>	10.70 \pm 0.00	26.35 \pm 0.02	50.32 \pm 0.01	111.28 \pm 0.58	489.87 \pm 0.41	4.71 \pm 0.01	11.11 \pm 0.23	5.25 \pm 0.02	5.16 \pm 0.02	11.24 \pm 0.03	16.74 \pm 0.05	17.56 \pm 0.01	44.44 \pm 0.02	5.21 \pm 0.02	12.33 \pm 0.14	25.65 \pm 0.03	<u>10.49 \pm 0.91</u>
MOBO Pareto	4.81 \pm 0.00	<u>10.51 \pm 0.02</u>	10.71 \pm 0.00	26.35 \pm 0.02	50.32 \pm 0.01	111.28 \pm 0.58	489.87 \pm 0.41	4.71 \pm 0.01	11.11 \pm 0.23	5.25 \pm 0.02	5.16 \pm 0.02	11.24 \pm 0.03	16.74 \pm 0.05	17.56 \pm 0.01	44.44 \pm 0.02	5.21 \pm 0.02	12.33 \pm 0.14	25.65 \pm 0.03	<u>10.49 \pm 0.91</u>
MOBO Pareto + PC	N/A	N/A	N/A	20.14 \pm 0.06	37.74 \pm 0.00	111.00 \pm 0.30	354.60 \pm 0.00	4.56 \pm 0.06	10.67 \pm 0.00	1.63 \pm 0.04	4.63 \pm 0.02	N/A	16.54 \pm 0.00	17.41 \pm 0.05	44.42 \pm 0.03	4.87 \pm 0.00	11.01 \pm 0.09	23.99 \pm 0.06	9.16 \pm 0.07

Table 11. Hypervolume results for MORL with 256 solutions and 100th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	MO-Hopper	MO-Swimmer
$\mathcal{D}(\text{best})$	4.21	2.85
End-to-End	4.76 ± 0.25	2.77 ± 0.03
End-to-End + GradNorm	5.02 ± 0.04	0.54 ± 0.00
End-to-End + PcGrad	4.00 ± 0.33	0.52 ± 0.00
Multi-Head	4.57 ± 0.28	1.70 ± 1.17
Multi-Head + GradNorm	3.78 ± 0.05	2.89 ± 0.07
Multi-Head + PcGrad	4.27 ± 0.61	1.52 ± 1.00
Multiple Models	4.58 ± 0.19	2.61 ± 0.14
Multiple Models + COMs	4.84 ± 0.16	2.94 ± 0.00
Multiple Models + RoMA	<u>5.07 ± 0.39</u>	2.61 ± 0.00
Multiple Models + IOM	5.32 ± 0.49	<u>2.94 ± 0.11</u>
Multiple Models + ICT	4.67 ± 0.12	2.69 ± 0.02
Multiple Models + Tri-Mentoring	4.93 ± 0.11	2.82 ± 0.10
MOBO	4.43 ± 0.08	2.61 ± 0.02
MOBO-ParEGO	N/A	N/A
MOBO-JES	N/A	N/A

Table 12. Hypervolume results for MOCO with 256 solutions and 100th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	Bi-CVRP-20	Bi-CVRP-50	Bi-CVRP-100	Bi-KP-50	Bi-KP-100	Bi-KP-200	Bi-TSP-20	Bi-TSP-50	Bi-TSP-100	Bi-TSP-500	Tri-TSP-20	Tri-TSP-50	Tri-TSP-100
$\mathcal{D}(\text{best})$	5.37	5.11	4.91	3.00	3.45	4.68	5.05	4.89	4.55	4.52	11.88	<u>9.82</u>	9.36
End-to-End	4.85 ± 0.18	4.70 ± 0.17	4.91 ± 0.02	2.98 ± 0.00	3.02 ± 0.00	3.71 ± 0.47	3.64 ± 0.08	4.57 ± 0.08	4.60 ± 0.01	4.20 ± 0.29	7.84 ± 0.37	4.67 ± 0.17	9.26 ± 0.23
End-to-End + GradNorm	4.77 ± 0.06	3.68 ± 0.20	3.84 ± 0.05	3.06 ± 0.00	2.84 ± 0.14	3.25 ± 0.01	3.12 ± 0.13	4.33 ± 0.00	4.04 ± 0.06	4.45 ± 0.02	7.84 ± 0.17	8.96 ± 0.07	9.41 ± 0.04
End-to-End + PcGrad	4.56 ± 0.06	4.32 ± 0.09	4.15 ± 0.34	3.16 ± 0.02	3.08 ± 0.03	3.52 ± 0.27	3.08 ± 0.03	4.68 ± 0.03	4.55 ± 0.02	4.17 ± 0.12	10.83 ± 0.03	8.15 ± 0.39	9.68 ± 0.15
Multi-Head	4.00 ± 0.06	4.03 ± 0.26	4.78 ± 0.16	3.11 ± 0.06	2.88 ± 0.04	4.03 ± 0.41	3.36 ± 0.14	4.60 ± 0.09	4.04 ± 0.00	3.70 ± 0.27	6.31 ± 0.14	6.43 ± 0.42	8.60 ± 0.13
Multi-Head + GradNorm	4.50 ± 0.51	3.69 ± 0.12	4.35 ± 0.57	2.88 ± 0.07	2.47 ± 0.01	2.98 ± 0.41	4.39 ± 0.17	3.40 ± 0.02	3.45 ± 0.35	3.83 ± 0.02	7.84 ± 0.20	6.48 ± 0.65	8.48 ± 0.23
Multi-Head + PcGrad	4.48 ± 0.48	4.24 ± 0.12	3.45 ± 0.11	<u>3.13 ± 0.06</u>	<u>2.60 ± 0.37</u>	<u>4.34 ± 0.10</u>	2.85 ± 0.10	3.89 ± 0.12	3.78 ± 0.00	2.62 ± 0.88	10.39 ± 0.14	7.46 ± 1.00	10.10 ± 0.07
Multiple Models	4.95 ± 0.06	4.88 ± 0.03	<u>4.92 ± 0.00</u>	<u>3.03 ± 0.02</u>	<u>3.19 ± 0.07</u>	<u>3.84 ± 0.54</u>	3.55 ± 0.05	3.27 ± 0.04	4.22 ± 0.18	<u>4.51 ± 0.01</u>	7.26 ± 0.09	6.90 ± 0.08	7.68 ± 0.38
Multiple Models + COMs	<u>5.28 ± 0.00</u>	4.27 ± 0.14	4.23 ± 0.10	2.97 ± 0.00	3.11 ± 0.05	4.05 ± 0.46	4.64 ± 0.05	4.54 ± 0.06	4.30 ± 0.07	<u>4.02 ± 0.10</u>	10.94 ± 0.46	8.55 ± 0.40	8.84 ± 0.26
Multiple Models + RoMA	4.56 ± 0.01	4.22 ± 0.23	3.97 ± 0.15	2.80 ± 0.06	3.11 ± 0.09	3.74 ± 0.26	4.25 ± 0.36	4.48 ± 0.04	4.31 ± 0.01	2.51 ± 0.69	9.37 ± 0.51	7.77 ± 0.03	9.10 ± 0.09
Multiple Models + IOM	5.28 ± 0.01	<u>5.11 ± 0.00</u>	4.93 ± 0.00	2.98 ± 0.02	2.86 ± 0.05	4.12 ± 0.21	<u>4.85 ± 0.04</u>	<u>4.79 ± 0.01</u>	4.53 ± 0.00	4.39 ± 0.09	<u>11.65 ± 0.03</u>	10.19 ± 0.05	<u>9.89 ± 0.02</u>
Multiple Models + ICT	4.15 ± 0.21	4.29 ± 0.17	3.96 ± 0.08	2.75 ± 0.11	2.68 ± 0.14	3.56 ± 0.09	4.40 ± 0.34	3.88 ± 0.24	3.75 ± 0.04	4.20 ± 0.11	7.09 ± 0.03	8.37 ± 0.02	7.50 ± 0.12
Multiple Models + Tri-Mentoring	4.12 ± 0.16	4.06 ± 0.20	4.09 ± 0.13	2.90 ± 0.10	2.88 ± 0.04	3.32 ± 0.05	3.96 ± 0.18	3.75 ± 0.11	4.17 ± 0.14	3.69 ± 0.39	7.50 ± 0.47	8.16 ± 0.23	8.23 ± 0.27
MOBO	3.38 ± 0.23	2.40 ± 0.09	1.58 ± 0.02	2.73 ± 0.14	2.33 ± 0.05	1.89 ± 0.06	2.42 ± 0.16	1.77 ± 0.01	1.56 ± 0.06	/	5.64 ± 0.04	3.36 ± 0.12	2.54 ± 0.03
MOBO-ParEGO	3.69 ± 0.13	2.77 ± 0.10	1.66 ± 0.02	/	/	N/A	2.70 ± 0.09	2.10 ± 0.01	1.75 ± 0.01	N/A	4.40 ± 0.14	3.54 ± 0.00	2.38 ± 0.01
MOBO-JES	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A

Table 13. Hypervolume results for Sci-Design with 256 solutions and 100th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	Molecule	Regex	RFP	ZINC
$\mathcal{D}(\text{best})$	2.26	2.82	3.36	4.01
End-to-End	<u>2.30 ± 0.48</u>	2.80 ± 0.00	3.80 ± 0.04	4.17 ± 0.00
End-to-End + GradNorm	1.10 ± 0.03	2.80 ± 0.00	4.11 ± 0.30	4.17 ± 0.00
End-to-End + PcGrad	1.54 ± 0.53	2.80 ± 0.00	3.84 ± 0.05	4.16 ± 0.08
Multi-Head	2.08 ± 0.00	2.80 ± 0.00	4.06 ± 0.29	4.16 ± 0.00
Multi-Head + GradNorm	1.62 ± 0.61	2.38 ± 0.00	4.08 ± 0.32	<u>4.21 ± 0.05</u>
Multi-Head + PcGrad	1.22 ± 0.10	2.80 ± 0.00	4.19 ± 0.22	4.12 ± 0.02
Multiple Models	2.78 ± 0.00	2.80 ± 0.00	<u>4.40 ± 0.02</u>	4.16 ± 0.00
Multiple Models + COMs	2.30 ± 0.00	2.21 ± 0.17	4.14 ± 0.35	4.12 ± 0.05
Multiple Models + RoMA	1.65 ± 0.02	2.80 ± 0.00	4.13 ± 0.29	4.16 ± 0.01
Multiple Models + IOM	1.75 ± 0.33	2.80 ± 0.00	4.13 ± 0.28	4.17 ± 0.00
Multiple Models + ICT	1.37 ± 0.17	2.80 ± 0.00	4.41 ± 0.00	4.10 ± 0.07
Multiple Models + Tri-Mentoring	2.03 ± 0.00	2.80 ± 0.00	4.12 ± 0.29	4.06 ± 0.01
MOBO	2.22 ± 0.08	5.12 ± 0.17	3.77 ± 0.00	4.26 ± 0.00
MOBO-ParEGO	2.16 ± 0.00	<u>3.83 ± 0.00</u>	/	4.05 ± 0.02
MOBO-JES	2.10 ± 1.04	N/A	N/A	N/A

Offline Multi-Objective Optimization

Table 14. Hypervolume results for RE with 256 solutions and 100th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	RE21	RE22	RE23	RE24	RE25	RE31	RE32	RE33	RE34	RE35	RE36	RE37	RE41	RE42	RE61
$\mathcal{D}(\text{best})$	4.42	4.78	4.75	4.59	4.79	10.23	10.53	10.59	48.06	10.96	7.57	4.72	36.17	12.28	135.87
End-to-End	4.42 \pm 0.00	4.84 \pm 0.00	4.84 \pm 0.00	4.38 \pm 0.00	4.84 \pm 0.00	10.56 \pm 0.00	10.64 \pm 0.00	10.69 \pm 0.00	52.86 \pm 0.05	11.69 \pm 0.00	9.25 \pm 1.00	6.21 \pm 0.00	44.13 \pm 0.02	20.04 \pm 0.01	144.30 \pm 0.02
End-to-End + GradNorm	4.81 \pm 0.01	<u>4.84 \pm 0.00</u>	2.64 \pm 0.00	4.38 \pm 0.00	<u>4.84 \pm 0.00</u>	10.65 \pm 0.00	10.63 \pm 0.00	9.90 \pm 0.00	51.38 \pm 0.03	11.52 \pm 0.00	9.16 \pm 0.02	6.22 \pm 0.01	41.26 \pm 0.81	13.46 \pm 0.00	141.37 \pm 0.03
End-to-End + PcGrad	4.90 \pm 0.05	4.84 \pm 0.00	<u>4.84 \pm 0.00</u>	4.38 \pm 0.00	4.60 \pm 0.24	10.65 \pm 0.00	10.65 \pm 0.00	10.41 \pm 0.07	52.83 \pm 0.08	11.68 \pm 0.02	<u>10.02 \pm 0.00</u>	5.52 \pm 0.00	43.53 \pm 0.37	14.27 \pm 0.12	142.98 \pm 0.38
Multi-Head	4.57 \pm 0.15	4.84 \pm 0.00	4.74 \pm 0.00	4.78 \pm 0.00	4.60 \pm 0.24	10.65 \pm 0.00	10.64 \pm 0.00	<u>10.69 \pm 0.00</u>	52.93 \pm 0.01	11.74 \pm 0.00	6.76 \pm 0.00	5.78 \pm 0.05	44.06 \pm 0.02	20.71 \pm 0.29	141.28 \pm 1.13
Multi-Head + GradNorm	4.91 \pm 0.00	4.83 \pm 0.01	4.49 \pm 0.09	2.64 \pm 0.00	3.95 \pm 0.00	10.65 \pm 0.00	10.63 \pm 0.00	5.85 \pm 0.00	52.84 \pm 0.00	11.52 \pm 0.00	0.02 \pm 0.00	6.36 \pm 0.01	43.77 \pm 0.09	19.01 \pm 0.04	143.82 \pm 0.20
Multi-Head + PcGrad	4.91 \pm 0.01	4.84 \pm 0.00	4.27 \pm 0.12	4.83 \pm 0.00	4.35 \pm 0.00	7.66 \pm 0.00	10.08 \pm 0.00	10.61 \pm 0.00	52.84 \pm 0.02	11.60 \pm 0.08	9.95 \pm 0.14	6.42 \pm 0.00	43.80 \pm 0.08	20.39 \pm 0.45	142.22 \pm 0.38
Multiple Models	4.94 \pm 0.00	4.84 \pm 0.00	4.84 \pm 0.00	4.82 \pm 0.00	4.84 \pm 0.00	10.65 \pm 0.00	10.63 \pm 0.00	10.67 \pm 0.00	54.16 \pm 0.01	11.70 \pm 0.00	10.52 \pm 0.00	6.49 \pm 0.00	<u>44.09 \pm 0.12</u>	20.89 \pm 0.07	<u>144.20 \pm 0.02</u>
Multiple Models + COMs	4.20 \pm 0.38	4.84 \pm 0.00	4.79 \pm 0.01	4.59 \pm 0.00	4.84 \pm 0.00	5.28 \pm 5.28	10.64 \pm 0.00	10.56 \pm 0.03	50.57 \pm 1.05	11.55 \pm 0.02	8.96 \pm 0.02	5.99 \pm 0.03	40.84 \pm 0.30	15.12 \pm 0.32	141.00 \pm 0.81
Multiple Models + RoMA	4.92 \pm 0.00	4.84 \pm 0.00	4.84 \pm 0.00	4.79 \pm 0.02	4.69 \pm 0.00	10.65 \pm 0.00	10.65 \pm 0.00	10.66 \pm 0.00	52.73 \pm 0.02	11.78 \pm 0.00	8.08 \pm 0.40	6.49 \pm 0.01	43.80 \pm 0.08	19.53 \pm 0.21	143.61 \pm 0.20
Multiple Models + IOM	<u>4.94 \pm 0.00</u>	4.84 \pm 0.00	4.84 \pm 0.00	4.84 \pm 0.00	4.84 \pm 0.00	10.65 \pm 0.00	10.65 \pm 0.00	10.68 \pm 0.00	<u>54.12 \pm 0.02</u>	<u>11.75 \pm 0.01</u>	10.02 \pm 0.01	<u>6.54 \pm 0.00</u>	43.92 \pm 0.01	<u>20.78 \pm 0.02</u>	143.30 \pm 0.14
Multiple Models + ICT	4.75 \pm 0.17	4.84 \pm 0.00	2.77 \pm 0.00	4.67 \pm 0.00	4.84 \pm 0.00	10.65 \pm 0.00	10.65 \pm 0.00	10.51 \pm 0.00	53.53 \pm 0.01	11.70 \pm 0.02	8.94 \pm 0.01	6.25 \pm 0.07	43.96 \pm 0.11	20.59 \pm 0.20	143.11 \pm 0.23
Multiple Models + Tri-Mentoring	4.91 \pm 0.00	4.84 \pm 0.00	2.76 \pm 0.00	4.83 \pm 0.00	4.70 \pm 0.00	10.65 \pm 0.00	10.65 \pm 0.00	10.54 \pm 0.00	53.39 \pm 0.02	11.75 \pm 0.00	9.72 \pm 0.06	6.38 \pm 0.06	43.81 \pm 0.13	20.30 \pm 0.11	143.82 \pm 0.07
MOBO	4.66 \pm 0.06	4.84 \pm 0.00	4.84 \pm 0.00	4.83 \pm 0.00	4.84 \pm 0.00	10.19 \pm 0.00	10.69 \pm 0.00	52.05 \pm 0.00	11.75 \pm 0.00	/	6.60 \pm 0.00	/	16.03 \pm 0.43	N/A	N/A
MOBO-ParEGO	4.65 \pm 0.04	4.61 \pm 0.00	4.84 \pm 0.00	3.74 \pm 0.00	4.71 \pm 0.00	10.64 \pm 0.01	9.77 \pm 0.02	10.61 \pm 0.03	49.27 \pm 1.14	0.00 \pm 0.00	0.00 \pm 0.00	5.87 \pm 0.05	N/A	N/A	N/A
MOBO-JES	4.85 \pm 0.03	4.84 \pm 0.00	4.83 \pm 0.00	4.82 \pm 0.00	4.84 \pm 0.00	10.28 \pm 0.00	10.65 \pm 0.00	10.61 \pm 0.03	50.30 \pm 0.00	11.59 \pm 0.02	9.43 \pm 0.10	/	N/A	N/A	N/A

Table 15. Average rank of different offline MOO methods on each type of task with 256 solutions and 50th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	Synthetic	MO-NAS	MORL	MOCO	Sci-Design	RE	Average Rank
$\mathcal{D}(\text{best})$	8.20 \pm 0.30	9.45 \pm 0.03	1.75 \pm 0.25	1.08 \pm 0.00	4.62 \pm 0.12	10.07 \pm 0.33	7.11 \pm 0.12
End-to-End	8.00 \pm 0.31	7.47 \pm 0.21	9.75 \pm 2.25	7.14 \pm 0.53	8.62 \pm 0.88	6.23 \pm 0.17	7.33 \pm 0.18
End-to-End + GradNorm	8.81 \pm 0.31	8.05 \pm 0.16	5.75 \pm 1.75	8.41 \pm 0.82	7.62 \pm 0.12	9.40 \pm 0.00	8.55 \pm 0.14
End-to-End + PcGrad	8.11 \pm 0.17	7.87 \pm 0.39	9.25 \pm 0.25	7.86 \pm 0.61	7.06 \pm 0.44	7.57 \pm 0.57	7.91 \pm 0.19
Multi-Head	7.09 \pm 0.97	5.03 \pm 0.03	5.75 \pm 1.75	9.02 \pm 0.40	6.81 \pm 0.44	7.73 \pm 0.47	6.90 \pm 0.41
Multi-Head + GradNorm	8.08 \pm 0.42	10.33 \pm 0.06	13.00 \pm 0.50	8.81 \pm 0.50	11.62 \pm 0.38	9.80 \pm 0.33	9.56 \pm 0.08
Multi-Head + PcGrad	7.52 \pm 0.64	8.76 \pm 0.66	6.75 \pm 2.25	8.61 \pm 0.14	11.21 \pm 0.46	8.13 \pm 0.13	8.30 \pm 0.39
Multiple Models	3.89 \pm 0.42	3.96 \pm 0.41	9.00 \pm 0.50	7.18 \pm 0.57	8.94 \pm 0.94	4.20 \pm 0.33	4.98 \pm 0.05
Multiple Models + COMs	8.41 \pm 0.09	6.29 \pm 0.03	8.00 \pm 0.00	5.96 \pm 0.88	7.00 \pm 0.50	9.45 \pm 0.18	7.51 \pm 0.05
Multiple Models + RoMA	8.77 \pm 0.33	5.05 \pm 0.37	<u>4.00 \pm 0.00</u>	6.81 \pm 0.35	7.12 \pm 0.62	7.93 \pm 0.07	7.05 \pm 0.16
Multiple Models + IOM	5.80 \pm 0.39	4.39 \pm 0.82	<u>6.00 \pm 1.00</u>	<u>3.69 \pm 0.08</u>	6.75 \pm 0.38	4.93 \pm 0.40	4.89 \pm 0.33
Multiple Models + ICT	8.19 \pm 0.34	12.71 \pm 0.18	6.50 \pm 0.00	8.69 \pm 0.00	8.50 \pm 0.25	8.20 \pm 0.20	9.49 \pm 0.09
Multiple Models + Tri-Mentoring	7.45 \pm 0.08	11.92 \pm 0.18	6.75 \pm 0.25	8.42 \pm 0.19	8.25 \pm 0.00	5.10 \pm 0.23	8.35 \pm 0.10
MOBO	10.50 \pm 1.50	6.08 \pm 0.53	11.50 \pm 0.50	12.62 \pm 0.21	6.58 \pm 0.08	8.50 \pm 0.50	8.63 \pm 0.39
MOBO-ParEGO	9.06 \pm 0.19	10.80 \pm 0.62	N/A	14.56 \pm 0.00	3.17 \pm 0.17	12.27 \pm 0.44	10.93 \pm 0.06
MOBO-JES	11.45 \pm 0.45	14.00 \pm 1.00	N/A	N/A	14.00 \pm 0.00	10.17 \pm 0.08	11.02 \pm 0.19

Table 16. Hypervolume results for synthetic functions with 256 solutions and 50th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	DTLZ1	DTLZ2	DTLZ3	DTLZ4	DTLZ5	DTLZ6	DTLZ7	OmniTest	VLMOP1	VLMOP2	VLMOP3	ZDT1	ZDT2	ZDT3	ZDT4	ZDT6
$\mathcal{D}(\text{best})$	10.52	9.43	9.71	10.76	9.06	8.20	8.32	3.87	2.28	1.64	45.14	4.04	4.70	5.12	5.46	4.76
End-to-End	10.06 \pm 0.00	10.65 \pm 0.00	10.65 \pm 0.00	9.98 \pm 0.35	8.63 \pm 2.01	9.42 \pm 0.00	6.37 \pm 0.07	4.35 \pm 0.00	0.00 \pm 0.00	4.18 \pm 0.02	46.76 \pm 0.09	2.69 \pm 0.00	3.21 \pm 0.00	5.46 \pm 0.00	3.04 \pm 0.02	4.87 \pm 0.02
End-to-End + GradNorm	10.65 \pm 0.00	10.36 \pm 0.28	10.63 \pm 0.02	10.28 \pm 0.48	8.50 \pm 2.07	8.69 \pm 0.68	8.62 \pm 2.08	2.32 \pm 0.04	0.00 \pm 0.00	2.67 \pm 1.21	38.20 \pm 0.17	4.76 \pm 0.00	4.01 \pm 0.17	5.27 \pm 0.03	3.02 \pm 0.02	2.55 \pm 0.23
End-to-End + PcGrad	10.62 \pm 0.02	8.22 \pm 1.99	10.65 \pm 0.00	10.76 \pm 0.00	8.01 \pm 0.07	7.80 \pm 0.80	10.52 \pm 0.00	4.32 \pm 0.03	1.36 \pm 1.36	4.08 \pm 0.10	34.65 \pm 0.06	4.37 \pm 0.29	5.70 \pm 0.01	4.45 \pm 0.94	2.99 \pm 0.02	1.87 \pm 0.10
Multi-Head	10.37 \pm 0.24	10.64 \pm 0.01	10.63 \pm 0.01	10.14 \pm 0.19	6.62 \pm 0.00	9.39 \pm 0.03	10.61 \pm 0.09	4.29 \pm 0.05	0.95 \pm 0.95	4.18 \pm 0.01	46.78 \pm 0.16	2.69 \pm 0.00	4.48 \pm 1.27	<u>5.50 \pm 0.03</u>	2.94 \pm 0.08	4.90 \pm 0.00
Multi-Head + GradNorm	<u>10.64 \pm 0.00</u>	10.37 \pm 0.13	10.50 \pm 0.12	10.76 \pm 0.00	7.97 \pm 0.95	8.67 \pm 0.78	9.58 \pm 0.93	3.43 \pm 0.90	0.00 \pm 0.00	4.06 \pm 0.01	29.52 \pm 0.54	<u>4.82 \pm 0.01</u>	4.32 \pm 0.24	4.14 \pm 1.07	3.16 \pm 0.06	4.83 \pm 0.03
Multi-Head + PcGrad	10.61 \pm 0.01	10.64 \pm 0.00	10.58 \pm 0.04	10.76 \pm 0.00	6.73 \pm 0.51	9.22 \pm 0.13	10.36 \pm 0.02	4.34 \pm 0.00	1.47 \pm 1.47	2.66 \pm 1.21	45.33 \pm 1.58	2.69 \pm 0.01	5.68 \pm 0.04	5.38 \pm 0.02	3.49 \pm 0.18	2.06 \pm 0.15
Multiple Models	10.64 \pm 0.00	10.63 \pm 0.02	10.64 \pm 0.00	10.76 \pm 0.00	8.52 \pm 1.90	10.19 \pm 0.37	10.56 \pm 0.03	4.35 \pm 0.00	0.56 \pm 0.56	4.22 \pm 0.00	46.93 \pm 0.00	4.75 \pm 0.00	5.56 \pm 0.00	5.71 \pm 0.01	3.70 \pm 0.38	4.87 \pm 0.01
Multiple Models + COMs	10.55 \pm 0.04	9.83 \pm 0.37	9.76 \pm 0.10	10.72 \pm 0.03	9.93 \pm 0.22	9.10 \pm 0.65	8.73 \pm 0.01	3.85 \pm 0.21	0.00 \pm 0.00	1.68 \pm 0.01	46.03 \pm 0.26	3.82 \pm 0.16	4.66 \pm 0.11	5.44 \pm 0.07	4.31 \pm 0.05	4.33 \pm 0.01
Multiple Models + RoMA	10.53 \pm 0.06	10.47 \pm 0.05	10.62 \pm 0.01	10.76 \pm 0.00	6.63 \pm 0.01	10.57 \pm 0.02	10.01 \pm 0.08	2.60 \pm 0.01	0.00 \pm 0.00	1.46 \pm 0.00	40.48 \pm 0.34	4.86 \pm 0.01	5.62 \pm 0.01	5.40 \pm 0.18	2.87 \pm 0.09	1.76 \pm 0.02
Multiple Models + IOM	10.61 \pm 0.00	8.93 \pm 0.23	9.63 \pm 0.07	10.76 \pm 0.00	<u>9.66 \pm 0.36</u>	9.25 \pm 0.27	10.55 \pm 0.15	4.34 \pm 0.00	0.58 \pm 0.58	3.73 \pm 0.03	<u>46.92 \pm 0.00</u>	4.62 \pm 0.03	5.72 \pm 0.00	5.50 \pm 0.01	4.39 \pm 0.44	4.8

Table 18. Hypervolume results for MORL with 256 solutions and 50th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	MO-Hopper	MO-Swimmer
$\mathcal{D}(\text{best})$	<u>4.21</u>	2.85
End-to-End	3.68 ± 0.00	2.04 ± 0.10
End-to-End + GradNorm	3.94 ± 0.23	2.06 ± 0.00
End-to-End + PcGrad	3.72 ± 0.01	1.95 ± 0.00
Multi-Head	3.74 ± 0.07	<u>2.66 ± 0.04</u>
Multi-Head + GradNorm	3.67 ± 0.00	1.87 ± 0.00
Multi-Head + PcGrad	3.86 ± 0.18	2.08 ± 0.02
Multiple Models	3.76 ± 0.01	1.91 ± 0.02
Multiple Models + COMs	3.72 ± 0.02	1.97 ± 0.00
Multiple Models + RoMA	4.74 ± 0.00	2.00 ± 0.00
Multiple Models + IOM	4.17 ± 0.18	1.96 ± 0.06
Multiple Models + ICT	3.70 ± 0.01	2.38 ± 0.11
Multiple Models + Tri-Mentoring	3.82 ± 0.03	1.98 ± 0.01
MOBO	3.68 ± 0.00	/
MOBO-ParEGO	N/A	N/A
MOBO-JES	N/A	N/A

Table 19. Hypervolume results for MOCO with 256 solutions and 50th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	Bi-CVRP-20	Bi-CVRP-50	Bi-CVRP-100	Bi-KP-50	Bi-KP-100	Bi-KP-200	Bi-TSP-20	Bi-TSP-50	Bi-TSP-100	Bi-TSP-500	Tri-TSP-20	Tri-TSP-50	Tri-TSP-100
$\mathcal{D}(\text{best})$	5.37	5.11	4.91	3.00	3.45	4.68	5.05	4.89	4.55	4.52	11.88	9.82	<u>9.36</u>
End-to-End	3.48 ± 0.08	3.30 ± 0.22	4.14 ± 0.02	2.40 ± 0.03	1.87 ± 0.00	<u>3.69 ± 0.00</u>	2.54 ± 0.22	4.12 ± 0.01	3.83 ± 0.58	3.35 ± 0.01	4.70 ± 0.08	3.69 ± 0.04	6.27 ± 0.56
End-to-End + GradNorm	3.26 ± 0.05	2.93 ± 0.15	2.95 ± 0.02	2.23 ± 0.30	<u>2.35 ± 0.22</u>	1.90 ± 0.00	2.26 ± 0.10	3.21 ± 0.27	3.03 ± 0.18	4.19 ± 0.06	4.84 ± 0.36	4.66 ± 0.30	8.02 ± 0.11
End-to-End + PcGrad	3.15 ± 0.07	3.39 ± 0.05	3.14 ± 0.24	2.02 ± 0.05	<u>1.95 ± 0.04</u>	2.35 ± 0.00	2.29 ± 0.03	3.86 ± 0.24	3.32 ± 0.02	3.65 ± 0.09	7.04 ± 1.00	5.06 ± 0.93	8.50 ± 0.48
Multi-Head	3.09 ± 0.11	3.21 ± 0.01	3.84 ± 0.26	<u>2.45 ± 0.01</u>	1.75 ± 0.04	2.49 ± 0.00	2.45 ± 0.07	4.00 ± 0.08	3.25 ± 0.05	3.04 ± 0.09	3.90 ± 0.14	4.22 ± 0.14	6.29 ± 0.94
Multi-Head + GradNorm	3.10 ± 0.14	3.12 ± 0.22	2.64 ± 0.16	2.21 ± 0.02	2.18 ± 0.17	2.20 ± 0.17	3.23 ± 0.05	2.80 ± 0.04	3.08 ± 0.27	3.18 ± 0.03	4.50 ± 0.09	5.43 ± 0.47	6.52 ± 0.51
Multi-Head + PcGrad	2.97 ± 0.15	3.11 ± 0.03	2.97 ± 0.03	2.33 ± 0.03	2.06 ± 0.14	2.35 ± 0.00	2.24 ± 0.02	3.20 ± 0.05	3.20 ± 0.01	2.27 ± 0.78	6.97 ± 0.02	4.75 ± 0.27	9.39 ± 0.00
Multiple Models	3.37 ± 0.03	3.38 ± 0.13	4.24 ± 0.03	2.42 ± 0.05	2.07 ± 0.01	2.47 ± 0.00	2.45 ± 0.09	2.48 ± 0.20	3.40 ± 0.19	<u>4.34 ± 0.03</u>	4.32 ± 0.13	4.63 ± 0.20	6.34 ± 0.42
Multiple Models + COMs	<u>3.89 ± 0.00</u>	3.49 ± 0.14	3.27 ± 0.22	2.14 ± 0.03	2.10 ± 0.06	2.30 ± 0.00	3.06 ± 0.05	3.93 ± 0.05	3.35 ± 0.20	3.71 ± 0.13	7.18 ± 0.37	5.88 ± 0.92	7.31 ± 0.23
Multiple Models + RoMA	3.23 ± 0.03	3.41 ± 0.08	2.95 ± 0.05	2.17 ± 0.13	2.01 ± 0.09	2.49 ± 0.03	2.90 ± 0.14	3.60 ± 0.20	3.84 ± 0.03	1.53 ± 0.03	6.08 ± 0.11	6.04 ± 0.07	7.67 ± 0.11
Multiple Models + IOM	3.50 ± 0.22	<u>3.54 ± 0.02</u>	<u>4.55 ± 0.14</u>	2.15 ± 0.03	2.02 ± 0.02	2.45 ± 0.10	<u>3.62 ± 0.30</u>	<u>4.54 ± 0.03</u>	<u>4.33 ± 0.03</u>	4.01 ± 0.26	<u>9.25 ± 0.08</u>	<u>9.07 ± 0.21</u>	9.17 ± 0.05
Multiple Models + ICT	3.16 ± 0.02	3.23 ± 0.20	3.19 ± 0.04	2.01 ± 0.15	2.03 ± 0.22	2.46 ± 0.11	2.67 ± 0.01	2.89 ± 0.11	2.97 ± 0.08	3.38 ± 0.10	4.72 ± 0.16	5.71 ± 0.04	5.96 ± 0.20
Multiple Models + Tri-Mentoring	3.10 ± 0.06	3.03 ± 0.01	3.26 ± 0.20	2.25 ± 0.02	1.97 ± 0.00	2.35 ± 0.31	2.69 ± 0.03	2.98 ± 0.26	3.57 ± 0.16	3.31 ± 0.14	4.53 ± 0.30	5.74 ± 0.35	5.65 ± 0.18
MOBO	2.77 ± 0.05	2.26 ± 0.14	1.42 ± 0.07	2.38 ± 0.05	1.97 ± 0.12	<u>2.04 ± 0.07</u>	2.14 ± 0.24	1.61 ± 0.05	1.51 ± 0.05	/	3.47 ± 0.16	2.69 ± 0.03	2.20 ± 0.07
MOBO-ParEGO	2.79 ± 0.01	2.21 ± 0.01	<u>1.20 ± 0.01</u>	/	/	N/A	2.18 ± 0.07	1.71 ± 0.01	<u>1.52 ± 0.00</u>	N/A	3.52 ± 0.09	2.70 ± 0.02	2.11 ± 0.02
MOBO-JES	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A

Table 20. Hypervolume results for Sci-Design with 256 solutions and 50th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	Molecule	Regex	RFP	ZINC
$\mathcal{D}(\text{best})$	2.26	2.82	3.36	4.01
End-to-End	1.07 ± 0.07	2.05 ± 0.00	3.64 ± 0.05	3.95 ± 0.04
End-to-End + GradNorm	1.07 ± 0.07	2.05 ± 0.00	3.73 ± 0.04	3.92 ± 0.00
End-to-End + PcGrad	<u>2.12 ± 0.04</u>	2.05 ± 0.00	3.70 ± 0.05	3.89 ± 0.06
Multi-Head	2.08 ± 0.00	2.05 ± 0.00	3.74 ± 0.00	3.86 ± 0.02
Multi-Head + GradNorm	1.00 ± 0.00	2.05 ± 0.00	3.69 ± 0.01	3.82 ± 0.01
Multi-Head + PcGrad	1.00 ± 0.00	2.05 ± 0.00	3.68 ± 0.02	3.86 ± 0.01
Multiple Models	1.10 ± 0.09	2.05 ± 0.00	3.70 ± 0.01	3.84 ± 0.00
Multiple Models + COMs	1.76 ± 0.14	2.38 ± 0.33	3.70 ± 0.00	3.86 ± 0.02
Multiple Models + RoMA	1.03 ± 0.00	2.05 ± 0.00	3.79 ± 0.04	3.91 ± 0.02
Multiple Models + IOM	1.02 ± 0.01	2.05 ± 0.00	<u>3.76 ± 0.03</u>	3.91 ± 0.02
Multiple Models + ICT	1.02 ± 0.02	2.05 ± 0.00	3.67 ± 0.00	3.96 ± 0.07
Multiple Models + Tri-Mentoring	1.41 ± 0.17	2.05 ± 0.00	3.75 ± 0.03	3.75 ± 0.00
MOBO	1.02 ± 0.02	<u>3.42 ± 0.25</u>	/	3.90 ± 0.01
MOBO-ParEGO	1.84 ± 0.00	3.44 ± 0.00	/	<u>4.00 ± 0.03</u>
MOBO-JES	1.00 ± 0.00	N/A	N/A	N/A

Offline Multi-Objective Optimization

Table 21. Hypervolume results for RE with 256 solutions and 50th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	RE21	RE22	RE23	RE24	RE25	RE31	RE32	RE33	RE34	RE35	RE36	RE37	RE41	RE42	RE61
$\mathcal{D}(\text{best})$	4.42	4.78	4.75	4.59	4.79	10.23	10.53	10.59	48.06	10.96	7.57	4.72	36.17	12.28	135.87
End-to-End	4.42 \pm 0.00	4.84 \pm 0.00	4.84 \pm 0.00	4.38 \pm 0.00	4.73 \pm 0.04	10.56 \pm 0.00	10.64 \pm 0.00	10.68 \pm 0.00	50.27 \pm 0.40	11.69 \pm 0.00	8.86 \pm 0.79	4.67 \pm 0.35	43.75 \pm 0.07	19.89 \pm 0.05	143.86 \pm 0.14
End-to-End + GradNorm	4.39 \pm 0.02	<u>4.84 \pm 0.00</u>	2.64 \pm 0.00	4.29 \pm 0.00	4.84 \pm 0.00	10.65 \pm 0.00	10.61 \pm 0.00	9.72 \pm 0.03	47.25 \pm 3.23	11.47 \pm 0.01	5.74 \pm 0.00	6.02 \pm 0.07	40.63 \pm 1.01	13.46 \pm 0.00	137.59 \pm 3.59
End-to-End + PcGrad	4.61 \pm 0.32	4.52 \pm 0.32	<u>4.84 \pm 0.00</u>	4.22 \pm 0.02	4.35 \pm 0.00	<u>10.65 \pm 0.00</u>	10.64 \pm 0.00	9.86 \pm 0.36	52.17 \pm 0.55	11.67 \pm 0.01	9.46 \pm 0.03	4.00 \pm 0.18	41.87 \pm 0.01	15.81 \pm 1.68	140.21 \pm 2.41
Multi-Head	4.56 \pm 0.14	4.83 \pm 0.01	4.59 \pm 0.10	4.11 \pm 0.01	3.82 \pm 0.30	10.64 \pm 0.00	10.64 \pm 0.00	10.47 \pm 0.22	51.24 \pm 0.12	11.73 \pm 0.00	6.76 \pm 0.00	4.43 \pm 0.01	<u>43.62 \pm 0.02</u>	20.20 \pm 0.15	140.38 \pm 0.56
Multi-Head + GradNorm	4.84 \pm 0.01	3.75 \pm 0.06	3.70 \pm 0.09	2.64 \pm 0.00	3.14 \pm 0.01	10.65 \pm 0.00	10.62 \pm 0.01	6.12 \pm 0.49	52.50 \pm 0.14	11.51 \pm 0.00	0.02 \pm 0.00	5.90 \pm 0.44	<u>43.41 \pm 0.16</u>	15.25 \pm 1.79	142.41 \pm 0.63
Multi-Head + PcGrad	4.79 \pm 0.03	4.84 \pm 0.00	3.42 \pm 0.57	3.77 \pm 0.00	4.35 \pm 0.00	7.64 \pm 0.00	10.08 \pm 0.00	10.11 \pm 0.35	52.48 \pm 0.05	11.50 \pm 0.00	9.64 \pm 0.00	6.32 \pm 0.05	43.60 \pm 0.02	19.69 \pm 0.96	139.81 \pm 2.17
Multiple Models	4.93 \pm 0.00	4.84 \pm 0.00	4.84 \pm 0.00	4.79 \pm 0.01	4.83 \pm 0.01	10.63 \pm 0.00	10.63 \pm 0.00	9.62 \pm 0.62	54.02 \pm 0.00	11.65 \pm 0.01	10.31 \pm 0.03	6.45 \pm 0.01	42.97 \pm 0.42	20.55 \pm 0.01	143.59 \pm 0.17
Multiple Models + COMs	3.90 \pm 0.10	4.83 \pm 0.00	4.76 \pm 0.02	4.59 \pm 0.00	<u>4.84 \pm 0.00</u>	5.28 \pm 5.28	10.62 \pm 0.00	10.26 \pm 0.31	48.14 \pm 2.03	11.41 \pm 0.02	8.18 \pm 0.15	5.68 \pm 0.20	39.96 \pm 0.64	13.00 \pm 0.46	138.74 \pm 0.89
Multiple Models + RoMA	4.88 \pm 0.00	4.84 \pm 0.00	4.83 \pm 0.00	3.66 \pm 0.01	3.40 \pm 0.01	10.60 \pm 0.00	10.64 \pm 0.00	10.11 \pm 0.05	50.37 \pm 0.46	11.76 \pm 0.01	3.76 \pm 0.05	<u>6.37 \pm 0.04</u>	43.33 \pm 0.04	17.14 \pm 0.23	131.51 \pm 4.58
Multiple Models + IOM	<u>4.93 \pm 0.01</u>	4.84 \pm 0.00	4.81 \pm 0.02	4.28 \pm 0.01	4.14 \pm 0.01	10.65 \pm 0.00	10.65 \pm 0.00	<u>10.64 \pm 0.03</u>	<u>53.83 \pm 0.06</u>	11.68 \pm 0.05	9.33 \pm 0.09	6.33 \pm 0.08	42.93 \pm 0.11	<u>20.54 \pm 0.02</u>	141.76 \pm 0.13
Multiple Models + ICT	4.70 \pm 0.15	4.84 \pm 0.00	2.76 \pm 0.00	3.23 \pm 0.00	4.74 \pm 0.00	10.62 \pm 0.01	2.77 \pm 0.00	9.80 \pm 0.50	53.26 \pm 0.07	11.68 \pm 0.04	8.00 \pm 0.16	6.14 \pm 0.09	43.33 \pm 0.15	16.04 \pm 0.41	142.65 \pm 0.50
Multiple Models + Tri-Mentoring	4.89 \pm 0.01	4.84 \pm 0.00	2.76 \pm 0.00	4.81 \pm 0.01	4.70 \pm 0.00	10.65 \pm 0.00	<u>10.65 \pm 0.00</u>	10.54 \pm 0.00	50.66 \pm 0.02	<u>11.75 \pm 0.00</u>	8.47 \pm 0.15	6.35 \pm 0.07	43.25 \pm 0.23	18.95 \pm 0.91	143.33 \pm 0.31
MOBO	/	/	/	/	/	/	/	/	/	/	/	/	/	/	/
MOBO-ParEGO	4.44 \pm 0.15	4.21 \pm 0.40	4.75 \pm 0.01	0.00 \pm 0.00	4.12 \pm 0.29	5.31 \pm 5.31	8.82 \pm 0.37	10.46 \pm 0.09	43.07 \pm 0.74	0.00 \pm 0.00	0.00 \pm 0.00	5.52 \pm 0.04	N/A	N/A	N/A
MOBO-JES	3.89 \pm 0.03	4.57 \pm 0.03	4.66 \pm 0.05	4.54 \pm 0.00	4.80 \pm 0.00	10.01 \pm 0.01	10.63 \pm 0.01	10.52 \pm 0.03	48.52 \pm 0.00	11.12 \pm 0.03	6.46 \pm 0.34	5.24 \pm 0.17	N/A	N/A	N/A

Table 22. Average rank of different offline MOO methods on each type of task with 32 solutions and 100th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	Synthetic	MO-NAS	MORL	MOCO	Sci-Design	RE	Average Rank
$\mathcal{D}(\text{best})$	10.66 \pm 0.16	9.11 \pm 0.32	3.50 \pm 0.50	1.23 \pm 0.15	6.12 \pm 0.12	12.37 \pm 0.03	8.30 \pm 0.13
End-to-End	6.69 \pm 0.06	5.89 \pm 0.11	6.50 \pm 1.00	5.31 \pm 0.54	3.06 \pm 0.31	8.13 \pm 0.13	6.31 \pm 0.09
End-to-End + GradNorm	7.33 \pm 0.05	6.76 \pm 0.18	5.25 \pm 1.25	7.92 \pm 0.08	10.54 \pm 0.21	10.03 \pm 0.50	8.01 \pm 0.02
End-to-End + PcGrad	7.58 \pm 0.64	6.18 \pm 0.24	<u>3.25 \pm 0.75</u>	6.88 \pm 0.04	5.52 \pm 0.35	7.97 \pm 0.03	6.96 \pm 0.21
Multi-Head	6.05 \pm 0.27	5.34 \pm 0.66	10.00 \pm 0.50	7.63 \pm 0.37	4.94 \pm 0.44	8.07 \pm 0.00	6.65 \pm 0.06
Multi-Head + GradNorm	7.55 \pm 0.17	7.74 \pm 0.21	9.50 \pm 0.50	10.69 \pm 0.23	11.75 \pm 0.50	9.70 \pm 0.70	8.96 \pm 0.33
Multi-Head + PcGrad	8.05 \pm 0.27	6.28 \pm 0.28	8.50 \pm 1.50	8.49 \pm 0.42	9.50 \pm 0.12	7.40 \pm 0.13	7.59 \pm 0.26
Multiple Models	4.98 \pm 0.14	3.76 \pm 0.50	10.00 \pm 0.50	5.42 \pm 0.58	9.25 \pm 0.00	5.45 \pm 0.08	<u>5.22 \pm 0.02</u>
Multiple Models + COMs	8.31 \pm 0.06	<u>4.75 \pm 0.31</u>	1.50 \pm 0.00	5.46 \pm 0.38	9.00 \pm 1.00	9.45 \pm 0.05	<u>6.93 \pm 0.07</u>
Multiple Models + RoMA	8.52 \pm 0.27	5.15 \pm 0.22	6.00 \pm 0.00	8.54 \pm 0.92	7.50 \pm 0.12	7.13 \pm 0.40	7.29 \pm 0.39
Multiple Models + IOM	6.44 \pm 0.09	4.77 \pm 0.15	6.75 \pm 1.25	<u>3.17 \pm 0.21</u>	5.06 \pm 0.44	3.87 \pm 0.13	4.69 \pm 0.05
Multiple Models + ICT	7.45 \pm 0.35	10.30 \pm 0.20	6.25 \pm 0.25	9.66 \pm 0.11	<u>4.88 \pm 1.25</u>	7.43 \pm 0.10	8.33 \pm 0.04
Multiple Models + Tri-Mentoring	5.92 \pm 0.52	9.39 \pm 1.35	10.50 \pm 0.00	10.15 \pm 0.23	6.88 \pm 0.00	6.30 \pm 0.30	7.88 \pm 0.05
MOBO	<u>9.57 \pm 0.00</u>	/	/	13.15 \pm 0.69	6.50 \pm 0.50	8.00 \pm 0.17	10.68 \pm 0.25
MOBO-ParEGO	7.38 \pm 0.38	11.00 \pm 1.00	N/A	13.70 \pm 0.50	/	<u>5.17 \pm 0.00</u>	8.95 \pm 0.16
MOBO-JES	11.21 \pm 0.01	13.50 \pm 0.50	N/A	N/A	7.00 \pm 5.00	7.29 \pm 0.12	9.12 \pm 0.30

Table 23. Hypervolume results for synthetic functions with 32 solutions and 100th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	DTLZ1	DTLZ2	DTLZ3	DTLZ4	DTLZ5	DTLZ6	DTLZ7	OmniTest	VLMOP1	VLMOP2	VLMOP3	ZDT1	ZDT2	ZDT3	ZDT4	ZDT6
$\mathcal{D}(\text{best})$	10.52	9.43	9.71	10.76	9.06	8.20	8.32	3.87	2.28	1.64	45.14 \pm 0.87	4.04	4.70	5.12	5.46	4.76
End-to-End	10.64 \pm 0.00	10.65 \pm 0.00	10.64 \pm 0.00	10.76 \pm 0.00	10.64 \pm 0.01	10.62 \pm 0.03	10.60 \pm 0.09	4.35 \pm 0.00	2.54 \pm 2.25	4.05 \pm 0.05	46.90 \pm 0.01	2.70 \pm 0.00	3.19 \pm 0.01	5.33 \pm 0.03	3.72 \pm 0.36	4.90 \pm 0.00
End-to-End + GradNorm	10.63 \pm 0.01	10.64 \pm 0.01	10.65 \pm 0.00	10.76 \pm 0.00	10.54 \pm 0.09	10.64 \pm 0.00	10.71 \pm 0.00	3.76 \pm 0.03	1.26 \pm 1.08	2.79 \pm 1.34	42.23 \pm 0.98	4.77 \pm 0.01	5.63 \pm 0.02	5.22 \pm 0.02	3.23 \pm 0.03	4.73 \pm 0.11
End-to-End + PcGrad	10.63 \pm 0.01	10.57 \pm 0.04	10.65 \pm 0.00	10.76 \pm 0.00	9.02 \pm 0.10	9.45 \pm 0.15	10.52 \pm 0.00	4.35 \pm 0.00	4.80 \pm 0.02	4.06 \pm 0.01	46.79 \pm 0.06	4.84 \pm 0.01	5.70 \pm 0.01	5.45 \pm 0.00	3.12 \pm 0.01	2.04 \pm 0.22
Multi-Head	10.37 \pm 0.26	10.65 \pm 0.00	10.64 \pm 0.00	10.76 \pm 0.00	10.61 \pm 0.03	10.65 \pm 0.00	10.52 \pm 0.00	4.24 \pm 0.00	2.57 \pm 2.25	4.08 \pm 0.01	46.93 \pm 0.00	2.72 \pm 0.00	5.72 \pm 0.00	5.41 \pm 0.10	3.70 \pm 0.23	4.87 \pm 0.01
Multi-Head + GradNorm	10.62 \pm 0.01	10.63 \pm 0.01	10.64 \pm 0.00	10.76 \pm 0.00	9.29 \pm 0.86	10.62 \pm 0.02	10.61 \pm 0.10	4.33 \pm 0.00	0.00 \pm 0.00	4.13 \pm 0.03	46.64 \pm 0.22	4.83 \pm 0.00	5.68 \pm 0.05	5.26 \pm 0.04	3.39 \pm 0.00	4.87 \pm 0.00
Multi-Head + PcGrad	10.63 \pm 0.00	10.63 \pm 0.00	10.61 \pm 0.03	10.76 \pm 0.00	9.08 \pm 0.35	10.59 \pm 0.01	10.49 \pm 0.01	4.35 \pm 0.00	4.80 \pm 0.01	3.99 \pm 0.01	46.91 \pm 0.00	2.72 \pm 0.04	5.69 \pm 0.03	5.45 \pm 0.00	3.64 \pm 0.17	2.05 \pm 0.18
Multiple Models	10.61 \pm 0.01	10.64 \pm 0.00	10.65 \pm 0.00	10.76 \pm 0.00	10.63 \pm 0.01	10.65 \pm 0.00	10.67 \pm 0.03	4.35 \pm 0.00	2.52 \pm 2.21	4.09 \pm 0.02	46.97 \pm 0.00	4.80 \pm 0.03	5.51 \pm 0.01	5.51 \pm 0.14	4.26 \pm 0.07	4.88 \pm 0.00
Multiple Models + COMs	10.63 \pm 0.00	10.48 \pm 0.08	10.55 \pm 0.04	10.76 \pm 0.00	9.14 \pm 0.44	9.50 \pm 0.15	9.14 \pm 0.10	4.41 \pm 0.00	4.78 \pm 0.01	4.87 \pm 0.00	46.81 \pm 0.12	4.21 \pm 0.07	4.85 \pm 0.02	5.25 \pm 0.24	3.99 \pm 0.10	4.59 \pm 0.02
Multiple Models + RoMA	10.63 \pm 0.01	10.57 \pm 0.03	10.64 \pm 0.00	10.76 \pm 0.00	9.10 \pm 0.48	10.60 \pm 0.00	10.12 \pm 0.05	3.97 \pm 0.06	4.78 \pm 0.01	1.46 \pm 0.00	44.15 \pm 2.36	4.83 \pm 0.01	5.65 \pm 0.00	5.80 \pm 0.00	3.18 \pm 0.05	1.84 \pm 0.07
Multiple Models + IOM	10.62 \pm 0.01	10.56 \pm 0.08	10.46 \pm 0.02	10.76 \pm 0.00	10.08 \pm 0.04	10.15 \pm 0.45	10.48 \pm 0.00	4.41 \pm 0.00	4.79 \pm 0.00	3.29 \pm 1.58	46.97 \pm 0.00	4.73 \pm 0.00	5.45 \pm 0.02	5.52 \pm 0.05	4.84 \pm 0.00	4.87 \pm 0.02
Multiple Models + ICT	10.63 \pm 0.00	10.62 \pm 0.01	10.56 \pm 0.09	10.76 \pm 0.00	7.98 \pm 0.53	10.61 \pm 0.01	10.54 \pm 0.00	4.35 \pm 0.00	4.80 \pm 0.01	3.99 \pm 0.01	46.97 \pm 0.00	4.73 \pm 0.15	5.70 \pm 0.01	5.45 \pm 0.08	3.84 \pm 0.06	2.96 \pm 0.56
Multiple Models + Tri-Mentoring	10.63 \pm 0.01	10.65 \pm 0.00	10.63 \pm 0.01	10.76 \pm 0.00	9.48 \pm 0.20	10.62 \pm 0.02	10.58 \pm 0.08	4.41 \pm 0.00	4.82 \pm 0.00	1.46 \pm 0.00	46.97 \pm 0.00	4.51 \pm 0.01	5.55 \pm 0.01	5.59 \pm 0.06	4.84 \pm 0.00	2.31 \pm 0.01
MOBO	/	/	/	/	/	/	10.34 \pm 0.01	/	/	/	/	/	/	/	/	/
MOBO-ParEGO	/	/	/	10.76 \pm 0.00	/	/	/	/	/	/	/	46.92 \pm 0.01	/	/	/	/
MOBO-JES	10.61 \pm 0.00	/	/	/	/	/	9.36 \pm 0.08	3.87 \pm 0.00	/	1.46 \pm 0.00	46.88 \pm 0.00	3.97 \pm 0.09	4.44 \pm 0.07	5.17 \pm 0.02	4.43 \pm 0.08	3.09 \pm 0.02

Table 25. Hypervolume results for MORL with 32 solutions and 100th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	MO-Hopper	MO-Swimmer
$\mathcal{D}(\text{best})$	4.21	2.85
End-to-End	4.04 ± 0.24	2.56 ± 0.13
End-to-End + GradNorm	4.42 ± 0.36	2.65 ± 0.00
End-to-End + PcGrad	4.51 ± 0.27	2.75 ± 0.00
Multi-Head	3.81 ± 0.04	2.36 ± 0.13
Multi-Head + GradNorm	3.71 ± 0.03	2.55 ± 0.00
Multi-Head + PcGrad	4.40 ± 0.24	2.18 ± 0.19
Multiple Models	3.87 ± 0.00	2.28 ± 0.11
Multiple Models + COMs	<u>4.90</u> <u>± 0.06</u>	<u>2.81</u> <u>± 0.00</u>
Multiple Models + RoMA	4.18 ± 0.03	/
Multiple Models + IOM	<u>4.63</u> <u>± 0.33</u>	2.23 ± 0.02
Multiple Models + ICT	3.95 ± 0.03	2.69 ± 0.02
Multiple Models + Tri-Mentoring	3.70 ± 0.01	2.41 ± 0.02
MOBO	/	/
MOBO-ParEGO	N/A	N/A
MOBO-JES	N/A	N/A

Table 26. Hypervolume results for MOCO with 32 solutions and 100th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	Bi-CVRP-20	Bi-CVRP-50	Bi-CVRP-100	Bi-KP-50	Bi-KP-100	Bi-KP-200	Bi-TSP-20	Bi-TSP-50	Bi-TSP-100	Bi-TSP-500	Tri-TSP-20	Tri-TSP-50	Tri-TSP-100
$\mathcal{D}(\text{best})$	5.37	5.11	<u>4.91</u>	3.00	3.45	4.68	5.05	4.89	4.55	4.52	11.88	9.82	9.36
End-to-End	5.05 ± 0.17	4.30 ± 0.12	4.53 ± 0.36	2.70 ± 0.04	2.33 ± 0.30	3.37 ± 0.00	3.44 ± 0.03	4.68 ± 0.12	<u>4.48</u> <u>± 0.02</u>	<u>4.48</u> <u>± 0.05</u>	6.87 ± 1.32	5.56 ± 0.70	<u>9.07</u> <u>± 0.04</u>
End-to-End + GradNorm	4.02 ± 0.27	3.75 ± 0.21	3.63 ± 0.00	2.67 ± 0.01	2.67 ± 0.02	2.69 ± 0.00	3.06 ± 0.30	3.87 ± 0.13	3.53 ± 0.00	4.11 ± 0.16	5.61 ± 0.01	6.29 ± 0.00	8.47 ± 0.12
End-to-End + PcGrad	3.59 ± 0.17	3.52 ± 0.40	3.63 ± 0.12	2.75 ± 0.00	2.58 ± 0.22	2.84 ± 0.15	3.14 ± 0.24	4.49 ± 0.02	4.18 ± 0.17	3.98 ± 0.02	9.31 ± 0.08	8.11 ± 0.00	8.54 ± 0.18
Multi-Head	4.65 ± 0.00	3.75 ± 0.12	4.88 ± 0.01	2.73 ± 0.03	2.45 ± 0.14	2.99 ± 0.24	3.10 ± 0.14	4.50 ± 0.02	3.48 ± 0.32	3.19 ± 0.04	5.14 ± 0.05	6.65 ± 1.16	8.34 ± 0.32
Multi-Head + GradNorm	3.77 ± 0.33	3.21 ± 0.07	3.04 ± 0.17	2.29 ± 0.16	2.24 ± 0.22	1.64 ± 0.00	3.69 ± 0.08	3.23 ± 0.01	3.27 ± 0.17	3.18 ± 0.08	5.96 ± 0.47	5.53 ± 0.30	6.73 ± 0.00
Multi-Head + PcGrad	4.22 ± 0.23	3.53 ± 0.73	3.09 ± 0.05	2.81 ± 0.00	2.35 ± 0.12	3.54 ± 0.00	3.78 ± 1.21	2.91 ± 0.15	3.26 ± 0.08	3.03 ± 0.20	6.93 ± 1.64	6.73 ± 0.27	8.67 ± 0.20
Multiple Models	5.01 ± 0.27	4.64 ± 0.13	4.62 ± 0.27	<u>2.84</u> <u>± 0.10</u>	<u>2.73</u> <u>± 0.27</u>	<u>3.63</u> <u>± 0.58</u>	2.71 ± 0.03	4.12 ± 0.54	4.23 ± 0.00	4.45 ± 0.00	6.36 ± 1.17	7.16 ± 0.68	8.65 ± 0.68
Multiple Models + COMs	<u>5.28</u> <u>± 0.00</u>	4.21 ± 0.23	3.52 ± 0.24	2.66 ± 0.02	2.73 ± 0.07	2.79 ± 0.38	4.60 ± 0.15	4.63 ± 0.07	3.96 ± 0.24	3.76 ± 0.15	<u>10.28</u> <u>± 0.86</u>	8.07 ± 0.15	8.11 ± 0.02
Multiple Models + RoMA	4.63 ± 0.11	3.55 ± 0.03	3.03 ± 0.20	2.57 ± 0.08	2.51 ± 0.33	2.38 ± 0.13	4.14 ± 0.11	3.72 ± 0.42	3.85 ± 0.23	1.76 ± 0.07	8.40 ± 0.76	5.89 ± 0.72	7.85 ± 0.69
Multiple Models + IOM	5.28 ± 0.00	<u>5.11</u> <u>± 0.00</u>	<u>4.92</u> <u>± 0.00</u>	2.64 ± 0.12	2.68 ± 0.23	3.39 ± 0.22	<u>4.86</u> <u>± 0.01</u>	<u>4.70</u> <u>± 0.01</u>	4.46 ± 0.06	4.00 ± 0.36	9.79 ± 0.09	<u>8.91</u> <u>± 0.24</u>	9.01 ± 0.37
Multiple Models + ICT	3.55 ± 0.17	4.01 ± 0.01	4.01 ± 0.37	2.36 ± 0.15	2.12 ± 0.00	2.31 ± 0.15	<u>3.37</u> <u>± 0.21</u>	<u>3.09</u> <u>± 0.18</u>	3.13 ± 0.07	4.11 ± 0.00	5.60 ± 0.15	<u>6.12</u> <u>± 0.25</u>	5.85 ± 0.20
Multiple Models + Tri-Mentoring	3.48 ± 0.20	3.82 ± 0.05	3.65 ± 0.00	2.04 ± 0.04	2.44 ± 0.11	2.45 ± 0.31	3.19 ± 0.20	2.99 ± 0.33	3.31 ± 0.10	3.34 ± 0.05	5.85 ± 0.97	6.15 ± 0.44	5.70 ± 0.19
MOBO	3.19 ± 0.38	2.50 ± 0.04	1.34 ± 0.02	2.54 ± 0.21	2.17 ± 0.14	2.08 ± 0.05	2.33 ± 0.08	1.81 ± 0.09	<u>1.62</u> <u>± 0.01</u>	1.26 ± 0.00	4.18 ± 0.37	3.20 ± 0.04	2.20 ± 0.09
MOBO-ParEGO	3.45 ± 0.03	2.63 ± 0.00	1.46 ± 0.01	/	/	N/A	/	<u>1.96</u> <u>± 0.01</u>	/	N/A	/	3.14 ± 0.01	/
MOBO-JES	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A	N/A

Table 27. Hypervolume results for Sci-Design with 32 solutions and 100th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	Molecule	Regex	RFP	ZINC
$\mathcal{D}(\text{best})$	2.26	2.82	3.36	4.01
End-to-End	1.95 ± 0.13	<u>2.80</u> <u>± 0.00</u>	4.34 ± 0.03	<u>4.12</u> <u>± 0.01</u>
End-to-End + GradNorm	1.05 ± 0.00	2.38 ± 0.00	3.46 ± 0.08	4.00 ± 0.01
End-to-End + PcGrad	3.33 ± 0.00	2.47 ± 0.00	3.62 ± 0.00	4.04 ± 0.04
Multi-Head	2.20 ± 0.38	2.80 ± 0.00	3.67 ± 0.00	4.12 ± 0.00
Multi-Head + GradNorm	1.06 ± 0.05	2.38 ± 0.00	3.67 ± 0.00	3.82 ± 0.00
Multi-Head + PcGrad	1.04 ± 0.00	2.47 ± 0.00	3.71 ± 0.00	3.92 ± 0.00
Multiple Models	1.19 ± 0.14	2.38 ± 0.00	3.70 ± 0.00	4.01 ± 0.01
Multiple Models + COMs	2.16 ± 0.09	2.05 ± 0.00	3.65 ± 0.00	3.97 ± 0.10
Multiple Models + RoMA	1.84 ± 0.10	2.47 ± 0.00	3.71 ± 0.00	3.95 ± 0.00
Multiple Models + IOM	1.72 ± 0.36	2.47 ± 0.00	<u>4.06</u> <u>± 0.35</u>	4.08 ± 0.03
Multiple Models + ICT	<u>2.65</u> <u>± 1.31</u>	2.47 ± 0.00	3.76 ± 0.00	4.05 ± 0.02
Multiple Models + Tri-Mentoring	2.03 ± 0.00	2.47 ± 0.00	3.75 ± 0.00	3.94 ± 0.00
MOBO	1.15 ± 0.02	/	/	4.18 ± 0.08
MOBO-ParEGO	/	/	/	/
MOBO-JES	2.10 ± 1.04	N/A	N/A	N/A

Table 28. Hypervolume results for RE with 32 solutions and 100th percentile evaluations, where the best and runner-up results are **bolded** and underlined, respectively.

Methods	RE21	RE22	RE23	RE24	RE25	RE31	RE32	RE33	RE34	RE35	RE36	RE37	RE41	RE42	RE61
<i>D</i> (best)	4.42	4.78	4.75	4.59	4.79	10.23	10.53	10.59	48.06	10.96	7.57	4.72	36.17	12.28	135.87
End-to-End	4.42 ± 0.00	4.84 ± 0.00	4.84 ± 0.00	4.38 ± 0.00	4.82 ± 0.02	10.58 ± 0.03	10.56 ± 0.08	10.68 ± 0.00	52.82 ± 0.05	11.61 ± 0.01	8.24 ± 0.00	6.20 ± 0.00	<u>42.53 ± 0.05</u>	17.09 ± 2.14	140.13 ± 1.42
End-to-End + GradNorm	4.81 ± 0.01	<u>4.84 ± 0.00</u>	2.64 ± 0.00	4.38 ± 0.00	4.84 ± 0.00	10.65 ± 0.00	10.63 ± 0.00	9.90 ± 0.00	51.98 ± 0.63	11.51 ± 0.00	8.63 ± 0.71	6.11 ± 0.10	39.21 ± 0.12	13.46 ± 0.00	140.24 ± 0.25
End-to-End + PcGrad	4.86 ± 0.01	4.84 ± 0.00	<u>4.84 ± 0.00</u>	4.40 ± 0.00	4.35 ± 0.00	<u>10.65 ± 0.00</u>	10.65 ± 0.00	10.41 ± 0.07	52.78 ± 0.04	11.66 ± 0.01	9.76 ± 0.11	5.52 ± 0.00	41.64 ± 0.31	15.92 ± 1.75	139.60 ± 0.28
Multi-Head	4.61 ± 0.13	4.84 ± 0.00	4.70 ± 0.04	4.78 ± 0.00	4.35 ± 0.00	10.65 ± 0.00	10.64 ± 0.00	10.65 ± 0.01	52.63 ± 0.22	11.70 ± 0.00	6.76 ± 0.00	5.72 ± 0.00	42.45 ± 0.40	19.30 ± 0.32	<u>141.50 ± 0.03</u>
Multi-Head + GradNorm	4.91 ± 0.00	4.65 ± 0.12	4.83 ± 0.00	3.51 ± 0.87	4.31 ± 0.53	10.65 ± 0.00	10.63 ± 0.00	5.82 ± 0.02	52.81 ± 0.00	11.51 ± 0.00	0.02 ± 0.00	6.26 ± 0.01	42.56 ± 0.11	15.82 ± 2.36	<u>140.23 ± 0.66</u>
Multi-Head + PcGrad	4.91 ± 0.01	4.84 ± 0.00	4.39 ± 0.01	4.83 ± 0.00	4.35 ± 0.00	7.66 ± 0.00	10.08 ± 0.00	10.52 ± 0.04	52.77 ± 0.01	11.71 ± 0.02	9.76 ± 0.18	6.34 ± 0.03	42.23 ± 0.17	20.19 ± 0.14	140.00 ± 0.12
Multiple Models	4.89 ± 0.01	4.84 ± 0.00	4.84 ± 0.00	4.82 ± 0.00	4.82 ± 0.00	10.65 ± 0.00	10.63 ± 0.00	10.61 ± 0.00	53.58 ± 0.08	11.61 ± 0.07	10.38 ± 0.04	6.30 ± 0.01	42.04 ± 0.28	20.70 ± 0.98	141.04 ± 0.60
Multiple Models + COMs	5.19 ± 0.00	4.82 ± 0.00	4.80 ± 0.00	4.59 ± 0.00	<u>4.84 ± 0.00</u>	10.56 ± 0.00	10.64 ± 0.00	10.39 ± 0.07	51.15 ± 0.13	11.57 ± 0.01	8.57 ± 0.20	5.85 ± 0.07	39.82 ± 0.10	21.13 ± 0.55	134.26 ± 1.43
Multiple Models + RoMA	4.81 ± 0.04	4.84 ± 0.00	4.84 ± 0.00	4.77 ± 0.05	<u>4.69 ± 0.00</u>	10.65 ± 0.00	<u>10.65 ± 0.00</u>	10.46 ± 0.04	52.07 ± 0.16	11.74 ± 0.00	8.95 ± 0.01	6.31 ± 0.01	41.87 ± 0.20	16.32 ± 0.06	139.91 ± 0.72
Multiple Models + IOM	<u>5.19 ± 0.00</u>	4.84 ± 0.00	4.84 ± 0.00	<u>4.83 ± 0.01</u>	4.84 ± 0.00	10.65 ± 0.00	<u>10.65 ± 0.00</u>	<u>10.67 ± 0.00</u>	<u>53.55 ± 0.08</u>	11.72 ± 0.02	9.79 ± 0.07	<u>6.34 ± 0.01</u>	42.46 ± 0.20	21.68 ± 0.00	139.47 ± 1.09
Multiple Models + ICT	5.19 ± 0.00	4.84 ± 0.00	2.87 ± 0.03	4.67 ± 0.00	4.82 ± 0.00	10.65 ± 0.00	2.77 ± 0.00	10.51 ± 0.00	52.81 ± 0.18	11.67 ± 0.00	9.75 ± 0.19	6.08 ± 0.05	42.06 ± 0.03	<u>21.68 ± 0.00</u>	139.24 ± 1.09
Multiple Models + Tri-Mentoring	5.19 ± 0.00	4.84 ± 0.00	2.65 ± 0.00	4.78 ± 0.03	4.74 ± 0.00	10.65 ± 0.00	10.65 ± 0.00	10.49 ± 0.00	52.91 ± 0.40	<u>11.73 ± 0.01</u>	8.92 ± 0.24	6.06 ± 0.12	42.18 ± 0.26	21.68 ± 0.00	141.87 ± 0.26
MOBO	/	4.84 ± 0.00	/	4.81 ± 0.01	4.84 ± 0.00	9.50 ± 0.00	/	/	/	11.61 ± 0.02	/	/	/	13.77 ± 0.13	N/A
MOBO-ParEGO	/	4.84 ± 0.00	4.84 ± 0.00	4.82 ± 0.00	4.84 ± 0.00	/	/	/	/	11.60 ± 0.00	<u>10.19 ± 0.23</u>	/	N/A	N/A	N/A
MOBO-JES	4.85 ± 0.03	4.84 ± 0.00	4.83 ± 0.00	4.82 ± 0.00	4.84 ± 0.00	10.28 ± 0.00	10.65 ± 0.00	10.61 ± 0.03	50.30 ± 0.00	11.59 ± 0.02	9.43 ± 0.10	6.20 ± 0.03	N/A	N/A	N/A