

$$\begin{aligned}
& \text{interface}(\text{showassumed} = 0) : \\
& \text{mykernel} := \frac{\text{Heaviside}(t)}{\tau} \cdot \exp\left(K \frac{t}{\tau}\right); \\
& \text{with(inttrans)} : \\
& \quad \text{assume}(\tau > 0) : \\
& \quad \text{kernelFour} := \text{fourier}(\text{mykernel}, t, \omega) \\
& \qquad \text{mykernel} := \frac{\text{Heaviside}(t) e^{K \frac{t}{\tau}}}{\tau} \\
& \qquad \text{kernelFour} := \frac{1}{I \omega \tau + 1} \tag{1}
\end{aligned}$$

$$\begin{aligned}
& \text{stdpR0} := \frac{\text{Heaviside}(t)}{\tau_p} A_+ \cdot \exp\left(K \frac{t}{\tau_p}\right); \\
& \text{stdpOR} := K \frac{\text{Heaviside}(t)}{\tau_m} A_K \cdot \exp\left(K \frac{t}{\tau_m}\right); \\
& \text{with(inttrans)} : \\
& \quad \text{assume}(\tau_p > 0, \tau_m > 0) : \\
& \quad \text{stdpFourR0} := \text{fourier}(\text{stdpR0}, t, \omega); \\
& \quad \text{stdpFourOR} := \text{fourier}(\text{stdpOR}, t, \omega) \\
& \qquad \text{stdpR0} := \frac{\text{Heaviside}(t) A_+ e^{K \frac{t}{\tau_p}}}{\tau_p} \\
& \qquad \text{stdpOR} := K \frac{\text{Heaviside}(t) A_- e^{K \frac{t}{\tau_m}}}{\tau_m} \\
& \qquad \text{stdpFourR0} := \frac{A_+}{I \omega \tau_p + 1} \\
& \qquad \text{stdpFourOR} := K \frac{A_-}{I \omega \tau_m + 1} \tag{2}
\end{aligned}$$

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$$\begin{aligned}
& \text{to_integrate} := \frac{1}{2 \pi} \cdot (\\
& \quad \text{eval}(\text{stdpFourR0}, \omega = K \omega) \cdot \text{kernelFour}^\alpha \cdot \text{conjugate}(\text{kernelFour}^\beta) + \\
& \quad \text{stdpFourOR} \cdot \text{kernelFour}^\alpha \cdot \text{conjugate}(\text{kernelFour}^\beta)) :
\end{aligned}$$

antisymm M10 inh-exc

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to_integrate_eval := eval(to_integrate, [\alpha = 1, \beta = 0]) :
assume(\tau_p > 0, \tau_m > 0, \tau > 0) :
res := int(to_integrate_eval, \omega = K \infty .. \infty) :
simplify(res, power, symbolic)

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$$\frac{A_+}{\tau_p + \tau} \quad (3)$$

#antisymm M01 exc-inh

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to_integrate_eval := eval(to_integrate, [\alpha = 0, \beta = 1]) :
assume(\tau_p > 0, \tau_m > 0, \tau > 0) :
res := int(to_integrate_eval, \omega = K \infty .. \infty) :
simplify(res, power, symbolic)

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$$K \frac{A_-}{\tau_m + \tau} \quad (4)$$

Now again for the symmetric

$$stdpsymm := \frac{1}{2 \cdot \tau_p} A_+ \cdot \exp\left(K \frac{\text{abs}(t)}{\tau_p}\right) K \frac{1}{2 \cdot \tau_m} A_K \cdot \exp\left(K \frac{\text{abs}(t)}{\tau_m}\right) ;$$

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with(inttrans) :
assume(\tau_p > 0, \tau_m > 0) :
stdpsymmFour := fourier(stdpsymm, t, \omega)

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$$stdpsymm := \frac{A_+ e^{K \frac{|t|}{\tau_p}}}{2 \tau_p} K \frac{A_- e^{K \frac{|t|}{\tau_m}}}{2 \tau_m}$$

$$stdpsymmFour := \frac{K A_- \omega^2 \tau_p^2 + A_+ \omega^2 \tau_m^2}{(\omega^2 \tau_m^2 + 1) (\omega^2 \tau_p^2 + 1)} K A_- + A_+ \quad (5)$$

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to_integrate_symm := \frac{1}{2 \pi} \cdot (stdpsymmFour \cdot \text{kernelFour}^\alpha
\cdot \text{conjugate}(\text{kernelFour}^\beta)) :
# Symmetric, M10 inh to exc
#The order is given by alpha and beta
to_integrate_eval := eval(to_integrate_symm, [\alpha = 1, \beta = 0]) :

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assume( $\tau_p > 0$ ,  $\tau_m > 0$  ,  $\tau > 0$  ) :
res := int(to_integrate_eval,  $\omega = K \infty \dots \infty$ ) :
Mcoef = simplify(res, power, symbolic)

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$$Mcoef = \frac{(K A_- + A_+) \tau K A_- \tau_p + A_+ \tau_m}{2 (\tau_p + \tau) (\tau_m + \tau)}$$

(6)

Symmetric, M01 , exc to inh

to_integrate_eval := eval(to_integrate_symm, [$\alpha = 0$, $\beta = 1$]) :

assume($\tau_p > 0$, $\tau_m > 0$, $\tau > 0$) :

res := int(to_integrate_eval, $\omega = K \infty \dots \infty$) :

Mcoef = simplify(res, power, symbolic)

$$Mcoef = \frac{(K A_- + A_+) \tau K A_- \tau_p + A_+ \tau_m}{2 (\tau_p + \tau) (\tau_m + \tau)} \quad (7)$$