Chapter 26

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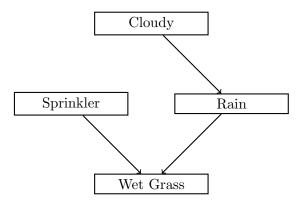
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Comments and Proofs

Exercises

Exercise 1

a. By conditioning on do(W = T), the graph becomes



The marginal for R uniform (but if we were in Vancouver, p(R=T)=1). Thus,

$$\begin{split} p(W = T|\operatorname{do}(S = T)) &= p(W = T, R = T|\operatorname{do}(S = T)) + p(W = T, R = F|\operatorname{do}(S = T)) \\ &= p(W = T|R = T, \operatorname{do}(S = T))p(R = T|\operatorname{do}(S = T)) \\ &+ p(W = T|R = F, \operatorname{do}(S = T))p(R = F|\operatorname{do}(S = T))) \\ &= p(W = T|R = T, \operatorname{do}(S = T))p(R = T) \\ &+ p(W = T|R = F, \operatorname{do}(S = T))p(R = F) \\ &= 0.9 \times 0.5 + 0.99 \times 0.5 \\ &= 0.945 \end{split}$$

b. Similarly, we have

$$\begin{split} p(W = T|\operatorname{do}(S = F)) &= p(W = T|R = T, \operatorname{do}(S = F))p(R = T) \\ &+ p(W = T|R = F, \operatorname{do}(S = F))p(R = F) \\ &= 0 \times 0.5 + 0.9 \times 0.5 \\ &= 0.45 \end{split}$$

 ${\bf c.}~~$ Since C is the root of the DAG, performing do-calculus makes no difference. Thus

$$p(S = T | do(C = T)) = p(S = T | C = T) = 0.1.$$

Unsurprisingly, we find out that sprinklers cause grass to become wet.