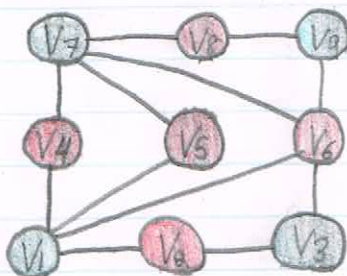


Tutorial:

①



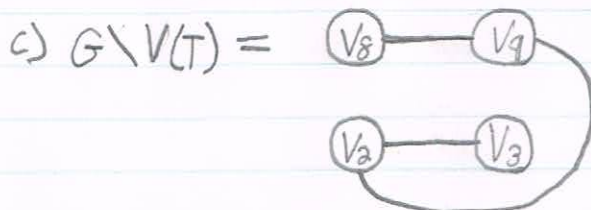
②

a) $M = \{V_1V_5, V_6V_7\}$

| T | $E(T)$ | $O(T)$ |
|---|-----------------|------------|
| $\{V_4\}, \emptyset$ | | |
| $\{V_4, V_6, V_7\}, \{V_4V_7, V_6V_7\}$ | V_4, V_6 | V_7 |
| $\{V_4, V_6, V_7, V_1, V_5\}, \{V_4V_7, V_6V_7, V_1V_4, V_1V_5\}$ | V_4, V_6, V_5 | V_7, V_1 |

b) $M = \{V_1V_5, V_4V_7\}$

each edge in matching has one end in $E(T)$ & one end in $O(T)$ so we are frustrated



$M' = \{V_8V_9, V_2V_3\}$
 $C' = \{V_2, V_8\}$

d)

$C' \cup O(T) = \{V_2, V_8\} \cup \{V_1, V_7\} = \{V_1, V_2, V_7, V_8\}$

$M \cup M' = \{V_1V_5, V_4V_7\} \cup \{V_8V_9, V_2V_3\}$
 $= \{V_1V_5, V_4V_7, V_8V_9, V_2V_3\}$

$|C' \cup O(T)| = |M \cup M'| = 4$

Remove all edges but:

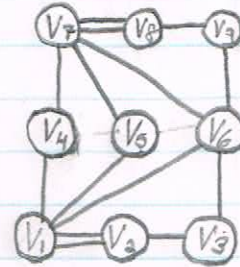
V_8V_9, V_2V_3, V_2V_9

ASK:

let $M = \{V_1V_2, V_7V_8\}$, let $r = V_5$:

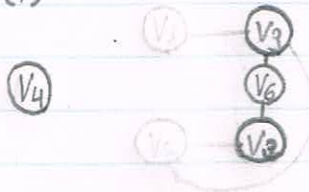
a)

| T | $E(T)$ | $O(T)$ |
|--|-----------------|-------------|
| $\{V_5\}, \emptyset$ | V_5 | \emptyset |
| $\{V_5, V_1, V_2\}, \{V_5, V_1, V_2\}$ | V_2, V_5 | V_1 |
| $\{V_5, V_1, V_2, V_7, V_8\}, \{V_5, V_1, V_2, V_7, V_8\}$ | V_2, V_5, V_8 | V_1, V_7 |



b) $M = \{V_1V_2, V_4V_7\}$ & each edge in matching has one end in $E(T)$ & one end in $O(T)$ So we are frustrated

c) $G \setminus V(T) =$



$$M' = \{V_4V_6\}$$

$$C' = \{V_6\}$$

d)

$$C' \cup O(T) = \{V_6\} \cup \{V_1, V_7\} = \{V_1, V_6, V_7\}$$

$$M \cup M' = \{V_1V_2, V_4V_7\} \cup \{V_4V_6\}$$

$$= \{V_1V_2, V_4V_7, V_4V_6\}$$

$$|C' \cup O(T)| = |M \cup M'| = 3$$