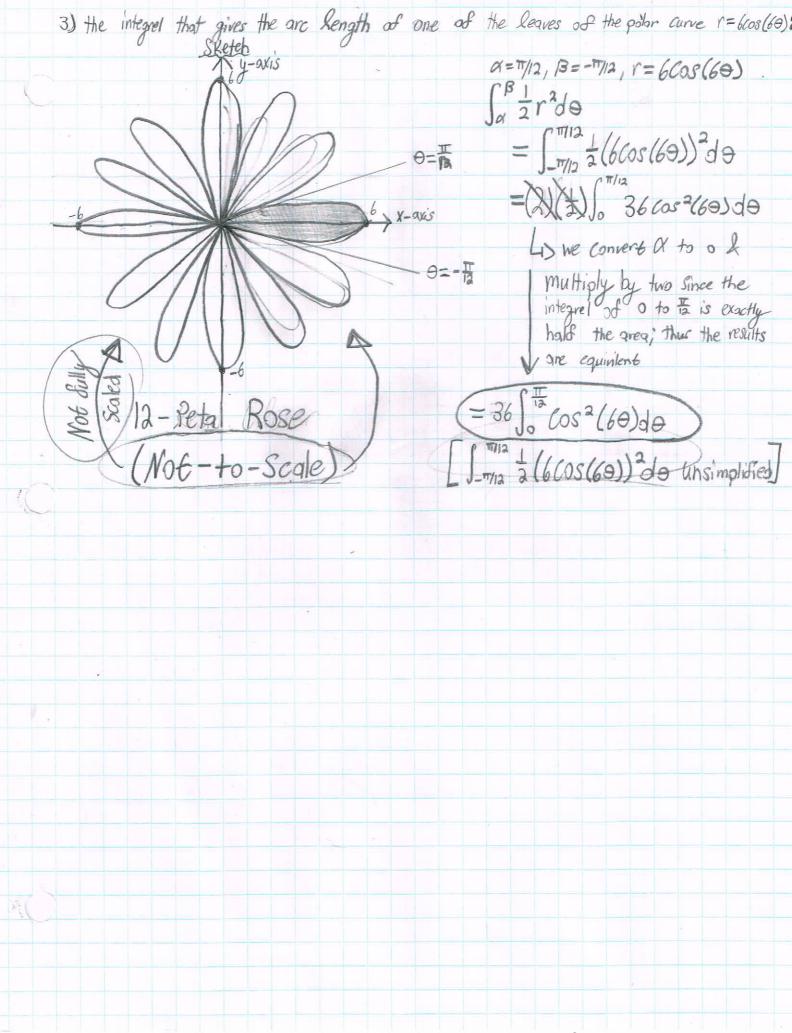
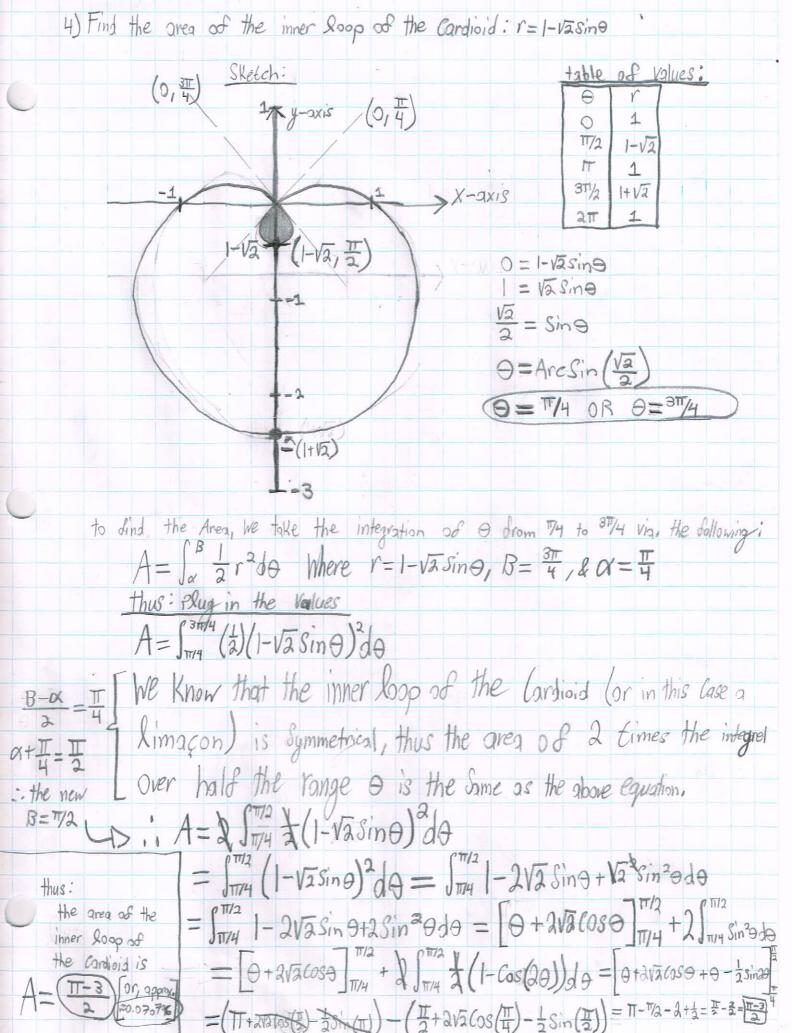
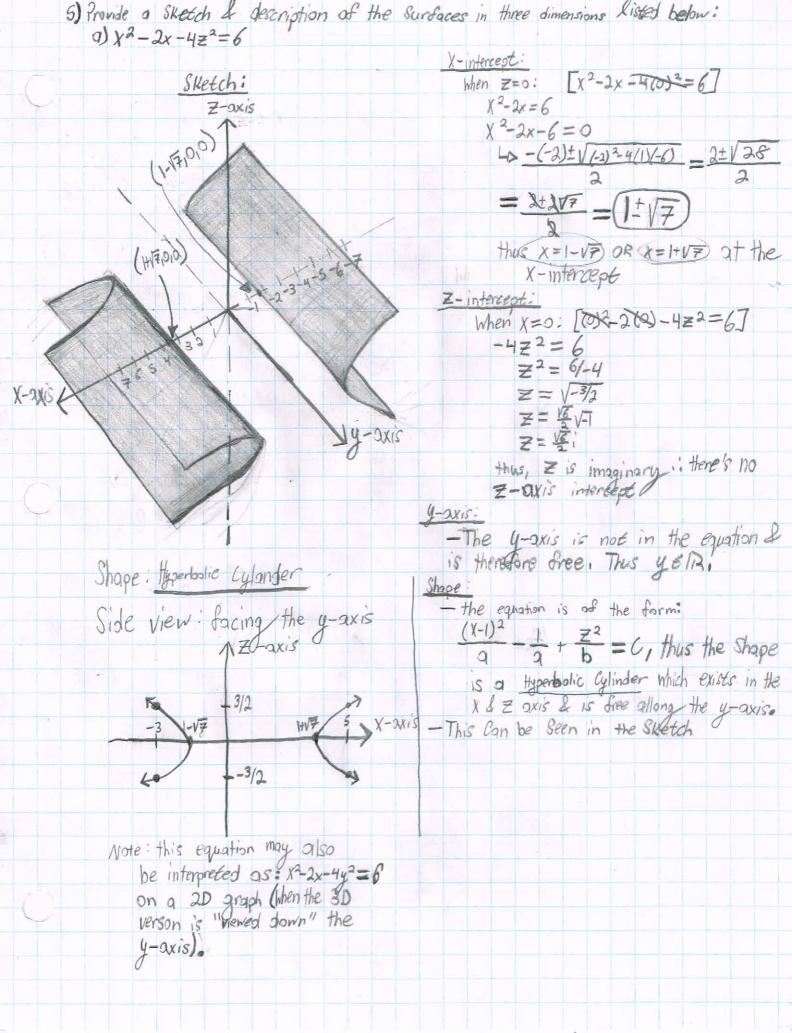
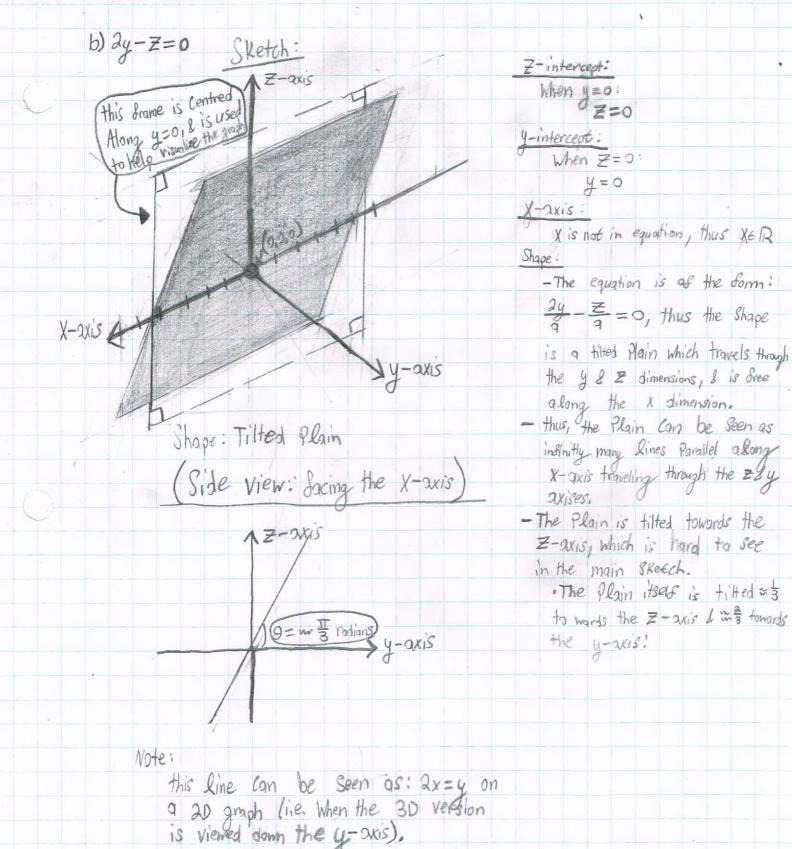


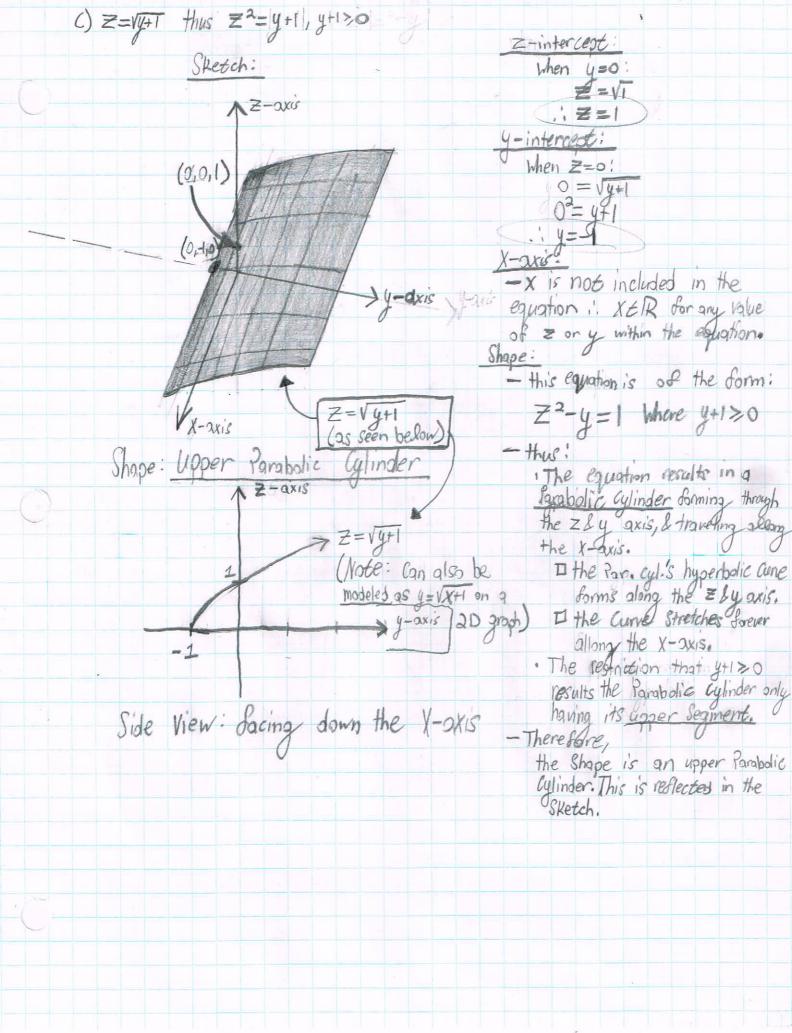
2) give the Slope of the tangent line to the Polar Curve ra= 9sin (30) at the Bint (3, =): When $\theta = \sqrt{6}$: Y = 3 & r of 3 is max. $y = rsin\theta \qquad dy/d\theta = rcos\theta + sin\theta \frac{dr}{d\theta}$ $y = rcos\theta \qquad dx/d\theta = -rsin\theta + cos\theta \frac{dr}{d\theta}$ thus: $\frac{dy}{dx} = \frac{dy/d\theta}{3x/d\theta} = \frac{r\cos\theta + \sin\theta \frac{dr}{d\theta}}{-r\sin\theta + \cos\theta}$ find rectangular Coordinates: ($\Theta=76 \& r=3$) $X = 3 cos (76) = 3 \sqrt{3}$ y=3sin(7/6)=3 Next, we find the Slope of the tangent line, .. We must find the derivative at the point! M= = When t= == We must also derive r: $\frac{9r}{4} = \sqrt{19}\sin(3\theta)/1 = 3 \cdot \frac{1}{2} |\sin(3\theta)|^{-1/2} \cdot 3\sin(3\theta) \cos(3\theta)$ $= \frac{9(\sin 3\theta)\cos(3\theta)}{2|\sin(3\theta)|^{1/2}} = \frac{9\sin(3\theta)\cos(3\theta)}{2|\sin(3\theta)|^{3/2}}$ Or, Simply = \(\frac{9008(30)}{2 \sin(30)} \) Such that 9 \(\sin(30) \ge 0 \) thus; $\frac{dy}{dt} = \frac{r\cos\theta + \sin\theta r'}{-r\sin\theta + \cos\theta r'} = \frac{(\sqrt{19}\sin(3\theta))}{(\frac{9\cos(3\theta)}{2\sqrt{\sin(3\theta)}})\sin\theta - (\sqrt{19}\sin(3\theta))}\sin\theta}$ $\frac{\text{let } t = \frac{176:}{(\sqrt{13}\sin(\frac{172}{12}))\cos(\frac{1}{16})} + \sin(\frac{1}{16}\cos(\frac{172}{12}))}{(\frac{3(\cos(\frac{172}{12}))}{2\sqrt{\sin(\frac{172}{12})}})\sin(\frac{1}{16})} = \frac{3\sqrt{3}12}{3} = \frac{2\sqrt{3}}{3} = \frac{2}{3}$ (M = - 13 ... the Slope of the tangent line is - V3.









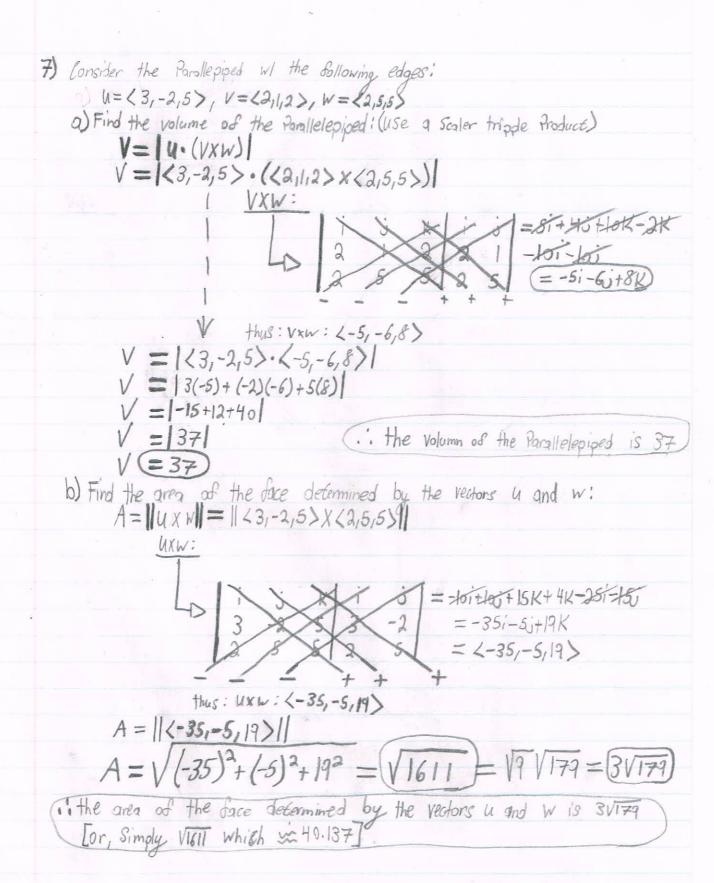


Projba = $-\frac{16}{13}\langle 2, -3, 0 \rangle = \langle -\frac{32}{13}, \frac{48}{13}, 0 \rangle$

c)
$$(q \cdot b)(c - b)$$
= $(4-2,4,1) \cdot (2,-3,0)((3,-4,2)-(2,-3,0))$
= $(-2(2)+4(-3)+4(0))((3-2,-4-c-3),2-0)$
= $(-4-12)(1,-1,2)$
= $-16(1,-1,2)$
= $(-16,16,-32)$

thus:
$$((q \cdot b)(c-b) = -16(1,-1,2) = (-16,16,-32)$$

$$d) (q-b) \times (b-c)$$
= $(2-2,4,1) - (2,-3,0) \times (2,-3,0) - (3,-4,2)$
= $(-2-2,4-(-3),1-0) \times (2-3,-3-(-4),0-2)$
= $(-4,7,1) \times (-1,1,-2)$
= $(-4,7,1) \times (-1,1,-2)$



C) Find the angle between u at the face determined by the vectors v and w.

Find the Plain Perpendicular to the one determined by v and w.

VXW; $\{2,1,1,2\} \times \{2,5,5\}$: |u| = 5i + 45 + 16k - 2k - 16i - 16j |u| = -5i - 6j + 8k |u| = -5

.: the angle between u & the face determined by v & W is 57.53° [or Simply 1.004 radians]

8) Give the Parametric equations of the line that Passes through the Point P(1,-2,-3) & is famillel to the vector <0,-1,5>. $r = 21, -2, -3 > 2 \quad V = 20, -1,5 >$ Vector equation: r= <1,-2,-3>+t<0,-1,5> thus, the Parametric equations of the line are: 4=-2-6 Z=-3+5t Determine is the points listed below are on this line: a) Q(1,-2,-1)!

① X=1 & X=1 thus I=1 : $t \in IR$ (t is any Real number) 2 y=-2-t & y=-2 thus -2=-2-t :(=5) 3 Z=-3+5 & Z=-1 thus -1=-3+5 ± 0=-2+5= In 3, we see that + must equal of but in 3 we see + must equal =, thus it is Contridictory to have the point (1,-2,-1) as t can only have one unique Value. I also NoT on the line b) W(1,5,-38): 1) X=1 & X=1 thus 1=1 is tER (t is any real number) g y=-2-t & y=5 thus 5=-2-t : (t=-₹) 3 Z=-3+56 & Z=-38 thus -38=-3+5t : (t=-7) Since both @ & 3 have that +=-7, & Since O States & may be any real number & since -7 is a real number), the point (1,5,738) is on the line. (W IS on the line)

9) Give the equation of the Plain that contains the line x=3t, y=1-2t, Z=1-t & is Perpendicular to the Plane X-y+3==3: $V=\langle 3,-2,-1\rangle$ is Parallel to the line n= <1,-1,3> is normal to the given Plain thus, Vxn:

= L-7,-10,-1>, this line is normal to the Plain were looking for When t=0 on the line:

we get 20,1,1>, which also a point on our Plain.

Use the point & the normal:

Point = 40,1,1>; normal = 4-7,-10,-1>

=-7x-10(y-1)-1(z-1)

= -7x - loy+lo-Z+l

= -7x - loy - 7 + 11 | -1| = -7x - loy - 7

or Simply; 11= 7x+log+Z

thus, the Plane were looking for is: (7x+loy+Z=11)

10) Identify I describe the quadric surfaces, a Sketch isn't necessary:

$$0) = 4x^2 - 3x + y^2 - 2z + 24$$

$$1 + \frac{1}{16} = -4x^2 - 3x + y^2 - 2z - 2z$$

$$24 = -4x^2 + 3x - y^2 + 2z + 2z$$

$$34 = -4(x^2 - 3x)^2 + 3/16 - y^2 + (2+1)^2 - 1$$

$$16 = -(2x - \frac{3}{4})^2 - y^2 + (2+1)^2$$

$$1 = -\frac{64(x - \frac{3}{8})^2}{391} - \frac{16y^2}{341} + \frac{16(z + 1)^2}{391}$$
This is of the Gorm:
$$1 = \frac{z^2}{c^2} - \frac{x^2}{9^2} - \frac{y^2}{9^2} = \frac{1}{3} + \frac{$$

b)
$$y = 2x^2 - 6x - z^2 + 5y$$

 $0 = 2(x^2 - 3x) + 4y - z^2$
 $0 = 2(x - \frac{3}{2})^2 - \frac{3}{2} + 4y - z^2$
 $\frac{1}{3} = 2(x - \frac{3}{2})^2 + 4y - z^2$
 $1 = \frac{4(x - \frac{3}{2})^2 + 6y - 2z^2}{9}$
 $1 = \frac{4(x - \frac{3}{2})^2 + 6y - 2z^2}{9}$

this is of the form:

 $1=Z-\frac{\chi^2}{2^2}-\frac{y^2}{h^2}$ as there is one linear term (y above), W/ two Augdratic terms (X&Z above) W/ Opposite Signs.

. Hyperbolic Paraboloid

the Graph:

The Paraboloid opens along the y-axis, in the negative direction.

The last Min of the Paraboloid (the Creast of the opening) is i $0 = 2(x^2 - 3x) + 4y - z^2$ when z = 0 d x = 3/20 = -4.5 + 44 4.5= 44

thus: the local Min. at the Positive y-axis is (3/2, 9/8,0)

- The Graph forms a Parabolic "Void" along the Positive y-axis

- The Graph Grows along the Z & X-axis conevery but always opens along the neg. y-axis & has a gap between the Pos. y-axis.

11) a) Give the equation of an elliptic Cone W/ centre at toing (1,-2,1), in the direction of the x-axis in rectangular & Cylindrical Coordinates. - An elliptic lone is of the form: Z2-12-12=0 1-3x11 X2-12-0 - Thus, if the Centre is at P(1,-2,1): $(\chi-1)^2 - \frac{(y+2)^2}{6^2} - \frac{(z-1)^2}{6^2} = 0$ is the equation in Rect. Coord. -If we let b=d=1 then we get a Simple equation: $((X-1)^2-(y+2)^2-(Z-1)^2=0$ - In General terms, the equation. $0 = \frac{(y+2)^2}{y^2} = \frac{(y+2)^2}{(x^2-1)^2}$ will satisfy the question (for rectangular Coordinates) - to Convert to Cylindrical Coordinates Ret X= reoso, y=rsino, z=Zithen: $(rloso-1)^a-(rsino+2)^a-(Z-1)^a=0$ - In General terms, the equation:

In General terms, the equation:
$$\frac{(r\cos\theta - 1)^2 - (r\sin\theta + 2)^2}{b^2} = \frac{(Z-1)^2}{c^2} = 0$$

b) Give the equation of an elliptic Paraboloid with Centre at the point (0,2,1) in the direction of the y-axis in rectangular and Spherical Coordinates:

- An elliptic Paraboloid is of the form:

$$Z - \frac{\chi^2}{q^2} - \frac{y^2}{b^2} = 0 \quad \text{in the direction} \quad y - \frac{\chi^2}{q^2} - \frac{z^2}{b^2} = 0$$

- Thus, if the Centre is at Bint (0,2,1):

$$(y-2) - \frac{x^2}{d^2} - \frac{(z-1)^2}{b^2} = 0 [(y-2) - x^2 - (z-1)^2 = 0 \text{ When } b=0=1]$$

- To Convert to Spherical Coordinates:

let X=Psinocoso, y=Psinosino, z=pcoso; then:

$PSinpsin\theta - 2 - (PSinpcose)^2 - (PCosp - 1)^2 = 0$
$0 = Psingsine - (Psingcose)^2 - (Pcosp-1)^2 - 2$
- In General Terms, the equation;
$0 = PSin psine - \frac{(PSinpCoSe)^2}{g^2} - \frac{(Pcosp-1)}{b^2}$
() Give the equation of a hyperboloid of one sheet with Center (0,0,4) in the
direction of the Z-axis in Cylindrical & Spherical Coordinates i
C) Give the equation of a hyperboloid of one Sheet With Center (0,0,4) in the direction of the Z-axis in Cylindrical & Spherical Coordinates: A hyperboloid of one Sheet has the general form in Cylindrical Coordinates:
Z=r2-1 [this is already in the direction of the z-axis]
- Thus, if we let the Centre be P(0,0,4):
$(Z-4)^2-r^2+1=0$ [when $a=b=c=1$]
- In General terms, the equation;
(Z-4)2 - 12 + 1 = 0, When d, e & R
-To Convert to Sphenical Coordinates:
let r=Psing, 0=0, Z=Pcosp; then:
$(2\cos\phi - 4)^2 - (2\sin\phi)^2 + 1 = 0$
- In General terms, the equation:
$\frac{(2\cos\phi - 4)^2}{d^2} - \frac{(2\sin\phi)^2}{e^2} + 1 = 0$, When de ER

ì