Lab 13: Trees

1.1 Information

Topics: Trees

Turn in: This is another on-paper "lab". Turn in a text file, PDF file, scanned or photographed images.

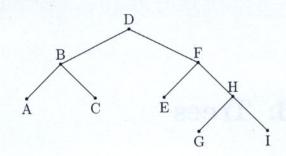
1.2 About: Efficiency

Every data structure has trade-offs. For example, it is faster to access items at some position in an array than it is to do so in a linked list. However, if the array is unsorted, there is not a good efficient way to search the array to find some specific data. If we were to build a sorted array, we would have to decide *when* to do the sorting...

- During Insert Locate the proper place for the new data
- After Insert Insert to the end, then re-sort the array

Either way, the act of inserting data into the array will slow down the process, since we would need to either shift n items over to make room for the new item, or perform a sorting algorithm; neither way is as efficient as simply putting data in the array at the end, but it might make access time more efficient.

When selecting a data structure to use, part of what we need to consider is what we're designing and how the data structure will be used - will we do a lot of inserts? Will we do a lot of accesses? If we're inserting data often but not reading that data very much, a structure like a Linked List or Unsorted Array might be fine, with O(1) time for the "push" function. If we don't do insertions very often, but need to read the data frequently, it would be better to keep our data sorted.



 $Smaller \longleftrightarrow Larger$

Trees, especially Binary Search Trees (which we will talk about on its own), are a type of structure where we can make a compromise. Specifically for a **Binary Search Tree**, insert and access are both $O(\log n)$ on average, because as we traverse through the tree, each step we're removing *half* of the search space.

We will return to Binary Search Trees later, but for now let's go over the terminology associated with Trees.

1.3 Intro to Trees

Tree: A collection of Nodes (or vertices) and Edges.

Edge: A path that connects two Nodes together. If we have N nodes, then there are N-1 edges.

Nodes: A vertex in the tree, usually associated with some data.

Root Node: The source Node of the tree; it has no parents. Each Tree has one Root Node, usually drawn at the top. All other Nodes descend from the Root Node.

Leaf Node: A Node with no children.

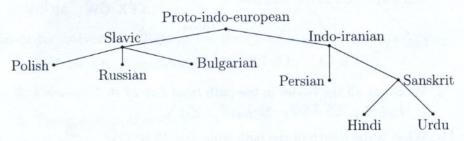
Node Family: We use family terminology to talk about how Nodes are related to each other.

- Parent node: Given some Node n, n's parent is the Node immediately above n, in the path between n and the root node. Each Node can have only 0 or 1 parent.
- **Ancestor node:** Given some Node n, an Ancestor of n is any Node along the path from n to the root node.
- Child node: Given some Node n, n's child is a Node that comes immediately below it in the tree. Node n lies in the path from its child to the root node. Each Node can have 0 or more children. With a Binary Search Tree, a Node can have 0, 1, or 2 children.
- **Descendant node:** Given some Node n, a Descendant is a Node that comes below it in the tree, where the Node n lies in the path from that descendant to the root node.
- Sibling node: Given some Node n, a Sibling of n is another Node where n and that Sibling share the same Parent node.

Question 1

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For the given tree:



- a. What are all the (listed) ancestors of Russian?
 - Slavic and Proto-Indo-European
- b. What are all the (listed) descendants of Indo iranian?

 Persian, Sanskrit, Hindi, Urdu
- c. What are all the (listed) siblings of Polish?

Pussian and Bulgarian

d. What are all the (listed) leaves of the tree?

Polish, Russian, Bulgarian, Persian. Hindi, Urder

Path: A path between two nodes, n_a and n_b , is a series of connecting edges between these two nodes.

Path Length: The Length of a Path is the amount of edges in the path.

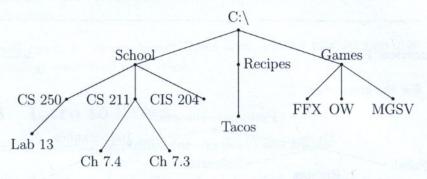
Node Depth: Given any node n, the Depth of n is the *length* of the path between n and the root.

Node Height: Given any node n, the Height of n is the longest path from n to a leaf. Leaves have a height of 0.

Question 2

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For the given tree:



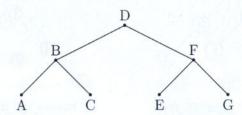
a. Write out all the Nodes in the path from $Lab\ 13$ to $C:\setminus$.

b. What is the length of the path from Lab 13 to C:\?

c. Find the Depths and Heights for the following:

Node	Depth	Height
Lab 13	3	0
Ch 7.3	3	0
Tacos	Z	0
MGSV	2	0
CS 211	2	1
School	1	2

1.3.1 Traversals



Since a Tree is not a linear structure, what order do you display its contents? There are three main methods you will see for traversing through a tree. Each of these are recursive, beginning at the root node. Once the end of a path is reached (by hitting a leaf), the recursion causes it to step back upwards through the tree.

Pre-order traversal Begin at the Root r node of some Tree/Subtree...

- 1. Process r
- 2. Traverse left, if available
- 3. Traverse right, if available

With the above tree, we process nodes as such:

In-order traversal Begin at the Root r node of some Tree/Subtree...

- 1. Traverse left, if available
- 2. Process r
- 3. Traverse right, if available

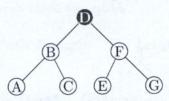
With the above tree, we process nodes as such:

Post-order traversal Begin at the Root r node of some Tree/Subtree...

- 1. Traverse left, if available
- 2. Traverse right, if available
- 3. Process r

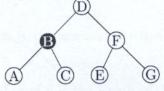
With the above tree, we process nodes as such:

Step-by-step pre-order illustration:



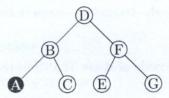
1. Begin at D. Process "D" then go left.

Output: D



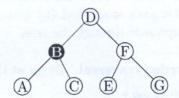
2. Process "B" then go left.

Output: D B



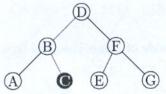
3. Process "A"; no more children, return (back to B).

Output: D B A



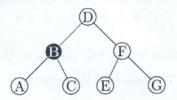
4. Go to right child.

Output: D B A



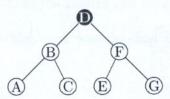
5. Process "C"; no more children, return (back to B).

Output: D B A C



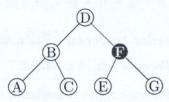
6. Done with left and right subtrees, return (back to D).

Output: D B A C



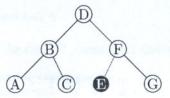
5. Go to right child.

Output: D B A C



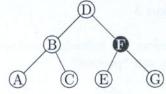
6. Process "F" then go left.

Output: D B A C F



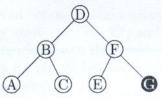
7. Process "E" then return (back to F).

Output: D B A C F E



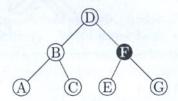
8. Go to right child.

Output: D B A C F E



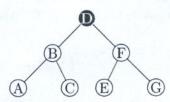
9. Process "G" then return (to F).

Output: D B A C F E G



10. Return (to D).

Output: D B A C F E G



11. Finished.

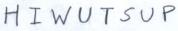
Output: D B A C F E G

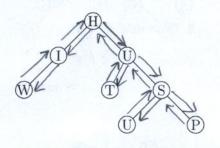
Hopefully these steps help you better visualize the recursive nature of tree traversal.

Question 3

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Traverse the following tree using **pre-order** traversal. Write out each Node as you "process" it.

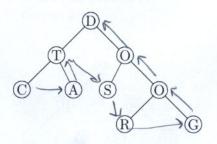




Question 4

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Traverse the following tree using **post-order** traversal. Write out each Node as you "process" it.

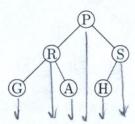


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Question 5

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Traverse the following tree using **in-order** traversal. Write out each Node as you "process" it.



GRAPHS

Question 6

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We have a Node class declared like this:

```
template <typename T>
struct Node
{
    T data;
    Node* ptrLeft; = nullptr;
    Node* ptrRight; = nullptr;
};
```

And we have nodes already declared, nodeA, nodeB, nodeC, nodeD. They store 'A', 'B', 'C', and 'D', respectively. Write some basic code to create a tree with these nodes. One will be a root. For each Node, the item to its left should be lower in value (A < B), and the item to its right should be greater (C > B).

void addNode (Node * added Node); int node (ount = 0; Node * ptr Root = nullptr;

```
int main()

{
add Node (& node C);
add Node (& node B);
add Node (& node A);
add Node (& node D);
return 0;

}

Void add Node (Node * added Node)

{
if (node (oun+==0))

{
ptr Root = added Node;
```

> ptr Root > ptr Left = ptr Root;

ptr Root > ptr Right = ptr Root;

node Count ++;

3
else if (added Node > data &

ptr Root -> data)

added Node -> ptr Right = ptr Root > ptr Root;

node Count ++;

3
else if (added Node > data > ptr Root > ptr Right;

node Count ++;

3
else if (added Node > data > ptr Root > ptr Right;

node Count ++;

added Node -> ptr Left = ptr Root > ptr Right;

node Count ++;

3