

# DESARROLLO SOLUCIÓN ENTREGA #1

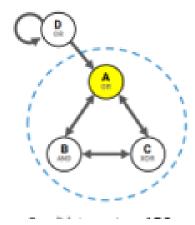
**Docente: Luz Enith Guerrero Mendieta** 

Presentado por:

Cristian David Gómez Becerra

Stiven Vélez Bedoya

# **Grafo Inicial**



| Entrada de datos   | Medida de<br>distancia | Esquema de partición | Resultados con<br>CM               | Resultados sin CM                  | Observaciones |
|--|------------------------|----------------------|------------------------------------|------------------------------------|---------------|
| Grafo:   | EMD                    | biparticion          | MIP:<br>Cut [B, C] ——//<br>——➤ [A] | MIP:<br>Cut [B, C] ——//<br>——➤ [A] |               |
|  |                        |                      | Phi:<br>Φ = 2.3125                 | Phi:<br>Φ = 2.3125                 |               |
| tpm = np.array([   |                        |                      | Time:<br>0.246312 s                | Time: 0.505238 s                   |               |
| [0, 0, 0],<br>[0, 0, 1],<br>[1, 0, 1],<br>[1, 0, 0],<br>[1, 1, 0], | EMD                    | tripartición         | MIP:<br>Cut [B, C] ——//<br>——➤ [A] | —→ [A]                             |               |
| [1, 1, 1],<br>[1, 1, 1],<br>[1, 1, 0]                              |                        |                      | Phi:<br>Φ = 2.3125                 | Phi:<br>Φ = 2.3125                 |               |
| 1)   |                        |                      | Time:<br>0.217384 s                | Time:<br>0.476244 s                |               |

| cm = np.array([                       | KLD | bipartición  | MIP:<br>Cut [B, C] ——//<br>——➤ [A] | MIP:<br>Cut [B, C] ——//<br>——➤ [A] |
|---------------------------------------|-----|--------------|------------------------------------|------------------------------------|
| [0, 0, 1],<br>[1, 0, 1],<br>[1, 1, 0] |     |              | Phi:<br>Φ = 2.3125                 | Phi:<br>Φ = 2.3125                 |
| 1)                                    |     |              | Time:<br>0.223403 s                | Time:<br>0.495682 s                |
|                                       | KLD | tripartición | MIP:                               | MIP:<br>Cut [B, C] ——//            |
|                                       |     |              | —→ [A] Phi: Φ = 2.3125             | —→ [A]  Phi: Φ = 2.3125            |
|                                       |     |              | Time: 0.223404 s                   | Time: 0.448496 s                   |
|                                       |     |              |                                    |                                    |

# • EMD-Bipartición-con CM

```
| 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts:
                   0%
Computing concepts:
                  0%
                                | 0/5 [00:00<?, ?it/s]
Computing concepts:
                    0%
                               | 0/5 [00:00<?, ?it/s]
Computing concepts:
                                | 0/6 [00:00<?, ?it/s]
                    0%
Computing concepts:
                    0%
                                | 0/6 [00:00<?, ?it/s]
Evaluating O cuts: 67%
                                4/6 [00:00<00:00, 36.80it/s]
Computing concepts:
                                | 0/5 [00:00<?, ?it/s]
                    0%
Computing concepts:
                    0%
                                | 0/5 [00:00<?, ?it/s]
MIP:
Cut [B, C] —/ /—≻ [A]
Phi:
\Phi = 2.3125
Time:
0.246312 s
```

#### EMD-Bipartición-sin CM

```
Evaluating \Phi cuts:
                    0%|
                               | 0/6 [00:00<?, ?it/s]
Computing concepts:
                   0%
                                 0/5 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/6 [00:00<?, ?it/s]
Evaluating O cuts: 50%
                                | 3/6 [00:00<00:00, 22.12it/s]
Computing concepts:
                    0%
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                    0%|
                                 | 0/5 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                 | 0/5 [00:00<?, ?it/s]
MIP:
Cut [B, C] —/ /—⊁ [A]
Phi:
\Phi = 2.3125
Time:
0.357047 s
In [16]:
```

# EMD-Tripartición-con CM

```
Evaluating O cuts:
                                | 0/6 [00:00<?, ?it/s]
                   0%|
                                | 0/5 [00:00<?, ?it/s]
Computing concepts:
                    0%
Computing concepts:
                    0%
                                 0/5 [00:00<?, ?it/s]
Computing concepts:
                                 | 0/6 [00:00<?, ?it/s]
                    0%
Computing concepts:
                    0%
                                 | 0/6 [00:00<?, ?it/s]
                                 | 0/5 [00:00<?, ?it/s]
Computing concepts: 0%
Evaluating \Phi cuts: 83%
                           | 5/6 [00:00<00:00, 39.37it/s]
Computing concepts:
                                 0/5 [00:00<?, ?it/s]
                    0%
MIP:
Cut [B, C] —/ /—> [A]
Phi:
\Phi = 2.3125
Time:
0.213141 s
```

EMD-Tripartición-sin CM

```
Evaluating O cuts:
                   0%
                            | 0/6 [00:00<?, ?it/s]
                                | 0/5 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts:
                    0%
                                | 0/5 [00:00<?, ?it/s]
Computing concepts: 0%
                                | 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts: 50%
                                3/6 [00:00<00:00, 22.45it/s]
Computing concepts:
                                | 0/6 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                | 0/5 [00:00<?, ?it/s]
Computing concepts: 0%
                                | 0/5 [00:00<?, ?it/s]
MIP:
Cut [B, C] —/ /—≻ [A]
Phi:
\Phi = 2.3125
Time:
0.36401 s
T- [40].
```

#### KLD-Bipartición-con CM

```
0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts: 0%
                               | 0/5 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts:
                    0%|
                               | 0/5 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                | 0/6 [00:00<?, ?it/s]
Computing concepts:
                                | 0/6 [00:00<?, ?it/s]
                    0%|
Computing concepts: 0%
                                0/5 [00:00<?, ?it/s]
Evaluating \Phi cuts: 83%
                           | 5/6 [00:00<00:00, 43.39it/s]
Computing concepts: 0%
                                0/5 [00:00<?, ?it/s]
MIP:
Cut [B, C] —/ /—≻ [A]
Phi:
\Phi = 2.3125
Time:
0.197516 s
```

#### KLD-Bipartición-sin CM

```
9% l
Evaluating \Phi cuts:
                                0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/5 [00:00<?, ?it/s]
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%|
Evaluating O cuts: 50%
                                 3/6 [00:00<00:00, 26.73it/s]
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0%
Computing concepts:
                     0%
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                                  | 0/5 [00:00<?, ?it/s]
                     0%
MIP:
Cut [B, C] —/ /—> [A]
Phi:
0 = 2.3125
Time:
0.343236 s
```

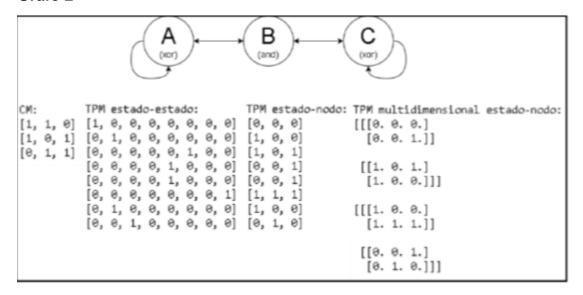
# KLD-Tripartición-con CM

```
| 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts: 0%
                                   | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                     0%
                                   | 0/5 [00:00<?, ?it/s]
Computing concepts:
                      0%
                                   | 0/6 [00:00<?, ?it/s]
Computing concepts:
Computing concepts:
                      9% l
                                   | 0/6 [00:00<?, ?it/s]
Computing concepts:
                      0%
                                   | 0/5 [00:00<?, ?it/s]
                                   | 0/5 [00:00<?, ?it/s]
Computing concepts:
                      0%
MIP:
Cut [B, C] —/ /—> [A]
Phi:
\Phi = 2.3125
Time:
0.172539 s
```

#### KLD-Tripartición-sin CM

```
Evaluating \Phi cuts:
                    0%
                                | 0/6 [00:00<?, ?it/s]
Computing concepts:
                   0%
                                 0/5 [00:00<?, ?it/s]
Computing concepts:
                    0%|
                                 0/5 [00:00<?, ?it/s]
                    0%
Computing concepts:
                                 0/6 [00:00<?, ?it/s]
Evaluating O cuts: 50%
                                | 3/6 [00:00<00:00, 25.07it/s]
Computing concepts:
                    0%
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                 | 0/5 [00:00<?, ?it/s]
                                 | 0/5 [00:00<?, ?it/s]
Computing concepts:
                    0%
Cut [B, C] —/ /—> [A]
Phi:
\Phi = 2.3125
Time:
0.351062 s
```

#### Grafo 2



# → Estado-estado

| Entrada de datos   | Medida de<br>distancia | Esquema de partición | Resultados con<br>CM                                       | Resultados sin<br>CM                                       | Observaciones |
|--|------------------------|----------------------|--|--|---------------|
| $\begin{array}{c} \hline \textbf{Grafo:} \\ \hline \begin{pmatrix} \textbf{A} & & \textbf{B} \\ & & \end{pmatrix} & \begin{matrix} \textbf{C} \\ & & \end{matrix} \\ \hline \begin{pmatrix} \textbf{O} & & \\ & & \end{matrix} \\ \hline \end{pmatrix} \\ \hline \begin{pmatrix} \textbf{O} & & \\ & & \end{matrix} \\ \hline \end{pmatrix}$ | EMD                    | biparticion          | MIP:<br>Cut [A, B] ——<br>//——➤ [C]                         | MIP:<br>Cut [A, B] ——<br>//——➤ [C]                         |               |
| tpm = np.array([ [1, 0, 0, 0, 0, 0, 0, 0], [0, 1, 0, 0, 0, 0, 0, 0], [0, 0, 0, 0, 0, 1, 0, 0], [0, 0, 0, 0, 1, 0, 0, 0], [0, 0, 0, 0, 1, 0, 0, 0],   |                        |                      | Phi:<br>Φ = 0.520834<br>Time:<br>0.341088 s                | Phi:<br>Φ = 0.520834<br>Time:<br>0.256316 s                |               |
| [0, 0, 0, 0, 1, 0, 0, 0],<br>[0, 0, 0, 0, 0, 0, 0, 1],<br>[0, 1, 0, 0, 0, 0, 0, 0],<br>[0, 0, 1, 0, 0, 0, 0, 0]  | EMD                    | tripartición         | MIP:<br>Cut [A, B] ——<br>//——➤ [C]<br>Phi:<br>Φ = 0.520834 | MIP:<br>Cut [A, B] ——<br>//——➤ [C]<br>Phi:<br>Φ = 0.520834 |               |
|  |                        |                      | Time:<br>0.271785 s  | Time:<br>0.296044 s  |               |

| <pre>cm = np.array([ [1, 1, 0], [1, 0, 1], [0, 1, 1] ])</pre> | KLD | bipartición  | MIP:<br>Cut [A, B] ——<br>//——➤ [C]<br>Phi:<br>Φ = 0.520834<br>Time:<br>0.262299 s | MIP:<br>Cut [A, B] ——<br>//——➤ [C]  Phi:<br>Φ = 0.520834  Time:<br>0.278293 s     |  |
|---|-----|--------------|---|---|--|
|   | KLD | tripartición | MIP: Cut [A, B] —— //——➤ [C]  Phi: Φ = 0.520834  Time: 0.277937 s                 | MIP:<br>Cut [A, B] ——<br>//——➤ [C]<br>Phi:<br>Φ = 0.520834<br>Time:<br>0.289227 s |  |

# EMD-Bipartición-con CM

```
Evaluating \Phi cuts:
                               | 0/6 [00:00<?, ?it/s]
Computing concepts: 0%
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts: 50%
                                | 3/6 [00:00<00:00, 27.85it/s]
                                | 0/6 [00:00<?, ?it/s]
Computing concepts:
Computing concepts:
                     0%
                                 | 0/5 [00:00<?, ?it/s]
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
MIP:
Cut [A, B] —/ /—⊁ [C]
Phi:
\Phi = 0.520834
Time:
0.341088 s
```

# • EMD-Bipartición-sin CM

```
Evaluating \Phi cuts:
                    0%
                                 0/6 [00:00<?, ?it/s]
Computing concepts:
                                  0/6 [00:00<?, ?it/s]
                     0%
Computing concepts:
                     0%
                                  | 0/5 [00:00<?, ?it/s]
                     0%
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
Evaluating O cuts: 50%
                                 3/6 [00:00<00:00, 29.79it/s]
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0%
Computing concepts:
                     0%
                                  0/5 [00:00<?, ?it/s]
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
MIP:
Cut [A, B] --/ /-->- [C]
Phi:
0 = 0.520834
Time:
0.256316 s
```

#### • EMD-Tripartición-con CM

```
Evaluating \Phi cuts:
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                      0%
                                   | 0/6 [00:00<?, ?it/s]
Computing concepts:
                      0%
                                   | 0/5 [00:00<?, ?it/s]
Computing concepts:
                                   | 0/6 [00:00<?, ?it/s]
                      0%
                                   | 0/6 [00:00<?, ?it/s]
Computing concepts:
                      0%
Evaluating \Phi cuts: 67%
                                  4/6 [00:00<00:00, 28.24it/s]
Computing concepts:
                                   0/5 [00:00<?, ?it/s]
                      0%
                                   | 0/6 [00:00<?, ?it/s]
Computing concepts:
                      0%
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
 \Phi = 0.520834
Time:
 0.271785 s
```

#### EMD-Tripartición-sin CM

```
Evaluating \Phi cuts:
                    9% l
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                   | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                   | 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts: 50%
                                 3/6 [00:00<00:00, 27.35it/s]
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0%
                                   | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                                   | 0/6 [00:00<?, ?it/s]
                     9%
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
 0 = 0.520834
Time:
 0.296044 s
```

#### KLD-Bipartición-con CM

```
Evaluating © cuts: 0%|
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts: 67%
                                  4/6 [00:00<00:00, 29.49it/s]
Computing concepts:
                                  | 0/5 [00:00<?, ?it/s]
                     0%
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0% l
MIP:
Cut [A, B] —/ /—➤ [C]
Phi:
\Phi = 0.520834
Time:
0.262299 s
```

#### KLD-Bipartición-sin CM

```
Evaluating \Phi cuts:
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0%
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                     9% l
                                  0/6 [00:00<?, ?it/s]
Evaluating © cuts: 50%
                                 3/6 [00:00<00:00, 29.20it/s]
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     9%
Computing concepts:
                     0%
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
MIP:
Cut [A, B] -/ /--> [C]
Phi:
 \Phi = 0.520834
Time:
0.278293 s
```

#### KLD-Tripartición-con CM

```
Evaluating O cuts:
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     9% l
                                  0/6 [00:00<?, ?it/s]
Evaluating © cuts: 50%
                                 3/6 [00:00<00:00, 27.94it/s]
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0%
Computing concepts:
                     0%|
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
\Phi = 0.520834
Time:
0.277937 s
```

#### • KLD-Tripartición-sin CM

```
Evaluating © cuts: 0%
                                0/6 [00:00<?, ?it/s]
Computing concepts:
                                 0/6 [00:00<?, ?it/s]
                    0%
Computing concepts:
                     0%
                                 | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/6 [00:00<?, ?it/s]
                                | 3/6 [00:00<00:00, 27.35it/s]
Evaluating \Phi cuts: 50%
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                                 | 0/5 [00:00<?, ?it/s]
                     0%
Computing concepts:
                     0%
                                 | 0/6 [00:00<?, ?it/s]
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
\Phi = 0.520834
Time:
0.289227 s
```

#### → Estado-nodo

| Entrada de datos  | Medida de<br>distancia | Esquema de partición | Resultados con<br>CM                        | Resultados sin<br>CM                                       | Observaciones |
|---|------------------------|----------------------|---|--|---------------|
| Grafo:  (A) (B) (C) (OT) (D) (D) (D) (D) (D) (D) (D) (D) (D) (D | EMD                    | biparticion          | MIP:<br>Cut [A, B] ——<br>//——➤ [C]          | MIP:<br>Cut [A, B] ——<br>//——➤ [C]                         |               |
| tpm = np.array([ [0, 0, 0], [1, 0, 0], [1, 0, 1], [0, 0, 1],    |                        |                      | Phi:<br>Φ = 0.520834<br>Time:<br>0.215677 s | Phi:<br>Φ = 0.520834<br>Time:<br>0.300695 s                |               |
| [0, 0, 1],<br>[1, 1, 1],<br>[1, 0, 0],<br>[0, 1, 0]             | EMD                    | tripartición         | MIP:  | MIP:<br>Cut [A, B] ——<br>//——➤ [C]<br>Phi:<br>Φ = 0.520834 |               |
|   |                        |                      | Time:<br>0.216105 s                         | Time:<br>0.316358 s  |               |

| <pre>cm = np.array([ [1, 1, 0], [1, 0, 1], [0, 1, 1] ])</pre> | KLD | bipartición  |   | MIP:<br>Cut [A, B] ——<br>//——➤ [C]<br>Phi:<br>Φ = 0.520834<br>Time:<br>0.300732 s |  |
|---|-----|--------------|---|---|--|
|   | KLD | tripartición | MIP:<br>Cut [A, B] ——<br>/ /—— ➤ [C]<br>Phi:<br>Φ = 0.520834<br>Time:<br>0.285125 s | MIP:<br>Cut [A, B] ——<br>//——➤ [C]<br>Phi:<br>Φ = 0.520834<br>Time:<br>0.416471 s |  |

# • EMD-Bipartición-con CM

```
| 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts:
                    0%
                                | 0/6 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts: 0%
                                | 0/5 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                | 0/6 [00:00<?, ?it/s]
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                    0%
Evaluating \Phi cuts: 67%
                                | 4/6 [00:00<00:00, 39.90it/s]
                                | 0/5 [00:00<?, ?it/s]
Computing concepts:
                    0%
Computing concepts:
                    0%
                                | 0/6 [00:00<?, ?it/s]
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
\Phi = 0.520834
Time:
0.215677 s
```

#### EMD-Bipartición-sin CM

```
0%|
Evaluating \Phi cuts:
                                0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%|
                                  | 0/5 [00:00<?, ?it/s]
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
Evaluating \Phi cuts: 50%
                                 3/6 [00:00<00:00, 25.89it/s]
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0%
Computing concepts:
                     0%
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0%
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
 0 = 0.520834
Time:
0.300695 s
```

# EMD-Tripartición-con CM

```
Evaluating \Phi cuts:
                                  | 0/6 [00:00<?, ?it/s]
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                      0%
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                      0%
                                   | 0/6 [00:00<?, ?it/s]
Computing concepts:
                      0%
                      0%
                                   | 0/6 [00:00<?, ?it/s]
Computing concepts:
Evaluating \Phi cuts: 67%
                                  4/6 [00:00<00:00, 34.53it/s]
Computing concepts:
                                   0/5 [00:00<?, ?it/s]
                      9%
                                   | 0/6 [00:00<?, ?it/s]
Computing concepts:
                      0%
MIP:
Cut [A, B] —/ /—> [C]
Phi:
 \Phi = 0.520834
Time:
0.216105 s
```

## EMD-Tripartición-sin CM

```
Evaluating \Phi cuts: 0%
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts: 0%
                                   | 0/6 [00:00<?, ?it/s]
                                   | 0/5 [00:00<?, ?it/s]
Computing concepts:
                      0%
Computing concepts:
                      0%|
                                   | 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts: 50%
                                  | 3/6 [00:00<00:00, 25.89it/s]
Computing concepts:
                                   | 0/6 [00:00<?, ?it/s]
                      9%
Computing concepts:
                      0%
                                   | 0/5 [00:00<?, ?it/s]
                                   | 0/6 [00:00<?, ?it/s]
Computing concepts:
                      0%
MIP:
 Cut [A, B] —/ /—> [C]
Phi:
 \Phi = 0.520834
Time:
 0.316358 s
```

#### KLD-bipartición-con CM

```
Evaluating \Phi cuts:
                     0% l
                                 0/6 [00:00<?, ?it/s]
Computing concepts:
                                   | 0/6 [00:00<?, ?it/s]
                      0%|
Computing concepts:
                      0%
                                   | 0/5 [00:00<?, ?it/s]
Computing concepts:
                      0%
                                   | 0/6 [00:00<?, ?it/s]
Computing concepts:
                      0%|
                                   | 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts: 67%
                                   4/6 [00:00<00:00, 33.35it/s]
Computing concepts:
                      0%
                                   | 0/5 [00:00<?, ?it/s]
Computing concepts:
                      9% l
                                   | 0/6 [00:00<?, ?it/s]
MIP:
Cut [A, B] -/ /-->- [C]
Phi:
\Phi = 0.520834
Time:
0.21994 s
```

# KLD-Bipartición-sin CM

```
Evaluating \Phi cuts:
                    0%|
                                0/6 [00:00<?, ?it/s]
Computing concepts: 0%
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  0/5 [00:00<?, ?it/s]
                                  | 0/6 [00:00<?, ?it/s]
                     0%
Computing concepts:
Evaluating \Phi cuts: 50%
                                 | 3/6 [00:00<00:00, 25.89it/s]
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0%
Computing concepts:
                     0%|
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     9%
MIP:
Cut [A, B] —/ /—> [C]
Phi:
\Phi = 0.520834
Time:
0.300732 s
```

#### KLD-Tripartición-con CM

```
Evaluating \Phi cuts:
                                  | 0/6 [00:00<?, ?it/s]
                     9% l
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                      0%
                                   | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
                                  | 3/6 [00:00<00:00, 25.89it/s]
Evaluating \Phi cuts: 50%
Computing concepts:
                                   | 0/6 [00:00<?, ?it/s]
                     0%
Computing concepts:
                     0%|
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                   | 0/6 [00:00<?, ?it/s]
Cut [A, B] —/ /—> [C]
Phi:
\Phi = 0.520834
Time:
0.285125 s
```

# • KLD-Tripartición-sin CM

```
Evaluating \Phi cuts:
                   0%|
                              0/6 [00:00<?, ?it/s]
Computing concepts:
                                | 0/6 [00:00<?, ?it/s]
                   0%
                                | 0/5 [00:00<?, ?it/s]
Computing concepts:
                    0%
Evaluating © cuts: 33%
                                2/6 [00:00<00:00, 15.21it/s]
Computing concepts: 0%
                                | 0/6 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                | 0/6 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                | 0/5 [00:00<?, ?it/s]
Evaluating \Phi cuts: 83%
                               | 5/6 [00:00<00:00, 16.72it/s]
Computing concepts:
                                0/6 [00:00<?, ?it/s]
                    0%
MIP:
Cut [A, B] —/ /—> [C]
Phi:
\Phi = 0.520834
Time:
 0.416471 s
```

# → TPM-Multidimensional estado-nodo

| Entrada de datos  | Medida de<br>distancia | Esquema de partición | Resultados con<br>CM  | Resultados sin<br>CM | Observaciones |
|---|------------------------|----------------------|---|----------------------|---------------|
| Grafo:  A B C (MOT) B (MOT) C | EMD                    | biparticion          | MIP:<br>Cut [A, B] ——<br>//——➤ [C]<br>Phi:<br>Φ = 0.520834<br>Time:<br>0.255029 s | Phi:                 |               |
| [1.0, 1.0, 1.0]],<br>[[0.0, 0.0, 1.0],<br>[0.0, 1.0, 0.0]]]   | EMD                    | tripartición         | MIP:<br>Cut [A, B] ——<br>//——➤ [C]<br>Phi:<br>Φ = 0.520834<br>Time:<br>0.231735 s | Phi:                 |               |

| <pre>cm = np.array([ [1, 1, 0], [1, 0, 1], [0, 1, 1] ])</pre> | KLD | bipartición  |                                | MIP:<br>Cut [A, B] ——————————————————————————————————— |  |
|---|-----|--------------|--------------------------------|--|--|
|   | KLD | tripartición | / / <b>──&gt;</b> [C]<br>Phi:  | 0.216126 s  MIP: Cut [A, B] — //— ➤ [C]  Phi:          |  |
|   |     |              | Φ = 0.520834  Time: 0.231697 s | Φ = 0.520834  Time: 0.216092 s                         |  |

# EMD-Bipartición-con CM

```
| 0/6 [00:00<?, ?it/s]
Evaluating O cuts:
                   0%
Computing concepts: 0%
                              0/6 [00:00<?, ?it/s]
Computing concepts: 0%
                              | 0/5 [00:00<?, ?it/s]
Computing concepts: 0%
                               | 0/6 [00:00<?, ?it/s]
Computing concepts:
                   0%
                               | 0/6 [00:00<?, ?it/s]
Evaluating © cuts: 67%
                              4/6 [00:00<00:00, 32.68it/s]
Computing concepts: 0%
                               0/5 [00:00<?, ?it/s]
Computing concepts:
                               | 0/6 [00:00<?, ?it/s]
                   0%
Cut [A, B] —/ /—➤ [C]
Phi:
\Phi = 0.520834
Time:
0.255029 s
```

#### • EMD-Bipartición-sin CM

```
0%
                                 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts:
Computing concepts:
                     0%
                                  0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     9% l
                                  | 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts: 67%
                                  4/6 [00:00<00:00, 34.55it/s]
Computing concepts:
                     0%
                                  0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
MIP:
Cut [A, B] —/ /—⊁ [C]
Phi:
0 = 0.520834
Time:
0.269397 s
```

#### EMD-Tripartición-con CM

```
Evaluating \Phi cuts:
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                      0%
                                   | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                   | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                   | 0/6 [00:00<?, ?it/s]
                      0%
                                   | 0/6 [00:00<?, ?it/s]
Computing concepts:
Evaluating \Phi cuts: 67%
                                  4/6 [00:00<00:00, 34.52it/s]
                                   | 0/5 [00:00<?, ?it/s]
Computing concepts:
                      0%
Computing concepts:
                      0%
                                   0/6 [00:00<?, ?it/s]
MIP:
Cut [A, B] —/ /—> [C]
Phi:
\Phi = 0.520834
Time:
0.231735 s
```

#### EMD-Tripartición-sin CM

```
| 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts:
                    0%
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                    0%
Computing concepts:
                     0%
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
                     9% I
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
Evaluating © cuts: 67%
                                  | 4/6 [00:00<00:00, 34.53it/s]
                     0%
                                  0/5 [00:00<?, ?it/s]
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
Cut [A, B] —/ /—≻ [C]
Phi:
\Phi = 0.520834
Time:
0.21608 s
```

KLD-Bipartición-con CM

```
| 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts:
                    0%
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                     0%
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     9% l
                                  | 0/6 [00:00<?, ?it/s]
Evaluating © cuts: 67%
                                 4/6 [00:00<00:00, 34.53it/s]
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
MIP:
Cut [A, B] —/ /—➤ [C]
Phi:
\Phi = 0.520834
Time:
0.231457 s
```

KLD-Bipartición-sin CM

```
Evaluating \Phi cuts:
                    0%|
                                | 0/6 [00:00<?, ?it/s]
                                | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                     0%
                                 | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts: 50%
                                 3/6 [00:00<00:00, 29.93it/s]
Computing concepts:
                                 | 0/6 [00:00<?, ?it/s]
                     0%
Computing concepts:
                     0%
                                 | 0/5 [00:00<?, ?it/s]
Computing concepts:
                                 | 0/6 [00:00<?, ?it/s]
                     0%
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
\Phi = 0.520834
Time:
0.216126 s
```

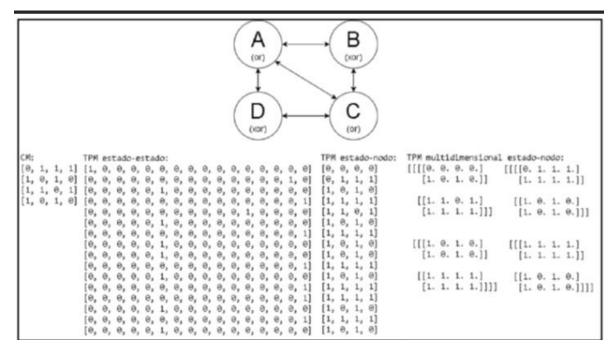
# KLD-Tripartición-con CM

```
Evaluating \Phi cuts:
                    0%
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%|
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%|
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
Evaluating O cuts: 67%
                                  4/6 [00:00<00:00, 34.52it/s]
Computing concepts:
                                  | 0/5 [00:00<?, ?it/s]
                     0%
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
\Phi = 0.520834
Time:
0.231697 s
```

# KLD-Tripartición-sin CM

```
Evaluating \Phi cuts:
                    0%
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0%
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0%
Computing concepts:
                     0%
                                  0/6 [00:00<?, ?it/s]
Evaluating © cuts: 67%
                                 4/6 [00:00<00:00, 32.03it/s]
                                  | 0/5 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0%
MIP:
Cut [A, B] —/ /—> [C]
\Phi = 0.520834
Time:
0.216092 s
```

#### Grafo 2



#### → Estado-estado

| Entrada de datos             | Medida<br>de<br>distancia | Esquema<br>de<br>partición | Resultados<br>con CM   | Resultados<br>sin CM   | Observaciones |
|------------------------------|---------------------------|----------------------------|--|--|---------------|
| Grafo:  A B (or) C (or) (or) | EMD                       | biparticion                | MIP:<br>Cut [A, B,<br>C] ——//<br>——➤ [D]<br>Phi:<br>Φ =<br>1.28125 | MIP:<br>Cut [A, B,<br>C] —//<br>—> [D]<br>Phi:<br>Φ =<br>1.28125 |               |
|                              |                           |                            | Time:<br>1.71135 s   | Time:<br>1.685544  |               |
|                              | EMD                       | tripartición               | MIP:<br>Cut [A, B,<br>C] ——//<br>——➤ [D]                           | C] <del></del> //  |               |
|                              |                           |                            | Phi:<br>Φ =<br>1.28125<br>Time:                                    | Phi:<br>Φ =<br>1.28125<br>Time:                                  |               |

```
tpm = np.array([
                                                      1.701052
                                                                1.617769
S
[0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0],
[0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0],
[0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0],
[0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0],
KLD
                                                      MIP:
                                                               MIP:
                                            bipartición
[0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0],
                                                      Cut [A, B,
                                                                Cut [A, B,
[0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0],
C] <del>---</del>//
                                                               c] ——//
[0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0],
                                                         -> [D]
                                                               —> [D]
Phi:
                                                               Phi:
[0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0],
                                                      Φ=
                                                                Φ=
[0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0],
                                                      1.28125
                                                               1.28125
                                                               Time:
                                                      Time:
cm = np.array([
                                                      1.665161
                                                                1.648836
[0, 1, 1, 1],
                                                               S
[1, 0, 1, 0],
                                    KLD
                                            tripartición
                                                     MIP:
                                                               MIP:
[1, 1, 0, 1],
[1, 0, 1, 0],
                                                      Cut [A, B,
                                                               Cut [A, B,
1)
                                                      c1 <del>---</del>//
                                                               Cl ——//
                                                         -> [D]
                                                               —> [D]
                                                      Phi:
                                                               Phi:
                                                      Φ=
                                                                Φ=
                                                      1.28125
                                                               1.28125
                                                      Time:
                                                               Time:
                                                      1.686463
                                                                1.562435
```

#### EMD-Bipartición-con CM

```
Computing concepts:
                                 | 0/13 [00:00<?, ?it/s]
                     0%
Evaluating © cuts: 79%
                                | 11/14 [00:01<00:00, 9.92it/s]
Computing concepts:
                                 | 0/15 [00:00<?, ?it/s]
                     0%
                                 | 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
Evaluating © cuts: 93%
                                | 13/14 [00:01<00:00, 9.97it/s]
Computing concepts: 0%
                                 | 0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—➤ [D]
Phi:
\Phi = 1.28125
Time:
 1.71135 s
```

# • EMD-Bipartición-sin CM

```
Computing concepts: 0%|
                               | 0/13 [00:00<?, ?it/s]
Evaluating © cuts: 79% | 11/14 [00:01<00:00, 10.13it/s]
Computing concepts: 0%
                               0/15 [00:00<?, ?it/s]
Computing concepts:
                    9% l
                               | 0/13 [00:00<?, ?it/s]
Evaluating © cuts: 93% | 13/14 [00:01<00:00, 10.18it/s]
Computing concepts: 0%
                             | 0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—➤ [D]
Phi:
\Phi = 1.28125
Time:
1.685544 s
```

## • EMD-Tripartición-con CM

```
| 0/13 [00:00<?, ?it/s]
                   0%|
Computing concepts:
Evaluating © cuts: 79%
                              | 11/14 [00:01<00:00, 9.97it/s]
Computing concepts: 0%
                               0/15 [00:00<?, ?it/s]
Computing concepts: 0%
                               | 0/13 [00:00<?, ?it/s]
Evaluating \Phi cuts: 93%
                            | 13/14 [00:01<00:00, 10.19it/s]
Computing concepts: 0%
                               0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—> [D]
\Phi = 1.28125
Time:
1.701052 s
```

#### EMD-Tripartición-sin CM

```
Computing concepts:
                    0%
                               0/13 [00:00<?, ?it/s]
Evaluating © cuts: 79% | 11/14 [00:00<00:00, 10.83it/s]
Computing concepts:
                               0/15 [00:00<?, ?it/s]
                    0%
                               | 0/13 [00:00<?, ?it/s]
Computing concepts:
                    0%
                              | 13/14 [00:01<00:00, 10.76it/s]
Evaluating \Phi cuts: 93%
                               0/13 [00:00<?, ?it/s]
Computing concepts: 0%
MIP:
Cut [A, B, C] —/ /—> [D]
\Phi = 1.28125
Time:
1.617769 s
```

#### KLD-Bipartición-con CM

```
Computing concepts: 0%
                                | 0/13 [00:00<?, ?it/s]
Evaluating \Phi cuts: 79%
                              | 11/14 [00:01<00:00, 10.07it/s]
Computing concepts:
                                | 0/15 [00:00<?, ?it/s]
Computing concepts:
                    0%
                               | 0/13 [00:00<?, ?it/s]
Evaluating 0 cuts: 93% | 13/14 [00:01<00:00, 10.18it/s]
                                | 0/13 [00:00<?, ?it/s]
Computing concepts: 0%
MIP:
Cut [A, B, C] —/ /—> [D]
Phi:
 0 = 1.28125
Time:
 1.665161 s
```

#### KLD-Bipartición-sin CM

```
Computing concepts:
                    0%
                                | 0/13 [00:00<?, ?it/s]
Evaluating O cuts: 79%
                              | 11/14 [00:01<00:00, 10.16it/s]
Computing concepts:
                    0%
                               0/15 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                | 0/13 [00:00<?, ?it/s]
Evaluating 0 cuts: 93% | 13/14 [00:01<00:00, 10.67it/s]
Computing concepts: 0%
                               | 0/13 [00:00<?, ?it/s]
MIP:
 Cut [A, B, C] -/ /-->- [D]
Phi:
 \Phi = 1.28125
Time:
1.648836 s
```

#### KLD-Tripartición-con CM

```
Computing concepts:
                                 | 0/13 [00:00<?, ?it/s]
                    0%
Evaluating © cuts: 79%
                                | 11/14 [00:01<00:00, 10.04it/s]
Computing concepts: 0%
                                0/15 [00:00<?, ?it/s]
Computing concepts: 0%
                                | 0/13 [00:00<?, ?it/s]
Evaluating \Phi cuts: 93%
                            | 13/14 [00:01<00:00, 10.34it/s]
Computing concepts: 0%
                                0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—> [D]
Phi:
\Phi = 1.28125
Time:
1.686463 s
```

#### • KLD-Tripartición-sin CM

```
Evaluating © cuts: 71% | 10/14 [00:00<00:00, 10.89it/s]
                               | 0/13 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts: 0%
                                | 0/15 [00:00<?, ?it/s]
Evaluating © cuts: 86%
                            | 12/14 [00:01<00:00, 10.94it/s]
Computing concepts:
                                | 0/13 [00:00<?, ?it/s]
                    0%
Computing concepts: 0%
                            | 0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—➤ [D]
Phi:
\Phi = 1.28125
Time:
1.562435 s
```

#### → Estado-nodo

| Entrada de datos   | Medida de<br>distancia | Esquema de partición | Resultados con CM  | Resultados sin CM  | Observaciones |
|--|------------------------|----------------------|--|--|---------------|
| Grafo:  A B (wr) C (wr) tpm = np.array([   | EMD                    | biparticion          | MIP:<br>Cut [A, B, C] ——/<br>/——➤ [D]<br>Phi:<br>Φ = 1.28125 | MIP:<br>Cut [A, B, C] ——/<br>/——➤ [D]<br>Phi:<br>Φ = 1.28125 |               |
| [0, 0, 0, 0],<br>[0, 1, 1, 1],   |                        |                      | Time:<br>2.08013 s   | Time:<br>1.750886 s  |               |
| [1, 0, 1, 0],<br>[1, 1, 1, 1],<br>[1, 1, 0, 1],<br>[1, 0, 1, 0],<br>[1, 1, 1, 1],<br>[1, 0, 1, 0], | EMD                    | tripartición         | MIP:<br>Cut [A, B, C] ——/<br>/——➤ [D]<br>Phi:                | MIP: Cut [A, B, C] ——/ /——➤ [D] Phi:                         |               |
| [1, 0, 1, 0],<br>[1, 1, 1, 1],<br>[1, 0, 1, 0],<br>[1, 1, 1, 1],<br>[1, 1, 1, 1],<br>[1, 0, 1, 0], |                        |                      | Φ = 1.28125 Time: 1.778046 s                                 | Φ = 1.28125 Time: 1.688907 s                                 |               |
| [1, 1, 1, 1],<br>[1, 0, 1, 0]<br>])  | KLD                    | bipartición          | MIP:<br>Cut [A, B, C] ——/<br>/——➤ [D]                        | /—→> [D]   |               |
| <pre>cm = np.array([ [0, 1, 1, 1], [1, 0, 1, 0], [1, 1, 0, 1], [1, 0, 1, 0], ])</pre>              |                        |                      | Phi:<br>Φ = 1.28125<br>Time:<br>1.680897 s                   | Phi:<br>Φ = 1.28125<br>Time:<br>1.66701 s                    |               |

| KLD | tripartición | MIP:              | MIP:                  |  |
|-----|--------------|-------------------|-----------------------|--|
|     |              | Cut [A, B, C] ——/ | Cut [A, B, C] ——/     |  |
|     |              | / <b>&gt;</b> [D] | / <del>&gt;</del> [D] |  |
|     |              |                   |                       |  |
|     |              | Phi:              | Phi:                  |  |
|     |              | Φ = 1.28125       | $\Phi = 1.28125$      |  |
|     |              |                   |                       |  |
|     |              | Time:             | Time:                 |  |
|     |              | 1.720237 s        | 1.644308 s            |  |
|     |              |                   |                       |  |
|     |              |                   |                       |  |

#### EMD-Bipartición-con CM

```
0/13 [00:00<?, ?it/s]
Computing concepts:
                    0%
Evaluating \Phi cuts: 79%
                                | 11/14 [00:01<00:00, 7.98it/s]
                    0%|
Computing concepts:
                                 | 0/15 [00:00<?, ?it/s]
                              | | 12/14 [00:01<00:00, 8.14it/s]
Evaluating © cuts: 86%
Computing concepts:
                               0/13 [00:00<?, ?it/s]
Computing concepts:
                            | 0/13 [00:00<?, ?it/s]
                    9%
MIP:
Cut [A, B, C] —/ /—≻ [D]
Phi:
\Phi = 1.28125
Time:
2.08013 s
```

#### • EMD-Bipartición-sin CM

```
Computing concepts:
                    0%
                                | 0/13 [00:00<?, ?it/s]
Evaluating \Phi cuts: 79%
                              | 11/14 [00:01<00:00, 9.56it/s]
                                | 0/15 [00:00<?, ?it/s]
Computing concepts: 0%
Evaluating \Phi cuts: 86%
                           | 12/14 [00:01<00:00, 9.29it/s]
                               | 0/13 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts: 0%
                               0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—➤ [D]
Phi:
\Phi = 1.28125
Time:
1.750886 s
```

# EMD-Tripartición-con CM

```
Computing concepts:
                     0%|
                                 | 0/13 [00:00<?, ?it/s]
Evaluating \Phi cuts: 79%
                                 | 11/14 [00:01<00:00, 9.24it/s]
Computing concepts:
                     0%|
                                 | 0/15 [00:00<?, ?it/s]
Evaluating \Phi cuts: 86%
                               | 12/14 [00:01<00:00, 8.99it/s]
Computing concepts:
                                 | 0/13 [00:00<?, ?it/s]
                     0%|
Computing concepts: 0%
                                | 0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—> [D]
\Phi = 1.28125
Time:
1.778046 s
```

# • EMD-Tripartición-sin CM

```
Computing concepts:
                    0%
                               | 0/13 [00:00<?, ?it/s]
Evaluating 0 cuts: 79% | 11/14 [00:01<00:00, 10.01it/s]
Computing concepts: 0%
                               0/15 [00:00<?, ?it/s]
Computing concepts: 0%
                               | 0/13 [00:00<?, ?it/s]
Evaluating © cuts: 93%
                             | 13/14 [00:01<00:00, 10.33it/s]
Computing concepts: 0%
                               | 0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—> [D]
 0 = 1.28125
Time:
 1.688907 s
```

#### KLD-Bipartición-con CM

```
Computing concepts:
                   0%
                                0/13 [00:00<?, ?it/s]
Evaluating \Phi cuts: 79%
                               | 11/14 [00:01<00:00, 9.83it/s]
Computing concepts: 0%
                                0/15 [00:00<?, ?it/s]
Computing concepts: 0%
                               | 0/13 [00:00<?, ?it/s]
Evaluating 0 cuts: 93% | 13/14 [00:01<00:00, 10.21it/s]
Computing concepts: 0%
                                | 0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—➤ [D]
Phi:
\Phi = 1.28125
Time:
1.680897 s
```

#### KLD-Bipartición-sin CM

```
Computing concepts:
                    0%|
                                | 0/13 [00:00<?, ?it/s]
Evaluating \Phi cuts: 79%
                                | 11/14 [00:01<00:00, 10.02it/s]
Computing concepts:
                    0%
                                | 0/15 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                | 0/13 [00:00<?, ?it/s]
                               | 13/14 [00:01<00:00, 10.21it/s]
Evaluating O cuts: 93%
Computing concepts: 0%
                                0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—> [D]
Phi:
\Phi = 1.28125
Time:
1.66701 s
```

# KLD-Tripartición-con CM

```
Computing concepts:
                   0% l
                               | 0/13 [00:00<?, ?it/s]
Evaluating 0 cuts: 79% 11/14 [00:01<00:00, 9.99it/s]
Computing concepts:
                   0%
                               | 0/15 [00:00<?, ?it/s]
Computing concepts:
                    0%
                               | 0/13 [00:00<?, ?it/s]
Evaluating 0 cuts: 93% | 13/14 [00:01<00:00, 10.15it/s]
Computing concepts: 0%
                               | 0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—> [D]
Phi:
\Phi = 1.28125
Time:
1.720237 s
```

# KLD-Tripartición-sin CM

```
0%|
                                | 0/13 [00:00<?, ?it/s]
Computing concepts:
Evaluating © cuts: 79% | 11/14 [00:01<00:00, 10.36it/s]
Computing concepts:
                                | 0/15 [00:00<?, ?it/s]
                    0%
                    0%
                                | 0/13 [00:00<?, ?it/s]
Computing concepts:
Evaluating \Phi cuts: 93%
                             | 13/14 [00:01<00:00, 10.53it/s]
                               0/13 [00:00<?, ?it/s]
Computing concepts: 0%
MIP:
Cut [A, B, C] —/ /—⊁ [D]
\Phi = 1.28125
Time:
1.644308 s
```

#### → Estado-nodo-multidimensional

| Entrada de datos | Medida de<br>distancia | <b>'</b> | Resultados<br>con CM | Resultados sin<br>CM | Observaciones |
|------------------|------------------------|----------|----------------------|----------------------|---------------|
|                  |                        |          |                      |                      |               |

| Grafo:   | EMD | biparticion  | MIP:                        | MIP:                             |
|--|-----|--------------|-----------------------------|----------------------------------|
| A B (wor)  |     |              | Cut [A, B, C]<br>//         | Cut [A, B, C]<br>——//——<br>➤ [D] |
| D C (or)  tpm = np.array([   |     |              | Phi:<br>Φ = 1.28125         | Phi:<br>Φ = 1.28125              |
| [[[[0.0, 0.0, 0.0, 0.0],<br>[1.0, 0.0, 1.0, 0.0]],<br>[[1.0, 1.0, 0.0, 1.0], |     |              | Time:<br>1.933 s            | Time:<br>1.670471 s              |
| [[1.0, 1.0, 1.0, 1.0]],<br>[[1.0, 1.0, 1.0, 1.0]],                           | EMD | tripartición | MIP:<br>Cut [A, B, C]       | MIP:<br>Cut [A, B, C]            |
| [1.0, 0.0, 1.0, 0.0]],<br>[[1.0, 1.0, 1.0, 1.0],                             |     |              | ➤ [D]                       | <b>≻</b> [D]                     |
| [1.0, 1.0, 1.0, 1.0]] ], [[[[0.0, 1.0, 1.0, 1.0],                            |     |              | Phi:<br>Φ = 1.28125         | Phi:<br>Φ = 1.28125              |
| [[[0.0, 1.0, 1.0, 1.0]],<br>[1.0, 1.0, 1.0, 1.0]],                           | KLD | bipartición  | Time:<br>1.665161 s<br>MIP: | Time:<br>1.733072 s<br>MIP:      |
| [[1.0, 0.0, 1.0, 0.0]]],<br>[[[1.0, 1.0, 1.0, 1.0],                          | KLD | Diparticion  | Cut [A, B, C]               | Cut [A, B, C]                    |
| [1.0, 1.0, 1.0, 1.0]],<br>[[1.0, 0.0, 1.0, 0.0],                             |     |              | ➤ [D]<br>Phi:               | ➤ [D] Phi:                       |
| [1.0, 0.0, 1.0, 0.0]] ] ]  |     |              | Φ = 1.28125<br>Time:        | Φ = 1.28125<br>Time:             |
| 1)   |     |              | 1.81586 s                   | 1.777333 s                       |
| <pre>cm = np.array([ [0, 1, 1, 1], [1, 0, 1, 0],</pre>                       | KLD | tripartición | MIP:<br>Cut [A, B, C]       | MIP:<br>Cut [A, B, C]            |
| [1, 0, 1, 0],<br>[1, 0, 1, 0],<br>[1, 0, 1, 0],                              |     |              | ➤ [D]                       | <b>≻</b> [D]                     |
|  |     |              | Phi:<br>Φ = 1.28125         | Phi:<br>Φ = 1.28125              |
|  |     |              | Time:<br>1.779506 s         | Time:<br>1.844154 s              |

# • EMD-Bipartición-con CM

```
| 0/13 [00:00<?, ?it/s]
Computing concepts:
                    0%
Evaluating © cuts: 79%
                                | 11/14 [00:01<00:00, 8.36it/s]
Computing concepts:
                    0%|
                                | 0/15 [00:00<?, ?it/s]
                                | 0/13 [00:00<?, ?it/s]
Computing concepts:
                    0%
Evaluating © cuts: 93%
                           | 13/14 [00:01<00:00, 8.96it/s]
Computing concepts: 0%
                                | 0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—➤ [D]
Phi:
\Phi = 1.28125
Time:
1.933 s
```

# EMD-Bipartición-sin CM

```
Computing concepts:
                    0%
                                0/13 [00:00<?, ?it/s]
Evaluating 0 cuts: 79% | 11/14 [00:01<00:00, 9.93it/s]
Computing concepts:
                    0%
                                | 0/15 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                | 0/13 [00:00<?, ?it/s]
Evaluating \Phi cuts: 93%
                                | 13/14 [00:01<00:00, 10.25it/s]
Computing concepts: 0%
                                | 0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—> [D]
\Phi = 1.28125
Time:
1.670471 s
```

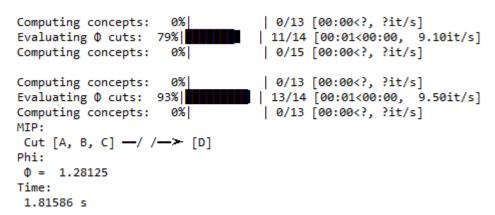
### EMD-Tripartición-con CM

```
Computing concepts:
                    0%
                               0/13 [00:00<?, ?it/s]
Evaluating 0 cuts: 79% | 11/14 [00:01<00:00, 10.23it/s]
Computing concepts:
                               0/15 [00:00<?, ?it/s]
Computing concepts:
                    0%
                               | 0/13 [00:00<?, ?it/s]
                             | 13/14 [00:01<00:00, 10.34it/s]
Evaluating © cuts: 93%
Computing concepts: 0%
                             0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—⊁ [D]
Phi:
\Phi = 1.28125
Time:
 1.665161 s
```

# EMD-Tripartición-sin CM

```
Computing concepts:
                    0%
                                | 0/13 [00:00<?, ?it/s]
Evaluating 0 cuts: 79% | 11/14 [00:01<00:00, 9.77it/s]
                                | 0/15 [00:00<?, ?it/s]
Computing concepts:
                    0%
Computing concepts:
                    0%|
                               | 0/13 [00:00<?, ?it/s]
Evaluating \Phi cuts: 93%
                             | 13/14 [00:01<00:00, 9.98it/s]
                                | 0/13 [00:00<?, ?it/s]
Computing concepts: 0%
MIP:
Cut [A, B, C] —/ /—> [D]
\Phi = 1.28125
Time:
1.733072 s
```

#### KLD-Bipartición-con CM



#### KLD-Bipartición-sin CM

```
| 0/13 [00:00<?, ?it/s]
Computing concepts:
                    0%
Evaluating \Phi cuts: 79%
                                | 11/14 [00:01<00:00, 9.07it/s]
                                | 0/15 [00:00<?, ?it/s]
Computing concepts: 0%
                    0%|
                                | 0/13 [00:00<?, ?it/s]
Computing concepts:
Evaluating © cuts: 93% | 13/14 [00:01<00:00, 9.06it/s]
Computing concepts: 0%
                                0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—> [D]
Phi:
\Phi = 1.28125
Time:
1.777333 s
```

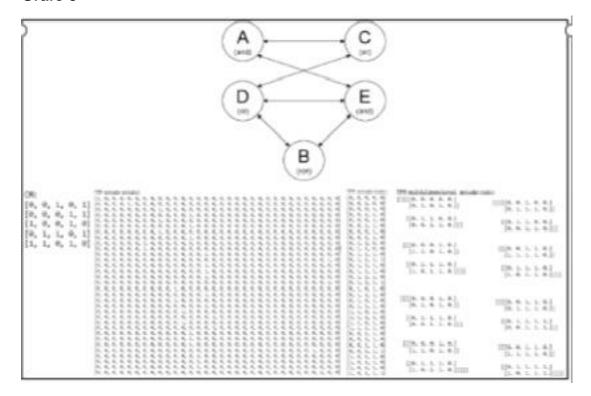
#### • KLD-Tripartición-con CM

```
Computing concepts: 0%
                                0/13 [00:00<?, ?it/s]
Evaluating O cuts: 79%
                               | 11/14 [00:01<00:00, 9.31it/s]
Computing concepts:
                    0%
                                | 0/15 [00:00<?, ?it/s]
Evaluating \Phi cuts: 86%
                             | 12/14 [00:01<00:00, 8.95it/s]
                               | 0/13 [00:00<?, ?it/s]
Computing concepts:
                    0%
Computing concepts: 0%
                               | 0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—➤ [D]
Phi:
\Phi = 1.28125
Time:
1.779506 s
```

# • KLD-Tripartición-sin CM

```
Computing concepts:
                    0%
                               | 0/13 [00:00<?, ?it/s]
Evaluating © cuts: 79%
                               | 11/14 [00:01<00:00, 9.08it/s]
Computing concepts:
                               | 0/15 [00:00<?, ?it/s]
                   0%
Evaluating © cuts: 86%
                           | 12/14 [00:01<00:00, 8.80it/s]
Computing concepts:
                   0%
                               | 0/13 [00:00<?, ?it/s]
Computing concepts: 0%
                           | 0/13 [00:00<?, ?it/s]
MIP:
Cut [A, B, C] —/ /—⊁ [D]
Phi:
\Phi = 1.28125
Time:
1.844154 s
```

# Grafo 3

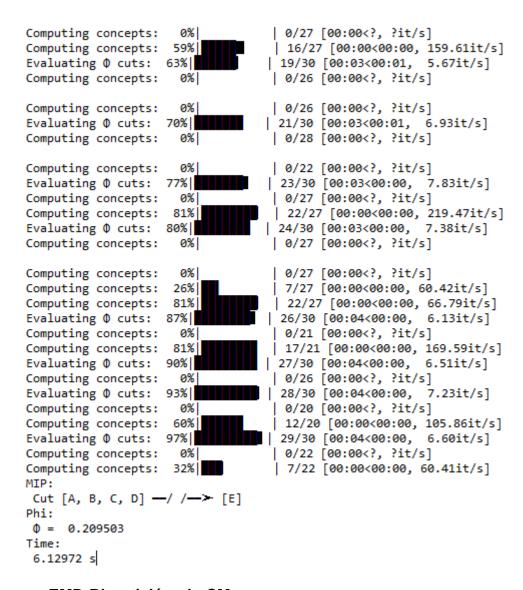


# → Estado-estado

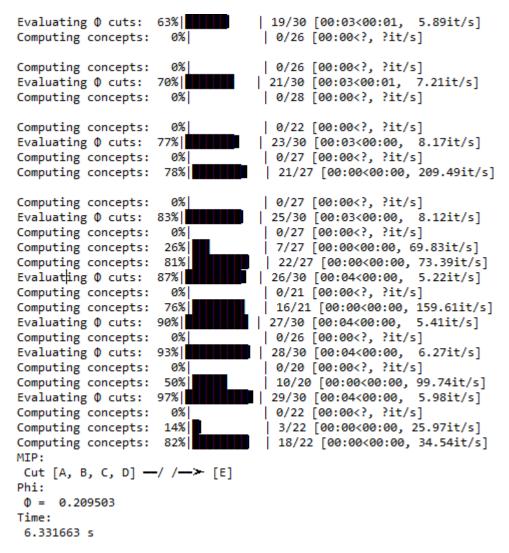
| Entrada de datos           | Medida de<br>distancia | Esquema de partición | Resultados con<br>CM                    | Resultados sin CM  |
|----------------------------|------------------------|----------------------|---|--|
| Grafo:    ton = np.array([ | EMD                    | biparticion          | —//——➤ [E] Phi: Φ = 0.209503            | MIP:<br>Cut [A, B, C, D] —<br>—//——➤ [E]<br>Phi:<br>Φ = 0.209503 |
|                            |                        |                      | Time:<br>6.12972 s                      | Time:<br>6.331663 s  |
|                            | EMD                    | tripartición         | MIP: Cut [A, B, C, D] — —//——➤ [E] Phi: | MIP: Cut [A, B, C, D] — —//——➤ [E] Phi:                          |
|                            |                        |                      | Φ = 0.209503  Time: 6.283878 s          | Φ = 0.209503  Time: 6.463549 s                                   |

| <pre>cm = np.array([ [0,0,1,0,1], [0,0,0,1,1], [1,0,0,1,0], [0,1,1,0,1], [1,1,0,1,0] ])</pre> | KLD | bipartición  | MIP:<br>Cut [A, B, C, D] —<br>—//——➤ [E]<br>Phi:<br>Φ = 0.209503<br>Time:<br>6.455328 s | MIP: Cut [A, B, C, D] — —//—→ [E]  Phi: Φ = 0.209503  Time: 6.738606 s                  |
|---|-----|--------------|---|---|
|   | KLD | tripartición | MIP:<br>Cut [A, B, C, D] —<br>—//— ➤ [E]<br>Phi:<br>Φ = 0.209503<br>Time:<br>6.454886 s | MIP:<br>Cut [A, B, C, D] —<br>—//— ➤ [E]<br>Phi:<br>Φ = 0.209503<br>Time:<br>6.286688 s |

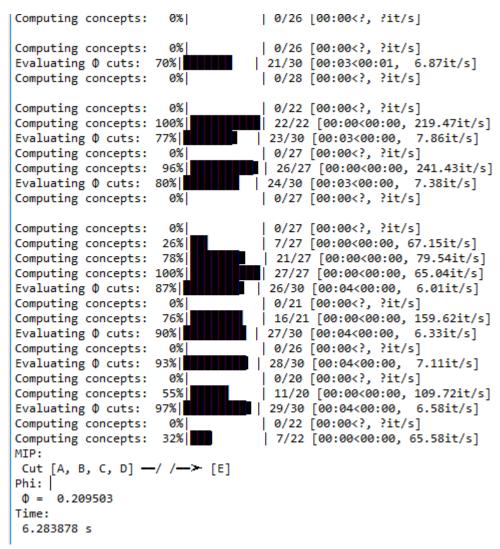
# • EMD-Bipartición-con CM



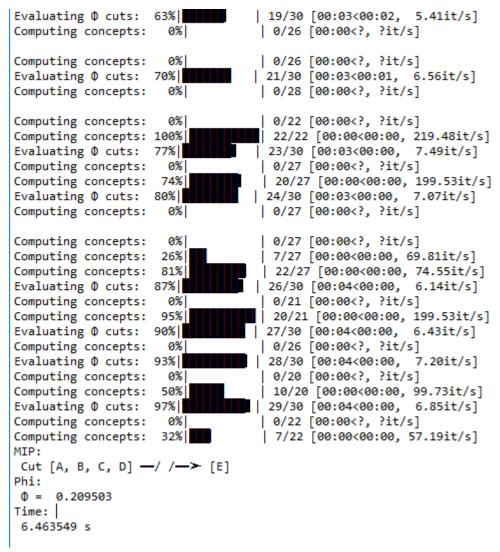
#### EMD-Bipartición-sin CM



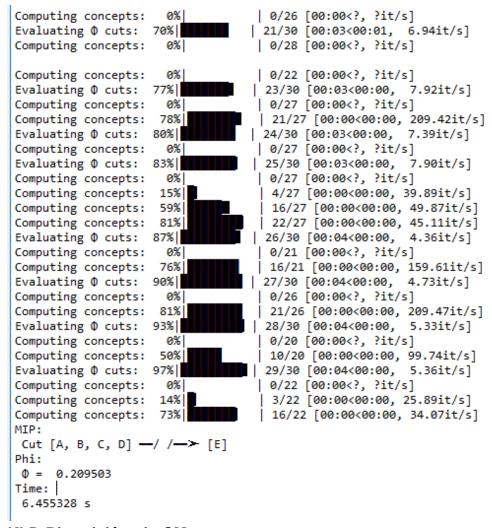
#### EMD-Tripartición-con CM



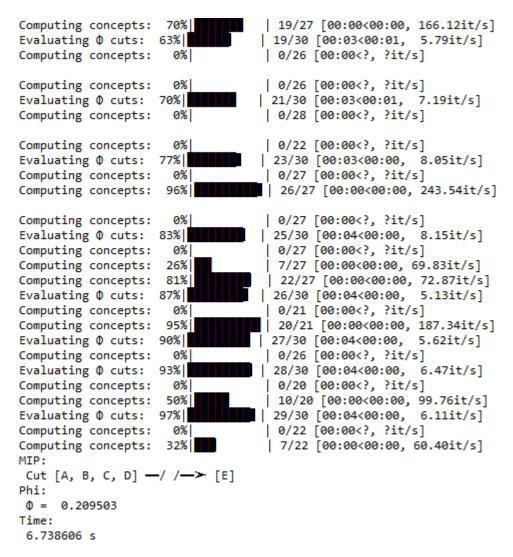
#### EMD-Tripartición-sin CM



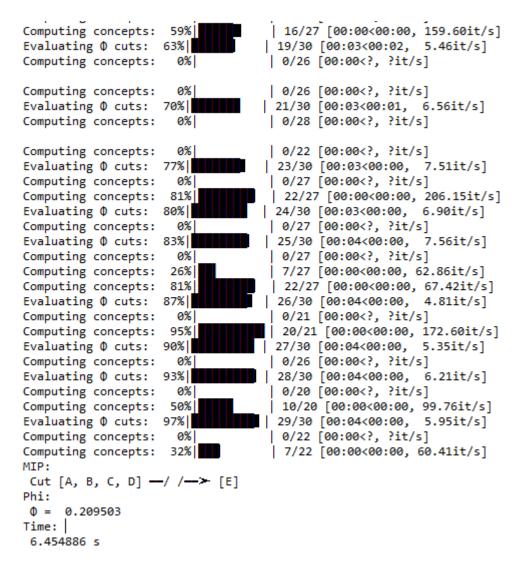
### KLD-Bipartición-con CM



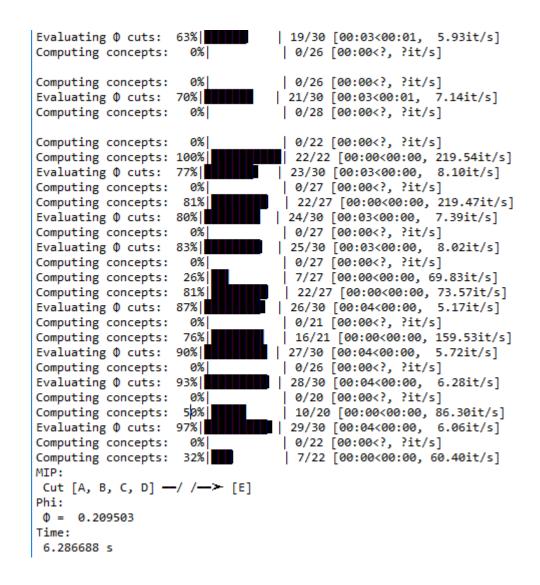
### KLD-Bipartición-sin CM



#### KLD-Tripartición-con CM



## KLD-Tripartición-sin CM

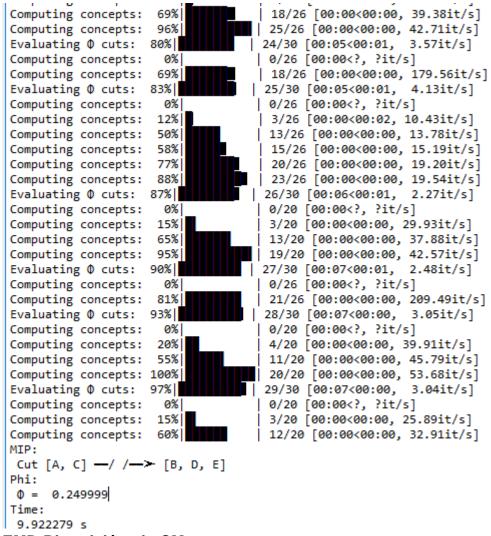


#### → Estado-nodo

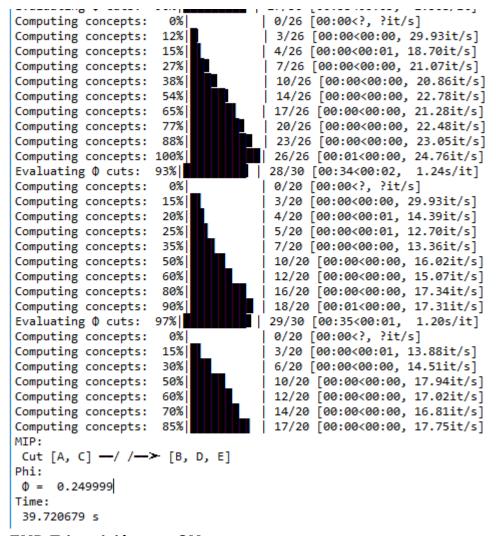
| Entrada de datos | Medida de<br>distancia | Esquema de<br>partición | Resultados con CM   | Resultados sin CM    |
|------------------|------------------------|-------------------------|---------------------|----------------------|
| Grafo:           | EMD                    | biparticion             | MIP:                | MIP:                 |
| (A) (C)          |                        |                         | Cut [A, C] ——/ /——  | Cut [A, C] ——/ /——   |
| (m) (m)          |                        |                         | ➤ [B, D, E]         | ➤ [B, D, E]          |
| D E evet         |                        |                         | Phi:                | Phi:                 |
|                  |                        |                         | Φ = 0.249999        | Φ = 0.249999         |
| B (009)          |                        |                         | Time:<br>9.922279 s | Time:<br>39.720679 s |

|  | 1   |              | 1                  | 1                  |
|--|-----|--------------|--------------------|--------------------|
| tpm = np.array([                       | EMD | tripartición | MIP:               | MIP:               |
| [0,0,0,0,0],                           |     |              | Cut [A, C] ——/ /—— | Cut [A, C] ——/ /—— |
| [0,0,1,0,1],                           |     |              | ➤ [B, D, E]        | ➤ [B, D, E]        |
| [0,0,0,1,1],                           |     |              | [5, 5, 2]          | [5, 5, 2]          |
| [0,0,1,1,1],                           |     |              |                    |                    |
| [1,0,0,1,0],                           |     |              | Phi:               | Phi:               |
| [1,0,1,1,1],                           |     |              | $\Phi = 0.249999$  | $\Phi = 0.249999$  |
| [1,0,0,1,1],                           |     |              |                    |                    |
| [1,0,1,1,1],                           |     |              | Time:              | Time:              |
| [0,1,1,0,1],                           |     |              | 12.107863 s        | 39.274809 s        |
| [0,1,1,0,1],                           |     | 1            |                    |                    |
| [0,1,1,1,1],                           | KLD | bipartición  | MIP:               | MIP:               |
| [0,1,1,1,1],                           |     |              | Cut [A, C] ——/ /—— | Cut [A, C] ——/ /—— |
| [1,1,1,1,1],                           |     |              | ➤ [B, D, E]        | ➤ [B, D, E]        |
| [1,1,1,1,1],                           |     |              |                    |                    |
| [1,1,1,1,1],                           |     |              | Phi:               | Phi:               |
| [1,1,1,1,1],                           |     |              |                    |                    |
| [1,1,0,1,0],                           |     |              | Φ = 0.249999       | Φ = 0.249999       |
| [1,1,1,1,1],                           |     |              |                    |                    |
| [1,1,0,1,1],                           |     |              | Time:              | Time:              |
| [1,1,1,1,1],                           |     |              | 10.109698 s        | 44.130286 s        |
| [1,1,0,1,0],                           |     |              |                    |                    |
| [1,1,1,1,1],                           |     |              |                    |                    |
| [1,1,0,1,1],<br>[1,1,1,1,1],           |     |              |                    |                    |
| [1,1,1,1,1],                           | KLD | tripartición | MIP:               | MIP:               |
| [1,1,1,1,1],                           |     |              | Cut [A, C] ——/ /—— | Cut [A, C] ——/ /—— |
| [1,1,1,1,1],                           |     |              | ➤ [B, D, E]        | ➤ [B, D, E]        |
| [1,1,1,1,1],                           |     |              | [6, 0, 1]          | / [B, D, L]        |
| [1,1,1,1,1],                           |     |              |                    |                    |
| [1,1,1,1,1],                           |     |              | Phi:               | Phi:               |
| [1,1,1,1,1],                           |     |              | $\Phi = 0.249999$  | Φ = 0.249999       |
| [1,1,1,1,1]                            |     |              |                    |                    |
| ])                                     |     |              | Time:              | Time:              |
|  |     |              | 10.796676 s        | 39.269661 s        |
|  |     |              | 10.7500703         | 35.2030013         |
|  |     |              |                    |                    |
| - nn - n |     |              |                    |                    |
| cm = np.array([                        |     |              |                    |                    |
| [0,0,1,0,1],<br>[0,0,0,1,1],           |     |              |                    |                    |
| [1,0,0,1,0],                           |     |              |                    |                    |
| [0,1,1,0,1],                           |     |              |                    |                    |
| [1,1,0,1,0]                            |     |              |                    |                    |
| ])                                     |     |              |                    |                    |
| 17                                     |     |              |                    |                    |
|  |     |              |                    |                    |
|  | 1   | J.           | I                  | l .                |

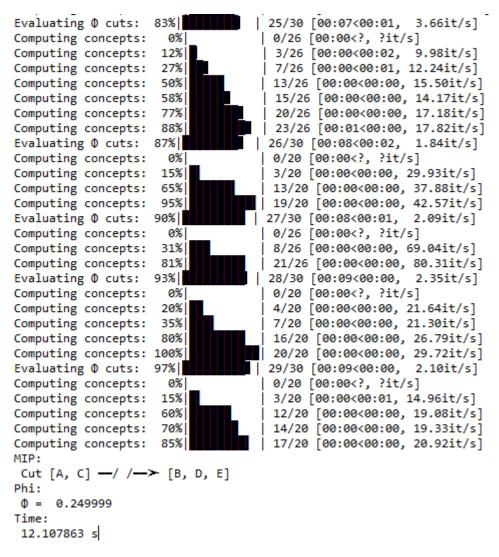
# • EMD-Bipartición-con CM



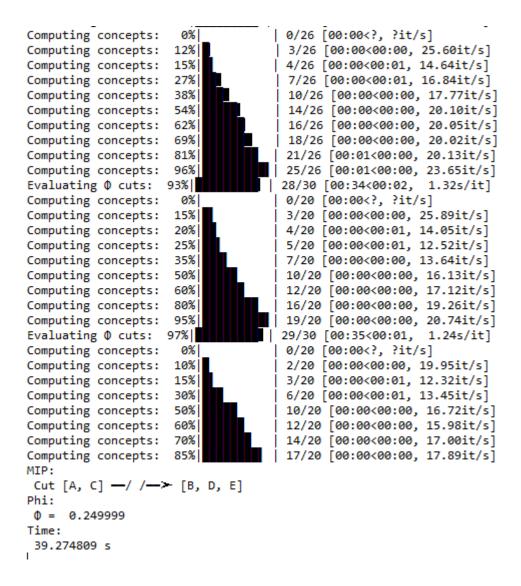
#### EMD-Bipartición-sin CM



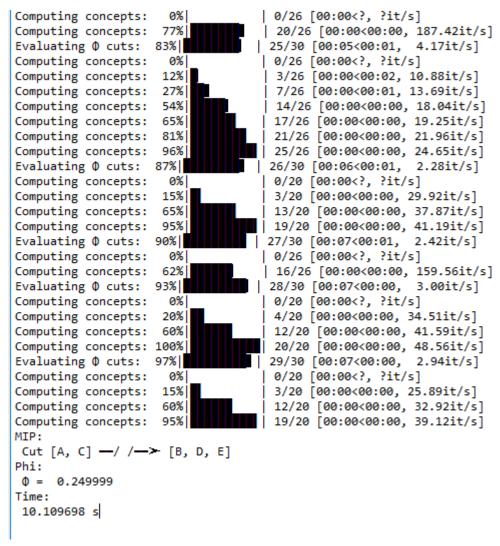
#### EMD-Tripartición-con CM



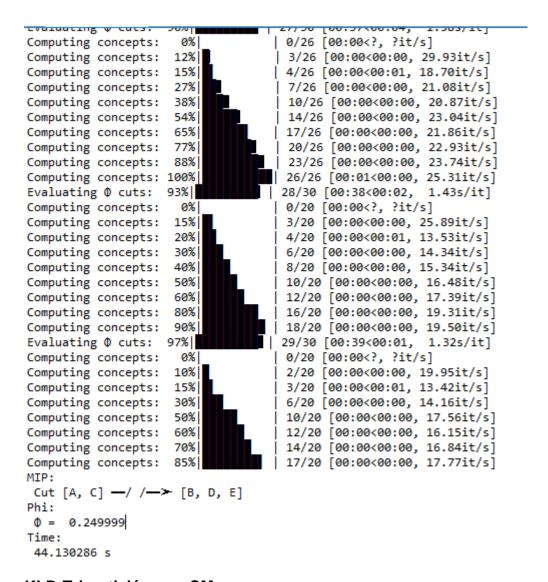
# EMD-Tripartición-sin CM



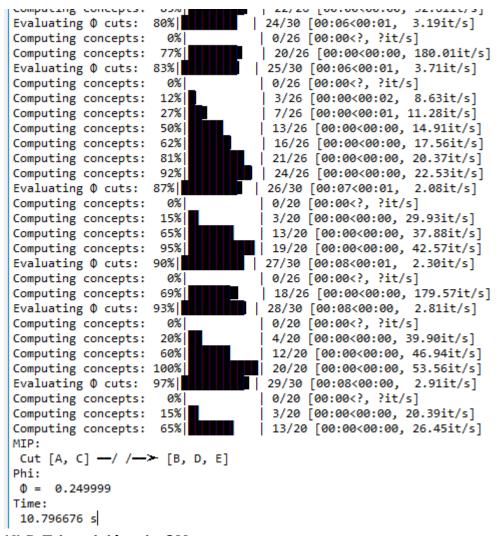
### KLD-Bipartición-con CM



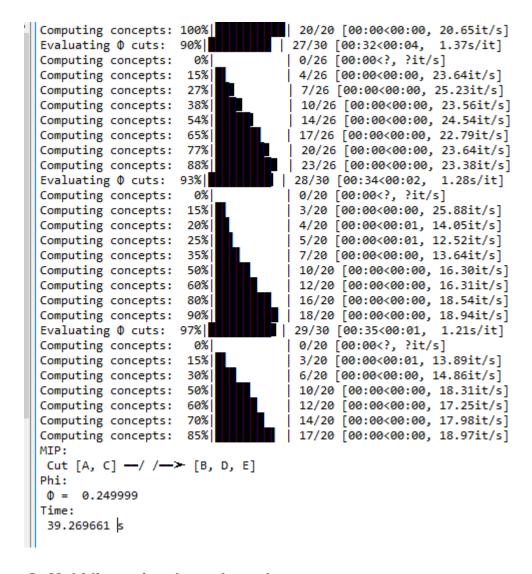
#### KLD-Bipartición-sin CM



## KLD-Tripartición-con CM



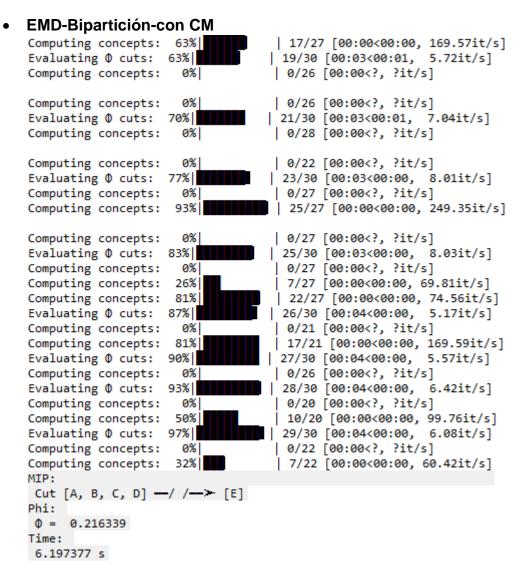
## KLD-Tripartición-sin CM



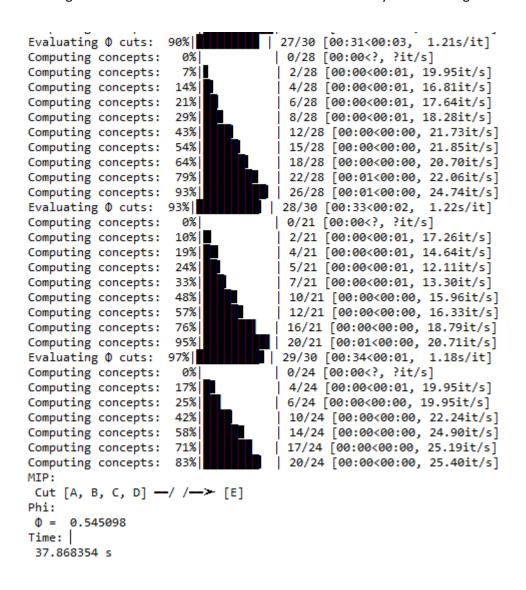
#### → Multidimensional estado-nodo

| Entrada de datos | Medida de<br>distancia | Esquema de partición | Resultados con CM     | Resultados sin CM     |
|------------------|------------------------|----------------------|-----------------------|-----------------------|
| Grafo:           | EMD                    | biparticion          | MIP:                  | MIP:                  |
| (A) (C)          |                        |                      | Cut [A, B, C, D] ——// | Cut [A, B, C, D] ——// |
| (ind)            |                        |                      | —— <b>&gt;</b> [E]    | —→ [E]                |
| D E (set)        |                        |                      | Phi:<br>Φ = 0.216339  | Phi:<br>Φ = 0.545098  |
| B (M)            |                        |                      | Time:<br>6.197377 s   | Time:<br>37.868354 s  |

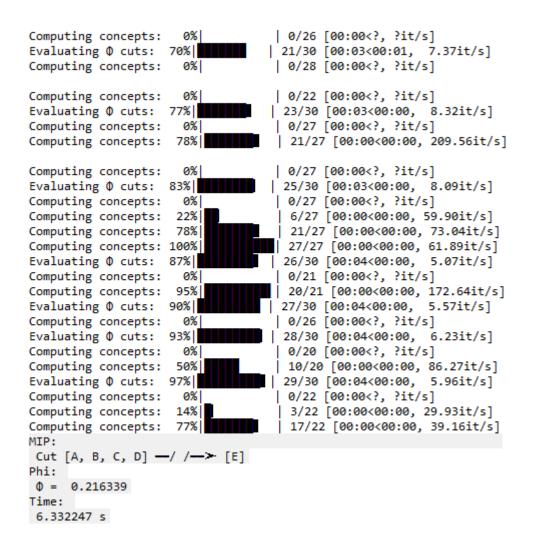
| tpm = np.array([ [[[[[0.0, 0.0, 0.0,0.0,0.0], [0.0, 1.0, 0.0,1.0,0.0]], [[0.0, 1.0, 1.0,0.0,0.0],                          | EMD  | tripartición | MIP:<br>Cut [A, B, C, D] ——//<br>——➤ [E] | MIP:<br>Cut [A, B, C, D] ——//<br>——➤ [E] |
|--|------|--------------|--|--|
| [0.0, 0.0, 1.0,1.0,0.0]],<br>[[[0.0, 0.0, 0.0,1.0,0.0],<br>[1.0, 1.0, 0.0,1.0,0.0]],<br>[[0.0, 1.0, 1.0,1.0,0.0],          |      |              | Phi:<br>Φ = 0.216339                     | Phi:<br>Φ = 0.545098                     |
| [i.e, e.e, 1.e,1.e,e.e]]], [[[[e.e, e.e, e.e,1.e,e.e], [e.e, 1.e, e.e,1.e,e.e]], [[e.e, 1.e, 1.e,1.e,e.e],                 | KLD  | bipartición  | Time:<br>6.332247 s<br>MIP:              | Time: 38.488696 s                        |
| [8.8, 8.8, 1.8,1.8,8.8]]],<br>[[[8.8, 8.8, 8.8,1.8,8.8],<br>[1.8, 1.8, 8.8,1.8,8.8]],                                      |      |              | Cut [A, B, C, D] ——// ——➤ [E] Phi:       | Cut [A, B, C, D] ——// ——➤ [E] Phi:       |
| [[0.0,1.0,1.0,1.0,0.0],<br>[1.0,0.0,1.0,1.0,0.0]]]]],<br>[[[[[0.0, 0.0, 1.0,0.0,0.0],<br>[0.0, 1.0, 1.0,1.0,0.0]],         |      |              | $\Phi$ = 0.216339                        | $\Phi$ = 0.545098 Time:                  |
| [[0.0, 1.0, 1.0,1.0,0.0],<br>[0.0, 0.0, 1.0,1.0,0.0]],<br>[[[0.0, 0.0, 1.0,1.0,0.0],<br>[1.0, 1.0, 1.0,1.0,0.0]],          | KLD  | tripartición | 6.330175 s<br>MIP:                       | 41.678278 s MIP:                         |
| [[0.0, 1.0, 1.0, 1.0,0.0],<br>[1.0, 0.0, 1.0,1.0,0.0]]]],<br>[[[[0.0, 0.0, 1.0,1.0,0.0],<br>[0.0, 1.0, 1.0,1.0,0.0]],      | INED | triparticion | Cut [A, B, C, D] ——// ——➤ [E]            |  |
| [[8.8, 1.8, 1.8, 1.8, 1.8],<br>[8.8, 8.8, 1.8, 1.8, 1.8]]],<br>[[[8.8, 8.8, 1.8, 1.8, 8.8],<br>[1.8, 1.8, 1.8, 1.8, 8.8]], |      |              | Phi:<br>Φ = 0.216339<br>Time:            | Phi: $\Phi = 0.545098$ Time:             |
| [[0.0, 1.0, 1.0,1.0,1.0],<br>[1.0, 0.0, 1.0,1.0,1.0]]]]]<br>])   |      |              | 6.279065 s                               | 39.336349 s                              |
| <pre>cm = np.array([ [0,0,1,0,1], [0,0,0,1,1], [1,0,0,1,0], [0,1,1,0,1], [1,1,0,1,0] ])</pre>                              |      |              |  |  |



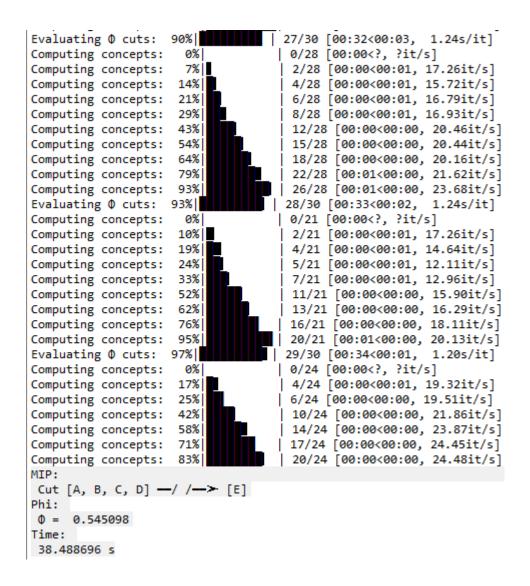
## EMD-Bipartición-sin CM



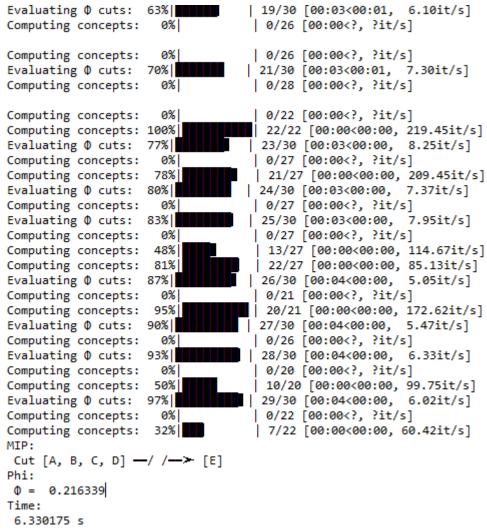
# • EMD-Tripartición-con CM



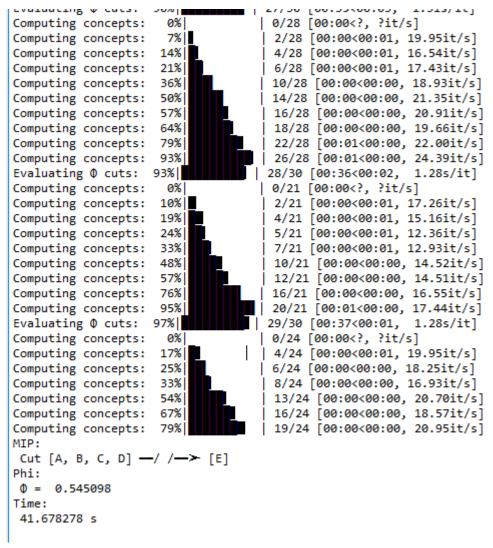
### EMD-Tripartición-sin CM



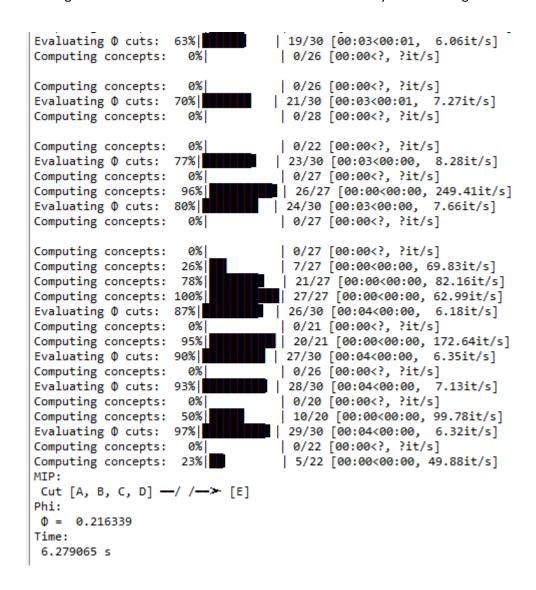
### KLD-Bipartición-con CM



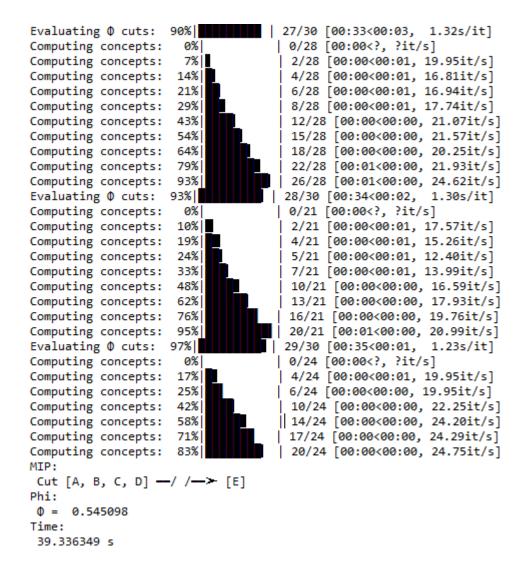
#### KLD-Bipartición-sin CM



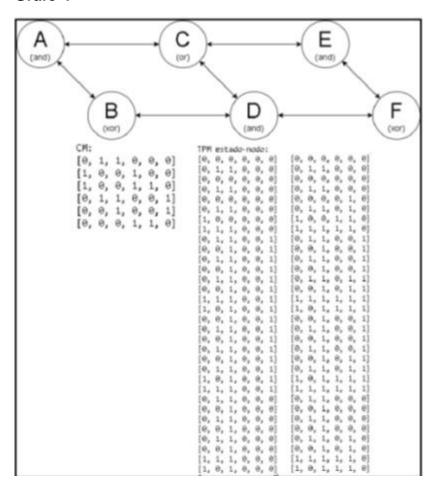
### KLD-Tripartición-con CM



### • KLD-tripartición-sin CM



# Grafo 4



# → Estado-nodo

| → Entrada de datos                                    | Medida<br>de<br>distancia | Esquema<br>de<br>partición | Resultados<br>con CM  | Resultados<br>sin CM   | Observaciones |
|---|---------------------------|----------------------------|---|--|---------------|
| Grafo:  A  (and)  B  (ind)  (ind)  F  (ind)  F  (ind) | EMD                       | biparticion                | MIP:<br>Cut [A, B,<br>C, E, F] —<br>—//—<br>➤ [D]<br>Phi:<br>Φ =<br>0.250981<br>Time:<br>5.380019 s | MIP: Cut [A, B, C, E, F] — —//— ➤ [D]  Phi: Φ = 0.250981  Time: 5.257774 s |               |

| Γ  | I   |              | 1 :                     |              |
|--|-----|--------------|-------------------------|--------------|
| tpm = np.array([                           | EMD | tripartición | MIP:                    | MIP:         |
| [0, 0, 0, 0, 0, 0],                        |     |              | Cut [A, B,              | Cut [A, B,   |
| [0, 1, 1, 0, 0, 0],                        |     |              | C, E, F] —              | C, E, F] —   |
| [0, 0, 0, 0, 0],                           |     |              |                         | · · · · =    |
| [0, 1, 1, 0, 0, 0],                        |     |              | <b>-</b> // <del></del> | <b>-</b> //  |
| [0, 0, 0, 0, 0, 0],                        |     |              | <b>≻</b> [D]            | <b>≻</b> [D] |
| [0, 1, 1, 0, 0, 0],                        |     |              |                         |              |
| [1, 0, 0, 0, 0, 0],                        |     |              | Phi:                    | Phi:         |
| [1, 1, 1, 0, 0, 0],                        |     |              | Φ =                     | Φ =          |
| [0, 1, 1, 0, 0, 1],                        |     |              | 0.250981                | 0.250981     |
| [0, 0, 1, 0, 0, 1],                        |     |              | 0.230301                | 0.230301     |
| [0, 1, 1, 0, 0, 1],<br>[0, 0, 1, 0, 0, 1], |     |              | <b>-</b> *              | <b>T</b>     |
| [0, 1, 1, 0, 0, 1],                        |     |              | Time:                   | Time:        |
| [0, 0, 1, 0, 0, 1],                        |     |              | 4.995994 s              | 5.316542 s   |
| [1, 1, 1, 0, 0, 1],                        | KLD | bipartición  | MIP:                    | MIP:         |
| [1, 0, 1, 0, 0, 1],                        |     |              | Cut [A, B,              | Cut [A, B,   |
| [0, 0, 1, 0, 0, 1],                        |     |              | C, E, F] —              | C, E, F] —   |
| [0, 1, 1, 0, 0, 1],                        |     |              |                         |              |
| [0, 0, 1, 0, 0, 1],                        |     |              | <b>-//</b>              | <b>-</b> //  |
| [0, 1, 1, 0, 0, 1],                        |     |              | <b>≻</b> [D]            | <b>≻</b> [D] |
| [0, 0, 1, 0, 0, 1],                        |     |              |                         |              |
| [0, 1, 1, 0, 0, 1],                        |     |              | Phi:                    | Phi:         |
| [1, 0, 1, 0, 0, 1],                        |     |              | Φ =                     | Φ =          |
| [1, 1, 1, 0, 0, 1],                        |     |              | 0.250981                | 0.250981     |
| [0, 1, 1, 0, 0, 0],                        |     |              | 0.230301                | 0.230301     |
| [0, 0, 1, 0, 0, 0],                        |     |              | T:                      | Time         |
| [0, 1, 1, 0, 0, 0],                        |     |              | Time:                   | Time:        |
| [0, 0, 1, 0, 0, 0],                        |     |              | 5.143403 s              | 5.167946 s   |
| [0, 1, 1, 0, 0, 0],                        | KLD | tripartición | MIP:                    | MIP:         |
| [0, 0, 1, 0, 0, 0],<br>[1, 1, 1, 0, 0, 0], |     |              | Cut [A, B,              | Cut [A, B,   |
| [1, 0, 1, 0, 0, 0],                        |     |              | C, E, F] —              | C, E, F] —   |
| [0, 0, 0, 0, 0, 0],                        |     |              |                         |              |
| [0, 1, 1, 0, 0, 0],                        |     |              | —// <del>—</del>        | <b>-</b> //  |
| [0, 0, 0, 0, 0, 0],                        |     |              | <b>≻</b> [D]            | <b>≻</b> [D] |
| [0, 1, 1, 0, 0, 0],                        |     |              |                         |              |
|  |     |              | Phi:                    | Phi:         |
|  |     |              | Φ =                     | Φ =          |
|  |     |              | 0.250981                | 0.250981     |
|  |     |              |                         |              |
|  |     |              | Time:                   | Time:        |
|  |     |              |                         |              |
|  |     |              | 5.128369 s              | 5.14777 s    |

```
[0, 0, 0, 0, 1, 0],
[0, 1, 1, 0, 1, 0],
[1, 0, 0, 1, 1, 0],
[1, 1, 1, 1, 1, 0],
[0, 1, 1, 0, 0, 1],
[0, 0, 1, 0, 0, 1],
[0, 1, 1, 0, 0, 1],
[0, 0, 1, 0, 0, 1],
[0, 1, 1, 0, 1, 1],
[0, 0, 1, 0, 1, 1],
[1, 1, 1, 1, 1, 1],
[1, 0, 1, 1, 1, 1],
[0, 0, 1, 0, 0, 1],
[0, 1, 1, 0, 0, 1],
[0, 0, 1, 0, 0, 1],
[0, 1, 1, 0, 0, 1],
[0, 0, 1, 0, 1, 1],
[0, 1, 1, 0, 1, 1],
[1, 0, 1, 1, 1, 1],
[1, 1, 1, 1, 1, 1],
[0, 1, 1, 0, 0, 0],
[0, 0, 1, 0, 0, 0],
[0, 1, 1, 0, 0, 0],
[0, 0, 1, 0, 0, 0],
[0, 1, 1, 0, 1, 0],
[0, 0, 1, 0, 1, 0],
[1, 1, 1, 1, 1, 0],
[1, 0, 1, 1, 1, 0],
1)
cm = np.array([
[0, 1, 1, 0, 0, 0],
[1, 0, 0, 1, 0, 0],
[1, 0, 0, 1, 1, 0],
[0, 1, 1, 0, 0, 1],
[0, 0, 1, 0, 0, 1],
[0, 0, 0, 1, 1, 0],
1)
```

# • EMD-Bipartición-con CM

```
Computing concepts: 0% | | 0/52 [00:00<?, ?it/s] Evaluating Φ cuts: 97% | | 60/62 [00:04<00:00, 12.88it/s] | 60/62 [00:04<00:00, 12.88it/s] | 0/41 [00:00<?, ?it/s] | 0/41 [00:00<?, ?it/s] | 0/38 [0
```

# • EMD-Bipartición-sin CM

```
Computing concepts: 0% | | 0/41 [00:00<?, ?it/s]

Evaluating Φ cuts: 98% | | 61/62 [00:04<00:00, 12.21it/s]

Computing concepts: 0% | | 0/38 [00:00<?, ?it/s]

MIP:

Cut [A, B, C, E, F] --/ /--> [D]

Phi:

Φ = 0.250981

Time:
5.257774 s
```

# EMD-Tripartición-con CM

```
Computing concepts: 0% | | 0/52 [00:00<?, ?it/s] Evaluating Φ cuts: 97% | 60/62 [00:04<00:00, 14.12it/s] | 60/62 [00:04<00:00, 14.12it/s] | 0/41 [00:00<?, ?it/s] | 0/41 [00:00<?, ?it/s] | 0/38 [00:
```

# EMD-Tripartición-sin CM

```
Computing concepts: 0% | | 0/41 [00:00<?, ?it/s]

Evaluating Φ cuts: 98% | | 61/62 [00:04<00:00, 12.00it/s]

Computing concepts: 0% | | 0/38 [00:00<?, ?it/s]

MIP:

Cut [A, B, C, E, F] —/ /—> [D]

Phi:

Φ = 0.250981

Time:
5.316542 s
```

# • KLD-Bipartición-con CM

```
Computing concepts: 0% | | 0/41 [00:00<?, ?it/s] Evaluating Φ cuts: 98% | | 61/62 [00:04<00:00, 13.83it/s] | 61/62 [00:00<?, ?it/s] | 0/38 [00:00<?, ?it/s] | MIP:

Cut [A, B, C, E, F] --/ /--> [D] | Phi:

Φ = 0.250981 | Time:
5.143403 s
```

# KLD-Bipartición-sin CM

```
Computing concepts: 0% | | 0/41 [00:00<?, ?it/s]

Evaluating Φ cuts: 98% | | 61/62 [00:04<00:00, 13.59it/s]

Computing concepts: 0% | | 0/38 [00:00<?, ?it/s]

MIP:

Cut [A, B, C, E, F] --/ /--> [D]

Phi:

Φ = 0.250981

Time:
5.167946 s
```

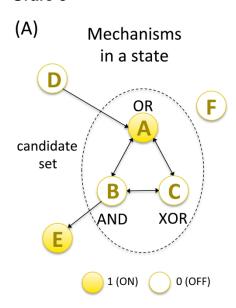
# KLD-Tripartición-con CM

```
Computing concepts: 0% | | 0/52 [00:00<?, ?it/s] Evaluating Φ cuts: 97% | | 60/62 [00:04<00:00, 13.50it/s] | 60/62 [00:04<00:00, 13.50it/s] | 0/41 [00:00<?, ?it/s] | 0/41 [00:00<?, ?it/s] | 0/38 [0
```

# • KLD-Tripartición-sin CM

```
Computing concepts: 0% | | 0/52 [00:00<?, ?it/s] | Evaluating Φ cuts: 97% | | 60/62 [00:04<00:00, 13.27it/s] | 0/41 [00:00<?, ?it/s] | 0/41 [00:00<?, ?it/s] | 0/41 [00:00<?, ?it/s] | O/38 [00:00<?,
```

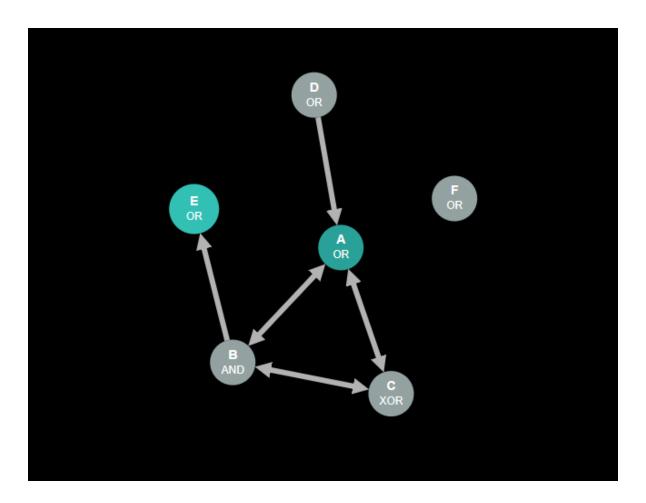
Grafo 5



(B) Transition Probability Matrix (TPM)

| $t_0$ ABC  | ABC<br>000 | 100 | 010 | 110 | 001 | 101 | 011 | 111 |
|------------|------------|-----|-----|-----|-----|-----|-----|-----|
| ABC<br>000 | 1          | 0   | 0   | 0   | 0   | 0   | 0   | 0   |
| 100        | 0          | 0   | 0   | 0   | 1   | 0   | 0   | 0   |
| 010        | 0          | 0   | 0   | 0   | 0   | 1   | 0   | 0   |
| 110        | 0          | 1   | 0   | 0   | 0   | 0   | 0   | 0   |
| 001        | 0          | 1   | 0   | 0   | 0   | 0   | 0   | 0   |
| 101        | 0          | 0   | 0   | 0   | 0   | 0   | 0   | 1   |
| 011        | 0          | 0   | 0   | 0   | 0   | 1   | 0   | 0   |
| 111        | 0          | 0   | 0   | 1   | 0   | 0   | 0   | 0   |

current state  $s_0(ABC) = 100$ 



# → Estado-nodo

| Entrada de datos | Medida de<br>distancia | Esquema de partición | Resultados con CM   | Resultados sin CM  |
|------------------|------------------------|----------------------|---|--|
| Grafo:           | EMD                    | ·                    | MIP: Cut [A, B] ——//—  → [C]  Phi: Φ = 1.916665  Time: 0.247361 s | MIP:<br>Cut [A, B] ——//—<br>→ [C]<br>Phi:<br>Φ = 1.916665<br>Time:<br>0.458124 s |

| ************************************** | T    | T            | 1                 |                   |
|--|------|--------------|-------------------|-------------------|
| in a state                             | EMD  | tripartición | MIP:              | MIP:              |
| D                                      |      |              | Cut [A, B] ——//—  | Cut [A, B] ——//—  |
| OR F                                   |      |              | <b>-&gt;</b> [C]  | <b>-&gt;</b> [C]  |
| A                                      |      |              | ر ال              | > [C]             |
| candidate /                            |      |              |                   |                   |
| set /                                  |      |              | Phi:              | Phi:              |
| B—C                                    |      |              | Φ = 1.916665      | $\Phi = 1.916665$ |
|  |      |              |                   |                   |
| AND XOR                                |      |              | Time a .          | Time              |
| (E) \                                  |      |              | Time:             | Time:             |
| ************************************** |      |              | 0.300724 s        | 0.460342 s        |
| 1 (ON) 0 (OFF)                         | KLD  | bipartición  | MIP:              | MIP:              |
|  | 1125 | Sipar tiolon |                   |                   |
| tpm = np.array([<br>[0,0,0,0,0,0],     |      |              | Cut [A, B] ——//—  |                   |
| [0,0,1,0,0,0],                         |      |              | <b>-&gt;</b> [C]  | <b>-&gt;</b> [C]  |
| [1,0,1,0,1,0],<br>[1,0,0,0,1,0],       |      |              |                   |                   |
| [1,0,0,0,0,0],<br>[1,1,1,0,0,0],       |      |              | Phi:              | Phi:              |
| [1,0,1,0,1,0],<br>[1,1,0,0,1,0],       |      |              |                   |                   |
| [1,0,0,0,0,0],                         |      |              | Φ = 1.916665      | $\Phi = 1.916665$ |
| [1,0,1,0,0,0],                         |      |              |                   |                   |
| [1,0,0,0,1,0],<br>[1,0,0,0,0,0],       |      |              | Time:             | Time:             |
| [1,1,1,0,0,0],                         |      |              | 0.255092 s        | 0.46486 s         |
| [1.1.0.0.1.0].                         |      |              | 0.2330323         | 0.40480 3         |
| [0,0,0,0,0,0],<br>[0,0,1,0,0,0],       |      |              |                   |                   |
| [1.0.1.0.1.0].                         |      |              |                   |                   |
| [1,0,0,0,0,0],                         | KLD  | tripartición | MIP:              | MIP:              |
| [1,0,1,0,1,0],                         | KLD  | triparticion |                   |                   |
| [1,1,0,0,1,0],                         |      |              | Cut [A, B] ——/ /— | Cut [A, B] ——/ /— |
| [1,0,1,0,0,0],                         |      |              | <b>-&gt;</b> [C]  | <b>-&gt;</b> [C]  |
| [1,0,0,0,1,0],                         |      |              |                   | 1-1               |
| [1,0,0,0,0,0],<br>[1,1,1,0,0,0],       |      |              | DI:               | DI:               |
| [1,0,1,0,1,0],                         |      |              | Phi:              | Phi:              |
| [0,0,0,0,0],                           |      |              | Φ = 1.916665      | $\Phi = 1.916665$ |
| [1,0,1,0,1,0],                         |      |              |                   |                   |
| [1,0,0,0,1,0],                         |      |              | Time:             | Time:             |
| [1,1,1,0,0,0],                         |      |              |                   |                   |
| [1,1,0,0,1,0],                         |      |              | 0.291669 s        | 0.438747 s        |
| [1,0,0,0,0,0],<br>[1,0,1,0,0,0],       |      |              |                   |                   |
| [1,0,1,0,1,0],<br>[1,0,0,0,1,0],       |      |              |                   |                   |
| [1,0,0,0,0,0],                         |      |              |                   |                   |
| [1,1,1,0,0,0],<br>[1,0,1,0,1,0],       |      |              |                   |                   |
| [1,1,0,0,1,0], [0,0,0,0,0],            |      |              |                   |                   |
| [8,8,1,8,8,8],                         |      |              |                   |                   |
| [1,0,1,0,1,0],<br>[1,0,0,0,1,0],       |      |              |                   |                   |
| [1,0,0,0,0,0],<br>[1,1,1,0,0,0],       |      |              |                   |                   |
| [1,0,1,0,1,0],                         |      |              |                   |                   |
| [1,1,0,0,1,0],<br>[1,0,0,0,0,0],       |      |              |                   |                   |
| [1,0,1,0,0,0],<br>[1,0,1,0,1,0],       |      |              |                   |                   |
| [1,0,0,0,1,0],                         |      |              |                   |                   |
| [1,0,0,0,0,0],<br>[1,1,1,0,0,0],       |      |              |                   |                   |
| [1,0,1,0,1,0],<br>[1,1,0,0,1,0]        |      |              |                   |                   |
| 1)                                     |      |              |                   |                   |
|  |      |              |                   |                   |
|  |      |              |                   |                   |
|  |      |              |                   |                   |

```
cm = np.array([
[0,1,1,0,0,0],
[1,0,1,0,1,0],
[1,1,0,0,0,0],
[1,0,0,0,0,0],
[0,0,0,0,0,0]]
])
```

# EMD-bipartición-con CM

```
Evaluating \Phi cuts:
                     0%
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/7 [00:00<?, ?it/s]
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0%
                                  | 0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%
                     0%
                                  | 0/7 [00:00<?, ?it/s]
Computing concepts:
Evaluating \Phi cuts: 67%
                                  4/6 [00:00<00:00, 39.90it/s]
Computing concepts:
                     0%
                                  0/6 [00:00<?, ?it/s]
Computing concepts:
                                  0/7 [00:00<?, ?it/s]
                     0%
MIP:
Cut [A, B] —/ /—➤ [C]
Phi:
\Phi = 1.916665
Time:
0.247361 s
```

#### EMD-bipartición-sin CM

```
Evaluating \Phi cuts:
                    0%
                                0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%|
                                  | 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts: 33%
                                 2/6 [00:00<00:00, 19.45it/s]
                                  0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                     0%
                                  | 0/7 [00:00<?, ?it/s]
Evaluating \Phi cuts: 67%
                                 4/6 [00:00<00:00, 19.25it/s]
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0%
Computing concepts:
                                  | 0/7 [00:00<?, ?it/s]
                     0%
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
\Phi = 1.916665
Time:
0.458124 s
```

# EMD-Tripartición-con CM

```
Evaluating \Phi cuts:
                                0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/6 [00:00<?, ?it/s]
                                 | 0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 3/6 [00:00<00:00, 29.93it/s]
Evaluating © cuts: 50%
Computing concepts:
                                 0/7 [00:00<?, ?it/s]
                     9%
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
                                  | 0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
0 = 1.916665
Time:
0.300724 s
```

# EMD-Tripartición-sin CM

```
Evaluating \Phi cuts:
                   0%
                                | 0/6 [00:00<?, ?it/s]
                               0/7 [00:00<?, ?it/s]
Computing concepts:
Computing concepts:
                               0/6 [00:00<?, ?it/s]
                    0%
Computing concepts:
                    0%
                                0/7 [00:00<?, ?it/s]
Evaluating \Phi cuts: 50%
                                3/6 [00:00<00:00, 21.64it/s]
Computing concepts:
                    0%
                                0/7 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                0/6 [00:00<?, ?it/s]
Evaluating O cuts: 83%
                               | 5/6 [00:00<00:00, 21.01it/s]
                                0/7 [00:00<?, ?it/s]
Computing concepts:
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
\Phi = 1.916665
Time:
0.460342 s
```

# KLD-Bipartición-con CM

```
0%
                                 | 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts:
Computing concepts:
                                  0/7 [00:00<?, ?it/s]
                   0%
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                                  | 0/7 [00:00<?, ?it/s]
                     0%|
Computing concepts:
                     9% l
                                  | 0/7 [00:00<?, ?it/s]
Evaluating © cuts: 67%
                                 4/6 [00:00<00:00, 37.47it/s]
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                     0%
                                  | 0/7 [00:00<?, ?it/s]
MIP:
Cut [A, B] —/ /—> [C]
Phi:
\Phi = 1.916665
Time:
0.255092 s
```

# KLD-Bipartición-sin CM

```
| 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts:
                    0%
                                | 0/7 [00:00<?, ?it/s]
Computing concepts:
                    0%
Computing concepts:
                    0%
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                 0/7 [00:00<?, ?it/s]
Evaluating \Phi cuts: 50%
                                3/6 [00:00<00:00, 21.09it/s]
Computing concepts:
                    9%
                                 0/7 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts: 83%
                               | 5/6 [00:00<00:00, 20.08it/s]
Computing concepts:
                                 0/7 [00:00<?, ?it/s]
                    0%
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
0 = 1.916665
Time:
0.46486 s
```

### KLD-Tripartición-con CM

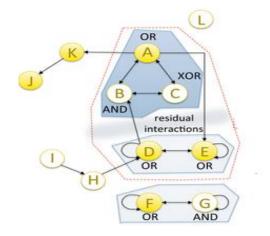
```
Evaluating \Phi cuts:
                    0%|
                                 0/6 [00:00<?, ?it/s]
                                 0/7 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts:
                     0%|
                                 | 0/6 [00:00<?, ?it/s]
                                  | 0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                     0%
                                  0/7 [00:00<?, ?it/s]
Evaluating © cuts: 67%
                                 4/6 [00:00<00:00, 36.80it/s]
Computing concepts:
                                 | 0/6 [00:00<?, ?it/s]
                     0%
Computing concepts:
                                  | 0/7 [00:00<?, ?it/s]
                     0%
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
\Phi = 1.916665
Time:
0.291669 s
```

# KLD-Tripartición-sin CM

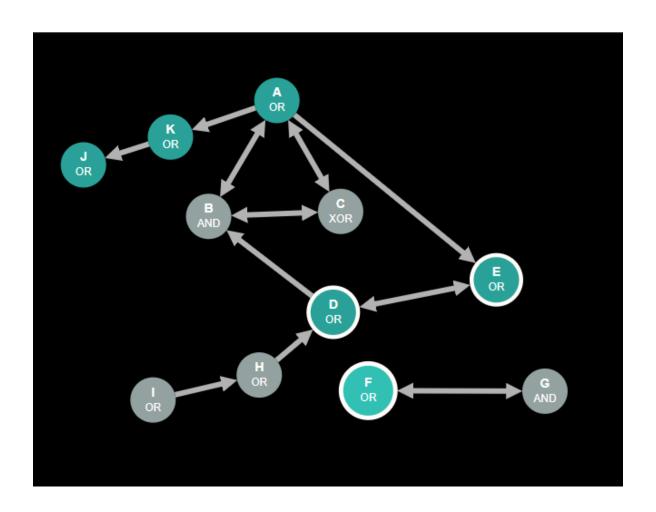
0.438747 s

```
0%
Evaluating \Phi cuts:
                                | 0/6 [00:00<?, ?it/s]
Computing concepts: 0%
                                 | 0/7 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                 | 0/7 [00:00<?, ?it/s]
                                3/6 [00:00<00:00, 22.81it/s]
Evaluating \Phi cuts: 50%
Computing concepts:
                                 0/7 [00:00<?, ?it/s]
                    9%
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%|
Evaluating O cuts: 83%
                                5/6 [00:00<00:00, 21.87it/s]
                                 | 0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%
MIP:
Cut [A, B] —/ /—➤ [C]
Phi:
\Phi = 1.916665
Time:
```

# Grafo 6



Estado inicial : (1, 0, 0, 1, 1, 1, 0)



## → Estado-nodo

| Entrada de datos   | Medida de<br>distancia | Esquema de partición | Resultados con<br>CM  | Resultados sin<br>CM   |
|--|------------------------|----------------------|---|--|
| Grafo:     Value   Control   Control | EMD                    | biparticion          | MIP:<br>Cut [A, B] —<br>//— ➤ [C]<br>Phi:<br>Φ = 1.916665<br>Time:<br>1.149807 s  | MIP:<br>Cut [A, B] —<br>//— ➤ [C]<br>Phi:<br>Φ = 1.916665<br>Time:<br>1.138073 s |
| [escasedescas][escalasease][licalaseaseas][licalaseaseas][licalaseaseaseaseaseaseaseaseaseaseaseaseasea  | EMD                    | tripartición         | MIP:<br>Cut [A, B] ——<br>//——➤ [C]  Phi:<br>Φ = 1.916665  Time:<br>1.088171 s     | MIP:<br>Cut [A, B] ———————————————————————————————————                           |
| [6,6,11,11,6,6,6][6,6,11,11,13,6,6][1,6,11,11,14,6,6,6][1,6,11,11,14,6,1][1,6,11,11,14,6,8][1,6,11,11,14,6,8][1,6,11,11,14,6,8][1,6,11,11,14,6,8][1,6,11,11,14,6,8][1,6,11,11,14,6,8][1,6,11,14,14,6,8][1,6,11,14,6,8][1,6,11,14,6,8][1,6,11,14,6,8][1,6,11,14,6,8,6,8][1,6,11,14,6,8,6,8][1,6,11,14,6,8,6,8][1,6,11,14,6,8,6,8][1,6,11,14,6,8,6,8][1,6,11,14,6,8,6,8][1,6,11,14,6,8,6,8][1,6,11,14,6,8,6,8][1,6,11,14,6,8,6,8][1,6,11,14,6,8,6,8][1,6,11,14,6,8,6,8][1,6,11,14,6,8,6,8][1,6,11,14,6,8,6,8][1,6,11,14,6,8,8][1,6,14,4,8,8][1,6,14,4,8][1,6,14,4,8][1,6,14,4,8][1,6,14,4 | KLD                    | bipartición          | MIP:<br>Cut [A, B] —<br>//— ➤ [C]<br>Phi:<br>Φ = 1.916665<br>Time:<br>1.087204 s  | IP: Cut [A, B] — //— ➤ [C]  Phi: Φ = 1.916665  Time: 1.08725 s                   |
|  | KLD                    | tripartición         | MIP:<br>Cut [A, B] ——<br>//——➤ [C]<br>Phi:<br>Φ = 1.916665<br>Time:<br>1.102643 s | MIP:<br>Cut [A, B] ——<br>//——→ [C]<br>Phi:<br>Φ = 1.916665<br>Time:<br>1.10255 s |

### EMD-Bipartición-con CM

```
Evaluating \Phi cuts:
                                 | 0/6 [00:00<?, ?it/s]
                                 0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                     0%
                                 | 0/6 [00:00<?, ?it/s]
                                  | 0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%|
Computing concepts:
                     0%
                                 0/7 [00:00<?, ?it/s]
Evaluating \Phi cuts: 67%
                                 4/6 [00:00<00:00, 33.36it/s]
Computing concepts:
                                 0/6 [00:00<?, ?it/s]
                     0%
                                  | 0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
0 = 1.916665
Time:
1.149807 s
```

## • EMD-Bipartición-sin CM

```
Evaluating \Phi cuts:
                                0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                                  | 0/7 [00:00<?, ?it/s]
                     0%
Computing concepts:
                     0%
                                  | 0/7 [00:00<?, ?it/s]
                                 4/6 [00:00<00:00, 34.52it/s]
Evaluating \Phi cuts: 67%
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0%
                                  0/7 [00:00<?, ?it/s]
Computing concepts:
                     9%
MIP:
Cut [A, B] —/ /—➤ [C]
Phi:
\Phi = 1.916665
Time:
1.138073 s
```

## EMD-Tripartición-con CM

```
Evaluating \phi cuts: 0\%
                             | 0/6 [00:00<?, ?it/s]
Computing concepts: 0%
                              0/7 [00:00<?, ?it/s]
Computing concepts: 0%
                              | 0/6 [00:00<?, ?it/s]
                               | 0/7 [00:00<?, ?it/s]
Computing concepts: 0%
                               | 0/7 [00:00<?, ?it/s]
Computing concepts:
                   0%|
Evaluating \Phi cuts: 67%
                             4/6 [00:00<00:00, 39.90it/s]
Computing concepts: 0%
                              0/6 [00:00<?, ?it/s]
Computing concepts: 0%
                               | 0/7 [00:00<?, ?it/s]
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
0 = 1.916665
Time:
1.088171 s
```

## • EMD-Tripartición-sin CM

```
Evaluating \Phi cuts:
                   0%
                              | 0/6 [00:00<?, ?it/s]
Computing concepts: 0%
                                0/7 [00:00<?, ?it/s]
                                | 0/6 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts: 0%
                                | 0/7 [00:00<?, ?it/s]
                                | 0/7 [00:00<?, ?it/s]
Computing concepts: 0%
                             4/6 [00:00<00:00, 34.52it/s]
Evaluating \Phi cuts: 67%
Computing concepts: 0%
                                0/6 [00:00<?, ?it/s]
Computing concepts: 0%
                               | 0/7 [00:00<?, ?it/s]
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
\Phi = 1.916665
Time:
1.114285 s
```

### KLD-Bipartición-con CM

```
Evaluating \Phi cuts:
                    0%
                                 0/6 [00:00<?, ?it/s]
                                  0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/7 [00:00<?, ?it/s]
Evaluating \Phi cuts: 67%
                                 4/6 [00:00<00:00, 34.52it/s]
Computing concepts:
                                  | 0/6 [00:00<?, ?it/s]
                     0%
Computing concepts:
                     0%
                                  | 0/7 [00:00<?, ?it/s]
Cut [A, B] —/ /—≻ [C]
Phi:
0 = 1.916665
Time:
1.087204 s
```

## • KLD-Bipartición-sin CM

```
Evaluating \Phi cuts:
                    0%|
                                 0/6 [00:00<?, ?it/s]
Computing concepts: 0%
                                 0/7 [00:00<?, ?it/s]
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                                  | 0/7 [00:00<?, ?it/s]
                     0%
                                  | 0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%
Evaluating © cuts: 67%
                                 4/6 [00:00<00:00, 39.90it/s]
                                 | 0/6 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                                  | 0/7 [00:00<?, ?it/s]
                     0%
MIP:
Cut [A, B] —/ /—> [C]
Phi:
\Phi = 1.916665
Time:
 1.08725 s
```

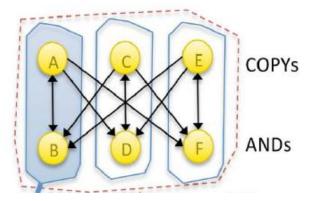
## • KLD-Tripartición-con CM

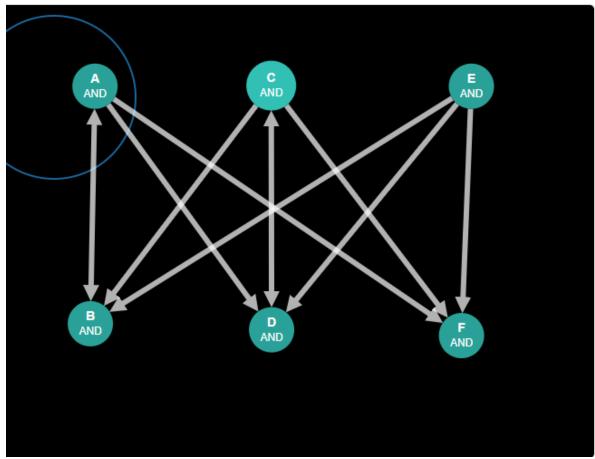
```
0%
                                 | 0/6 [00:00<?, ?it/s]
Evaluating \Phi cuts:
                                  | 0/7 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
Computing concepts:
                      0%
Computing concepts:
                      0%
                                  | 0/7 [00:00<?, ?it/s]
Computing concepts:
                     9% l
                                  | 0/7 [00:00<?, ?it/s]
Evaluating \Phi cuts: 67%
                                  4/6 [00:00<00:00, 39.37it/s]
Computing concepts:
                     0%
                                  | 0/6 [00:00<?, ?it/s]
                                   0/7 [00:00<?, ?it/s]
Computing concepts:
                      0%
MIP:
Cut [A, B] —/ /—≻ [C]
Phi:
\Phi = 1.916665
Time:
1.102643 s
```

### **KLD-Tripartición-sin CM**

Evaluating  $\Phi$  cuts: | 0/6 [00:00<?, ?it/s] Computing concepts: 0% 0/7 [00:00<?, ?it/s] Computing concepts: 0% | 0/6 [00:00<?, ?it/s] Computing concepts: 0% 0/7 [00:00<?, ?it/s] Evaluating  $\Phi$  cuts: 50% 3/6 [00:00<00:00, 29.14it/s] Computing concepts: 0% 0/7 [00:00<?, ?it/s] Computing concepts: 0% | 0/6 [00:00<?, ?it/s] Computing concepts: 0% | 0/7 [00:00<?, ?it/s] MIP: Cut [A, B] —/ /—➤ [C] Phi: 0 = 1.916665Time: 1.10255 s

# Grafo 7





## → Estado-nodo

| Entrada de datos   | Medida de<br>distancia | Esquema de partición | Resultados con<br>CM   | Resultados sin<br>CM  |
|--|------------------------|----------------------|--|---|
| Tem = np.array([ [0,0,0,1,0], [0,0,0,1,0], [1,0,0,0,1,0], [1,0,0,1,0], [1,0,0,0,1,0], [1,0,0,0,1,0], [1,0,0,1,0], [1,0,1,0], [1,0,1,0], [1,0,1,0], [1,0,1,0], [1,0,1,0], [1,0,1,0], [1,0,1,0], [1,0,1,0], [1,0,1,0], [1,0,1,0], [1,0,1,0], [1,0,0,1,0], [1,0,0,1,0], [1,0,0,0], [1,0,0,0], [1,0,0,0], [1,0,0,0], [1,0,0,0], [1,0,0,0], [1,0,0], [1,0,0], [1,0,0], [1,1], [1,0], [1,1], [1,1], [1,1] | EMD                    | biparticion          | MIP:<br>Cut [A, B] ——/<br>/——➤ [C, D]<br>Phi:<br>Φ = 0.3125<br>Time:<br>0.398937 s | MIP:<br>Cut [A, B] —///—> [C, D]  Phi:<br>Φ = 0.3125  Time:<br>0.400629 s |
|  | EMD                    | tripartición         | MIP:<br>Cut [A, B] ——/<br>/——➤ [C, D]<br>Phi:<br>Φ = 0.3125<br>Time:<br>0.369676 s | MIP:<br>Cut [A, B] —///—> [C, D]  Phi:<br>Φ = 0.3125  Time:<br>0.369705 s |
|  | KLD                    | bipartición          | MIP:<br>Cut [A, B] ——/<br>/——➤ [C, D]<br>Phi:<br>Φ = 0.3125<br>Time:<br>0.378836 s | MIP:<br>Cut [A, B] —///—> [C, D]  Phi:<br>Φ = 0.3125  Time:<br>0.384262 s |
| <pre>[1,0,0,0,1,0], [1,0,0,0,1,0], [0,1,0,1,0,1], [1,0,0,0,0,0], [0,1,0,1,0,1], [0,0,1,0,0,0], [0,1,0,1,0,1], [0,0,0,0,0,0]] ])</pre>  | KLD                    | tripartición         | MIP:<br>Cut [A, B] —///— ➤ [C, D]<br>Phi:<br>Φ = 0.3125<br>Time:<br>0.365484 s     | MIP: Cut [A, B] —/ /——➤ [C, D]  Phi: Φ = 0.3125  Time: 0.413015 s         |

```
EMD-Bipartición-con CM
Evaluating \Phi cuts:
                     0%
                                  0/14 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/11 [00:00<?, ?it/s]
Computing concepts:
                                  | 0/13 [00:00<?, ?it/s]
                     0%|
Computing concepts:
                      0%
                                  | 0/11 [00:00<?, ?it/s]
Evaluating \Phi cuts: 29%
                                  | 4/14 [00:00<00:00, 39.71it/s]
Computing concepts:
                     0%
                                  | 0/13 [00:00<?, ?it/s]
                                  | 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                      0%
                                  | 0/11 [00:00<?, ?it/s]
                                  | 0/11 [00:00<?, ?it/s]
Computing concepts:
                      0%
Computing concepts:
                      0% l
                                  | 0/13 [00:00<?, ?it/s]
Evaluating O cuts: 64%
                                  9/14 [00:00<00:00, 41.72it/s]
Computing concepts:
                                  | 0/13 [00:00<?, ?it/s]
                      0%
Computing concepts:
                      0%
                                  | 0/11 [00:00<?, ?it/s]
Computing concepts:
                                  | 0/13 [00:00<?, ?it/s]
                     0%
Computing concepts:
                     0%
                                   | 0/11 [00:00<?, ?it/s]
                                   | 0/11 [00:00<?, ?it/s]
Computing concepts:
                      0%
MIP:
Cut [A, B] —/ /—≻ [C, D]
Phi:
 \Phi = 0.3125
Time:
0.398937 s
```

### EMD-Bipartición-sin CM

```
Evaluating \Phi cuts:
                    0%|
                                | 0/14 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 0/11 [00:00<?, ?it/s]
                                 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                     0%
                                 | 0/11 [00:00<?, ?it/s]
Evaluating \Phi cuts: 29%
                                 4/14 [00:00<00:00, 39.89it/s]
Computing concepts:
                                 | 0/13 [00:00<?, ?it/s]
                     0%
Computing concepts:
                     0%
                                 | 0/13 [00:00<?, ?it/s]
Computing concepts:
                                 | 0/11 [00:00<?, ?it/s]
                     0%
                     0%
Computing concepts:
                                 | 0/11 [00:00<?, ?it/s]
                                 8/14 [00:00<00:00, 39.90it/s]
Evaluating \Phi cuts: 57%
                                 | 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                     0%
                                 | 0/13 [00:00<?, ?it/s]
                                 | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                     0%
                                 | 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/11 [00:00<?, ?it/s]
Cut [A, B] —/ /—> [C, D]
Phi:
\Phi = 0.3125
Time:
0.400629 s
```

### EMD-Tripartición-con CM

```
| 0/14 [00:00<?, ?it/s]
Evaluating © cuts:
                     0%|<sup>°</sup>
Computing concepts:
                                   | 0/11 [00:00<?, ?it/s]
                      0%
Computing concepts:
                      0%
                                   | 0/11 [00:00<?, ?it/s]
Computing concepts:
                      0%
                                   | 0/13 [00:00<?, ?it/s]
Computing concepts:
                                   | 0/11 [00:00<?, ?it/s]
                      0%
Computing concepts:
                      9% I
                                   | 0/13 [00:00<?, ?it/s]
Evaluating © cuts: 36%
                                  | 5/14 [00:00<00:00, 49.87it/s]
Computing concepts:
                      0%
                                   0/13 [00:00<?, ?it/s]
Computing concepts:
                      0%
                                   | 0/11 [00:00<?, ?it/s]
Computing concepts:
                      0%
                                   | 0/11 [00:00<?, ?it/s]
Computing concepts:
                      0%
                                   | 0/13 [00:00<?, ?it/s]
Computing concepts:
                      9% I
                                   | 0/13 [00:00<?, ?it/s]
                      0%
Computing concepts:
                                   | 0/11 [00:00<?, ?it/s]
                                  | 11/14 [00:00<00:00, 50.70it/s]
Evaluating Φ cuts: 79%
Computing concepts:
                      0%
                                   | 0/13 [00:00<?, ?it/s]
                                   | 0/11 [00:00<?, ?it/s]
Computing concepts:
                      0%
Computing concepts:
                      0%
                                   | 0/11 [00:00<?, ?it/s]
Cut [A, B] —/ /—≻ [C, D]
Phi:
\Phi = 0.3125
Time:
0.369676 s
```

## • EMD-Tripartición-sin CM

```
Evaluating \phi cuts: 0\%
                           0/14 [00:00<?, ?it/s]
Computing concepts: 0%
                              0/11 [00:00<?, ?it/s]
Computing concepts: 0%
                              0/11 [00:00<?, ?it/s]
                              | 0/13 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts: 0%
                              | 0/11 [00:00<?, ?it/s]
Computing concepts: 0%
                              | 0/13 [00:00<?, ?it/s]
                   0%
Computing concepts:
                              0/13 [00:00<?, ?it/s]
Evaluating O cuts: 43%
                             6/14 [00:00<00:00, 51.78it/s]
Computing concepts: 0%
                              0/11 [00:00<?, ?it/s]
Computing concepts: 0%
                              | 0/11 [00:00<?, ?it/s]
Computing concepts: 0%
                              | 0/13 [00:00<?, ?it/s]
Computing concepts: 0%
                              0/13 [00:00<?, ?it/s]
                               | 0/11 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts: 0%
                               0/13 [00:00<?, ?it/s]
Evaluating \Phi cuts: 86% | 12/14 [00:00<00:00, 51.78it/s]
Computing concepts: 0%
                              | 0/11 [00:00<?, ?it/s]
Computing concepts: 0%
                           | 0/11 [00:00<?, ?it/s]
MIP:
Cut [A, B] —/ /—≻ [C, D]
Phi:
\Phi = 0.3125
Time:
0.369705 s
```

### • KLD-Bipartición-con CM

```
Evaluating \Phi cuts:
                    0%|
                                 | 0/14 [00:00<?, ?it/s]
                                  | 0/11 [00:00<?, ?it/s]
Computing concepts:
                    0%
Computing concepts:
                     0%
                                  0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/13 [00:00<?, ?it/s]
                                  | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0% l
                     0%
                                  | 0/13 [00:00<?, ?it/s]
Computing concepts:
Evaluating \Phi cuts: 36%
                                 | 5/14 [00:00<00:00, 49.87it/s]
                                  | 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                     0%
                                  | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/13 [00:00<?, ?it/s]
Evaluating \Phi cuts: 71%
                                  | 10/14 [00:00<00:00, 49.88it/s]
Computing concepts:
                                  | 0/11 [00:00<?, ?it/s]
                     0%
Computing concepts:
                                  | 0/13 [00:00<?, ?it/s]
                     0%
                                  | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                                  | 0/11 [00:00<?, ?it/s]
                     0%
MIP:
Cut [A, B] —/ /—≻ [C, D]
Phi:
\Phi = 0.3125
Time:
0.378836 s
```

### KLD-Bipartición-sin CM

```
0%
Evaluating \Phi cuts:
                                 0/14 [00:00<?, ?it/s]
Computing concepts: 0%
                                 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/13 [00:00<?, ?it/s]
                                 | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                     0%
                                 | 0/13 [00:00<?, ?it/s]
Computing concepts:
Evaluating © cuts: 36%
                                 | 5/14 [00:00<00:00, 49.31it/s]
                                 | 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                     0%
                                 | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/13 [00:00<?, ?it/s]
Evaluating \Phi cuts: 71%
                                 | 10/14 [00:00<00:00, 49.41it/s]
Computing concepts:
                                 | 0/11 [00:00<?, ?it/s]
                     0%
Computing concepts:
                     0%
                                 | 0/13 [00:00<?, ?it/s]
Computing concepts:
                                 | 0/11 [00:00<?, ?it/s]
                     0%
                                 | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
MIP:
Cut [A, B] -/ /--> [C, D]
Phi:
\Phi = 0.3125
Time:
0.384262 s
```

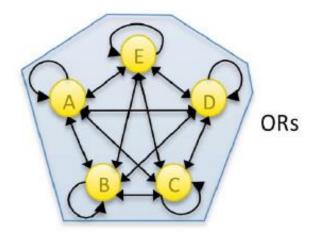
### • KLD-Tripatición-con CM

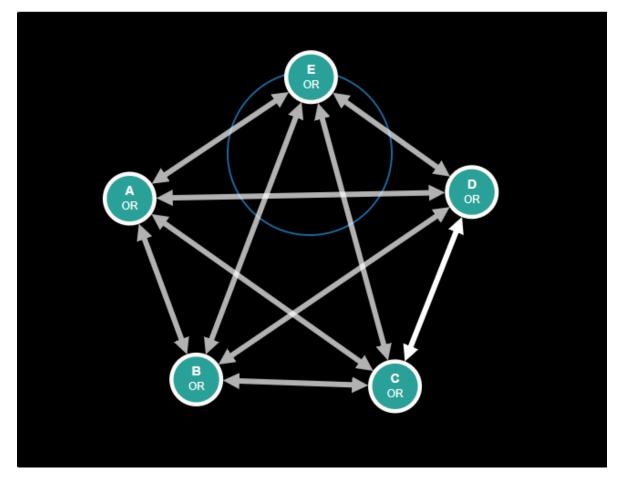
```
0% | ´
                                 | 0/14 [00:00<?, ?it/s]
Evaluating \Phi cuts:
Computing concepts:
                     0%
                                 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/13 [00:00<?, ?it/s]
Evaluating © cuts: 43%
                                 6/14 [00:00<00:00, 51.78it/s]
Computing concepts:
                     0%
                                 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                  | 0/11 [00:00<?, ?it/s]
Evaluating © cuts: 79%
                                 | 11/14 [00:00<00:00, 51.19it/s]
                                  | 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
Computing concepts:
                     0%
                                  | 0/11 [00:00<?, ?it/s]
Computing concepts:
                                  | 0/11 [00:00<?, ?it/s]
                     0%
MIP:
Cut [A, B] —/ /—≻ [C, D]
Phi:
0 = 0.3125
Time:
0.365484 s
```

## • KLD-Tripartición-sin CM

```
Evaluating © cuts: 0%|
                                | 0/14 [00:00<?, ?it/s]
                                 | 0/11 [00:00<?, ?it/s]
Computing concepts:
                    0%
Computing concepts:
                    0%
                                 0/11 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                 | 0/13 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                 | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%|
                                 | 0/13 [00:00<?, ?it/s]
Evaluating © cuts: 43%
                                 6/14 [00:00<00:00, 51.78it/s]
Computing concepts:
                    0%
                                 0/11 [00:00<?, ?it/s]
Computing concepts:
                    0%
                                 | 0/11 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/13 [00:00<?, ?it/s]
Computing concepts:
                     0%
                                 | 0/11 [00:00<?, ?it/s]
Evaluating © cuts: 79%
                                | 11/14 [00:00<00:00, 47.84it/s]
                                 | 0/13 [00:00<?, ?it/s]
Computing concepts:
                    0%
Computing concepts:
                    0%
                                 | 0/11 [00:00<?, ?it/s]
Computing concepts: 0%
                                 | 0/11 [00:00<?, ?it/s]
MIP:
Cut [A, B] —/ /—≻ [C, D]
Phi:
\Phi = 0.3125
Time:
0.413015 s
```

Grafo 8





## → Estado-nodo

| Entrada de datos  | Medida de<br>distancia | Esquema de partición | Resultados con CM   | Resultados sin CM   |
|---|------------------------|----------------------|---|---|
| Tym = np.array([ [0,0,0,0,0], [1,1,1,1,1], [1,1,1], [1,1,1], [1,1,1], [1,1], | EMD                    | biparticion          | MIP:<br>Cut [A] ——//——<br>➤ [B, C, D, E]<br>Phi:<br>Φ = 0.003057<br>Time:<br>180.102077 s | MIP:<br>Cut [A] —//—<br>➤ [B, C, D, E]<br>Phi:<br>Φ = 0.003057<br>Time:<br>175.997137 s |
|   | EMD                    | tripartición         | MIP:<br>Cut [A] ——//——  ➤ [B, C, D, E]  Phi:<br>Φ = 0.003057  Time:<br>189.102577 s       | MIP:<br>Cut [A] —//—<br>➤ [B, C, D, E]<br>Phi:<br>Φ = 0.003057<br>Time:<br>178.882237 s |
|   | KLD                    | bipartición          | MIP:<br>Cut [A] ——//——<br>➤ [B, C, D, E]<br>Phi:<br>Φ = 0.003057<br>Time:<br>183.202997 s | MIP:<br>Cut [A] —//—<br>➤ [B, C, D, E]<br>Phi:<br>Φ = 0.003057<br>Time:<br>175.23443 s  |
|   | KLD                    | tripartición         | MIP:<br>Cut [A] ——//——<br>➤ [B, C, D, E]<br>Phi:<br>Φ = 0.003057<br>Time:<br>179.102077 s | MIP:<br>Cut [A] —//—<br>➤ [B, C, D, E]<br>Phi:<br>Φ = 0.003057<br>Time:<br>176.00092 s  |

```
cm = np.array([
[1,1,1,1,1],
[1,1,1,1,1],
[1,1,1,1,1],
[1,1,1,1,1]]
])
```

Variación en el tiempo y consumo de las particiones con CM Computing concepts: 77% | 20/26 [00:04<00:01, 4.01it/s] | 21/26 [00:05<00:01, 3.61it/s] Computing concepts: 81% Computing concepts: 92% | 24/26 [00:05<00:00, 4.53it/s] Computing concepts: 96% 25/26 [00:05<00:00, 4.29it/s] | 26/26 [00:05<00:00, 4.73it/s] Computing concepts: 100% Evaluating Φ cuts: 23% | 7/30 [00:43<02:21, 6.17s/it] | 0/20 [00:00<?, ?it/s] Computing concepts: 0% Computing concepts: 5% | 1/20 [00:00<00:02, 6.38it/s] Computing concepts: 10% | 2/20 [00:00<00:03, 4.90it/s] Computing concepts: 15% | 3/20 [00:01<00:08, 2.10it/s] Computing concepts: 20% | 4/20 [00:01<00:06, 2.61it/s] Computing concepts: 25% | 5/20 [00:02<00:06, 2.32it/s] Computing concepts: 35% | 7/20 [00:02<00:04, 2.92it/s] Computing concepts: 45% 9/20 [00:03<00:03, 3.03it/s] Computing concepts: 50% | 10/20 [00:03<00:03, 3.15it/s] Computing concepts: 55% | 11/20 [00:03<00:03, 2.65it/s] Computing concepts: 60% | 12/20 [00:04<00:02, 3.24it/s] | 14/20 [00:04<00:01, 3.83it/s] Computing concepts: 70% Computing concepts: 75% | 15/20 [00:04<00:01, 3.00it/s] Computing concepts: 90% | 18/20 [00:05<00:00, 3.79it/s] | 19/20 [00:05<00:00, 3.67it/s] Computing concepts: 95% Computing concepts: 100% | 20/20 [00:05<00:00, 4.18it/s] Evaluating Φ cuts: 27% | 8/30 [00:49<02:12, 6.04s/it] Computing concepts: 0% | 0/26 [00:00<?, ?it/s] Computing concepts: 4%

| 0/26 [00:00<?, ?it/s] | 1/26 [00:00<00:04, 5.36it/s] | 2/26 [00:00<00:05, 4.62it/s] | 3/26 [00:00<00:05, 4.53it/s] | 4/26 [00:01<00:08, 2.63it/s] | 5/26 [00:01<00:07, 2.83it/s] | 6/26 [00:02<00:07, 2.77it/s] | 8/26 [00:02<00:05, 3.49it/s]

Computing concepts:

Computing concepts: 12%

Computing concepts: 15%

Computing concepts: 19%

Computing concepts: 23%

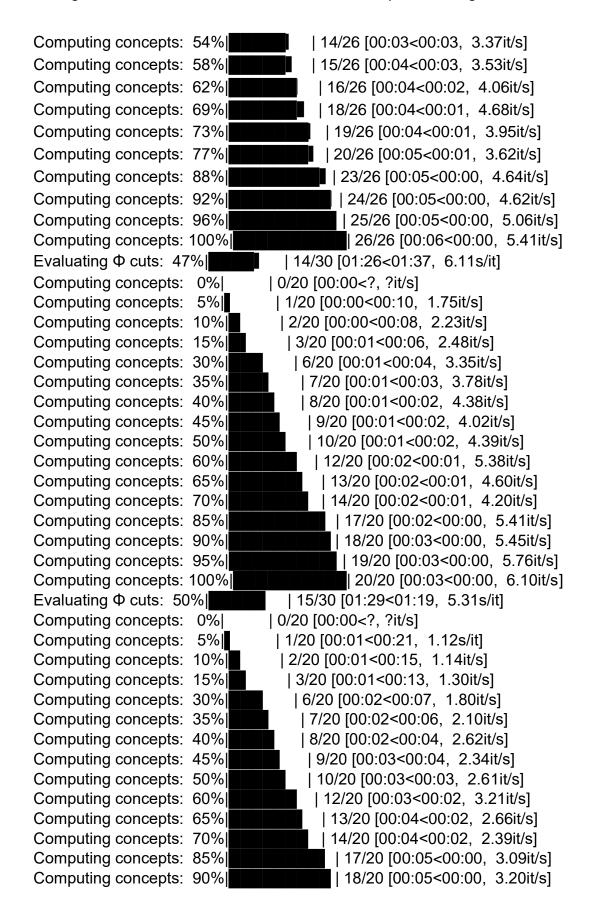
Computing concepts: 31%

8%|

```
Computing concepts: 38%
                                  10/26 [00:02<00:03, 4.43it/s]
Computing concepts: 42%
                                   | 11/26 [00:02<00:03, 4.02it/s]
Computing concepts: 46%
                                    | 12/26 [00:03<00:04, 3.46it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.53it/s]
Computing concepts: 54%
                                    | 14/26 [00:03<00:03, 3.18it/s]
Computing concepts: 58%
                                    | 15/26 [00:04<00:03, 3.66it/s]
Computing concepts: 62%
                                     | 16/26 [00:04<00:02, 4.18it/s]
Computing concepts: 69%
                                     | 18/26 [00:04<00:01, 4.98it/s]
Computing concepts: 73%
                                      | 19/26 [00:04<00:02, 3.34it/s]
Computing concepts: 77%
                                      | 20/26 [00:05<00:02, 2.66it/s]
Computing concepts: 88%
                                      | 23/26 [00:05<00:00, 3.40it/s]
Computing concepts: 92%
                                        24/26 [00:06<00:00, 3.38it/s]
Computing concepts: 96%
                                        | 25/26 [00:06<00:00, 3.91it/s]
Computing concepts: 100%
                                         | 26/26 [00:06<00:00, 4.45it/s]
Evaluating Φ cuts: 30%
                               9/30 [00:55<02:09, 6.17s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 4%
                               1/26 [00:00<00:07, 3.20it/s]
Computing concepts:
                               2/26 [00:00<00:07, 3.36it/s]
                     8%
Computing concepts: 12%
                                 3/26 [00:01<00:10, 2.27it/s]
                                 | 4/26 [00:01<00:08, 2.49it/s]
Computing concepts: 15%
Computing concepts: 19%
                                 | 5/26 [00:01<00:07, 2.98it/s]
Computing concepts: 23%
                                 | 6/26 [00:01<00:05, 3.54it/s]
Computing concepts: 27%
                                 | 7/26 [00:02<00:06, 3.11it/s]
                                  | 9/26 [00:02<00:04, 3.69it/s]
Computing concepts: 35%
Computing concepts: 42%
                                   | 11/26 [00:03<00:03, 4.00it/s]
Computing concepts: 46%
                                    1 12/26 [00:03<00:03, 4.44it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:02, 4.44it/s]
Computing concepts: 54%
                                    14/26 [00:04<00:03, 3.13it/s]
Computing concepts: 58%
                                    | 15/26 [00:04<00:03, 3.64it/s]
                                     | 16/26 [00:04<00:02, 3.59it/s]
Computing concepts: 62%
                                     | 17/26 [00:04<00:02, 4.01it/s]
Computing concepts: 65%
                                      | 19/26 [00:04<00:01, 4.53it/s]
Computing concepts: 73%
Computing concepts: 77%
                                      20/26 [00:05<00:01, 3.86it/s]
                                      | 21/26 [00:05<00:01, 3.01it/s]
Computing concepts: 81%
Computing concepts: 92%
                                        24/26 [00:06<00:00, 3.94it/s]
Computing concepts: 96%
                                        25/26 [00:06<00:00, 3.85it/s]
Computing concepts: 100%
                                         26/26 [00:06<00:00, 4.36it/s]
Evaluating Φ cuts: 33%
                                | 10/30 [01:02<02:05, 6.28s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts: 4%
                               | 1/26 [00:00<00:05, 4.28it/s]
```

```
Computing concepts: 8%
                               2/26 [00:00<00:08, 2.68it/s]
Computing concepts: 12%
                                 3/26 [00:01<00:07, 3.04it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:06, 3.62it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:06, 3.32it/s]
Computing concepts: 27%
                                 | 7/26 [00:01<00:04, 4.09it/s]
                                  9/26 [00:02<00:03, 5.10it/s]
Computing concepts: 35%
Computing concepts: 38%
                                  | 10/26 [00:02<00:03, 4.51it/s]
Computing concepts: 42%
                                   | 11/26 [00:02<00:03, 3.81it/s]
Computing concepts: 46%
                                    | 12/26 [00:02<00:03, 4.34it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:02, 4.47it/s]
Computing concepts: 54%
                                    | 14/26 [00:03<00:03, 3.74it/s]
Computing concepts: 58%
                                    | 15/26 [00:03<00:02, 4.24it/s]
Computing concepts: 62%
                                     | 16/26 [00:03<00:02, 4.04it/s]
Computing concepts: 69%
                                     | 18/26 [00:04<00:01, 4.86it/s]
Computing concepts: 73%
                                      | 19/26 [00:04<00:01, 3.86it/s]
Computing concepts: 77%
                                      | 20/26 [00:04<00:01, 3.45it/s]
Computing concepts: 88%
                                      | 23/26 [00:05<00:00, 4.45it/s]
Computing concepts: 92%
                                        | 24/26 [00:05<00:00, 3.89it/s]
Computing concepts: 96%
                                        | 25/26 [00:05<00:00, 4.12it/s]
Computing concepts: 100%
                                         | 26/26 [00:05<00:00, 4.16it/s]
Evaluating Φ cuts: 37%
                                11/30 [01:08<01:57, 6.17s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts:
                               | 1/26 [00:00<00:05, 4.50it/s]
                     4%|
Computing concepts: 8%
                               2/26 [00:00<00:05, 4.02it/s]
Computing concepts: 12%
                                 3/26 [00:00<00:05, 4.36it/s]
Computing concepts: 15%
                                 | 4/26 [00:00<00:05, 4.23it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:08, 2.59it/s]
Computing concepts: 23%
                                 | 6/26 [00:01<00:06, 3.10it/s]
Computing concepts: 27%
                                 | 7/26 [00:02<00:05, 3.59it/s]
Computing concepts: 31%
                                  | 8/26 [00:02<00:06, 2.89it/s]
Computing concepts: 38%
                                  10/26 [00:02<00:04, 3.60it/s]
Computing concepts: 46%
                                    1 12/26 [00:03<00:03, 4.26it/s]
Computing concepts: 50%
                                    13/26 [00:03<00:03, 3.42it/s]
Computing concepts: 54%
                                    14/26 [00:03<00:03, 3.60it/s]
Computing concepts: 58%
                                    | 15/26 [00:04<00:03, 3.27it/s]
Computing concepts: 62%
                                     | 16/26 [00:04<00:03, 3.33it/s]
Computing concepts: 69%
                                     | 18/26 [00:04<00:02, 3.99it/s]
Computing concepts: 73%
                                      | 19/26 [00:05<00:02, 3.46it/s]
Computing concepts: 77%
                                      20/26 [00:05<00:02, 2.83it/s]
```

```
Computing concepts: 88%
                                       23/26 [00:05<00:00, 3.62it/s]
                                        24/26 [00:06<00:00, 3.86it/s]
Computing concepts: 92%
Computing concepts: 96%
                                        25/26 [00:06<00:00, 4.36it/s]
Computing concepts: 100%
                                         26/26 [00:06<00:00, 4.84it/s]
Evaluating Φ cuts: 40%
                                | 12/30 [01:14<01:52, 6.24s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 4%
                               1/26 [00:00<00:04, 5.66it/s]
Computing concepts:
                               | 2/26 [00:00<00:04, 5.16it/s]
                     8%|
Computing concepts: 12%
                                 3/26 [00:00<00:04, 5.03it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:07, 2.84it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:06, 3.01it/s]
Computing concepts: 23%
                                 | 6/26 [00:01<00:05, 3.53it/s]
Computing concepts: 27%
                                  | 7/26 [00:02<00:05, 3.26it/s]
Computing concepts: 38%
                                  10/26 [00:02<00:03, 4.32it/s]
Computing concepts: 42%
                                   | 11/26 [00:02<00:03, 4.39it/s]
Computing concepts: 46%
                                    | 12/26 [00:02<00:03, 3.84it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.89it/s]
Computing concepts: 54%
                                    14/26 [00:03<00:03, 3.41it/s]
Computing concepts: 58%
                                    | 15/26 [00:03<00:03, 3.38it/s]
Computing concepts: 62%
                                     | 16/26 [00:03<00:02, 3.92it/s]
Computing concepts: 69%
                                     | 18/26 [00:04<00:01, 4.72it/s]
Computing concepts: 73%
                                      19/26 [00:04<00:01, 3.95it/s]
Computing concepts: 77%
                                      20/26 [00:04<00:01, 3.54it/s]
Computing concepts: 88%
                                     | 23/26 [00:05<00:00, 4.37it/s]
Computing concepts: 92%
                                        | 24/26 [00:05<00:00, 4.32it/s]
Computing concepts: 96%
                                        | 25/26 [00:05<00:00, 4.48it/s]
Computing concepts: 100%
                                         | 26/26 [00:05<00:00, 4.92it/s]
Evaluating Φ cuts: 43%
                                 | 13/30 [01:20<01:44, 6.13s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 4%
                               | 1/26 [00:00<00:07, 3.19it/s]
                               2/26 [00:00<00:06, 3.74it/s]
Computing concepts: 8%
Computing concepts: 12%
                                 3/26 [00:00<00:06, 3.74it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:08, 2.46it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:07, 2.64it/s]
Computing concepts: 23%
                                  | 6/26 [00:01<00:06, 3.16it/s]
Computing concepts: 27%
                                  | 7/26 [00:02<00:06, 2.89it/s]
Computing concepts: 35%
                                  9/26 [00:02<00:04, 3.57it/s]
Computing concepts: 42%
                                   | 11/26 [00:02<00:03, 4.12it/s]
Computing concepts: 46%
                                    | 12/26 [00:03<00:03, 3.58it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.92it/s]
```



```
Computing concepts: 95%
                                        | 19/20 [00:05<00:00, 3.75it/s]
Computing concepts: 100%
                                          20/20 [00:05<00:00, 4.26it/s]
Evaluating Φ cuts: 53%
                                  | 16/30 [01:35<01:15, 5.42s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts:
                               | 1/26 [00:00<00:07, 3.33it/s]
                     4%|
Computing concepts: 8%
                               2/26 [00:00<00:06, 3.88it/s]
Computing concepts: 12%
                                 3/26 [00:00<00:06, 3.60it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:09, 2.42it/s]
                                 | 5/26 [00:01<00:07, 2.80it/s]
Computing concepts: 19%
Computing concepts: 23%
                                 | 6/26 [00:01<00:05, 3.34it/s]
Computing concepts: 27%
                                 | 7/26 [00:02<00:06, 3.12it/s]
Computing concepts: 35%
                                  9/26 [00:02<00:04, 3.73it/s]
Computing concepts: 42%
                                   11/26 [00:02<00:03, 4.51it/s]
Computing concepts: 46%
                                    | 12/26 [00:03<00:04, 3.18it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.69it/s]
Computing concepts: 54%
                                    | 14/26 [00:03<00:03, 3.27it/s]
Computing concepts: 58%
                                    | 15/26 [00:04<00:03, 3.31it/s]
Computing concepts: 62%
                                     | 16/26 [00:04<00:02, 3.84it/s]
Computing concepts: 69%
                                     | 18/26 [00:04<00:01, 4.57it/s]
Computing concepts: 73%
                                      19/26 [00:05<00:02, 3.19it/s]
Computing concepts: 77%
                                      20/26 [00:05<00:01, 3.02it/s]
Computing concepts: 88%
                                      | 23/26 [00:05<00:00, 3.82it/s]
Computing concepts: 92%
                                        24/26 [00:06<00:00, 3.71it/s]
Computing concepts: 96%
                                        | 25/26 [00:06<00:00, 4.19it/s]
Computing concepts: 100%
                                         26/26 [00:06<00:00, 4.54it/s]
Evaluating Φ cuts: 57%
                                  | 17/30 [01:42<01:14, 5.74s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts:
                     4%|
                               1/26 [00:00<00:04, 5.91it/s]
Computing concepts:
                     8%|
                               2/26 [00:00<00:05, 4.75it/s]
Computing concepts: 12%
                                 3/26 [00:00<00:05, 4.25it/s]
                                 | 4/26 [00:01<00:08, 2.57it/s]
Computing concepts: 15%
                                 | 5/26 [00:01<00:07, 2.91it/s]
Computing concepts: 19%
Computing concepts: 23%
                                 | 6/26 [00:01<00:05, 3.44it/s]
Computing concepts: 27%
                                  | 7/26 [00:02<00:06, 3.10it/s]
Computing concepts: 38%
                                  10/26 [00:02<00:03, 4.12it/s]
Computing concepts: 42%
                                   11/26 [00:02<00:03, 3.89it/s]
Computing concepts: 46%
                                    | 12/26 [00:03<00:04, 2.95it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:04, 3.10it/s]
Computing concepts: 54%
                                    14/26 [00:04<00:04, 2.63it/s]
Computing concepts: 58%
                                    15/26 [00:04<00:03, 3.01it/s]
```

```
Computing concepts: 62%
                                     | 16/26 [00:04<00:02, 3.52it/s]
                                     | 18/26 [00:04<00:01, 4.13it/s]
Computing concepts: 69%
                                      | 19/26 [00:05<00:01, 3.53it/s]
Computing concepts: 73%
Computing concepts: 77%
                                      20/26 [00:05<00:01, 3.12it/s]
Computing concepts: 88%
                                      | 23/26 [00:05<00:00, 4.07it/s]
Computing concepts: 92%
                                        24/26 [00:06<00:00, 3.95it/s]
                                        | 25/26 [00:06<00:00, 4.29it/s]
Computing concepts: 96%
Computing concepts: 100%
                                         26/26 [00:06<00:00, 4.66it/s]
Evaluating Φ cuts: 60%
                                  | 18/30 [01:48<01:11, 5.96s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
                               | 1/26 [00:00<00:04, 5.83it/s]
Computing concepts:
                     4%
Computing concepts: 8%
                               2/26 [00:00<00:04, 5.25it/s]
Computing concepts: 12%
                                 3/26 [00:00<00:04, 5.56it/s]
Computing concepts: 15%
                                 | 4/26 [00:00<00:04, 5.16it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:07, 2.89it/s]
                                  | 6/26 [00:01<00:05, 3.46it/s]
Computing concepts: 23%
Computing concepts: 27%
                                  | 7/26 [00:01<00:04, 4.00it/s]
Computing concepts: 31%
                                  | 8/26 [00:02<00:05, 3.54it/s]
Computing concepts: 38%
                                  | 10/26 [00:02<00:03, 4.16it/s]
                                    | 12/26 [00:02<00:02, 5.04it/s]
Computing concepts: 46%
                                    | 13/26 [00:03<00:03, 4.05it/s]
Computing concepts: 50%
Computing concepts: 54%
                                    | 14/26 [00:03<00:03, 3.93it/s]
Computing concepts: 58%
                                    | 15/26 [00:03<00:03, 3.50it/s]
Computing concepts: 62%
                                     | 16/26 [00:03<00:02, 3.78it/s]
Computing concepts: 69%
                                     | 18/26 [00:04<00:01, 4.69it/s]
Computing concepts: 73%
                                      | 19/26 [00:04<00:01, 3.88it/s]
Computing concepts: 77%
                                      20/26 [00:04<00:01, 3.57it/s]
Computing concepts: 88%
                                       | 23/26 [00:04<00:00, 4.63it/s]
Computing concepts: 92%
                                        24/26 [00:05<00:00, 4.27it/s]
Computing concepts: 96%
                                        | 25/26 [00:05<00:00, 4.45it/s]
                                         | 26/26 [00:05<00:00, 4.87it/s]
Computing concepts: 100%
Evaluating Φ cuts: 63%
                                  | 19/30 [01:54<01:04, 5.86s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 4%
                               | 1/26 [00:00<00:07, 3.16it/s]
                               | 2/26 [00:01<00:11, 2.14it/s]
Computing concepts: 8%
Computing concepts: 12%
                                 | 3/26 [00:01<00:09, 2.42it/s]
                                 | 4/26 [00:01<00:07, 2.94it/s]
Computing concepts: 15%
Computing concepts: 19%
                                 | 5/26 [00:02<00:08, 2.47it/s]
Computing concepts: 27%
                                  | 7/26 [00:02<00:06, 3.05it/s]
Computing concepts: 35%
                                  9/26 [00:02<00:04, 3.91it/s]
```

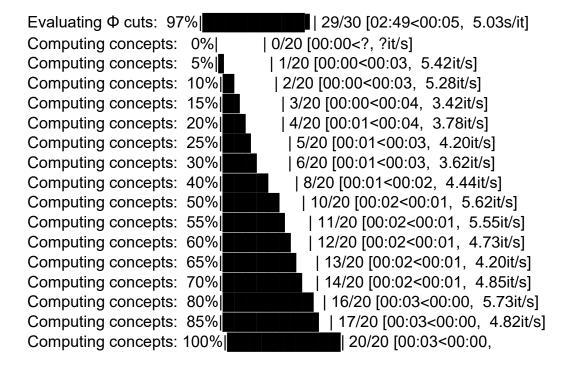
```
Computing concepts: 38%
                                  10/26 [00:02<00:04, 3.92it/s]
Computing concepts: 42%
                                   | 11/26 [00:03<00:05, 2.94it/s]
Computing concepts: 46%
                                    | 12/26 [00:03<00:04, 3.47it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.47it/s]
Computing concepts: 54%
                                    | 14/26 [00:04<00:03, 3.10it/s]
Computing concepts: 58%
                                    | 15/26 [00:04<00:02, 3.67it/s]
Computing concepts: 62%
                                     | 16/26 [00:04<00:02, 3.75it/s]
Computing concepts: 69%
                                     18/26 [00:04<00:01, 4.32it/s]
Computing concepts: 73%
                                      | 19/26 [00:05<00:01, 3.59it/s]
Computing concepts: 77%
                                      | 20/26 [00:05<00:01, 3.12it/s]
Computing concepts: 88%
                                      | 23/26 [00:06<00:00, 3.95it/s]
Computing concepts: 92%
                                        | 24/26 [00:06<00:00, 4.16it/s]
Computing concepts: 96%
                                        | 25/26 [00:06<00:00, 4.55it/s]
Computing concepts: 100%
                                         26/26 [00:06<00:00, 4.90it/s]
Evaluating Φ cuts: 67%
                                  20/30 [02:00<01:01, 6.10s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 4%
                               | 1/26 [00:00<00:05, 4.36it/s]
Computing concepts:
                               2/26 [00:00<00:06, 3.99it/s]
                     8%|
Computing concepts: 12%
                                 | 3/26 [00:01<00:08, 2.61it/s]
Computing concepts: 15%
                                 4/26 [00:01<00:07, 3.01it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:05, 3.58it/s]
Computing concepts: 23%
                                  | 6/26 [00:01<00:04, 4.06it/s]
Computing concepts: 27%
                                  | 7/26 [00:02<00:05, 3.58it/s]
Computing concepts: 35%
                                  9/26 [00:02<00:03, 4.43it/s]
Computing concepts: 42%
                                   11/26 [00:02<00:03, 4.67it/s]
Computing concepts: 46%
                                    | 12/26 [00:02<00:02, 5.02it/s]
                                    | 13/26 [00:03<00:02, 4.48it/s]
Computing concepts: 50%
Computing concepts: 54%
                                    | 14/26 [00:03<00:03, 3.67it/s]
Computing concepts: 58%
                                    | 15/26 [00:03<00:02, 4.18it/s]
Computing concepts: 62%
                                     | 16/26 [00:03<00:02, 4.14it/s]
Computing concepts: 65%
                                      | 17/26 [00:04<00:01, 4.56it/s]
Computing concepts: 73%
                                      | 19/26 [00:04<00:01, 5.35it/s]
Computing concepts: 77%
                                      20/26 [00:04<00:01, 4.00it/s]
Computing concepts: 81%
                                      | 21/26 [00:05<00:01, 3.42it/s]
                                        24/26 [00:05<00:00, 4.26it/s]
Computing concepts: 92%
                                        | 25/26 [00:05<00:00, 4.30it/s]
Computing concepts: 96%
                                         26/26 [00:05<00:00, 4.73it/s]
Computing concepts: 100%
Evaluating Φ cuts: 70%
                                  21/30 [02:06<00:54, 6.03s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
                               | 1/26 [00:00<00:04, 6.23it/s]
Computing concepts: 4%
```

```
| 2/26 [00:00<00:04, 5.30it/s]
Computing concepts: 8%
Computing concepts: 12%
                                 | 3/26 [00:00<00:05, 4.16it/s]
                                 | 4/26 [00:01<00:08, 2.60it/s]
Computing concepts: 15%
Computing concepts: 19%
                                 | 5/26 [00:01<00:07, 2.94it/s]
Computing concepts: 23%
                                  | 6/26 [00:02<00:07, 2.76it/s]
Computing concepts: 31%
                                  | 8/26 [00:02<00:05, 3.39it/s]
                                  | 10/26 [00:02<00:03, 4.33it/s]
Computing concepts: 38%
Computing concepts: 42%
                                   | 11/26 [00:02<00:03, 4.28it/s]
Computing concepts: 46%
                                    | 12/26 [00:03<00:03, 3.59it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.88it/s]
Computing concepts: 54%
                                    | 14/26 [00:03<00:03, 3.37it/s]
Computing concepts: 58%
                                    15/26 [00:03<00:02, 4.00it/s]
Computing concepts: 62%
                                     | 16/26 [00:04<00:02, 4.43it/s]
Computing concepts: 69%
                                     | 18/26 [00:04<00:01, 5.01it/s]
                                      | 19/26 [00:04<00:01, 4.00it/s]
Computing concepts: 73%
Computing concepts: 77%
                                      20/26 [00:05<00:01, 3.36it/s]
Computing concepts: 88%
                                      | 23/26 [00:05<00:00, 4.34it/s]
Computing concepts: 92%
                                        24/26 [00:05<00:00, 4.37it/s]
Computing concepts: 96%
                                        | 25/26 [00:05<00:00, 4.75it/s]
Computing concepts: 100%
                                         26/26 [00:05<00:00, 5.09it/s]
                                   | 22/30 [02:12<00:48, 6.02s/it]
Evaluating Φ cuts: 73%
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 5%
                                | 1/20 [00:00<00:02, 6.64it/s]
Computing concepts: 10%
                                | 2/20 [00:00<00:02, 6.24it/s]
                                 | 3/20 [00:00<00:04, 3.47it/s]
Computing concepts: 15%
Computing concepts: 20%
                                 | 4/20 [00:01<00:03, 4.10it/s]
Computing concepts: 25%
                                  | 5/20 [00:01<00:03, 3.87it/s]
                                   | 7/20 [00:01<00:02, 4.77it/s]
Computing concepts: 35%
Computing concepts: 45%
                                    9/20 [00:01<00:02, 5.23it/s]
Computing concepts: 50%
                                    | 10/20 [00:02<00:01, 5.30it/s]
Computing concepts: 55%
                                     | 11/20 [00:02<00:02, 4.49it/s]
Computing concepts: 60%
                                     | 12/20 [00:02<00:01, 5.11it/s]
                                      | 14/20 [00:02<00:00, 6.03it/s]
Computing concepts: 70%
Computing concepts: 75%
                                      | 15/20 [00:02<00:01, 4.73it/s]
                                       | 18/20 [00:03<00:00, 5.90it/s]
Computing concepts: 90%
                                        | 19/20 [00:03<00:00, 5.90it/s]
Computing concepts: 95%
Computing concepts: 100%
                                         20/20 [00:03<00:00, 6.08it/s]
Evaluating Φ cuts: 77%
                                   23/30 [02:16<00:36, 5.28s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts:
                     4%|
                               | 1/26 [00:00<00:04, 5.54it/s]
                               2/26 [00:00<00:05, 4.52it/s]
Computing concepts: 8%
```

```
Computing concepts: 12%
                                 3/26 [00:01<00:10, 2.24it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:08, 2.49it/s]
                                 | 5/26 [00:01<00:06, 3.00it/s]
Computing concepts: 19%
Computing concepts: 23%
                                 | 6/26 [00:02<00:07, 2.71it/s]
Computing concepts: 31%
                                  | 8/26 [00:02<00:05, 3.30it/s]
Computing concepts: 38%
                                  | 10/26 [00:02<00:03, 4.20it/s]
Computing concepts: 42%
                                   | 11/26 [00:03<00:03, 3.94it/s]
Computing concepts: 46%
                                    | 12/26 [00:03<00:04, 2.94it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.45it/s]
                                    | 14/26 [00:04<00:03, 3.43it/s]
Computing concepts: 54%
Computing concepts: 58%
                                    | 15/26 [00:04<00:03, 2.84it/s]
                                     | 16/26 [00:04<00:02, 3.37it/s]
Computing concepts: 62%
Computing concepts: 65%
                                      | 17/26 [00:05<00:02, 3.42it/s]
Computing concepts: 73%
                                      19/26 [00:05<00:01, 4.13it/s]
Computing concepts: 77%
                                      20/26 [00:05<00:01, 3.29it/s]
Computing concepts: 81%
                                      | 21/26 [00:06<00:01, 2.67it/s]
Computing concepts: 92%
                                        | 24/26 [00:06<00:00, 3.47it/s]
Computing concepts: 96%
                                        25/26 [00:06<00:00, 3.59it/s]
Computing concepts: 100%
                                          26/26 [00:07<00:00, 4.04it/s]
Evaluating Φ cuts: 80%
                                   | 24/30 [02:23<00:34, 5.82s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts:
                     4%
                               | 1/26 [00:00<00:04, 5.36it/s]
Computing concepts:
                               2/26 [00:00<00:05, 4.48it/s]
                     8%|
                                 | 3/26 [00:00<00:04, 4.87it/s]
Computing concepts: 12%
Computing concepts: 15%
                                 | 4/26 [00:00<00:04, 4.89it/s]
                                 | 5/26 [00:01<00:07, 2.83it/s]
Computing concepts: 19%
Computing concepts: 23%
                                 | 6/26 [00:01<00:06, 3.09it/s]
                                  | 7/26 [00:02<00:06, 2.94it/s]
Computing concepts: 27%
Computing concepts: 35%
                                  9/26 [00:02<00:04, 3.58it/s]
Computing concepts: 42%
                                   11/26 [00:02<00:03, 4.34it/s]
                                    | 12/26 [00:03<00:04, 3.50it/s]
Computing concepts: 46%
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.72it/s]
Computing concepts: 54%
                                    | 14/26 [00:03<00:03, 3.68it/s]
Computing concepts: 58%
                                    | 15/26 [00:04<00:03, 3.27it/s]
                                     | 16/26 [00:04<00:02, 3.80it/s]
Computing concepts: 62%
Computing concepts: 65%
                                     | 17/26 [00:04<00:02, 3.54it/s]
                                     | 18/26 [00:04<00:01, 4.05it/s]
Computing concepts: 69%
Computing concepts: 77%
                                       20/26 [00:05<00:01, 4.15it/s]
Computing concepts: 81%
                                       21/26 [00:05<00:01, 3.64it/s]
Computing concepts: 92%
                                        24/26 [00:05<00:00, 4.48it/s]
```

```
Computing concepts: 96%
                                        | 25/26 [00:06<00:00, 4.20it/s]
Computing concepts: 100%
                                          26/26 [00:06<00:00, 4.52it/s]
Evaluating Φ cuts: 83%
                                    25/30 [02:29<00:29, 5.96s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts:
                     4%|
                               | 1/26 [00:00<00:08, 2.86it/s]
                               | 2/26 [00:00<00:07, 3.14it/s]
Computing concepts: 8%
Computing concepts: 12%
                                 | 3/26 [00:01<00:10, 2.23it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:08, 2.50it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:06, 3.04it/s]
Computing concepts: 23%
                                  | 6/26 [00:01<00:05, 3.61it/s]
Computing concepts: 27%
                                  | 7/26 [00:02<00:05, 3.25it/s]
Computing concepts: 35%
                                   9/26 [00:02<00:04, 3.85it/s]
Computing concepts: 42%
                                   11/26 [00:02<00:03, 4.81it/s]
Computing concepts: 46%
                                    | 12/26 [00:03<00:03, 4.40it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.65it/s]
Computing concepts: 54%
                                    | 14/26 [00:03<00:03, 3.91it/s]
Computing concepts: 58%
                                    | 15/26 [00:04<00:03, 3.26it/s]
Computing concepts: 62%
                                     | 16/26 [00:04<00:02, 3.81it/s]
                                      | 17/26 [00:04<00:02, 4.04it/s]
Computing concepts: 65%
Computing concepts: 69%
                                     | 18/26 [00:04<00:01, 4.45it/s]
Computing concepts: 77%
                                      20/26 [00:04<00:01, 5.16it/s]
Computing concepts: 81%
                                      | 21/26 [00:05<00:01, 4.16it/s]
Computing concepts: 85%
                                      | 22/26 [00:05<00:01, 3.52it/s]
Computing concepts: 96%
                                        25/26 [00:05<00:00, 4.49it/s]
Computing concepts: 100%
                                         26/26 [00:06<00:00, 4.88it/s]
Evaluating Φ cuts: 87%
                                   | 26/30 [02:35<00:23, 6.00s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 5%
                                | 1/20 [00:00<00:03, 4.94it/s]
Computing concepts: 10%
                                2/20 [00:00<00:03, 5.37it/s]
                                 | 3/20 [00:01<00:06, 2.81it/s]
Computing concepts: 15%
Computing concepts: 20%
                                 | 4/20 [00:01<00:04, 3.38it/s]
Computing concepts: 30%
                                  | 6/20 [00:01<00:03, 4.20it/s]
Computing concepts: 40%
                                   | 8/20 [00:01<00:02, 5.06it/s]
Computing concepts: 45%
                                     9/20 [00:02<00:02, 4.18it/s]
Computing concepts: 50%
                                    | 10/20 [00:02<00:02, 4.31it/s]
Computing concepts: 55%
                                     11/20 [00:02<00:03, 2.97it/s]
                                     | 12/20 [00:02<00:02, 3.57it/s]
Computing concepts: 60%
Computing concepts: 65%
                                      | 13/20 [00:03<00:01, 3.98it/s]
                                      | 15/20 [00:03<00:01, 4.53it/s]
Computing concepts: 75%
Computing concepts: 80%
                                      | 16/20 [00:03<00:00, 4.20it/s]
Computing concepts: 95%
                                        | 19/20 [00:03<00:00, 5.29it/s]
```

```
Computing concepts: 100%
                                         20/20 [00:04<00:00, 5.52it/s]
Evaluating Φ cuts: 90%
                                     | 27/30 [02:39<00:16, 5.45s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts: 4%
                               | 1/26 [00:00<00:04, 5.42it/s]
Computing concepts: 8%
                               2/26 [00:00<00:05, 4.46it/s]
                                 | 3/26 [00:00<00:05, 4.12it/s]
Computing concepts: 12%
Computing concepts: 15%
                                 | 4/26 [00:01<00:09, 2.44it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:07, 2.68it/s]
Computing concepts: 23%
                                  | 6/26 [00:02<00:06, 3.16it/s]
Computing concepts: 27%
                                  | 7/26 [00:02<00:05, 3.64it/s]
Computing concepts: 31%
                                  | 8/26 [00:02<00:05, 3.13it/s]
Computing concepts: 38%
                                   10/26 [00:02<00:04, 3.87it/s]
Computing concepts: 46%
                                    | 12/26 [00:03<00:02, 4.87it/s]
                                    | 13/26 [00:03<00:02, 4.55it/s]
Computing concepts: 50%
                                    | 14/26 [00:03<00:03, 3.59it/s]
Computing concepts: 54%
Computing concepts: 58%
                                    | 15/26 [00:03<00:02, 4.23it/s]
Computing concepts: 62%
                                     | 16/26 [00:04<00:02, 4.34it/s]
                                      | 17/26 [00:04<00:02, 3.77it/s]
Computing concepts: 65%
                                     | 18/26 [00:04<00:02, 3.99it/s]
Computing concepts: 69%
Computing concepts: 77%
                                      20/26 [00:04<00:01, 4.58it/s]
Computing concepts: 81%
                                       | 21/26 [00:05<00:01, 3.79it/s]
Computing concepts: 85%
                                       | 22/26 [00:05<00:01, 3.28it/s]
                                        | 25/26 [00:05<00:00, 4.23it/s]
Computing concepts: 96%
Computing concepts: 100%
                                         26/26 [00:06<00:00, 4.83it/s]
Evaluating Φ cuts: 93%
                                     28/30 [02:45<00:11, 5.65s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 5%
                                | 1/20 [00:00<00:02, 7.24it/s]
Computing concepts: 10%
                                | 2/20 [00:00<00:02, 6.66it/s]
Computing concepts: 15%
                                 | 3/20 [00:00<00:02, 6.42it/s]
Computing concepts: 20%
                                 4/20 [00:01<00:04, 3.79it/s]
Computing concepts: 25%
                                  | 5/20 [00:01<00:03, 4.24it/s]
Computing concepts: 30%
                                  | 6/20 [00:01<00:02, 4.89it/s]
Computing concepts: 35%
                                   | 7/20 [00:01<00:02, 4.47it/s]
                                    | 10/20 [00:01<00:01, 5.22it/s]
Computing concepts: 50%
Computing concepts: 55%
                                     | 11/20 [00:02<00:01, 5.57it/s]
Computing concepts: 60%
                                     | 12/20 [00:02<00:01, 5.00it/s]
Computing concepts: 65%
                                      13/20 [00:02<00:01, 4.84it/s]
Computing concepts: 70%
                                      | 14/20 [00:02<00:01, 5.05it/s]
Computing concepts: 80%
                                      | 16/20 [00:03<00:00, 5.34it/s]
Computing concepts: 85%
                                       | 17/20 [00:03<00:00, 4.76it/s]
Computing concepts: 100%
                                         20/20 [00:03<00:00, 5.93it/s]
```



## Variación en el tiempo y consumo de las particiones sin CM

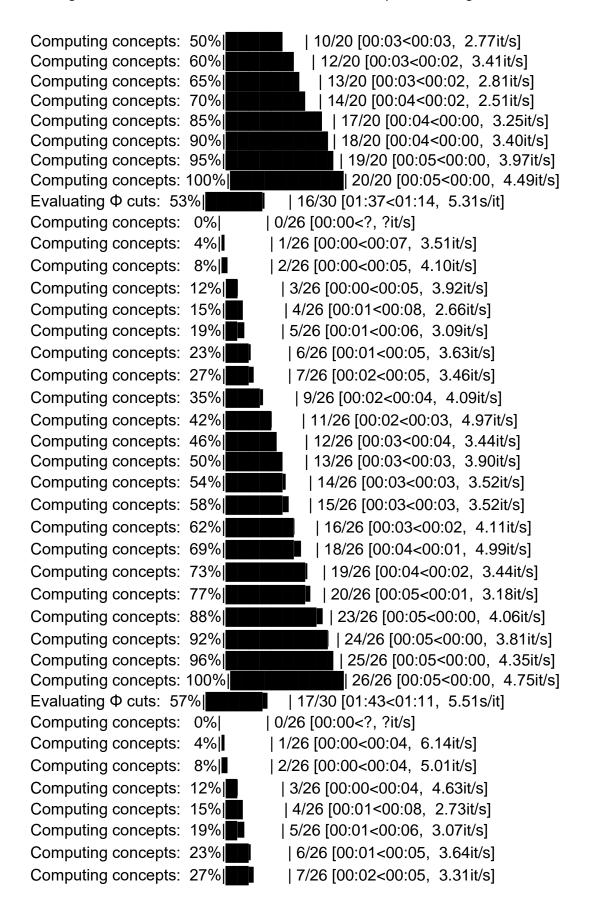
```
Computing concepts: 77%
                                      20/26 [00:04<00:01, 4.32it/s]
Computing concepts: 81%
                                      | 21/26 [00:04<00:01, 3.60it/s]
Computing concepts: 92%
                                        | 24/26 [00:05<00:00, 4.33it/s]
Computing concepts: 96%
                                        | 25/26 [00:05<00:00, 3.90it/s]
Computing concepts: 100%
                                         | 26/26 [00:05<00:00, 4.26it/s]
Evaluating Φ cuts: 23%
                               7/30 [00:43<02:18, 6.03s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 5%
                                | 1/20 [00:00<00:03, 5.41it/s]
Computing concepts: 10%
                                | 2/20 [00:00<00:04, 4.25it/s]
Computing concepts: 15%
                                 | 3/20 [00:01<00:09, 1.78it/s]
Computing concepts: 20%
                                 | 4/20 [00:02<00:07, 2.19it/s]
Computing concepts: 25%
                                  | 5/20 [00:02<00:07, 1.98it/s]
Computing concepts: 35%
                                   | 7/20 [00:03<00:05, 2.43it/s]
Computing concepts: 45%
                                    9/20 [00:03<00:04, 2.59it/s]
Computing concepts: 50%
                                    | 10/20 [00:04<00:03, 2.70it/s]
Computing concepts: 55%
                                     | 11/20 [00:04<00:04, 2.15it/s]
Computing concepts: 60%
                                     | 12/20 [00:04<00:03, 2.53it/s]
                                     | 14/20 [00:05<00:01, 3.04it/s]
Computing concepts: 70%
Computing concepts: 75%
                                      | 15/20 [00:06<00:02, 2.33it/s]
Computing concepts: 90%
                                       | 18/20 [00:06<00:00, 2.98it/s]
                                        | 19/20 [00:06<00:00, 2.89it/s]
Computing concepts: 95%
Computing concepts: 100%
                                         20/20 [00:06<00:00, 3.34it/s]
Evaluating Φ cuts: 27%
                               | 8/30 [00:50<02:19, 6.32s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
```

```
Computing concepts: 4%
                               1/26 [00:00<00:05, 4.23it/s]
Computing concepts: 8%
                               2/26 [00:00<00:06, 3.56it/s]
Computing concepts: 12%
                                 | 3/26 [00:00<00:06, 3.63it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:09, 2.23it/s]
Computing concepts: 19%
                                 | 5/26 [00:02<00:08, 2.36it/s]
Computing concepts: 23%
                                 | 6/26 [00:02<00:08, 2.34it/s]
Computing concepts: 31%
                                  | 8/26 [00:02<00:06, 2.95it/s]
Computing concepts: 38%
                                  | 10/26 [00:03<00:04, 3.75it/s]
Computing concepts: 42%
                                   11/26 [00:03<00:04, 3.40it/s]
Computing concepts: 46%
                                    | 12/26 [00:03<00:04, 2.98it/s]
Computing concepts: 50%
                                    | 13/26 [00:04<00:04, 2.94it/s]
Computing concepts: 54%
                                    14/26 [00:04<00:04, 2.72it/s]
Computing concepts: 58%
                                    | 15/26 [00:04<00:03, 3.15it/s]
Computing concepts: 62%
                                     | 16/26 [00:04<00:02, 3.55it/s]
Computing concepts: 69%
                                     | 18/26 [00:05<00:01, 4.20it/s]
Computing concepts: 73%
                                      19/26 [00:05<00:02, 2.77it/s]
Computing concepts: 77%
                                      20/26 [00:06<00:02, 2.45it/s]
Computing concepts: 88%
                                      | 23/26 [00:06<00:00, 3.20it/s]
Computing concepts: 92%
                                        | 24/26 [00:06<00:00, 3.40it/s]
Computing concepts: 96%
                                        | 25/26 [00:07<00:00, 3.92it/s]
Computing concepts: 100%
                                         | 26/26 [00:07<00:00, 4.36it/s]
                               9/30 [00:57<02:18, 6.62s/it]
Evaluating Φ cuts: 30%
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts:
                     4%|
                               1/26 [00:00<00:06, 3.60it/s]
Computing concepts: 8%
                               2/26 [00:00<00:06, 3.63it/s]
Computing concepts: 12%
                                 | 3/26 [00:01<00:09, 2.45it/s]
                                 | 4/26 [00:01<00:08, 2.70it/s]
Computing concepts: 15%
Computing concepts: 19%
                                 | 5/26 [00:01<00:06, 3.24it/s]
                                 | 6/26 [00:01<00:05, 3.82it/s]
Computing concepts: 23%
                                 | 7/26 [00:02<00:05, 3.40it/s]
Computing concepts: 27%
Computing concepts: 35%
                                  9/26 [00:02<00:04, 4.07it/s]
                                   | 11/26 [00:02<00:03, 4.45it/s]
Computing concepts: 42%
                                    | 12/26 [00:03<00:02, 4.96it/s]
Computing concepts: 46%
Computing concepts: 50%
                                    | 13/26 [00:03<00:02, 4.86it/s]
Computing concepts: 54%
                                    | 14/26 [00:03<00:03, 3.45it/s]
Computing concepts: 58%
                                    | 15/26 [00:03<00:02, 4.02it/s]
                                     | 16/26 [00:04<00:02, 3.85it/s]
Computing concepts: 62%
                                      | 17/26 [00:04<00:02, 4.34it/s]
Computing concepts: 65%
Computing concepts: 73%
                                      19/26 [00:04<00:01, 4.84it/s]
Computing concepts: 77%
                                      | 20/26 [00:04<00:01, 3.91it/s]
```

```
Computing concepts: 81%
                                        21/26 [00:05<00:01, 2.78it/s]
Computing concepts: 92%
                                        24/26 [00:05<00:00, 3.59it/s]
Computing concepts: 96%
                                        | 25/26 [00:06<00:00, 3.34it/s]
Computing concepts: 100%
                                         26/26 [00:06<00:00, 3.79it/s]
Evaluating Φ cuts: 33%
                                | 10/30 [01:04<02:11, 6.56s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts: 4%
                               1/26 [00:00<00:06, 3.81it/s]
Computing concepts: 8%
                               | 2/26 [00:01<00:10, 2.38it/s]
Computing concepts: 12%
                                 3/26 [00:01<00:08, 2.70it/s]
                                 | 4/26 [00:01<00:07, 3.14it/s]
Computing concepts: 15%
                                 | 5/26 [00:01<00:07, 2.87it/s]
Computing concepts: 19%
Computing concepts: 27%
                                 | 7/26 [00:02<00:05, 3.56it/s]
Computing concepts: 35%
                                  9/26 [00:02<00:03, 4.37it/s]
Computing concepts: 38%
                                  10/26 [00:02<00:04, 3.82it/s]
Computing concepts: 42%
                                   11/26 [00:03<00:04, 3.29it/s]
Computing concepts: 46%
                                    1 12/26 [00:03<00:03, 3.67it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.56it/s]
                                    | 14/26 [00:04<00:03, 3.21it/s]
Computing concepts: 54%
Computing concepts: 58%
                                    | 15/26 [00:04<00:03, 3.42it/s]
Computing concepts: 62%
                                     | 16/26 [00:04<00:03, 3.24it/s]
                                     | 18/26 [00:04<00:02, 3.90it/s]
Computing concepts: 69%
Computing concepts: 73%
                                      | 19/26 [00:05<00:02, 3.23it/s]
                                      | 20/26 [00:05<00:02, 2.84it/s]
Computing concepts: 77%
Computing concepts: 88%
                                     | 23/26 [00:06<00:00, 3.65it/s]
                                        | 24/26 [00:06<00:00, 3.21it/s]
Computing concepts: 92%
Computing concepts: 96%
                                        | 25/26 [00:06<00:00, 3.59it/s]
Computing concepts: 100%
                                         26/26 [00:06<00:00, 3.92it/s]
Evaluating Φ cuts: 37%
                                | 11/30 [01:11<02:06, 6.67s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 4%
                               | 1/26 [00:00<00:04, 5.23it/s]
Computing concepts: 8%
                               2/26 [00:00<00:05, 4.09it/s]
Computing concepts: 12%
                                 3/26 [00:00<00:05, 4.22it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:06, 3.63it/s]
Computing concepts: 19%
                                 | 5/26 [00:02<00:09, 2.18it/s]
Computing concepts: 23%
                                  | 6/26 [00:02<00:07, 2.59it/s]
Computing concepts: 27%
                                  | 7/26 [00:02<00:06, 3.07it/s]
                                  | 8/26 [00:02<00:06, 2.58it/s]
Computing concepts: 31%
Computing concepts: 38%
                                  | 10/26 [00:03<00:04, 3.27it/s]
Computing concepts: 46%
                                    | 12/26 [00:03<00:03, 3.93it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.35it/s]
```

```
Computing concepts: 54%
                                    | 14/26 [00:04<00:03, 3.59it/s]
Computing concepts: 58%
                                    | 15/26 [00:04<00:03, 3.32it/s]
Computing concepts: 62%
                                     | 16/26 [00:04<00:02, 3.37it/s]
Computing concepts: 69%
                                     18/26 [00:05<00:01, 4.02it/s]
Computing concepts: 73%
                                      19/26 [00:05<00:01, 3.61it/s]
Computing concepts: 77%
                                      20/26 [00:05<00:02, 2.95it/s]
Computing concepts: 88%
                                      | 23/26 [00:06<00:00, 3.76it/s]
Computing concepts: 92%
                                        24/26 [00:06<00:00, 4.06it/s]
Computing concepts: 96%
                                        25/26 [00:06<00:00, 4.62it/s]
Computing concepts: 100%
                                         1 26/26 [00:06<00:00, 4.95it/s]
Evaluating Φ cuts: 40%
                                | 12/30 [01:17<02:00, 6.67s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 4%
                               | 1/26 [00:00<00:04, 5.96it/s]
                               2/26 [00:00<00:04, 5.49it/s]
Computing concepts:
                     8%|
Computing concepts: 12%
                                 3/26 [00:00<00:04, 5.33it/s]
                                 | 4/26 [00:01<00:07, 3.11it/s]
Computing concepts: 15%
Computing concepts: 19%
                                | 5/26 [00:01<00:06, 3.27it/s]
Computing concepts: 23%
                                 | 6/26 [00:01<00:05, 3.78it/s]
Computing concepts: 27%
                                  | 7/26 [00:02<00:05, 3.44it/s]
Computing concepts: 38%
                                  | 10/26 [00:02<00:03, 4.58it/s]
Computing concepts: 42%
                                   11/26 [00:02<00:03, 4.32it/s]
Computing concepts: 46%
                                    | 12/26 [00:02<00:04, 3.30it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.41it/s]
Computing concepts: 54%
                                    14/26 [00:03<00:03, 3.23it/s]
Computing concepts: 58%
                                    15/26 [00:03<00:03, 3.31it/s]
                                     | 16/26 [00:03<00:02, 3.74it/s]
Computing concepts: 62%
Computing concepts: 69%
                                     | 18/26 [00:04<00:01, 4.61it/s]
Computing concepts: 73%
                                      | 19/26 [00:04<00:01, 3.55it/s]
Computing concepts: 77%
                                      20/26 [00:05<00:01, 3.15it/s]
Computing concepts: 88%
                                     | 23/26 [00:05<00:00, 4.01it/s]
Computing concepts: 92%
                                       24/26 [00:05<00:00, 4.18it/s]
Computing concepts: 96%
                                        | 25/26 [00:05<00:00, 4.39it/s]
Computing concepts: 100%
                                         26/26 [00:05<00:00, 4.87it/s]
Evaluating Φ cuts: 43%
                                 | 13/30 [01:23<01:49, 6.45s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts:
                               | 1/26 [00:00<00:06, 3.97it/s]
                     4%|
                               2/26 [00:00<00:06, 3.99it/s]
Computing concepts: 8%
                                3/26 [00:00<00:05, 3.99it/s]
Computing concepts: 12%
                                 | 4/26 [00:01<00:08, 2.70it/s]
Computing concepts: 15%
Computing concepts: 19%
                                | 5/26 [00:01<00:07, 2.94it/s]
```

```
Computing concepts: 23%
                                  | 6/26 [00:01<00:05, 3.48it/s]
Computing concepts: 27%
                                  | 7/26 [00:02<00:05, 3.32it/s]
Computing concepts: 35%
                                   9/26 [00:02<00:04, 4.10it/s]
Computing concepts: 42%
                                    | 11/26 [00:02<00:03, 4.74it/s]
Computing concepts: 46%
                                    | 12/26 [00:02<00:03, 4.04it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:02, 4.61it/s]
Computing concepts: 54%
                                    | 14/26 [00:03<00:03, 3.87it/s]
Computing concepts: 58%
                                    | 15/26 [00:03<00:02, 4.15it/s]
Computing concepts: 62%
                                     | 16/26 [00:03<00:02, 4.62it/s]
Computing concepts: 69%
                                     | 18/26 [00:04<00:01, 5.25it/s]
                                      | 19/26 [00:04<00:01, 4.30it/s]
Computing concepts: 73%
Computing concepts: 77%
                                      20/26 [00:04<00:01, 3.61it/s]
                                       | 23/26 [00:05<00:00, 4.67it/s]
Computing concepts: 88%
Computing concepts: 92%
                                        24/26 [00:05<00:00, 4.76it/s]
Computing concepts: 96%
                                        | 25/26 [00:05<00:00, 5.31it/s]
Computing concepts: 100%
                                         26/26 [00:05<00:00, 5.53it/s]
Evaluating Φ cuts: 47%
                                 | 14/30 [01:29<01:38, 6.18s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 5%
                                | 1/20 [00:00<00:10, 1.87it/s]
                                | 2/20 [00:00<00:07, 2.38it/s]
Computing concepts: 10%
                                 | 3/20 [00:00<00:06, 2.69it/s]
Computing concepts: 15%
Computing concepts: 30%
                                  | 6/20 [00:01<00:03, 3.64it/s]
Computing concepts: 35%
                                   | 7/20 [00:01<00:03, 4.07it/s]
Computing concepts: 40%
                                   | 8/20 [00:01<00:02, 4.79it/s]
Computing concepts: 45%
                                    9/20 [00:01<00:02, 4.45it/s]
                                    | 10/20 [00:01<00:02, 4.80it/s]
Computing concepts: 50%
                                     | 12/20 [00:02<00:01, 5.76it/s]
Computing concepts: 60%
Computing concepts: 65%
                                      | 13/20 [00:02<00:01, 4.88it/s]
Computing concepts: 70%
                                      | 14/20 [00:02<00:01, 4.45it/s]
                                       | 17/20 [00:02<00:00, 5.74it/s]
Computing concepts: 85%
Computing concepts: 90%
                                       | 18/20 [00:02<00:00, 5.79it/s]
                                        | 19/20 [00:03<00:00, 6.43it/s]
Computing concepts: 95%
Computing concepts: 100%
                                         20/20 [00:03<00:00, 6.74it/s]
Evaluating Φ cuts: 50%
                                 | 15/30 [01:32<01:19, 5.29s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 5%
                                | 1/20 [00:01<00:19, 1.03s/it]
                                | 2/20 [00:01<00:14, 1.25it/s]
Computing concepts: 10%
Computing concepts: 15%
                                 | 3/20 [00:01<00:12, 1.41it/s]
Computing concepts: 30%
                                  | 6/20 [00:01<00:07, 1.94it/s]
Computing concepts: 35%
                                   | 7/20 [00:02<00:05, 2.27it/s]
Computing concepts: 40%
                                   8/20 [00:02<00:04, 2.82it/s]
Computing concepts: 45%
                                    | 9/20 [00:02<00:04, 2.48it/s]
```



```
Computing concepts: 38%
                                  10/26 [00:02<00:03, 4.39it/s]
Computing concepts: 42%
                                   | 11/26 [00:02<00:03, 4.16it/s]
Computing concepts: 46%
                                    | 12/26 [00:03<00:04, 3.09it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.26it/s]
Computing concepts: 54%
                                    | 14/26 [00:03<00:04, 2.74it/s]
Computing concepts: 58%
                                    | 15/26 [00:04<00:03, 3.17it/s]
Computing concepts: 62%
                                     | 16/26 [00:04<00:02, 3.70it/s]
Computing concepts: 69%
                                     | 18/26 [00:04<00:01, 4.31it/s]
Computing concepts: 73%
                                      | 19/26 [00:04<00:01, 3.73it/s]
Computing concepts: 77%
                                      | 20/26 [00:05<00:01, 3.37it/s]
Computing concepts: 88%
                                       23/26 [00:05<00:00, 4.36it/s]
Computing concepts: 92%
                                        | 24/26 [00:05<00:00, 4.14it/s]
Computing concepts: 96%
                                        | 25/26 [00:05<00:00, 4.65it/s]
Computing concepts: 100%
                                         26/26 [00:06<00:00, 5.02it/s]
Evaluating Φ cuts: 60%
                                  | 18/30 [01:50<01:08, 5.69s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts:
                               1/26 [00:00<00:03, 6.80it/s]
                     4%|
Computing concepts:
                               2/26 [00:00<00:04, 5.89it/s]
                     8%|
Computing concepts: 12%
                                 3/26 [00:00<00:03, 6.13it/s]
                                 | 4/26 [00:00<00:03, 5.59it/s]
Computing concepts: 15%
Computing concepts: 19%
                                 | 5/26 [00:01<00:06, 3.06it/s]
Computing concepts: 23%
                                  | 6/26 [00:01<00:05, 3.72it/s]
                                  | 7/26 [00:01<00:04, 4.29it/s]
Computing concepts: 27%
Computing concepts: 31%
                                  | 8/26 [00:02<00:04, 3.80it/s]
Computing concepts: 38%
                                  | 10/26 [00:02<00:03, 4.50it/s]
Computing concepts: 46%
                                    12/26 [00:02<00:02, 5.39it/s]
Computing concepts: 50%
                                    | 13/26 [00:02<00:02, 4.36it/s]
Computing concepts: 54%
                                    14/26 [00:03<00:02, 4.26it/s]
Computing concepts: 58%
                                    | 15/26 [00:03<00:02, 3.76it/s]
Computing concepts: 62%
                                     | 16/26 [00:03<00:02, 4.06it/s]
Computing concepts: 69%
                                     18/26 [00:03<00:01, 4.94it/s]
Computing concepts: 73%
                                      | 19/26 [00:04<00:01, 4.23it/s]
Computing concepts: 77%
                                      20/26 [00:04<00:01, 3.84it/s]
Computing concepts: 88%
                                       23/26 [00:04<00:00, 4.94it/s]
Computing concepts: 92%
                                        24/26 [00:04<00:00, 4.63it/s]
                                        | 25/26 [00:05<00:00, 5.07it/s]
Computing concepts: 96%
                                         26/26 [00:05<00:00, 5.43it/s]
Computing concepts: 100%
Evaluating Φ cuts: 63%
                                   | 19/30 [01:55<01:01, 5.55s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts: 4%
                               | 1/26 [00:00<00:07, 3.51it/s]
```

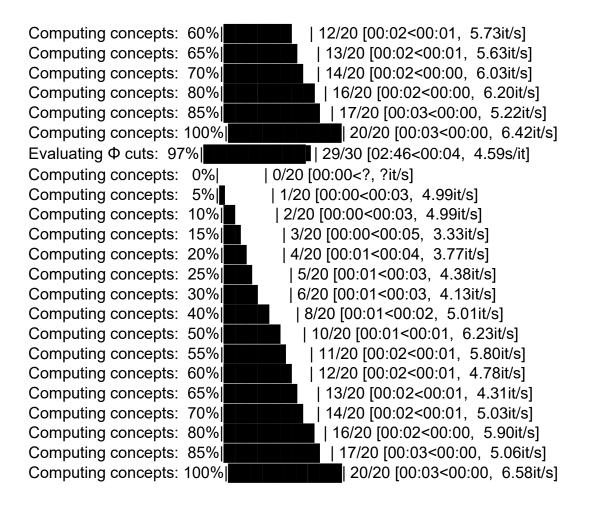
```
Computing concepts: 8%
                               2/26 [00:01<00:10, 2.30it/s]
Computing concepts: 12%
                                 3/26 [00:01<00:08, 2.61it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:06, 3.18it/s]
Computing concepts: 19%
                                | 5/26 [00:01<00:07, 2.70it/s]
Computing concepts: 27%
                                 | 7/26 [00:02<00:05, 3.34it/s]
                                  9/26 [00:02<00:03, 4.27it/s]
Computing concepts: 35%
Computing concepts: 38%
                                  | 10/26 [00:02<00:03, 4.17it/s]
Computing concepts: 42%
                                   | 11/26 [00:03<00:04, 3.01it/s]
Computing concepts: 46%
                                    | 12/26 [00:03<00:03, 3.53it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.58it/s]
Computing concepts: 54%
                                    | 14/26 [00:04<00:03, 3.28it/s]
Computing concepts: 58%
                                    | 15/26 [00:04<00:02, 3.86it/s]
Computing concepts: 62%
                                     | 16/26 [00:04<00:02, 4.06it/s]
Computing concepts: 69%
                                     | 18/26 [00:04<00:01, 4.70it/s]
Computing concepts: 73%
                                      | 19/26 [00:05<00:01, 3.95it/s]
Computing concepts: 77%
                                     | 20/26 [00:05<00:01, 3.31it/s]
Computing concepts: 88%
                                      | 23/26 [00:05<00:00, 4.06it/s]
Computing concepts: 92%
                                       | 24/26 [00:05<00:00, 4.21it/s]
Computing concepts: 96%
                                        | 25/26 [00:06<00:00, 4.71it/s]
Computing concepts: 100%
                                         26/26 [00:06<00:00, 5.02it/s]
Evaluating Φ cuts: 67%
                                  20/30 [02:01<00:57, 5.80s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts:
                               | 1/26 [00:00<00:05, 4.31it/s]
                     4%|
Computing concepts: 8%
                               | 2/26 [00:00<00:05, 4.11it/s]
Computing concepts: 12%
                                 3/26 [00:01<00:08, 2.69it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:07, 3.13it/s]
Computing concepts: 19%
                                | 5/26 [00:01<00:05, 3.73it/s]
Computing concepts: 23%
                                 | 6/26 [00:01<00:04, 4.28it/s]
Computing concepts: 27%
                                 | 7/26 [00:02<00:05, 3.80it/s]
Computing concepts: 35%
                                  9/26 [00:02<00:03, 4.67it/s]
Computing concepts: 42%
                                   | 11/26 [00:02<00:02, 5.01it/s]
Computing concepts: 46%
                                    | 12/26 [00:02<00:02, 5.38it/s]
Computing concepts: 50%
                                    13/26 [00:02<00:02, 4.85it/s]
Computing concepts: 54%
                                    14/26 [00:03<00:02, 4.10it/s]
Computing concepts: 58%
                                    15/26 [00:03<00:02, 4.65it/s]
Computing concepts: 62%
                                     | 16/26 [00:03<00:02, 4.60it/s]
Computing concepts: 65%
                                     | 17/26 [00:03<00:01, 5.22it/s]
Computing concepts: 73%
                                      | 19/26 [00:03<00:01, 6.09it/s]
Computing concepts: 77%
                                      20/26 [00:04<00:01, 4.56it/s]
                                      | 21/26 [00:04<00:01, 3.92it/s]
Computing concepts: 81%
```

```
Computing concepts: 92%
                                        24/26 [00:04<00:00, 4.88it/s]
Computing concepts: 96%
                                        | 25/26 [00:05<00:00, 4.91it/s]
Computing concepts: 100%
                                         26/26 [00:05<00:00, 5.30it/s]
Evaluating Φ cuts: 70%
                                   | 21/30 [02:06<00:50, 5.66s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts:
                               | 1/26 [00:00<00:03, 6.51it/s]
                     4%|
                               | 2/26 [00:00<00:04, 5.50it/s]
Computing concepts: 8%
Computing concepts: 12%
                                 | 3/26 [00:00<00:04, 4.92it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:08, 2.73it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:07, 2.96it/s]
Computing concepts: 23%
                                  | 6/26 [00:02<00:06, 2.92it/s]
Computing concepts: 31%
                                  | 8/26 [00:02<00:05, 3.57it/s]
Computing concepts: 38%
                                  | 10/26 [00:02<00:03, 4.58it/s]
Computing concepts: 42%
                                    | 11/26 [00:02<00:03, 4.50it/s]
                                    | 12/26 [00:03<00:03, 3.82it/s]
Computing concepts: 46%
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 4.11it/s]
Computing concepts: 54%
                                     | 14/26 [00:03<00:03, 3.58it/s]
Computing concepts: 58%
                                    | 15/26 [00:03<00:02, 4.22it/s]
Computing concepts: 62%
                                     | 16/26 [00:03<00:02, 4.76it/s]
Computing concepts: 69%
                                     18/26 [00:04<00:01, 5.33it/s]
Computing concepts: 73%
                                      | 19/26 [00:04<00:01, 4.33it/s]
Computing concepts: 77%
                                      20/26 [00:04<00:01, 3.67it/s]
Computing concepts: 88%
                                      | 23/26 [00:05<00:00, 4.75it/s]
Computing concepts: 92%
                                        24/26 [00:05<00:00, 4.93it/s]
Computing concepts: 96%
                                        | 25/26 [00:05<00:00, 5.24it/s]
Computing concepts: 100%
                                         26/26 [00:05<00:00, 5.56it/s]
Evaluating Φ cuts: 73%
                                    22/30 [02:12<00:45, 5.64s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 5%
                                | 1/20 [00:00<00:02, 7.24it/s]
Computing concepts: 10%
                                | 2/20 [00:00<00:02, 6.87it/s]
Computing concepts: 15%
                                 | 3/20 [00:00<00:04, 3.79it/s]
                                 | 4/20 [00:00<00:03, 4.47it/s]
Computing concepts: 20%
Computing concepts: 25%
                                  | 5/20 [00:01<00:03, 4.13it/s]
                                   | 7/20 [00:01<00:02, 5.13it/s]
Computing concepts: 35%
Computing concepts: 45%
                                     9/20 [00:01<00:01. 5.68it/s]
Computing concepts: 50%
                                    | 10/20 [00:01<00:01, 5.75it/s]
Computing concepts: 55%
                                     | 11/20 [00:02<00:01, 4.94it/s]
Computing concepts: 60%
                                     | 12/20 [00:02<00:01, 5.52it/s]
                                      | 14/20 [00:02<00:00, 6.57it/s]
Computing concepts: 70%
                                      | 15/20 [00:02<00:00, 5.53it/s]
Computing concepts: 75%
                                        | 18/20 [00:02<00:00, 6.82it/s]
Computing concepts: 90%
```

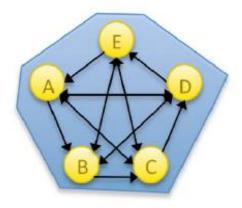
```
Computing concepts: 95%
                                        | 19/20 [00:03<00:00, 6.72it/s]
Computing concepts: 100%
                                          20/20 [00:03<00:00, 6.97it/s]
Evaluating Φ cuts: 77%
                                  | 23/30 [02:15<00:34, 4.92s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts:
                               | 1/26 [00:00<00:03, 6.51it/s]
                     4%|
Computing concepts: 8%
                               2/26 [00:00<00:04, 5.18it/s]
Computing concepts: 12%
                                 | 3/26 [00:01<00:09, 2.44it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:07, 2.75it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:06, 3.30it/s]
Computing concepts: 23%
                                  | 6/26 [00:02<00:06, 2.97it/s]
Computing concepts: 31%
                                  | 8/26 [00:02<00:04, 3.62it/s]
Computing concepts: 38%
                                  | 10/26 [00:02<00:03, 4.57it/s]
Computing concepts: 42%
                                   11/26 [00:02<00:03, 4.31it/s]
Computing concepts: 46%
                                    1 12/26 [00:03<00:04. 3.20it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.77it/s]
Computing concepts: 54%
                                    | 14/26 [00:03<00:03, 3.75it/s]
Computing concepts: 58%
                                    15/26 [00:04<00:03, 3.21it/s]
Computing concepts: 62%
                                     | 16/26 [00:04<00:02, 3.75it/s]
Computing concepts: 65%
                                      | 17/26 [00:04<00:02, 3.80it/s]
Computing concepts: 73%
                                      | 19/26 [00:04<00:01, 4.57it/s]
Computing concepts: 77%
                                      20/26 [00:05<00:01, 3.60it/s]
Computing concepts: 81%
                                      | 21/26 [00:05<00:01, 2.90it/s]
Computing concepts: 92%
                                        24/26 [00:06<00:00, 3.77it/s]
Computing concepts: 96%
                                        | 25/26 [00:06<00:00, 3.92it/s]
Computing concepts: 100%
                                         26/26 [00:06<00:00, 4.45it/s]
Evaluating Φ cuts: 80%
                                   | 24/30 [02:22<00:32, 5.39s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts:
                     0%|
Computing concepts:
                               | 1/26 [00:00<00:03, 6.51it/s]
                     4%|
Computing concepts:
                               2/26 [00:00<00:04, 5.33it/s]
                     8%|
                                 | 3/26 [00:00<00:04, 5.68it/s]
Computing concepts: 12%
Computing concepts: 15%
                                 | 4/26 [00:00<00:03, 5.59it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:06, 3.13it/s]
Computing concepts: 23%
                                  | 6/26 [00:01<00:05, 3.52it/s]
Computing concepts: 27%
                                  | 7/26 [00:01<00:05, 3.33it/s]
Computing concepts: 35%
                                  9/26 [00:02<00:04, 4.15it/s]
Computing concepts: 42%
                                   11/26 [00:02<00:02, 5.05it/s]
Computing concepts: 46%
                                    1 12/26 [00:02<00:03, 4.20it/s]
Computing concepts: 50%
                                    | 13/26 [00:02<00:02, 4.60it/s]
Computing concepts: 54%
                                    | 14/26 [00:03<00:02, 4.42it/s]
Computing concepts: 58%
                                    | 15/26 [00:03<00:02, 3.78it/s]
```

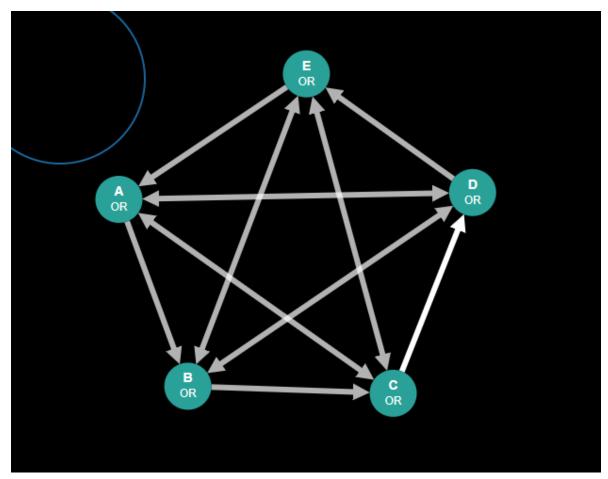
```
Computing concepts: 62%
                                     | 16/26 [00:03<00:02, 3.92it/s]
Computing concepts: 65%
                                      | 17/26 [00:03<00:02, 3.66it/s]
                                     | 18/26 [00:04<00:02, 3.98it/s]
Computing concepts: 69%
Computing concepts: 77%
                                      | 20/26 [00:04<00:01, 4.10it/s]
Computing concepts: 81%
                                      | 21/26 [00:04<00:01, 3.70it/s]
Computing concepts: 92%
                                        24/26 [00:05<00:00, 4.71it/s]
                                        | 25/26 [00:05<00:00, 4.45it/s]
Computing concepts: 96%
Computing concepts: 100%
                                         26/26 [00:05<00:00, 4.60it/s]
Evaluating Φ cuts: 83%
                                   | 25/30 [02:27<00:27, 5.49s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts:
                               1/26 [00:00<00:06, 3.71it/s]
                     4%|
Computing concepts: 8%
                               | 2/26 [00:00<00:06, 3.65it/s]
Computing concepts: 12%
                                 | 3/26 [00:01<00:08, 2.56it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:07, 2.94it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:06, 3.48it/s]
Computing concepts: 23%
                                  | 6/26 [00:01<00:05, 3.70it/s]
Computing concepts: 27%
                                  | 7/26 [00:02<00:05, 3.28it/s]
Computing concepts: 35%
                                   9/26 [00:02<00:04, 3.80it/s]
Computing concepts: 42%
                                   11/26 [00:02<00:03, 4.79it/s]
                                    | 12/26 [00:03<00:03, 4.32it/s]
Computing concepts: 46%
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 3.74it/s]
Computing concepts: 54%
                                    14/26 [00:03<00:02, 4.06it/s]
Computing concepts: 58%
                                    | 15/26 [00:03<00:03, 3.42it/s]
Computing concepts: 62%
                                     | 16/26 [00:04<00:02, 3.98it/s]
Computing concepts: 65%
                                      | 17/26 [00:04<00:02, 4.24it/s]
Computing concepts: 69%
                                     | 18/26 [00:04<00:01, 4.78it/s]
Computing concepts: 77%
                                      20/26 [00:04<00:01, 5.49it/s]
Computing concepts: 81%
                                      | 21/26 [00:05<00:01, 4.49it/s]
Computing concepts: 85%
                                       | 22/26 [00:05<00:01, 3.85it/s]
Computing concepts: 96%
                                        | 25/26 [00:05<00:00, 4.87it/s]
Computing concepts: 100%
                                         26/26 [00:05<00:00, 5.27it/s]
Evaluating Φ cuts: 87%
                                   | 26/30 [02:33<00:22, 5.58s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
                                | 1/20 [00:00<00:03, 5.61it/s]
Computing concepts: 5%
                                | 2/20 [00:00<00:02, 6.19it/s]
Computing concepts: 10%
Computing concepts: 15%
                                 | 3/20 [00:00<00:04, 3.73it/s]
Computing concepts: 20%
                                 | 4/20 [00:00<00:03, 4.40it/s]
Computing concepts: 30%
                                  | 6/20 [00:01<00:02, 5.42it/s]
Computing concepts: 40%
                                   | 8/20 [00:01<00:01, 6.42it/s]
                                    9/20 [00:01<00:02, 5.40it/s]
Computing concepts: 45%
Computing concepts: 50%
                                    | 10/20 [00:01<00:01, 5.69it/s]
```

```
Computing concepts: 55%
                                     | 11/20 [00:01<00:01, 4.95it/s]
Computing concepts: 60%
                                     | 12/20 [00:02<00:01, 5.52it/s]
Computing concepts: 65%
                                      | 13/20 [00:02<00:01, 5.80it/s]
                                       | 15/20 [00:02<00:00, 6.20it/s]
Computing concepts: 75%
Computing concepts: 80%
                                      | 16/20 [00:02<00:00, 5.22it/s]
                                        | 19/20 [00:03<00:00, 6.42it/s]
Computing concepts: 95%
Computing concepts: 100%
                                         20/20 [00:03<00:00, 6.86it/s]
Evaluating Φ cuts: 90%
                                     | 27/30 [02:36<00:14, 4.86s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
                               | 1/26 [00:00<00:04, 5.77it/s]
Computing concepts:
                     4%|
                               2/26 [00:00<00:04, 4.86it/s]
Computing concepts: 8%
Computing concepts: 12%
                                 3/26 [00:00<00:05, 4.58it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:08, 2.72it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:07, 2.92it/s]
Computing concepts: 23%
                                  | 6/26 [00:01<00:05, 3.49it/s]
Computing concepts: 27%
                                  | 7/26 [00:02<00:04, 4.01it/s]
Computing concepts: 31%
                                  | 8/26 [00:02<00:05, 3.51it/s]
Computing concepts: 38%
                                   | 10/26 [00:02<00:03, 4.27it/s]
                                    | 12/26 [00:02<00:02, 5.28it/s]
Computing concepts: 46%
                                    | 13/26 [00:03<00:02, 5.07it/s]
Computing concepts: 50%
Computing concepts: 54%
                                    | 14/26 [00:03<00:03, 3.87it/s]
Computing concepts: 58%
                                     | 15/26 [00:03<00:02, 4.50it/s]
                                     | 16/26 [00:03<00:02, 4.44it/s]
Computing concepts: 62%
Computing concepts: 65%
                                      | 17/26 [00:04<00:02, 3.82it/s]
Computing concepts: 69%
                                     | 18/26 [00:04<00:02, 4.00it/s]
Computing concepts: 77%
                                      20/26 [00:04<00:01, 4.82it/s]
Computing concepts: 81%
                                       | 21/26 [00:04<00:01, 3.93it/s]
Computing concepts: 85%
                                       | 22/26 [00:05<00:01, 3.46it/s]
Computing concepts: 96%
                                        | | 25/26 [00:05<00:00, 4.44it/s]
Computing concepts: 100%
                                         26/26 [00:05<00:00, 4.90it/s]
                                     | 28/30 [02:42<00:10, 5.12s/it]
Evaluating Φ cuts: 93%
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 5%
                                | 1/20 [00:00<00:03, 5.91it/s]
                                | 2/20 [00:00<00:03, 5.75it/s]
Computing concepts: 10%
Computing concepts: 15%
                                 | 3/20 [00:00<00:02, 5.80it/s]
Computing concepts: 20%
                                 | 4/20 [00:01<00:04, 3.63it/s]
Computing concepts: 25%
                                  | 5/20 [00:01<00:03, 4.11it/s]
Computing concepts: 30%
                                  | 6/20 [00:01<00:02, 4.75it/s]
Computing concepts: 35%
                                   | 7/20 [00:01<00:02, 4.42it/s]
Computing concepts: 50%
                                    | 10/20 [00:01<00:01, 5.35it/s]
Computing concepts: 55%
                                     | 11/20 [00:02<00:01, 5.87it/s]
```



# Grafo 9





# → Estado-nodo

| Entrada de datos   | Medida de<br>distancia | Esquema de partición | Resultados con CM   | Resultados sin CM   |
|--|------------------------|----------------------|---|---|
| Grafo:   | EMD                    | biparticion          | MIP:<br>Cut [A, C] —//—<br>→ [B, D, E]<br>Phi:<br>Φ = 0.056123<br>Time:<br>58.900532 s        | MIP:<br>Cut [A, C] —//—<br>→ [B, D, E]<br>Phi:<br>Φ = 0.056123<br>Time:<br>92.620368 s  |
| <pre>tpm = np.array([   [0,0,0,0,0],   [0,1,1,1,0],   [0,0,1,1,1],   [1,0,0,1,1],   [1,1,1],   [1,1,1],   [1,1,1],   [1,1,1],   [1,1,1],   [1,1,1],   [1,1,1],   [1,1,1],   [1,1,1],   [1,1,1],   [1,1,1],   [1,1</pre> | EMD                    | tripartición         | MIP:<br>Cut [A, C] —//—<br>→ [B, D, E]<br>Phi:<br>Φ = 0.056123<br>Time:<br>59.000532 s        | MIP:<br>Cut [A, C] —//—<br>→ [B, D, E]<br>Phi:<br>Φ = 0.056123<br>Time:<br>92.634038 s  |
|  | KLD                    | bipartición          | MIP:<br>Cut [A, C] ——//—<br>→ [B, D, E]<br>Phi:<br>Φ = 0.056123<br>Time:<br>57.287965 s       | MIP:<br>Cut [A, C] ——//—<br>→ [B, D, E]<br>Phi:<br>Φ = 0.056123<br>Time:<br>94.820368 s |
|  | KLD                    | tripartición         | MIP:<br>Cut [A, C] ——//—<br>—> [B, D, E]<br>Phi:<br>$\Phi = 0.056123$<br>Time:<br>58.809456 s | MIP:<br>Cut [A, C] ——//—<br>→ [B, D, E]<br>Phi:<br>Φ = 0.056123<br>Time:<br>93.314567 s |

```
cm = np.array([
  [0,1,1,1,0],
  [0,0,1,1,1],
  [1,0,0,1],
  [1,1,1,0,0]
])
```

## Variación en el tiempo y consumo en las diferentes particiones con CM

```
Evaluating Φ cuts: 0%
                            | 0/30 [00:00<?, ?it/s]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
                                | 2/20 [00:00<00:00, 19.95it/s]
Computing concepts: 10%
                                 | 3/20 [00:00<00:01, 10.37it/s]
Computing concepts: 15%
Computing concepts: 30%
                                  | 6/20 [00:00<00:01, 12.00it/s]
Computing concepts: 55%
                                     | 11/20 [00:00<00:00, 15.22it/s]
Computing concepts: 65%
                                     | 13/20 [00:00<00:00, 13.75it/s]
Computing concepts: 85%
                                      | 17/20 [00:00<00:00, 16.01it/s]
Evaluating Φ cuts: 3%
                             | 1/30 [00:00<00:27, 1.05it/s]
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts: 15%
                                 | 3/20 [00:00<00:00, 21.74it/s]
Computing concepts: 20%
                                 | 4/20 [00:00<00:01, 11.41it/s]
Computing concepts: 35%
                                   | 7/20 [00:00<00:00, 13.15it/s]
Computing concepts: 50%
                                    | 10/20 [00:00<00:00, 15.78it/s]
Computing concepts: 70%
                                      | 14/20 [00:00<00:00, 18.88it/s]
Computing concepts: 85%
                                       | 17/20 [00:00<00:00, 18.52it/s]
Evaluating Φ cuts: 7%
                             | 2/30 [00:01<00:26, 1.06it/s]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 15%
                                 | 4/26 [00:00<00:01, 17.29it/s]
Computing concepts: 31%
                                  | 8/26 [00:00<00:00, 19.86it/s]
Computing concepts: 54%
                                     | 14/26 [00:00<00:00, 24.17it/s]
Computing concepts: 69%
                                     | 18/26 [00:00<00:00, 27.41it/s]
Computing concepts: 85%
                                       | 22/26 [00:00<00:00, 27.35it/s]
Evaluating Φ cuts: 10%
                              3/30 [00:02<00:24, 1.11it/s]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 15%
                                 | 3/20 [00:00<00:01, 11.41it/s]
Computing concepts: 40%
                                   | 8/20 [00:00<00:00, 14.36it/s]
Computing concepts: 50%
                                    | 10/20 [00:00<00:00, 14.60it/s]
Computing concepts: 60%
                                     | 12/20 [00:00<00:00, 15.88it/s]
```

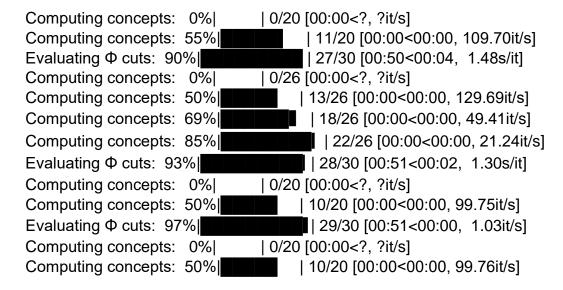
```
Computing concepts: 75%
                                       | 15/20 [00:00<00:00, 17.01it/s]
Computing concepts: 95%
                                        | 19/20 [00:00<00:00, 19.87it/s]
Evaluating Φ cuts: 13%
                              4/30 [00:03<00:23, 1.09it/s]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts: 4%
                               | 1/26 [00:00<00:05, 4.49it/s]
Computing concepts: 12%
                                 3/26 [00:01<00:06, 3.43it/s]
Computing concepts: 27%
                                  | 7/26 [00:01<00:04, 4.63it/s]
Computing concepts: 35%
                                   9/26 [00:01<00:03, 5.59it/s]
Computing concepts: 46%
                                    | 12/26 [00:01<00:02, 6.57it/s]
Computing concepts: 50%
                                    | 13/26 [00:02<00:02, 4.75it/s]
                                    | 15/26 [00:02<00:02, 4.64it/s]
Computing concepts: 58%
                                     | 18/26 [00:02<00:01, 6.21it/s]
Computing concepts: 69%
Computing concepts: 81%
                                      | | 21/26 [00:02<00:00, 7.95it/s]
Computing concepts: 88%
                                     | 23/26 [00:03<00:00, 6.40it/s]
Evaluating Φ cuts: 17%
                              | 5/30 [00:07<00:41, 1.65s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
                                 | 4/26 [00:00<00:00, 34.52it/s]
Computing concepts: 15%
                                  | 6/26 [00:00<00:00, 21.90it/s]
Computing concepts: 23%
Computing concepts: 42%
                                   | 11/26 [00:00<00:00, 26.33it/s]
Computing concepts: 54%
                                    | 14/26 [00:00<00:00, 25.17it/s]
Computing concepts: 65%
                                      | 17/26 [00:00<00:00, 25.38it/s]
Computing concepts: 81%
                                      | 21/26 [00:00<00:00, 25.57it/s]
Evaluating Φ cuts: 20%
                               6/30 [00:07<00:33, 1.41s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 23%
                                  | 6/26 [00:00<00:00, 59.06it/s]
Computing concepts: 42%
                                    | 11/26 [00:00<00:00, 37.04it/s]
Computing concepts: 65%
                                      | 17/26 [00:00<00:00, 36.99it/s]
Computing concepts: 81%
                                     | 21/26 [00:00<00:00, 18.46it/s]
Evaluating Φ cuts: 23%
                               7/30 [00:08<00:29, 1.30s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 15%
                                 | 3/20 [00:00<00:01, 10.53it/s]
Computing concepts: 25%
                                  | 5/20 [00:00<00:01, 12.27it/s]
Computing concepts: 45%
                                    9/20 [00:00<00:00, 14.69it/s]
Computing concepts: 55%
                                     | 11/20 [00:00<00:00, 14.84it/s]
                                      | 15/20 [00:00<00:00, 16.71it/s]
Computing concepts: 75%
Evaluating Φ cuts: 27%
                               | 8/30 [00:09<00:26, 1.20s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 12%
                                 | 3/26 [00:00<00:02, 10.53it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:07, 2.76it/s]
Computing concepts: 23%
                                  | 6/26 [00:01<00:06, 3.11it/s]
Computing concepts: 31%
                                  | 8/26 [00:01<00:04, 3.77it/s]
```

```
Computing concepts: 46%
                                    1 12/26 [00:02<00:03, 4.31it/s]
Computing concepts: 54%
                                    | 14/26 [00:03<00:02, 4.21it/s]
Computing concepts: 69%
                                     | 18/26 [00:03<00:01, 5.40it/s]
Computing concepts: 73%
                                      | 19/26 [00:03<00:01, 6.26it/s]
Computing concepts: 77%
                                      | 20/26 [00:03<00:00, 6.82it/s]
Computing concepts: 92%
                                        | 24/26 [00:03<00:00, 9.08it/s]
Evaluating Φ cuts: 30%
                               9/30 [00:13<00:41, 1.98s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts:
                               | 1/26 [00:00<00:03, 6.71it/s]
                     4%|
                               2/26 [00:00<00:04, 5.02it/s]
Computing concepts: 8%
Computing concepts: 12%
                                 3/26 [00:01<00:10, 2.26it/s]
Computing concepts: 27%
                                  | 7/26 [00:01<00:06, 2.90it/s]
Computing concepts: 42%
                                   | 11/26 [00:02<00:04, 3.51it/s]
Computing concepts: 50%
                                    | 13/26 [00:02<00:03, 4.25it/s]
Computing concepts: 54%
                                    | 14/26 [00:02<00:02, 5.13it/s]
Computing concepts: 73%
                                     | 19/26 [00:02<00:01, 6.98it/s]
Computing concepts: 81%
                                      | 21/26 [00:03<00:00, 6.05it/s]
Computing concepts: 92%
                                       | 24/26 [00:03<00:00, 7.54it/s]
Evaluating Φ cuts: 33%
                                | 10/30 [00:17<00:49, 2.50s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
                               2/26 [00:00<00:10, 2.22it/s]
Computing concepts: 8%
Computing concepts: 19%
                                 | 5/26 [00:01<00:07, 2.77it/s]
Computing concepts: 27%
                                  | 7/26 [00:01<00:05, 3.54it/s]
Computing concepts: 42%
                                   | 11/26 [00:02<00:03, 4.28it/s]
Computing concepts: 50%
                                    | 13/26 [00:02<00:02, 5.10it/s]
Computing concepts: 54%
                                    | 14/26 [00:02<00:03, 3.86it/s]
                                     | 18/26 [00:02<00:01, 5.00it/s]
Computing concepts: 69%
Computing concepts: 73%
                                      | 19/26 [00:03<00:01, 4.26it/s]
                                      | 22/26 [00:03<00:00, 5.73it/s]
Computing concepts: 85%
Computing concepts: 92%
                                       24/26 [00:03<00:00, 6.47it/s]
Evaluating Φ cuts: 37%
                                | 11/30 [00:20<00:53, 2.83s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 19%
                                 | 5/26 [00:00<00:00, 21.58it/s]
Computing concepts: 38%
                                  | 10/26 [00:00<00:00, 25.38it/s]
Computing concepts: 54%
                                    | 14/26 [00:00<00:00, 26.37it/s]
Computing concepts: 73%
                                      19/26 [00:00<00:00, 27.54it/s]
Computing concepts: 92%
                                       24/26 [00:00<00:00, 31.42it/s]
Evaluating Φ cuts: 40%
                                | 12/30 [00:21<00:39, 2.22s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
```

```
Computing concepts: 8%
                               2/26 [00:00<00:02, 8.54it/s]
Computing concepts: 12%
                                 | 3/26 [00:00<00:03, 7.32it/s]
                                 | 4/26 [00:01<00:07, 3.00it/s]
Computing concepts: 15%
Computing concepts: 27%
                                  | 7/26 [00:01<00:05, 3.73it/s]
Computing concepts: 42%
                                    | 11/26 [00:01<00:03, 4.91it/s]
Computing concepts: 46%
                                    | 12/26 [00:02<00:03, 3.57it/s]
                                    | 14/26 [00:02<00:03, 3.74it/s]
Computing concepts: 54%
Computing concepts: 69%
                                     18/26 [00:03<00:01, 4.78it/s]
Computing concepts: 77%
                                    | 20/26 [00:03<00:01, 4.71it/s]
Computing concepts: 92%
                                       | 24/26 [00:03<00:00, 6.41it/s]
Evaluating Φ cuts: 43%
                                 13/30 [00:25<00:44, 2.63s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 12%
                                 | 3/26 [00:00<00:01, 12.13it/s]
Computing concepts: 35%
                                   9/26 [00:00<00:01, 15.49it/s]
Computing concepts: 46%
                                    | 12/26 [00:00<00:01, 10.65it/s]
Computing concepts: 96%
                                        | 25/26 [00:00<00:00, 14.69it/s]
Evaluating Φ cuts: 47%
                                 | 14/30 [00:26<00:34, 2.14s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 60%
                                    | 12/20 [00:00<00:00, 106.79it/s]
Evaluating Φ cuts: 50%
                                 | 15/30 [00:26<00:23, 1.57s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 5%
                                | 1/20 [00:00<00:03, 4.99it/s]
Computing concepts: 15%
                                 | 3/20 [00:00<00:02, 5.87it/s]
Computing concepts: 40%
                                   | 8/20 [00:00<00:01, 7.98it/s]
Computing concepts: 50%
                                    | 10/20 [00:00<00:01, 9.03it/s]
Computing concepts: 65%
                                      | 13/20 [00:00<00:00, 10.84it/s]
Computing concepts: 85%
                                      | 17/20 [00:00<00:00, 13.23it/s]
Computing concepts: 100%
                                         20/20 [00:01<00:00, 15.89it/s]
Evaluating Φ cuts: 53%
                                  | 16/30 [00:27<00:19, 1.42s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
                                 | 4/26 [00:00<00:01, 14.34it/s]
Computing concepts: 15%
                                  | 7/26 [00:00<00:01, 14.87it/s]
Computing concepts: 27%
Computing concepts: 35%
                                   9/26 [00:00<00:01, 13.35it/s]
Computing concepts: 42%
                                   | 11/26 [00:00<00:01, 14.46it/s]
Computing concepts: 50%
                                    | 13/26 [00:00<00:00, 15.62it/s]
Computing concepts: 58%
                                    | 15/26 [00:01<00:00, 11.07it/s]
                                     | 18/26 [00:01<00:00, 13.45it/s]
Computing concepts: 69%
Computing concepts: 85%
                                       22/26 [00:01<00:00, 16.55it/s]
Evaluating Φ cuts: 57%
                                  | 17/30 [00:29<00:18, 1.44s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 8%
                               2/26 [00:00<00:02, 11.21it/s]
```

```
Computing concepts: 12%
                                 3/26 [00:00<00:02, 10.09it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:08, 2.45it/s]
                                 | 5/26 [00:01<00:08, 2.35it/s]
Computing concepts: 19%
Computing concepts: 27%
                                  | 7/26 [00:02<00:07, 2.55it/s]
Computing concepts: 46%
                                    | 12/26 [00:02<00:03, 3.54it/s]
Computing concepts: 54%
                                    | 14/26 [00:02<00:02, 4.56it/s]
Computing concepts: 62%
                                     | 16/26 [00:03<00:01, 5.17it/s]
Computing concepts: 73%
                                      19/26 [00:03<00:01, 5.25it/s]
Computing concepts: 77%
                                     20/26 [00:04<00:01, 3.74it/s]
Computing concepts: 88%
                                     | | 23/26 [00:04<00:00, 4.74it/s]
Evaluating Φ cuts: 60%
                                  | 18/30 [00:33<00:28, 2.33s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
                                  | 8/26 [00:00<00:01, 15.51it/s]
Computing concepts: 31%
Computing concepts: 69%
                                     | 18/26 [00:00<00:00, 20.58it/s]
Computing concepts: 88%
                                     | 23/26 [00:00<00:00, 22.14it/s]
Evaluating Φ cuts: 63%
                                  | 19/30 [00:34<00:20, 1.91s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 8%
                               2/26 [00:01<00:12, 1.97it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:07, 2.69it/s]
Computing concepts: 38%
                                  | 10/26 [00:01<00:04, 3.66it/s]
Computing concepts: 46%
                                    | 12/26 [00:01<00:02, 4.80it/s]
Computing concepts: 54%
                                    | 14/26 [00:01<00:02, 4.75it/s]
Computing concepts: 62%
                                     | 16/26 [00:02<00:01, 5.32it/s]
Computing concepts: 73%
                                      | 19/26 [00:02<00:01, 5.35it/s]
Computing concepts: 77%
                                     20/26 [00:03<00:01, 3.98it/s]
Computing concepts: 92%
                                       | 24/26 [00:03<00:00, 5.11it/s]
Evaluating Φ cuts: 67%
                                  | 20/30 [00:37<00:23, 2.38s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 4%
                               | 1/26 [00:00<00:05, 4.85it/s]
Computing concepts: 12%
                                 | 3/26 [00:00<00:06, 3.81it/s]
Computing concepts: 27%
                                 | 7/26 [00:01<00:03, 5.14it/s]
Computing concepts: 35%
                                  9/26 [00:01<00:02, 6.10it/s]
Computing concepts: 42%
                                   | 11/26 [00:01<00:02, 6.25it/s]
Computing concepts: 54%
                                    | 14/26 [00:02<00:02, 5.87it/s]
Computing concepts: 62%
                                     | 16/26 [00:02<00:01, 6.69it/s]
Computing concepts: 77%
                                     | 20/26 [00:02<00:00, 7.43it/s]
                                      | 21/26 [00:03<00:01, 4.24it/s]
Computing concepts: 81%
Computing concepts: 96%
                                        | | 25/26 [00:03<00:00, 5.42it/s]
Evaluating Φ cuts: 70%
                                  | 21/30 [00:41<00:24, 2.75s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
```

```
| 3/26 [00:00<00:00, 25.89it/s]
Computing concepts: 12%
Computing concepts: 15%
                                 | 4/26 [00:00<00:05, 3.80it/s]
                                 | 5/26 [00:01<00:05, 3.94it/s]
Computing concepts: 19%
Computing concepts: 23%
                                 | 6/26 [00:01<00:05, 3.53it/s]
Computing concepts: 42%
                                   | 11/26 [00:01<00:03, 4.75it/s]
Computing concepts: 50%
                                    | 13/26 [00:01<00:02, 5.90it/s]
Computing concepts: 58%
                                    | 15/26 [00:02<00:01, 6.11it/s]
Computing concepts: 73%
                                      19/26 [00:02<00:01, 6.85it/s]
                                    | 20/26 [00:02<00:01, 4.40it/s]
Computing concepts: 77%
Computing concepts: 88%
                                      | 23/26 [00:03<00:00, 5.63it/s]
Computing concepts: 96%
                                       | 25/26 [00:03<00:00, 6.58it/s]
Evaluating Φ cuts: 73%
                                   22/30 [00:44<00:23, 2.94s/it]
Computing concepts: 0%
                               0/20 [00:00<?, ?it/s]
Computing concepts: 60%
                                    | 12/20 [00:00<00:00, 119.71it/s]
Evaluating Φ cuts: 77%
                                   23/30 [00:45<00:14, 2.11s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 12%
                                 | 3/26 [00:00<00:01, 14.96it/s]
Computing concepts: 31%
                                  | 8/26 [00:00<00:00, 18.61it/s]
Computing concepts: 54%
                                    | 14/26 [00:00<00:00, 23.28it/s]
                                     | 17/26 [00:00<00:00, 24.02it/s]
Computing concepts: 65%
Computing concepts: 77%
                                    20/26 [00:00<00:00, 23.65it/s]
Computing concepts: 92%
                                      | 24/26 [00:00<00:00, 26.94it/s]
Evaluating Φ cuts: 80%
                                   | 24/30 [00:45<00:10, 1.74s/it]
Computing concepts: 0%
                               0/26 [00:00<?, ?it/s]
                                  | 9/26 [00:00<00:00, 38.84it/s]
Computing concepts: 35%
Computing concepts: 58%
                                    | 15/26 [00:00<00:00, 23.65it/s]
Computing concepts: 96%
                                      | 25/26 [00:00<00:00, 30.24it/s]
Evaluating Φ cuts: 83%
                                   25/30 [00:46<00:07, 1.48s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 8%
                               2/26 [00:00<00:02, 8.63it/s]
                                 | 3/26 [00:00<00:07, 3.25it/s]
Computing concepts: 12%
                                 | 4/26 [00:01<00:05, 3.72it/s]
Computing concepts: 15%
Computing concepts: 27%
                                 | 7/26 [00:01<00:04, 4.38it/s]
Computing concepts: 50%
                                    | 13/26 [00:01<00:02, 5.54it/s]
Computing concepts: 54%
                                    | 14/26 [00:02<00:02, 5.17it/s]
Computing concepts: 62%
                                     | 16/26 [00:02<00:01, 6.65it/s]
                                     | 18/26 [00:02<00:01, 7.58it/s]
Computing concepts: 69%
Computing concepts: 81%
                                      | 21/26 [00:02<00:00, 7.26it/s]
Computing concepts: 85%
                                      22/26 [00:03<00:00, 5.36it/s]
                                   | 26/30 [00:50<00:08, 2.03s/it]
Evaluating Φ cuts: 87%
```



Variación en el tiempo y consumo en las diferentes particiones sin CM

```
Evaluating Φ cuts: 0%
                            1 0/30 [00:00<?, ?it/s]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 5%
                                | 1/20 [00:00<00:04, 4.16it/s]
                                | 2/20 [00:00<00:03, 4.65it/s]
Computing concepts: 10%
Computing concepts: 15%
                                 | 3/20 [00:00<00:03, 4.64it/s]
Computing concepts: 20%
                                 | 4/20 [00:00<00:02, 5.51it/s]
Computing concepts: 30%
                                  | 6/20 [00:00<00:02, 6.57it/s]
Computing concepts: 50%
                                    | 10/20 [00:01<00:01, 8.60it/s]
                                     | 12/20 [00:01<00:00, 8.85it/s]
Computing concepts: 60%
Computing concepts: 70%
                                     | 14/20 [00:01<00:00, 9.46it/s]
                                      | 16/20 [00:01<00:00, 11.18it/s]
Computing concepts: 80%
Computing concepts: 90%
                                       | 18/20 [00:01<00:00, 10.84it/s]
Evaluating Φ cuts: 3%
                             | 1/30 [00:01<00:52, 1.81s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
                                | 2/20 [00:00<00:01, 10.90it/s]
Computing concepts: 10%
Computing concepts: 15%
                                 | 3/20 [00:00<00:01, 10.26it/s]
Computing concepts: 20%
                                 | 4/20 [00:00<00:02, 6.66it/s]
                                  | 6/20 [00:00<00:01, 8.26it/s]
Computing concepts: 30%
Computing concepts: 35%
                                   | 7/20 [00:00<00:01, 7.76it/s]
Computing concepts: 50%
                                    | 10/20 [00:00<00:01, 9.52it/s]
Computing concepts: 60%
                                     | 12/20 [00:01<00:00, 10.93it/s]
                                     | 14/20 [00:01<00:00, 11.61it/s]
Computing concepts: 70%
Computing concepts: 80%
                                      | 16/20 [00:01<00:00, 12.64it/s]
Computing concepts: 90%
                                       | 18/20 [00:01<00:00, 13.41it/s]
Evaluating Φ cuts: 7%
                             2/30 [00:03<00:48, 1.75s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts: 8%
                               2/26 [00:00<00:01, 14.87it/s]
```

```
Computing concepts: 15%
                                 | 4/26 [00:00<00:02, 10.86it/s]
                                  | 6/26 [00:00<00:01, 12.51it/s]
Computing concepts: 23%
Computing concepts: 31%
                                  | 8/26 [00:00<00:01, 12.73it/s]
Computing concepts: 50%
                                    | 13/26 [00:00<00:00, 15.89it/s]
Computing concepts: 58%
                                    | 15/26 [00:00<00:00, 14.45it/s]
Computing concepts: 65%
                                      | 17/26 [00:01<00:00, 14.68it/s]
Computing concepts: 73%
                                      | 19/26 [00:01<00:00, 15.94it/s]
Computing concepts: 81%
                                      | 21/26 [00:01<00:00, 15.12it/s]
Computing concepts: 88%
                                       | 23/26 [00:01<00:00, 14.98it/s]
                                         26/26 [00:01<00:00, 17.15it/s]
Computing concepts: 100%
Evaluating Φ cuts: 10%
                              | 3/30 [00:05<00:46, 1.72s/it]
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts: 10%
                                | 2/20 [00:00<00:01, 14.33it/s]
                                 | 3/20 [00:00<00:02, 7.59it/s]
Computing concepts: 15%
Computing concepts: 30%
                                  | 6/20 [00:00<00:01, 8.20it/s]
Computing concepts: 40%
                                   | 8/20 [00:00<00:01, 9.49it/s]
Computing concepts: 45%
                                    9/20 [00:00<00:01, 8.60it/s]
Computing concepts: 55%
                                     | 11/20 [00:01<00:01, 8.63it/s]
                                      | 13/20 [00:01<00:00, 9.82it/s]
Computing concepts: 65%
Computing concepts: 75%
                                      | 15/20 [00:01<00:00, 10.63it/s]
Computing concepts: 85%
                                      | 17/20 [00:01<00:00, 11.46it/s]
Computing concepts: 100%
                                         | 20/20 [00:01<00:00, 13.37it/s]
Evaluating Φ cuts: 13%
                              4/30 [00:06<00:45, 1.75s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
                               | 1/26 [00:00<00:06, 3.69it/s]
Computing concepts: 4%
Computing concepts: 12%
                                 | 3/26 [00:01<00:08, 2.86it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:05, 3.77it/s]
Computing concepts: 27%
                                  | 7/26 [00:01<00:04, 4.69it/s]
                                   | 9/26 [00:01<00:03, 5.39it/s]
Computing concepts: 35%
Computing concepts: 46%
                                    | 12/26 [00:02<00:02, 6.15it/s]
Computing concepts: 50%
                                    | 13/26 [00:02<00:03, 3.88it/s]
                                    | 14/26 [00:02<00:02, 4.68it/s]
Computing concepts: 54%
Computing concepts: 58%
                                    | 15/26 [00:03<00:03, 3.48it/s]
Computing concepts: 65%
                                      | 17/26 [00:03<00:02, 4.47it/s]
Computing concepts: 77%
                                    | 20/26 [00:03<00:01, 6.00it/s]
Computing concepts: 85%
                                      | 22/26 [00:04<00:00, 4.68it/s]
                                         26/26 [00:04<00:00, 6.19it/s]
Computing concepts: 100%
Evaluating Φ cuts: 17%
                              | 5/30 [00:11<01:03, 2.53s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
                               2/26 [00:00<00:01, 15.17it/s]
Computing concepts: 8%
                                 | 4/26 [00:00<00:01, 16.14it/s]
Computing concepts: 15%
```

```
Computing concepts: 19%
                                 | 5/26 [00:00<00:02, 8.55it/s]
Computing concepts: 27%
                                 | 7/26 [00:00<00:01, 9.76it/s]
Computing concepts: 42%
                                   | 11/26 [00:00<00:01, 11.82it/s]
Computing concepts: 50%
                                    | 13/26 [00:00<00:01, 11.50it/s]
Computing concepts: 58%
                                    | 15/26 [00:01<00:01, 10.87it/s]
Computing concepts: 65%
                                     | 17/26 [00:01<00:00, 12.04it/s]
Computing concepts: 77%
                                    | 20/26 [00:01<00:00, 13.32it/s]
Computing concepts: 85%
                                      | 22/26 [00:01<00:00, 13.84it/s]
Computing concepts: 96%
                                       | 25/26 [00:01<00:00, 15.87it/s]
Evaluating Φ cuts: 20%
                               6/30 [00:13<00:55, 2.32s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 8%
                               2/26 [00:00<00:01, 15.62it/s]
                                 3/26 [00:00<00:04, 4.93it/s]
Computing concepts: 12%
                                 | 5/26 [00:00<00:03, 6.27it/s]
Computing concepts: 19%
Computing concepts: 31%
                                  | 8/26 [00:01<00:02, 7.06it/s]
Computing concepts: 42%
                                   11/26 [00:01<00:01, 7.84it/s]
Computing concepts: 46%
                                    | 12/26 [00:01<00:03, 4.09it/s]
                                    | 14/26 [00:01<00:02, 5.29it/s]
Computing concepts: 54%
Computing concepts: 58%
                                    | 15/26 [00:02<00:02, 4.72it/s]
Computing concepts: 65%
                                     | 17/26 [00:02<00:01, 6.13it/s]
Computing concepts: 77%
                                     20/26 [00:02<00:00, 7.84it/s]
Computing concepts: 85%
                                      | 22/26 [00:02<00:00, 6.10it/s]
                                       | 25/26 [00:03<00:00, 7.96it/s]
Computing concepts: 96%
Evaluating Φ cuts: 23%
                               7/30 [00:16<00:59, 2.58s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 10%
                                | 2/20 [00:00<00:01, 15.15it/s]
Computing concepts: 15%
                                 | 3/20 [00:00<00:02, 8.13it/s]
                                  | 5/20 [00:00<00:01, 8.64it/s]
Computing concepts: 25%
Computing concepts: 35%
                                   | 7/20 [00:00<00:01, 10.41it/s]
Computing concepts: 45%
                                    9/20 [00:00<00:00, 11.50it/s]
Computing concepts: 55%
                                    | 11/20 [00:01<00:00, 10.72it/s]
                                     | 14/20 [00:01<00:00, 12.40it/s]
Computing concepts: 70%
                                      | 16/20 [00:01<00:00, 12.74it/s]
Computing concepts: 80%
Computing concepts: 90%
                                       | 18/20 [00:01<00:00, 13.73it/s]
Computing concepts: 100%
                                         20/20 [00:01<00:00, 13.61it/s]
Evaluating Φ cuts: 27%
                               8/30 [00:17<00:50, 2.30s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 8%
                               2/26 [00:00<00:01, 14.49it/s]
Computing concepts: 12%
                                 | 3/26 [00:00<00:02, 8.15it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:08, 2.69it/s]
Computing concepts: 23%
                                 | 6/26 [00:01<00:06, 2.98it/s]
```

```
Computing concepts: 31%
                                  | 8/26 [00:02<00:04, 3.60it/s]
Computing concepts: 42%
                                   11/26 [00:02<00:03, 4.76it/s]
Computing concepts: 46%
                                    | 12/26 [00:02<00:04, 3.45it/s]
                                    | 14/26 [00:03<00:03, 3.47it/s]
Computing concepts: 54%
Computing concepts: 69%
                                     | 18/26 [00:03<00:01, 4.43it/s]
Computing concepts: 73%
                                      | 19/26 [00:03<00:01, 5.03it/s]
Computing concepts: 77%
                                      | 20/26 [00:03<00:01, 5.80it/s]
Computing concepts: 92%
                                        | 24/26 [00:04<00:00, 7.39it/s]
Evaluating Φ cuts: 30%
                               9/30 [00:22<01:00, 2.88s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
                               2/26 [00:00<00:04, 5.46it/s]
Computing concepts: 8%
Computing concepts: 12%
                                 | 3/26 [00:01<00:10, 2.26it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:06, 3.03it/s]
Computing concepts: 27%
                                  | 7/26 [00:02<00:05, 3.23it/s]
Computing concepts: 38%
                                  | 10/26 [00:02<00:03, 4.38it/s]
Computing concepts: 46%
                                    | 12/26 [00:02<00:03, 4.12it/s]
Computing concepts: 50%
                                    | 13/26 [00:03<00:03, 4.00it/s]
Computing concepts: 54%
                                    14/26 [00:03<00:02, 4.65it/s]
Computing concepts: 62%
                                     | 16/26 [00:03<00:01, 5.79it/s]
Computing concepts: 73%
                                      | 19/26 [00:03<00:00, 7.34it/s]
Computing concepts: 81%
                                      | 21/26 [00:04<00:01, 4.47it/s]
Computing concepts: 92%
                                       24/26 [00:04<00:00, 5.35it/s]
Computing concepts: 96%
                                        | 25/26 [00:04<00:00, 5.57it/s]
Evaluating Φ cuts: 33%
                                | 10/30 [00:26<01:09, 3.47s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 8%
                               2/26 [00:00<00:11, 2.06it/s]
Computing concepts: 15%
                                 4/26 [00:01<00:07, 2.82it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:08, 2.54it/s]
Computing concepts: 27%
                                 | 7/26 [00:01<00:05, 3.20it/s]
                                   | 11/26 [00:02<00:03, 3.90it/s]
Computing concepts: 42%
Computing concepts: 50%
                                    | 13/26 [00:02<00:02, 4.50it/s]
Computing concepts: 54%
                                    | 14/26 [00:02<00:03, 3.63it/s]
Computing concepts: 62%
                                     | 16/26 [00:03<00:02, 4.68it/s]
Computing concepts: 69%
                                     | 18/26 [00:03<00:01, 5.36it/s]
Computing concepts: 73%
                                      | 19/26 [00:03<00:01, 4.06it/s]
Computing concepts: 77%
                                      | 20/26 [00:03<00:01, 4.83it/s]
                                      | 23/26 [00:04<00:00, 5.87it/s]
Computing concepts: 88%
Computing concepts: 92%
                                        24/26 [00:04<00:00, 6.70it/s]
Evaluating Φ cuts: 37%
                                | 11/30 [00:31<01:10, 3.73s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
```

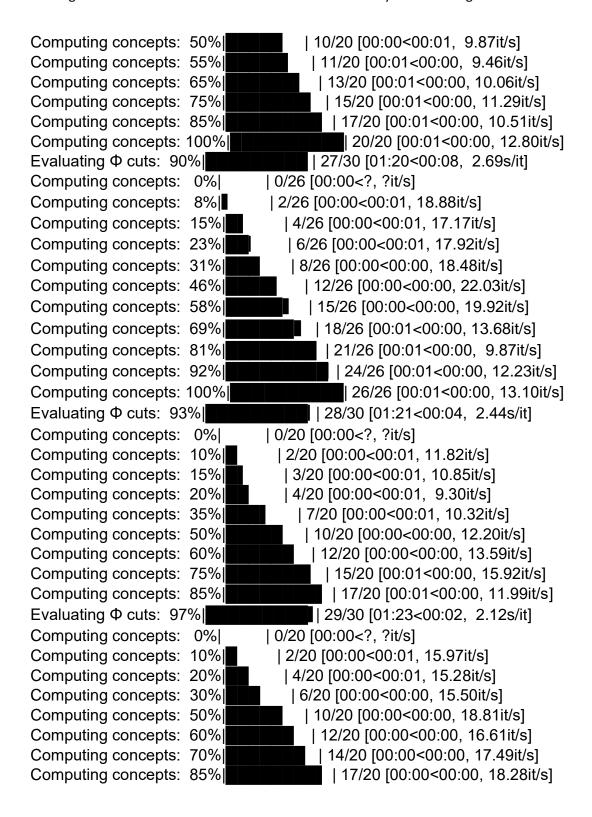
```
Computing concepts: 8%
                               2/26 [00:00<00:01, 17.28it/s]
Computing concepts: 15%
                                 | 4/26 [00:00<00:01, 17.28it/s]
                                 | 5/26 [00:00<00:02, 8.72it/s]
Computing concepts: 19%
Computing concepts: 27%
                                 | 7/26 [00:00<00:01, 10.50it/s]
Computing concepts: 35%
                                  9/26 [00:00<00:01, 11.58it/s]
Computing concepts: 46%
                                    | 12/26 [00:00<00:01, 13.36it/s]
Computing concepts: 54%
                                    | 14/26 [00:01<00:00, 12.25it/s]
Computing concepts: 62%
                                     | 16/26 [00:01<00:00, 11.59it/s]
Computing concepts: 73%
                                     | 19/26 [00:01<00:00, 11.79it/s]
Computing concepts: 88%
                                     23/26 [00:01<00:00, 13.74it/s]
Computing concepts: 96%
                                       | 25/26 [00:01<00:00, 13.97it/s]
Evaluating Φ cuts: 40%
                                | 12/30 [00:33<00:57, 3.18s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 8%
                               2/26 [00:00<00:03, 6.65it/s]
Computing concepts: 12%
                                 | 3/26 [00:00<00:04, 5.58it/s]
Computing concepts: 15%
                                 4/26 [00:01<00:08, 2.53it/s]
Computing concepts: 23%
                                 | 6/26 [00:01<00:05, 3.40it/s]
Computing concepts: 27%
                                  | 7/26 [00:01<00:06, 3.03it/s]
Computing concepts: 42%
                                   11/26 [00:02<00:03, 3.96it/s]
                                    | 12/26 [00:02<00:04, 3.26it/s]
Computing concepts: 46%
Computing concepts: 54%
                                    | 14/26 [00:03<00:03, 3.24it/s]
Computing concepts: 58%
                                    | 15/26 [00:03<00:02, 3.90it/s]
                                     | 18/26 [00:03<00:01, 4.74it/s]
Computing concepts: 69%
Computing concepts: 73%
                                      | 19/26 [00:03<00:01, 5.29it/s]
Computing concepts: 77%
                                     20/26 [00:04<00:01, 3.54it/s]
Computing concepts: 88%
                                     | 23/26 [00:04<00:00, 4.71it/s]
Computing concepts: 96%
                                       | 25/26 [00:04<00:00, 5.82it/s]
Evaluating Φ cuts: 43%
                                 | 13/30 [00:38<01:02, 3.67s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 8%
                               2/26 [00:00<00:01, 13.84it/s]
                                 3/26 [00:00<00:03, 7.56it/s]
Computing concepts: 12%
Computing concepts: 15%
                                 | 4/26 [00:01<00:08, 2.61it/s]
Computing concepts: 23%
                                 | 6/26 [00:01<00:05, 3.47it/s]
Computing concepts: 27%
                                 | 7/26 [00:01<00:06, 3.02it/s]
Computing concepts: 35%
                                  | 9/26 [00:02<00:04, 4.05it/s]
Computing concepts: 46%
                                    | 12/26 [00:02<00:03, 4.44it/s]
Computing concepts: 54%
                                    | 14/26 [00:02<00:02, 5.43it/s]
Computing concepts: 58%
                                    | 15/26 [00:02<00:01, 6.11it/s]
Computing concepts: 73%
                                      | 19/26 [00:03<00:01, 6.35it/s]
Computing concepts: 77%
                                      20/26 [00:03<00:00, 6.65it/s]
```

```
Computing concepts: 88%
                                      | 23/26 [00:03<00:00, 7.76it/s]
Computing concepts: 96%
                                        | 25/26 [00:03<00:00, 9.10it/s]
Evaluating Φ cuts: 47%
                                 | 14/30 [00:42<01:00, 3.78s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 5%
                                | 1/20 [00:00<00:17, 1.11it/s]
                                 | 3/20 [00:01<00:11, 1.42it/s]
Computing concepts: 15%
Computing concepts: 35%
                                   | 7/20 [00:01<00:06. 1.96it/s]
                                    | 9/20 [00:02<00:04, 2.35it/s]
Computing concepts: 45%
Computing concepts: 60%
                                     | 12/20 [00:02<00:02, 3.09it/s]
                                      | 13/20 [00:02<00:02, 2.88it/s]
Computing concepts: 65%
Computing concepts: 70%
                                     | 14/20 [00:03<00:02, 2.78it/s]
Computing concepts: 85%
                                      | 17/20 [00:03<00:00, 3.67it/s]
Computing concepts: 95%
                                        | 19/20 [00:03<00:00, 4.84it/s]
Evaluating Φ cuts: 50%
                                 | 15/30 [00:45<00:55, 3.71s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
Computing concepts: 5%
                                | 1/20 [00:00<00:04, 3.95it/s]
Computing concepts: 10%
                                | 2/20 [00:00<00:03, 4.82it/s]
Computing concepts: 15%
                                 | 3/20 [00:00<00:03, 5.42it/s]
                                   | 7/20 [00:00<00:01, 7.10it/s]
Computing concepts: 35%
Computing concepts: 45%
                                    | 9/20 [00:00<00:01, 7.69it/s]
Computing concepts: 55%
                                     | 11/20 [00:00<00:00, 9.37it/s]
Computing concepts: 65%
                                      | 13/20 [00:01<00:00, 9.13it/s]
Computing concepts: 75%
                                      | 15/20 [00:01<00:00, 9.80it/s]
Computing concepts: 85%
                                      | 17/20 [00:01<00:00, 11.57it/s]
Computing concepts: 95%
                                        | 19/20 [00:01<00:00, 11.65it/s]
Evaluating Φ cuts: 53%
                                  | 16/30 [00:47<00:43, 3.12s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 8%
                               2/26 [00:00<00:01, 15.24it/s]
Computing concepts: 15%
                                 | 4/26 [00:00<00:01, 11.59it/s]
Computing concepts: 23%
                                  | 6/26 [00:00<00:01, 12.48it/s]
Computing concepts: 27%
                                  | 7/26 [00:00<00:01, 11.01it/s]
Computing concepts: 42%
                                    | 11/26 [00:00<00:01, 13.32it/s]
Computing concepts: 50%
                                    | 13/26 [00:00<00:00, 13.41it/s]
                                    | 15/26 [00:01<00:00, 13.20it/s]
Computing concepts: 58%
Computing concepts: 73%
                                      | 19/26 [00:01<00:00, 15.11it/s]
Computing concepts: 81%
                                      | 21/26 [00:01<00:00, 16.00it/s]
Computing concepts: 92%
                                       24/26 [00:01<00:00, 18.12it/s]
Evaluating Φ cuts: 57%
                                  | 17/30 [00:48<00:34, 2.66s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 8%
                               2/26 [00:00<00:01, 14.11it/s]
Computing concepts: 12%
                                 3/26 [00:00<00:01, 12.20it/s]
Computing concepts: 15%
                                 | 4/26 [00:01<00:06, 3.21it/s]
```

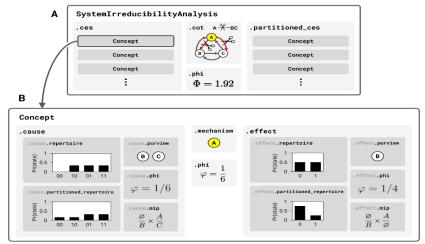
```
Computing concepts: 19%
                                 | 5/26 [00:01<00:06, 3.41it/s]
Computing concepts: 27%
                                 | 7/26 [00:01<00:05, 3.57it/s]
                                   | 11/26 [00:01<00:03, 4.85it/s]
Computing concepts: 42%
Computing concepts: 50%
                                    | 13/26 [00:02<00:02, 5.73it/s]
Computing concepts: 58%
                                    | 15/26 [00:02<00:01, 5.66it/s]
                                     | 18/26 [00:02<00:01, 7.12it/s]
Computing concepts: 69%
Computing concepts: 77%
                                     20/26 [00:03<00:01, 4.43it/s]
                                      | 23/26 [00:03<00:00, 5.45it/s]
Computing concepts: 88%
                                        | 24/26 [00:03<00:00, 6.31it/s]
Computing concepts: 92%
                                         26/26 [00:04<00:00, 7.66it/s]
Computing concepts: 100%
Evaluating Φ cuts: 60%
                                  | 18/30 [00:53<00:37, 3.10s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 8%
                               2/26 [00:00<00:01, 14.48it/s]
Computing concepts: 15%
                                 | 4/26 [00:00<00:01, 15.71it/s]
Computing concepts: 19%
                                 | 5/26 [00:00<00:02, 7.69it/s]
Computing concepts: 31%
                                  | 8/26 [00:01<00:02, 6.93it/s]
Computing concepts: 46%
                                    | 12/26 [00:01<00:01, 9.21it/s]
Computing concepts: 54%
                                    | 14/26 [00:01<00:01, 10.40it/s]
Computing concepts: 62%
                                     | 16/26 [00:01<00:00, 10.57it/s]
                                      | 19/26 [00:01<00:00, 11.31it/s]
Computing concepts: 73%
Computing concepts: 81%
                                      | 21/26 [00:01<00:00, 9.65it/s]
Computing concepts: 88%
                                      | 23/26 [00:02<00:00, 9.44it/s]
                                        | 26/26 [00:02<00:00, 11.89it/s]
Computing concepts: 100%
Evaluating Φ cuts: 63%
                                  19/30 [00:55<00:31, 2.87s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
                               | 2/26 [00:00<00:11, 2.01it/s]
Computing concepts: 8%
Computing concepts: 15%
                                 | 4/26 [00:01<00:08, 2.71it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:06, 3.31it/s]
Computing concepts: 35%
                                  9/26 [00:01<00:03, 4.56it/s]
Computing concepts: 42%
                                   11/26 [00:01<00:03, 4.98it/s]
Computing concepts: 50%
                                    | 13/26 [00:01<00:02, 6.02it/s]
Computing concepts: 58%
                                    | 15/26 [00:02<00:02, 5.48it/s]
Computing concepts: 62%
                                     | 16/26 [00:02<00:02, 4.91it/s]
Computing concepts: 69%
                                     | 18/26 [00:02<00:01, 6.31it/s]
Computing concepts: 77%
                                     20/26 [00:03<00:01, 4.06it/s]
                                      | 23/26 [00:03<00:00, 5.44it/s]
Computing concepts: 88%
Computing concepts: 96%
                                       | 25/26 [00:04<00:00, 5.68it/s]
Evaluating Φ cuts: 67%
                                  20/30 [00:59<00:32, 3.24s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
                               | 1/26 [00:00<00:06, 3.89it/s]
Computing concepts: 4%
```

```
Computing concepts: 12%
                                 | 3/26 [00:01<00:07, 3.17it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:05, 4.17it/s]
Computing concepts: 27%
                                 | 7/26 [00:01<00:03, 5.14it/s]
Computing concepts: 35%
                                  9/26 [00:01<00:02, 5.78it/s]
Computing concepts: 42%
                                   11/26 [00:02<00:02, 5.41it/s]
Computing concepts: 50%
                                    | 13/26 [00:02<00:01, 6.88it/s]
Computing concepts: 58%
                                    | 15/26 [00:02<00:01, 5.68it/s]
                                     | 16/26 [00:02<00:01, 5.46it/s]
Computing concepts: 62%
Computing concepts: 73%
                                     | 19/26 [00:03<00:00, 7.23it/s]
                                      | 21/26 [00:03<00:01, 4.60it/s]
Computing concepts: 81%
Computing concepts: 96%
                                       | 25/26 [00:04<00:00, 5.77it/s]
Evaluating Φ cuts: 70%
                                  21/30 [01:03<00:31, 3.53s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 8%
                               2/26 [00:00<00:01, 13.39it/s]
Computing concepts: 15%
                                 | 4/26 [00:00<00:03, 5.57it/s]
Computing concepts: 19%
                                 | 5/26 [00:01<00:04, 5.12it/s]
Computing concepts: 23%
                                 | 6/26 [00:01<00:05, 3.89it/s]
Computing concepts: 38%
                                  | 10/26 [00:01<00:03, 5.33it/s]
                                    | 12/26 [00:02<00:02, 5.50it/s]
Computing concepts: 46%
Computing concepts: 54%
                                    | 14/26 [00:02<00:02, 5.08it/s]
Computing concepts: 69%
                                     | 18/26 [00:02<00:01, 6.70it/s]
Computing concepts: 77%
                                    | 20/26 [00:03<00:01, 4.36it/s]
                                     1 23/26 [00:03<00:00, 5.44it/s]
Computing concepts: 88%
Computing concepts: 96%
                                        | 25/26 [00:04<00:00, 5.83it/s]
Evaluating Φ cuts: 73%
                                   22/30 [01:07<00:29, 3.70s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
                                | 2/20 [00:00<00:01, 17.26it/s]
Computing concepts: 10%
Computing concepts: 15%
                                 | 3/20 [00:00<00:03, 5.66it/s]
Computing concepts: 25%
                                  | 5/20 [00:00<00:02, 6.15it/s]
                                   | 7/20 [00:01<00:01, 6.92it/s]
Computing concepts: 35%
Computing concepts: 45%
                                    9/20 [00:01<00:01, 6.07it/s]
                                    | 11/20 [00:01<00:01, 6.24it/s]
Computing concepts: 55%
Computing concepts: 75%
                                      | 15/20 [00:02<00:00, 7.42it/s]
                                       | 18/20 [00:02<00:00, 9.30it/s]
Computing concepts: 90%
                                         | 20/20 [00:02<00:00, 10.00it/s]
Computing concepts: 100%
Evaluating Φ cuts: 77%
                                  | 23/30 [01:10<00:23, 3.31s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 8%
                               2/26 [00:00<00:01, 18.82it/s]
Computing concepts: 12%
                                 | 3/26 [00:00<00:02, 9.81it/s]
Computing concepts: 19%
                                 | 5/26 [00:00<00:01, 11.27it/s]
```

```
Computing concepts: 23%
                                  | 6/26 [00:00<00:01, 10.05it/s]
Computing concepts: 38%
                                   | 10/26 [00:00<00:01, 12.79it/s]
Computing concepts: 46%
                                    | 12/26 [00:00<00:01, 12.27it/s]
Computing concepts: 54%
                                    | 14/26 [00:00<00:00, 13.44it/s]
Computing concepts: 62%
                                     | 16/26 [00:01<00:00, 12.52it/s]
                                     | 18/26 [00:01<00:00, 14.09it/s]
Computing concepts: 69%
Computing concepts: 77%
                                    | 20/26 [00:01<00:00, 12.10it/s]
Computing concepts: 85%
                                      | | 22/26 [00:01<00:00, 12.74it/s]
Computing concepts: 96%
                                       | 25/26 [00:01<00:00, 13.68it/s]
Evaluating Φ cuts: 80%
                                   | 24/30 [01:12<00:17, 2.89s/it]
Computing concepts: 0%
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 8%
                               2/26 [00:00<00:01, 18.87it/s]
                                 | 4/26 [00:00<00:01, 15.10it/s]
Computing concepts: 15%
Computing concepts: 19%
                                 | 5/26 [00:00<00:01, 10.84it/s]
Computing concepts: 27%
                                  | 7/26 [00:00<00:01, 10.21it/s]
Computing concepts: 35%
                                  9/26 [00:00<00:01, 9.76it/s]
Computing concepts: 46%
                                    | 12/26 [00:01<00:01, 10.66it/s]
Computing concepts: 58%
                                    | 15/26 [00:01<00:01, 8.54it/s]
                                    | 18/26 [00:01<00:00, 10.72it/s]
Computing concepts: 69%
Computing concepts: 81%
                                      | 21/26 [00:01<00:00, 12.98it/s]
Computing concepts: 96%
                                       | 25/26 [00:02<00:00, 15.30it/s]
Evaluating Φ cuts: 83%
                                   25/30 [01:14<00:13, 2.65s/it]
                               | 0/26 [00:00<?, ?it/s]
Computing concepts: 0%
Computing concepts: 8%
                               2/26 [00:00<00:03, 6.67it/s]
                                 3/26 [00:01<00:07, 2.90it/s]
Computing concepts: 12%
Computing concepts: 15%
                                 | 4/26 [00:01<00:07, 3.01it/s]
Computing concepts: 27%
                                  | 7/26 [00:01<00:05, 3.55it/s]
Computing concepts: 42%
                                    | 11/26 [00:02<00:03, 4.87it/s]
Computing concepts: 50%
                                    | 13/26 [00:02<00:02, 4.75it/s]
Computing concepts: 58%
                                    | 15/26 [00:02<00:02, 4.99it/s]
Computing concepts: 65%
                                      | 17/26 [00:03<00:01, 5.49it/s]
Computing concepts: 77%
                                     | 20/26 [00:03<00:00, 7.08it/s]
Computing concepts: 85%
                                      | 22/26 [00:04<00:00, 4.57it/s]
Computing concepts: 96%
                                        | 25/26 [00:04<00:00, 6.12it/s]
Evaluating Φ cuts: 87%
                                   | 26/30 [01:18<00:12, 3.12s/it]
Computing concepts: 0%
                               | 0/20 [00:00<?, ?it/s]
                                | 2/20 [00:00<00:00, 19.95it/s]
Computing concepts: 10%
Computing concepts: 15%
                                 | 3/20 [00:00<00:01, 9.15it/s]
                                  | 6/20 [00:00<00:01, 10.71it/s]
Computing concepts: 30%
                                    9/20 [00:00<00:01, 10.70it/s]
Computing concepts: 45%
```



### **Datos adicionales**



### Nota:

Para evitar construir TPM y matrices de conectividad a mano, puede utilizar la interfaz gráfica de usuario para PyPhi disponible en línea en

http://integratedinformationtheory.org/calculate.html. Usted puede construir las redes que se muestran en las figuras y luego usar el botón Exportar para obtener un archivo JSON que represente la red. Luego puede importar el archivo a Python así:

network = pyphi.network.from\_json('path/to/network.json')