
Algorithm 7 Symbolic Full-Pivoting Strategy.

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1: Require: A  $m \times n$  matrix A.
2:   The  $k$ -th pivoting stage.
3: procedure SYMBOLICPIVOTING(A,  $k$ )                                ▷ Symbolic pivoting procedure for the  $k$ -th pivot
4:    $d^r, d^c \leftarrow \text{ComputeDegrees}(\mathbf{A})$                         ▷ Calculate the row and column degrees of A
5:   for  $i$  from  $k$  to  $m$  do                                          ▷ Iterate over the rows
6:     for  $j$  from  $k$  to  $n$  do                                          ▷ Iterate over the columns
7:        $D_{ij} \leftarrow \infty$                                           ▷ Set the combined degree matrix to infinity
8:       if  $A_{ij} \neq 0$  then  $D_{ij} \leftarrow d_i^r \max(0, d_j^c - 1) + d_j^c \max(0, d_i^r - 1)$   ▷ The combined degree
9:     end for
10:  end for
11:   $\mathcal{P} \leftarrow \text{Sort}(\mathbf{D})$                                           ▷ Find the permutation that sorts the pivots list by degree cost
12:   $q, l \leftarrow 0, 0$                                           ▷ Initialize the temporary pivot row and column indices
13:   $p, p_c, p_n \leftarrow \infty, \infty, \infty$   ▷ Initialize the temporary pivot value, complexity and numerical value
14:  for all  $(i, j)$  in  $\mathcal{P}$  do                                          ▷ Iterate on the permutation set
15:    if  $p_c \neq \infty$  and  $D_{ij} > D_{ql}$  then break                    ▷ No more good pivots to check
16:     $t \leftarrow A_{ij}$                                           ▷ Get the pivot value
17:    if  $\text{Signature}(t) = 0$  then continue                            ▷ Skip the next pivot
18:     $t \leftarrow \text{Simplify}(t)$                                           ▷ Try to simplify the pivot expression
19:     $t_c \leftarrow \text{ExpressionComplexity}(t)$                         ▷ Calculate the computational cost of the pivot
20:     $t_n \leftarrow \infty$                                           ▷ Set the default numerical value of the pivot to infinity
21:    if  $t$  is numeric then  $t_n \leftarrow \max(1, \text{abs}(t))$           ▷ Set the numerical value of the pivot
22:    if  $t_c < p_c$  or  $(t_c = p_c \text{ and } t_n > p_n)$  then          ▷ If the pivot is better than the current one
23:       $q, l \leftarrow i, j$                                           ▷ Update the best pivot row and column indices
24:       $p, p_c, p_n \leftarrow t, t_c, t_n$                         ▷ Update the best pivot value, complexity and numerical value
25:    end if
26:  end for
27: return  $p, q, l$                                           ▷ The  $k$ -th pivot and its position
28: end procedure
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