Appendix Team 3 Quantum_Computing

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This R Markdown file will be provided as appendix to the final report of Team 3. Referring this appendix will follow the format of (Appendix I-"outline item of Markdown file"). For example, referring the code of Hypothesis 2 will display as following in the report: (Appendix I-1.2). Please use a browser to interpret the html file.

0. Install & import packages

Install

1. Data collection & cleaning

Data set is given and contains patents regarding quantum computing.

1.1 Import data

df_qc <- read.csv("Quantum_computing.csv", sep=";")

1.2 Clean Data

```
# Drop Rows where Inventors, Applicants or IPC classes or empty or NA
 df_qc \leftarrow df_qc[!(is.na(df_qc\$IPC) \mid df_qc\$IPC=""),]
 df_qc \leftarrow df_qc[!(is.na(df_qc*Inventors) \mid df_qc*Inventors=""),]
 df_qc <- df_qc[!(is.na(df_qc$Applicants) | df_qc$Applicants=""), ]
 \# df\_qc gets transformed where each row represents an inventor
 df_qc <- df_qc %%
        mutate(Inventors=strsplit(Inventors, "\n")) %%
         unnest (Inventors)
  \# \ Clean \ Inventors \& \ Applicants: \ Needed \ to \ adapt \ the \ igraph \ object \ cleaning \ df_qc\$Inventors & \ gsub("_", "_", df_qc\$Inventors) \ df_qc\$Inventors & \ gsub("_", "...", df_qc\$Inventors) \ df_qc\$Inventors & \ chartr("[]]", "...", df_qc\$Inventors) \ df_qc\$Inventors & \ chartr("<>", "...", df_qc\$Inventors) \ df_qc\$Applicants & \ gsub("_", "_", df_qc\$Applicants) \ df_qc\$Applicants & \ sub("_$", "", df_qc\$Applicants) \ df_qc\$Applicants & \ gsub("-", "...", df_qc\$Applicants) \ df_qc\$Applicants & \ chartr("[]]", "...", df_qc\$Applicants) \ df_qc\$Applicants & \ chartr("[]]", "...", df_qc\$Applicants) \ df_qc\$Applicants & \ chartr("[]]", "...", df_qc\$Applicants) \ df_qc\$Applicants & \ chartr("<="", "...", df_qc\$Applicants) \ df_qc\$Applicants & \ chartr("<=", "...", df_qc\$Applicants) \ df_qc\$Applicants & \ chartr("<="", "...", df_qc\$Applicants) 
 # Replace _ if its last character
 df_qcInventors \leftarrow sub("_$", "", df_qcInventors)
 \# df qc gets transformed where each row represents an applicant in connection
               with each inventor
 df_applicants_qc <- df_qc %>%
        mutate(Applicants=strsplit(Applicants, "\n")) %%
         unnest (Applicants)
```

2. Create necessary objects

2.1 Create the edge list

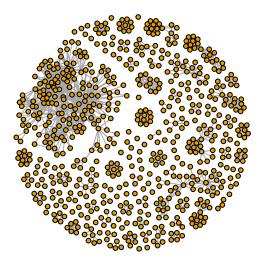
```
#rename to columns
names(edge_list)[names(edge_list) == "Inventors.x"] <- "from"
names(edge_list)[names(edge_list) == "Inventors.y"] <- "to"
# Selecting of applicant type is based on the majority of type occurrences
identify_applicant_type <- function(x){</pre>
  industrial <- "_INC_ | INC_ | LLC_ | _CORP_ | _CORPORATION_"
  academic <- "UNIV_ UNIV_ INST_ INST_ INST | RESEARCH_ RESEARCH_ RESEARCH
      COUNCIL | COUNCIL | COUNCIL "
  if(grepl(industrial, x)){
    return ("industrial")
  }else{
    if (grepl(academic, x)){
      return ( "academic ")
    }else{
      return("private")
  }
edge list $group <- NA
for (i in 1:nrow(edge_list)){
  row <- edge_list[i,]
  edge_list[i, "group"] <- identify_applicant_type(row$Applicants)</pre>
2.2 Create the edge matrix
unique_nodes <- unique(c(edge_list$from, edge_list$to))</pre>
edges_length <- length(unique_nodes)</pre>
edge_matrix <- matrix (, nrow = edges_length, ncol = edges_length, dimnames =
    list (unique_nodes, unique_nodes))
edge_{\mathbf{matrix}}[is.na(edge_{\mathbf{matrix}})] = 0
for(i in 1:edges_length) {
  prim_inventor <- edge_list [[i, "from"]]</pre>
  sec_inventor <- edge_list [[i, "to"]]
  edge_matrix[prim_inventor, sec_inventor] <- edge_matrix[prim_inventor, sec_
      inventor] + 1
rm(\;list = c\;(\;"prim\_inventor\;"\;,"sec\_inventor\;"\;,\;"i\;"\;)\;)
```

2.3 Create the graph object

```
df_visNetwork <- data.frame(from=edge_list$from, to=edge_list$to)
network_graph <- graph_from_data_frame(
    df_visNetwork,
    directed = FALSE) %%
    simplify(remove.loops = TRUE)</pre>
```

3. Network visualization

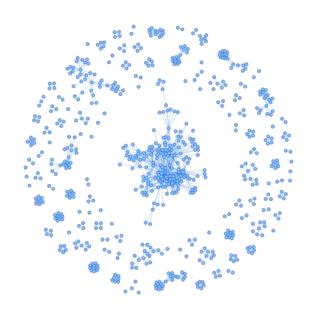
3.1 Preview of network graph with fruchtermanreingold Layout



Network graph based on fruchtermanreingold layout

3.2 Preview of network graph with visNetwork

```
vis_data <- toVisNetworkData(network_graph)
vis_network <- visNetwork(nodes = vis_data$nodes, edges = vis_data$edges)
vis_network %%
visEdges(arrows = list(to = list(enabled= FALSE)), length=30) %%
visIgraphLayout(layout = "layout_nicely")</pre>
```



4. Answering Hypothesis

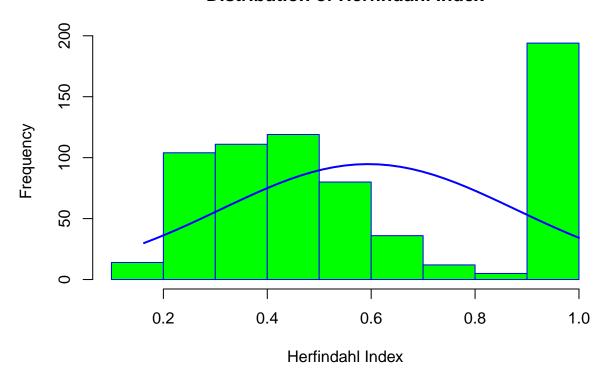
• H1: We expect more generalists to adopt the broker role in a network than specialists.

```
# Create data objects that are required for calculations
df_ipc_qc <- df_qc %%
   mutate(IPC=strsplit(IPC, "\n")) %%
   unnest(IPC)

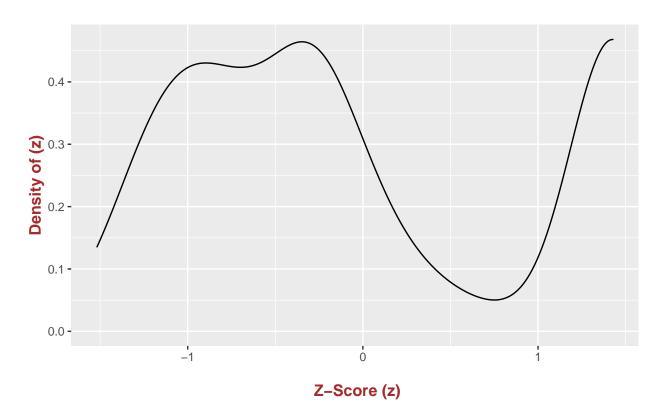
df_ipc_qc$IPC <- substring(df_ipc_qc$IPC, 1, 4)
unique_inventors <- unique(df_ipc_qc$Inventors)</pre>
```

```
df h1 <- data.frame(Inventor=unique_inventors, Betw_Centr = 0, Degree_Centr=0,
    Degree_Centr_ZScore = 0, Herf_Index = 0, Herf_Index_ZScore = 0, IsBroker=
    "NotBroker", Diversity_Type="None", Applicant_Type="", IsPeripheralPlayer=
    "NotPeripheralPlayer")
# Measure betweenness centrality for each inventor to determine the brokerage
library (omnivor)
##
## Attache Paket: 'omnivor'
## Die folgenden Objekte sind maskiert von 'package:igraph':
##
       degree distribution, diameter
##
betw_centr <- betweeness_centrality(network_graph, normalized=T) # normalized
   = T \text{ or } F \longrightarrow c larify
df_betw_centr <- data.frame(as.list(betw_centr))</pre>
t_df_betw_centr <- transpose(df_betw_centr)
t df betw centr$Inventor <- colnames(df betw centr)
for(inventor in unique_inventors){
  sub\_df\_qc \leftarrow df\_qc[df\_qc$Inventors == inventor,]
  if(nrow(sub\_df\_qc) > 1){
    centr <- t_df_betw_centr [t_df_betw_centr$Inventor == inventor, "V1"]
    df_h1[df_h1$Inventor == inventor, "Betw_Centr"] <- centr
}
# Mark who is a broker
for (i in 1:nrow(df_h1)){
  row <- df_h1[i,]
  if((row\$Betw\_Centr > 0))
    df h1[df h1$Inventor == row$Inventor, "IsBroker"] <- "Broker"
}
# Calculate the Herf Index for each inventor
for(inventor in unique_inventors){
  df_{ipc} = qc_{sub} \leftarrow df_{ipc} = qc[df_{ipc} = qc$Inventors = inventor,]
  ipc table <- table(df ipc qc sub$IPC)
  total_ipcs <- sum(ipc_table)
  {\bf table\_as\_df <\!\!\!- as.data.frame(ipc\_table)}
  herf_index \leftarrow 0
  for (i in 1:nrow(table_as_df)){
    row <- table_as_df[i,]
    val <- row$Freq
    herf_index <- herf_index + (val / total_ipcs)^2
  df_h1[df_h1$Inventor = inventor, "Herf_Index"] <- herf_index
}
## Plot Herf Index distribution
# Histogram overlaid with kernel density curve
```

Distribution of Herfindahl Index



Distribution of Herf-Index Z-Scores



```
# Evaluate who is a Specialist

# H >= (Top 10% Herfindhal index z-score distribution)

# Calculate top 10%

# P(Z > c) = 0.1 ==> P(Z < c) = 0.9

# use linear interpolation to approximate nearest values

# For further information, see: https://socratic.org/questions/what-is-the-z-
score-corresponding-to-the-top-10-percent-of-any-data-set

nearest_value_z_top10_roof <- 1.29 # Z score for 0.9015, Standard normal table

nearest_value_z_top10_floor <- 1.28 # Z score 0.8997, Standard normal table

nearest_value_p_top10_roof <- 0.9015

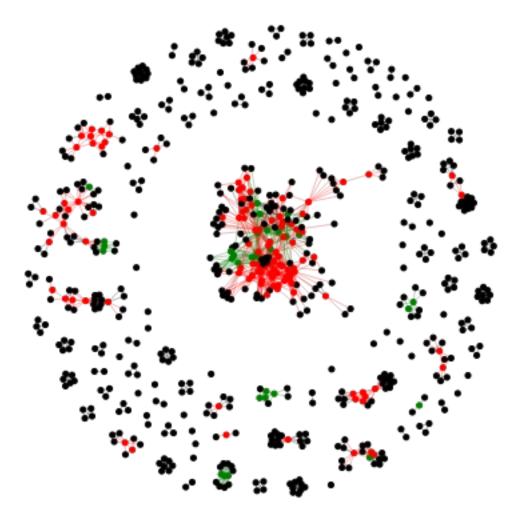
nearest_value_p_top10_floor <- 0.8997
```

- $top10_way_0.9 \leftarrow ((0.9 nearest_value_p_top10_roof) / (nearest_value_p_top10_floor nearest_value_p_top10_roof))$
- $\begin{array}{l} \text{raw_score_top_10} \longleftarrow \mathbf{mean}(\mathbf{df_h1\$Herf_Index}) \, + \, ((\, \mathbf{z_score_top_10}) \, * \, \mathbf{sd}(\mathbf{df_h1\$Herf_Index}) \\ \, \mathbf{Index})) \end{array}$
- $\#\!\#$ Author with a Herf Index over 0.9585829 are evaluated as part of the top 10%.

```
for (i in 1:nrow(df_h1)){
  row <- df_h1[i,]
  sub df gc <- df gc | df gc$Inventors == row$Inventor, |
  # Include amount of published pantents evaluation of inventor, to avoid
      inventor that have only published one patent, where no clear IPC classes
       diversity is observable
  # TODO: CRITICAL OPINION, CHECK
  if((row\$Herf\_Index >= raw\_score\_top\_10) & (nrow(sub\_df\_qc) > 1))
    df_h1[df_h1$Inventor == row$Inventor, "Diversity_Type"] <- "Specialist"
  }
}
# Evaluate who is a Generalist
# Lowest 10% Herfindhal index distribution
\# For more information, see: https://www.dummies.com/article/academics-the-
    arts/math/statistics/how-to-find-a-percentile-for-a-normal-distribution
    -169600/
# Use linear interpolation
nearest_value_z_lowest10_roof \leftarrow -1.28 # Z score for 0.1003, Standard normal
nearest_value_z_lowest10_floor <- -1.29 # Z score for 0.0985, Standard normal
nearest_value_p_lowest10_roof <- 0.1003
nearest_value_p_lowest10_floor <- 0.0985
lowest10\_way\_0.9 \leftarrow ((0.1 - nearest\_value\_p\_lowest10\_roof) / (nearest\_value\_p\_lowest10\_roof)
   lowest10_floor - nearest_value_p_lowest10_roof))
z score lowest 10 <- nearest_value z lowest 10 roof + ((nearest_value z
   lowest10_floor - nearest_value_z_lowest10_roof) * (lowest10_way_0.9))
raw\_score\_lowest\_10 \leftarrow mean(df_h1\$Herf\_Index) + ((z\_score\_lowest\_10) * sd(df\_
   h1$Herf_Index))
cat("Author_{\sqcup}with_{\sqcup}a_{\sqcup}Herf_{\sqcup}Index_{\sqcup}under", raw\_score\_lowest\_10, "are_{\sqcup}evaluated_{\sqcup}as_{\sqcup}
    part \, \Box \, of \, \Box \, the \, \Box \, lowest \, \Box \, 10\%.")
## Author with a Herf Index under 0.2298311 are evaluated as part of the
   lowest 10%.
for (i in 1:nrow(df_h1)){
  row <- df_h1[i,]
  sub\_df\_qc \leftarrow df\_qc[df\_qc$Inventors == row$Inventor,]
  # Include amount of published patents evaluation of inventor, to avoid
      inventor that have only published one patent, where no clear IPC classes
       diversity is observable
  # TODO: CRITICAL OPINION, CHECK
  if((row$Herf_Index <= raw_score_lowest_10) & (nrow(sub_df_qc) > 1)){
    df_h1[df_h1$Inventor == row$Inventor, "Diversity_Type"] <- "Generalist"
  }
}
\# Connect brokerage and generalist/specialist distribution in final numbers
broker diversity <- df h1 df h1$IsBroker == "Broker" & df h1$Diversity Type!=
     "None",
```

```
cat("Inutotal", nrow(broker_diversity), "brokersuwithugivenudiversityutypesu
     were identified.")
## In total 30 brokers with given diversity types were identified.
print(table(broker diversity $Diversity Type))
## Generalist Specialist
##
                20
\mathbf{cat} \, (\, {}^{\mathsf{T}}\mathbf{From} \, {}_{\sqcup}\, \mathbf{these} \, {}_{\sqcup}\, \mathbf{brokers} \, , \, {}_{\sqcup}\, \mathbf{we} \, {}_{\sqcup}\, \mathbf{identified} \, {}_{\sqcup}\, \mathbf{20} \, {}_{\sqcup}\, \mathbf{Generalists} \, , \, {}_{\sqcup}\, \mathbf{which} \, {}_{\sqcup}\, \mathbf{equals} \, {}_{\sqcup}\, \mathbf{to} \, {}_{\sqcup}\, \mathbf{a} \, {}_{\sqcup} \,
     distribution _{\square} of ", (20/\text{nrow}(\text{broker\_diversity})) * 100, "%_\n")
## From these brokers, we identified 20 Generalists, which equals to a
     distribution of 66.66667 %
\operatorname{\mathbf{cat}}( \operatorname{"From}_{\sqcup} \operatorname{these}_{\sqcup} \operatorname{brokers}, _{\sqcup} \operatorname{we}_{\sqcup} \operatorname{identified}_{\sqcup} 10_{\sqcup} \operatorname{Specialists}, _{\sqcup} \operatorname{which}_{\sqcup} \operatorname{equals}_{\sqcup} \operatorname{to}_{\sqcup} \operatorname{a}_{\sqcup}
     distribution of ", (10/nrow(broker_diversity)) * 100, "%")
## From these brokers, we identified 10 Specialists, which equals to a
     distribution of 33.33333 %
print ("There u are u more u generalist suthan u specialist subased u on u the u broker u
     distribution.")
## [1] "There are more generalists than specialists based on the broker
     distribution."
# Visualize key players
nodes_groups <- vector()
for (current_node in vis_data$nodes$id){
   if (current node %in% df h1$Inventor[df h1$IsBroker == "Broker"]) {
      if(current_node %in% broker_diversity$Inventor){
         nodes groups <- c(nodes groups, "Green")
      }else{
         nodes_groups <- c(nodes_groups, "Red")
   }else{
      nodes_groups <- c(nodes_groups, "Black")
}
\#vis\_data\$nodes\$group \leftarrow nodes\_groups
vis_data$nodes$color <- nodes_groups
vis_network_2 <- visNetwork(nodes = vis_data$nodes, edges = vis_data$edges,
     width = 100\%
\# Red Nodes = Broker in general
# Green Nodes = Broker with Diversity Type
\# Black Nodes = Others
```

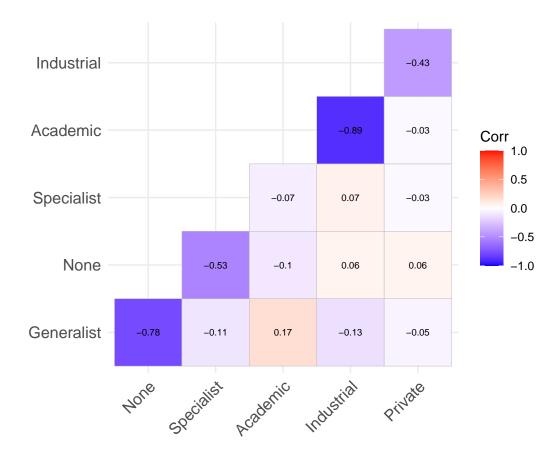
```
vis_network_2 %%
visPhysics(solver = "forceAtlas2Based", forceAtlas2Based = list(
    gravitationalConstant = -100, avoidOverlap = 1)) %%
visIgraphLayout(layout = "layout_nicely", physics = FALSE, smooth=F)
```



• H2: We expect that more generalists who adopt the broker role in a network to be of academic origin.

```
# We are continuing using the dataframe from H1.
# Determine origin of each inventor | view & use dataframe "edge_list"
\# Selecting of applicant type is based on the majority of type occurrences,
    see function "identify_applicant_type" in 2.1
\mathbf{df}_{-}\mathbf{h2} \leftarrow \mathbf{data}.\mathbf{frame}(\mathbf{from} = \mathbf{edge\_list\$from}\,,\ \mathbf{to} = \mathbf{edge\_list\$to}\,,\ \mathbf{group} = \mathbf{edge\_list\$}
    group)
for (i in 1:nrow(df_h1)){
  row <- df_h1[i,]
  df_{sub} \leftarrow df_{h2}[df_{h2}f_{rom} = row$Inventor,]
  df h1[df h1$Inventor == row$Inventor, "Applicant_Type"] <- names(which.max(
       table(df_sub$group)))
}
table_applicant_type <- table(df_h1$Applicant_Type)
cat("Overall_Distribution_of_applicant_types_through_all_Inventors")
## Overall Distribution of applicant types through all Inventors
print(table_applicant_type)
##
##
      academic industrial
                                  private
##
             65
                          514
                                        96
df_applicant_type <- as.data.frame(table_applicant_type)</pre>
df_applicant_type$Distribution <- df_applicant_type$Freq / sum(df_applicant_
    type$Freq)
# Calculate distribution of diversities types of the identified generalist who
      are brokers
generalist_with_applicant_type <- df_h1[df_h1$IsBroker == "Broker" & df_h1$
    Diversity_Type == "Generalist",
# Output results in numbers
print(table(generalist_with_applicant_type$Applicant_Type))
##
##
      academic industrial
               3
##
                           17
amount generalists <- nrow(generalist with applicant type)
\mathbf{cat} ( \texttt{"From"} , \ \mathbf{amount\_generalists} \ , \texttt{"generalists} \ , \texttt{\_we\_identified} \ \texttt{\_3} \texttt{\_of} \texttt{\_academic} \texttt{\_} 
    origin, \square which \square equals \square to \square a \square distribution \square of \square, (3/amount_generalists) * 100,
    "%<sub>□</sub>\n")
## From 20 generalists, we identified 3 of academic origin, which equals to a
    distribution of 15 %
```

```
\mathtt{cat} ("From", amount_generalists, "generalists, \( \tu \mathtt{we} \) identified \( \tu 17 \) of \( \tu industrial \)
    origin , \_which \_equals \_to \_a \_distribution \_of ", (17/amount\_generalists) * 100,
     "%_\n")
## From 20 generalists, we identified 17 of industrial origin, which equals to
     a distribution of 85\%
# Draw Conclusion from subset on larger distribution by utilizing the
    correlation coefficient based on pearson's method
pairwise\_comp \leftarrow df_h1[c(7,8,9)]
pairwise_comp$IsBroker <- factor(pairwise_comp$IsBroker)
pairwise_comp$Diversity_Type <- factor(pairwise_comp$Diversity_Type)
pairwise_comp$Applicant_Type <- factor(pairwise_comp$Applicant_Type)
pairwise_comp <- pairwise_comp [pairwise_comp$IsBroker == "Broker",]
# Convert to bivariate binary distribution (Diversity and Applicant Type), as
    the data set is based on only brokers
mm <- model.matrix(~ IsBroker + Diversity_Type + Applicant_Type, data=pairwise
   _comp, contrasts.arg = lapply(pairwise_comp[, sapply(pairwise_comp, is.
    factor), drop = FALSE, contrasts, contrasts = FALSE)
# pairwise.complete.obs means that the correlation or covariance between each
    pair of variables is computed using all complete pairs of observations on
    those variables
\operatorname{mm}_{\underline{\phantom{a}}}\operatorname{cor} \leftarrow \operatorname{cor}(\operatorname{mm}, \operatorname{use}=\operatorname{"pairwise.complete.obs"}, \operatorname{method} = \operatorname{c}(\operatorname{"pearson"}))
## Warning in cor(mm, use = "pairwise.complete.obs", method = c("pearson")):
## Standardabweichung ist Null
mm cor \%\% ggcorrplot(show.diag = F, type = "lower", lab=TRUE, lab size = 2.5)
```



 $\textbf{cat}(\, "\, Correlation \, \bot \, of \, \bot \, Generalist \, \bot \, and \, \bot \, Academic \, \bot \, is \, \bot \, 0.17 \, , \, \bot \, given \, \bot \, that \, \bot \, the \, \bot \, inspected \, \bot \, inventors \, \bot \, are \, \bot \, brokers \, . \, ")$

Correlation of Generalist and Academic is 0.17, given that the inspected inventors are brokers.

 $\begin{array}{l} \textbf{cat} (\, "\, Correlation \, \bot \, of \, \bot \, Generalist \, \bot \, and \, \bot \, Industrial \, \bot \, is \, \bot \, -0.13 \, , \, \bot \, given \, \bot \, that \, \bot \, the \, \bot \, inspected \, \bot \, inventors \, \bot \, are \, \bot \, brokers \, . \, " \,) \end{array}$

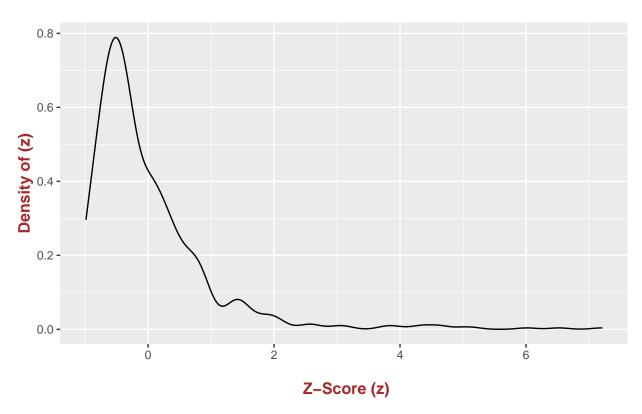
Correlation of Generalist and Industrial is -0.13, given that the inspected inventors are brokers.

Despite the measurement of 20 generalists, where 3 inventors are of academic origin, the overall correlation factor of generalist in combination with academic is higher.

• H3: We expect peripheral players to be specialists.

```
# Calculate out-degree centrality for each inventor
degree_centrality <- degree (network_graph, mode = "out", normalized = T)
df degree centr <- data.frame(as.list(degree centrality))
t_df_degree_centr <- transpose(df_degree_centr)
t_df_degree_centr$Inventor <- colnames(df_degree_centr)
\# Add out-degree centrality to df h1
for(i in 1:nrow(t_df_degree_centr)){
      row <- t_df_degree_centr[i,]
      df_h1 [df_h1$Inventor == row$Inventor, "Degree_Centr"] <- row$V1
# Calculate Z scores for Degree_Centr
# Adapt approach from H1 towards calculating lowest 10%
df_h1 <- df_h1 %% mutate(Degree_Centr_ZScore = (Degree_Centr - mean(Degree_
          Centr))/sd(Degree_Centr))
mean degree centr <- (mean(df h1$Degree Centr))
cat("Mean_of_degree_centrality_distribution:",mean_degree_centr,"\n")
## Mean of degree centrality distribution: 0.008567975
sd_degree_centr <- sd(df_h1$Degree_Centr)
cat("Standard_Deviation_of_degree_centrality_distribution:",sd_degree_centr,"\
          n")
## Standard Deviation of degree centrality distribution: 0.008695654
raw_score_lowest_10_degree_centr <- abs(mean(df_h1$Degree_Centr) + (z_score_
          lowest\_10 \ * \ \mathbf{sd} (\ \mathbf{df}\_h1\$Degree\_Centr))) \ \# \ \mathit{Take} \ \ \mathit{absolute} \ \ \mathit{value} \ , \ \ \mathit{as} \ \ \mathit{standard}
            deviation is larger than mean —> TODO: CHECK IF ABS() IS ALLOWED
\mathbf{cat}("\mathrm{Author}_{\sqcup}\mathrm{with}_{\sqcup}\mathrm{a}_{\sqcup}\mathrm{Degree}_{\sqcup}\mathrm{Centrality}_{\sqcup}\mathrm{of}_{\sqcup}\mathrm{under}", \mathrm{raw}_\mathrm{score}_\mathrm{lowest}_{\perp}10_\mathrm{degree}_{\perp}
          centr \;, \;\; "are \sqcup evaluated \sqcup as \sqcup part \sqcup of \sqcup the \sqcup lowest \sqcup 10\% \sqcup and \sqcup therefore \sqcup are \sqcup lowest \sqcup 10\% 
           peripheral_players.")
## Author with a Degree Centrality of under 0.002576956 are evaluated as part
           of the lowest 10% and therefore are peripheral players.
# Plot Distribution of Degree Centrality Z-Scores
ggplot (df h1, aes (x = Degree Centr ZScore)) +
      geom density() +
       labs(x = " \setminus L \subseteq Score (z)", y = "Density (z)", title = "Distribution (of (z)")
                 Degree Centrality Z-Scores \n") +
       theme(plot.title = element_text(hjust = 0.5),
                         axis.title.x = element_text(face="bold", colour="brown", size = 12),
                         axis.title.y = element_text(face="bold", colour="brown", size = 12))
```

Distribution of Degree Centrality Z-Scores



```
\# Get the distribution of generalist/specialist based on the peripheral
                         players
 for (i in 1:nrow(df_h1)){
               row <- df_h1[i,]
               sub\_df\_qc \leftarrow df\_qc[df\_qc$Inventors == row$Inventor,]
               if(row$Degree_Centr <= raw_score_lowest_10_degree_centr){</pre>
                             df_h1[df_h1$Inventor == row$Inventor, "IsPeripheralPlayer"] <-- "
                                                    PeripheralPlayer "
  }
  peripheral_diversity <- df_h1[df_h1$IsPeripheralPlaye == "PeripheralPlayer" &
                        df_h1$Diversity_Type != "None",]
 table (peripheral_diversity $Diversity_Type)
##
## Generalist Specialist
##
 print ("Only one of each Diversity Types identified.")
## [1] "Only one of each Diversity Types identified."
 \mathbf{print} \ (\ ^{\mathsf{u}} \mathbf{Based} \ _{\mathsf{u}} \mathbf{on} \ _{\mathsf{u}} \mathbf{that} \ _{\mathsf{u}} \mathbf{measurement} \ _{\mathsf{u}} \mathbf{no} \ _{\mathsf{u}} \mathbf{answer} \ _{\mathsf{u}} \mathbf{towards} \ _{\mathsf{u}} \mathbf{the} \ _{\mathsf{u}} \mathbf{hypothesis} \ _{\mathsf{u}} \mathbf{3} \ _{\mathsf{u}} \mathbf{can} \ _{\mathsf{u}} \mathbf{be} \ _{\mathsf{u}} \mathbf{n} \mathbf{answer} \mathbf{no} \mathbf
                        made.")
```

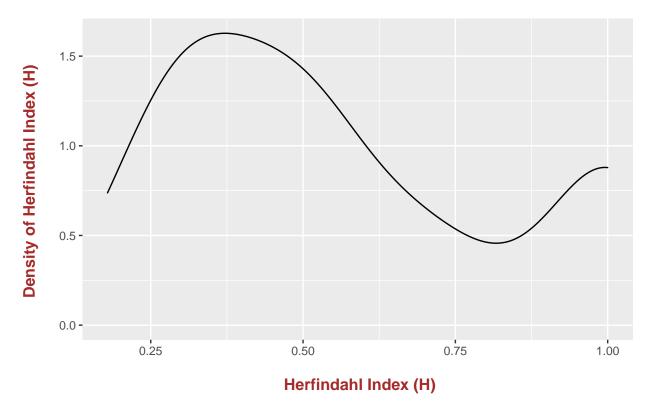
```
## [1] "Based on that measurement no answer towards the hypothesis 3 can be
    made."

# Get the distribution of Herf Index based on the peripheral players
df_peripheral <- df_h1[df_h1$IsPeripheralPlaye == "PeripheralPlayer",]

ggplot(df_peripheral, aes(x = Herf_Index)) +
    geom_density() +
    labs(x = "\n_Herfindahl_Index_U(H)",
        y = "Density_of_Herfindahl_Index_U(H)_\n",
        title = "Distribution_of_Herf_Index_based_on_peripheral_players\n") +
    theme(plot.title = element_text(hjust = 0.5),
        axis.title.x = element_text(face="bold", colour="brown", size = 12),</pre>
```

Distribution of Herf Index based on peripheral players

axis.title.y = element_text(face="bold", colour="brown", size = 12))



 $\begin{aligned} \textbf{print} \big(\, \text{"Interpretation} \, | \, \text{of} \, | \, \text{Herfindahl} \, | \, \text{Index} \, | \, \text{Distribution} \, | \, \text{based} \, | \, \text{on} \, | \, \text{existing} \, | \, \\ \text{peripheral} \, | \, \text{players} : \, \text{"} \, \big) \end{aligned}$

[1] "Interpretation of Herfindahl Index Distribution based on existing peripheral players:"

 $\mathbf{print} \left(\text{"There} \sqcup i \, s \sqcup a \sqcup t \, \text{rends} \sqcup t \, \text{owards} \sqcup a \sqcup l \, \text{ower} \sqcup h \, \text{erf} \sqcup i \, \text{ndex} \sqcup v \, \text{alue} \sqcup observable . \text{"} \right)$

[1] "There is a trends towards a lower herf index value observable."

 $\begin{aligned} \mathbf{print} \left(\text{"This} \sqcup \text{allows} \sqcup \text{us} \sqcup \text{to} \sqcup \text{derive} \sqcup \text{an} \sqcup \text{orientation} \sqcup \text{of} \sqcup \text{peripheral} \sqcup \text{players} \sqcup \text{towards} \sqcup \text{the} \sqcup \text{generalists} \sqcup \text{segment} . \sqcup \text{This} \sqcup \text{is} \sqcup \text{contrary} \sqcup \text{to} \sqcup \text{our} \sqcup \text{stated} \sqcup \text{hypothesis} . \end{aligned} \right) \end{aligned}$

```
## [1] "This allows us to derive an orientation of peripheral players towards
   the generalists segment. This is contrary to our stated hypothesis."
# Visualize results
vis_data_h3 <- toVisNetworkData(network_graph)
vis_network_h3 <- visNetwork(nodes = vis_data_h3$nodes, edges = vis_data_h3$</pre>
   edges)
nodes_groups_h3 <- vector()
for (current_node in vis_data_h3$nodes$id){
  if (current_node %in% df_h1$Inventor[df_h1$IsPeripheralPlayer == "
     PeripheralPlayer"]) {
    nodes_groups_h3 <- c(nodes_groups_h3, "Blue")
    nodes\_groups\_h3 \leftarrow c(nodes\_groups\_h3, "Black")
}
vis_data_h3$nodes$color <- nodes_groups_h3
vis_network_h3 <- visNetwork(nodes = vis_data_h3$nodes, edges = vis_data_h3$
   edges, width = 100\%
# Blue Nodes = Peripheral Players
\# Black Nodes = Not Peripheral Players
vis_network_h3 %>%
  visPhysics (solver = "forceAtlas2Based",
             forceAtlas2Based = list(gravitationalConstant = -100,
                 avoidOverlap = 1)) %%
  visIgraphLayout(layout = "layout_nicely", physics = FALSE, smooth=F)
```

