# Appendix Team 3 Quantum\_Computing

Group 3

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This R Markdown file will be provided as appendix to the final report of Team 3. Referring this appendix will follow the format of (Appendix I-"outline item of Markdown file"). For example, referring the code of Hypothesis 2 will display as following in the report: (Appendix I-4.H2). Please use a browser to interpret the html file. Otherwise, an attached PDF is available for use, although this was created using the native latex version of RStudio and the plots are not interactive.

### 0. Install & import packages

#### Install

# 1. Data collection & cleaning

Data set is given and contains patents regarding quantum computing.

### 1.1 Import data

```
df_qc <- read.csv("Quantum_computing.csv", sep=";")
```

#### 1.2 Clean Data

```
# Drop Rows where Inventors, Applicants or IPC classes or empty or NA
df_qc \leftarrow df_qc[!(is.na(df_qc\$IPC) \mid df_qc\$IPC=""),]
df_qc \leftarrow df_qc[!(is.na(df_qc\$Inventors) \mid df_qc\$Inventors=""),]
df_qc \leftarrow df_qc[!(is.na(df_qc\$Applicants) \mid df_qc\$Applicants=""),]
\# df_q c gets transformed where each row represents an inventor
df_qc <- df_qc %%
   mutate(Inventors=strsplit(Inventors, "\n")) %%
    unnest (Inventors)
# Clean Inventors & Applicants: Needed to adapt the igraph object cleaning
df_qc$Inventors & Applicants: Needed to daupt the type df_qc$Inventors <- gsub("_", "_", df_qc$Inventors)
df_qc$Inventors <- gsub("-", ".", df_qc$Inventors)
df_qc$Inventors <- chartr("[]", "..", df_qc$Inventors)
df_qc$Inventors <- chartr("<>", "..", df_qc$Inventors)
df_qc$Applicants <- gsub("_", "_", df_qc$Applicants)
df_qc$Applicants <- sub("_$", "", df_qc$Applicants)
df_qc$Applicants <- gsub("-", ".", df_qc$Applicants)
df_qc$Applicants <- gsub("-", ".", df_qc$Applicants)
df_qc$Applicants <= chartr("[]", "..", df_qc$Applicants)
df_qc$Applicants <= chartr("<>", "..", df_qc$Applicants)
# Replace _ if its last character of cell
df_qc$Inventors <- sub("_$", "", df_qc$Inventors)
\# df_qc gets transformed where each row represents an applicant in connection
      with each inventor
df_applicants_qc <- df_qc %%
   mutate(Applicants=strsplit(Applicants, "\n")) %%
    unnest (Applicants)
```

# 2. Create necessary objects

#### 2.1 Create the edge list

```
edge_list <- df_qc %%
  select(Inventors, Title, Applicants, No) %%
  inner_join(., select(., Inventors, No), by="No") %%
  filter(Inventors.x != Inventors.y) %%
  unique %%
  arrange(Title, No)

# Include the patents, where there is only one author
for (i in 1:nrow(df_qc)){
  row <- df_qc[i,]</pre>
```

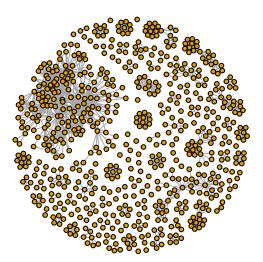
```
if(sum(df_qc$No = row$No) = 1)
              {\tt edge\_list} \left[ \mathbf{nrow} ( \, {\tt edge\_list} \, ) \, + \, 1 \, , \right] < - \, \mathbf{list} \left( \mathbf{row\$Inventors} \, , \, \, \mathbf{row\$Title} \, , \, \, \mathbf{row\$Ti
                         Applicants, row$No, row$Inventors)
       }
}
#rename to columns
names(edge_list)[names(edge_list) == "Inventors.x"] <- "from"
names(edge_list) [names(edge_list) == "Inventors.y"] <- "to"
# Selecting of applicant type is based on the majority of type occurrences
identify_applicant_type <- function(x){</pre>
       industrial <- "_INC_|INC_|LLC_|_LLC_|_CORP_|_CORPORATION_"
       academic <- "UNIV UNIV INST INST INST RESEARCH RESEARCH RESEARCH
                 COUNCIL_|_COUNCIL_|_COUNCIL"
       if(grepl(industrial, x)){
              return("industrial")
       }else{
              if (grepl(academic, x)){
                    return ( "academic ")
              }else{
                    return ("private")
edge_list$group <- NA
for (i in 1:nrow(edge_list)){
      row <- edge_list[i,]
       edge_list[i, "group"] <- identify_applicant_type(row$Applicants)</pre>
2.2 Create the edge matrix
unique_nodes <- unique(c(edge_list$from, edge_list$to))</pre>
edges_length <- length(unique_nodes)
edge_matrix <- matrix (, nrow = edges_length, ncol = edges_length, dimnames =
            list (unique_nodes , unique_nodes ) )
edge_{matrix}[is.na(edge_{matrix})] = 0
for(i in 1:edges_length) {
       prim_inventor <- edge_list [[i, "from"]]
       sec_inventor <- edge_list [[i, "to"]]
       edge_matrix[prim_inventor, sec_inventor] <- edge_matrix[prim_inventor, sec_
                  inventor] + 1
}
rm(list=c("prim_inventor", "sec_inventor", "i"))
```

#### 2.3 Create the graph object

```
df_visNetwork <- data.frame(from=edge_list$from, to=edge_list$to)
network_graph <- graph_from_data_frame(
    df_visNetwork,
    directed = FALSE) %%
    simplify(remove.loops = TRUE)</pre>
```

## 3. Network visualization

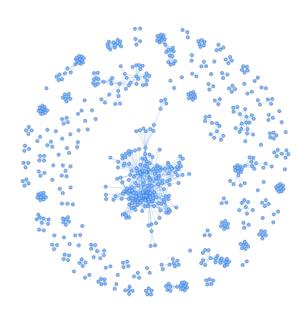
#### 3.1 Preview of network graph with fruchtermanreingold Layout



Network graph based on fruchtermanreingold layout

#### 3.2 Preview of network graph with visNetwork

```
vis_data <- toVisNetworkData(network_graph)
vis_network <- visNetwork(nodes = vis_data$nodes, edges = vis_data$edges)
vis_network %%
visEdges(arrows = list(to = list(enabled= FALSE)), length=30) %%
visIgraphLayout(layout = "layout_nicely")</pre>
```



# 4. Answering Hypothesis

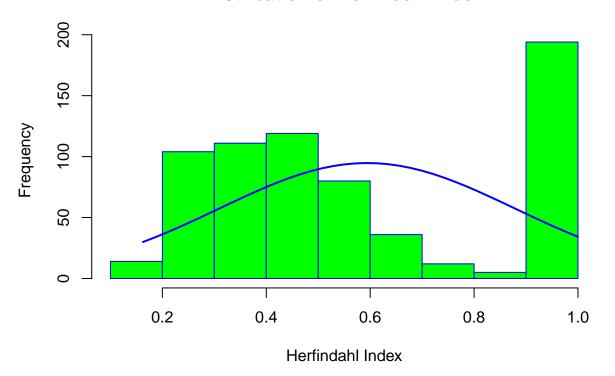
• H1: We expect more generalists to adopt the broker role in a network than specialists.

```
# Create data objects that are required for calculations
df_ipc_qc <- df_qc %%
   mutate(IPC=strsplit(IPC, "\n")) %%
   unnest(IPC)

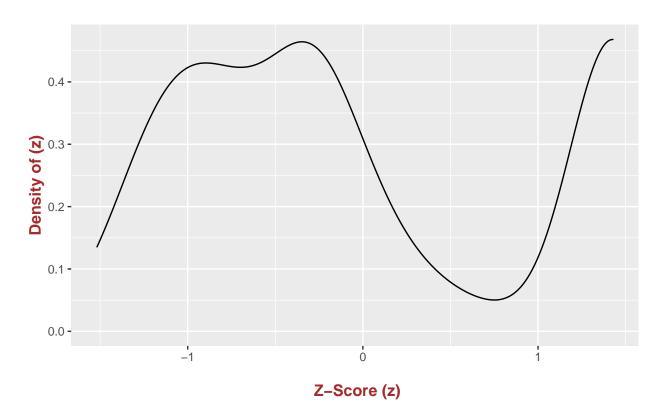
df_ipc_qc$IPC <- substring(df_ipc_qc$IPC, 1, 4)
unique_inventors <- unique(df_ipc_qc$Inventors)</pre>
```

```
df h1 <- data.frame(Inventor=unique_inventors, Betw_Centr = 0, Degree_Centr=0,
    Degree_Centr_ZScore = 0, Herf_Index = 0, Herf_Index_ZScore = 0, IsBroker=
    "NotBroker", Diversity_Type="None", Applicant_Type="", IsPeripheralPlayer=
   "NotPeripheralPlayer")
# Measure betweenness centrality for each inventor to determine the brokerage
library (omnivor)
##
## Attache Paket: 'omnivor'
## Die folgenden Objekte sind maskiert von 'package:igraph':
##
       degree distribution, diameter
##
betw_centr <- betweeness_centrality(network_graph, normalized=T) # normalized!
df_betw_centr <- data.frame(as.list(betw_centr))</pre>
t df betw centr <- transpose (df betw centr)
t_df_betw_centr$Inventor <- colnames(df_betw_centr)
for(inventor in unique_inventors){
  sub\_df\_qc \leftarrow df\_qc[df\_qc$Inventors == inventor,]
  \# Exclude inventors that have <= 1 patents published as there can be no
      betweenness centrality measured
  if(nrow(sub\_df\_qc) > 1){
    centr <- t_df_betw_centr [t_df_betw_centr$Inventor == inventor, "V1"]
    df_h1 [df_h1$Inventor == inventor, "Betw_Centr"] <- centr
  }
}
# Mark who is a broker
for (i in 1:nrow(df_h1)){
  row <- df_h1[i,]
  if((row\$Betw\_Centr > 0))
    df h1[df h1$Inventor == row$Inventor, "IsBroker"] <- "Broker"
}
# Calculate the Herf Index for each inventor
for(inventor in unique_inventors){
  df_{ipc} = qc_{sub} \leftarrow df_{ipc} = qc[df_{ipc} = qc$Inventors = inventor,]
  ipc_table <- table(df_ipc_qc_sub$IPC)
  total_ipcs <- sum(ipc_table)
  table_as_df <- as.data.frame(ipc_table)
  herf_index \leftarrow 0
  for (i in 1:nrow(table_as_df)){
    row <- table_as_df[i,]
    val <- row$Freq
    herf_index <- herf_index + (val / total_ipcs)^2
  df_h1[df_h1$Inventor = inventor, "Herf_Index"] <- herf_index
## Plot Herf Index distribution
```

### **Distribution of Herfindahl Index**



### Distribution of Herf-Index Z-Scores



```
# Evaluate who is a Specialist

# H >= (Top 10% Herfindhal index z-score distribution)

# Calculate top 10%

# P(Z > c) = 0.1 ==> P(Z < c) = 0.9

# use linear interpolation to approximate nearest values

# For further information, see: https://socratic.org/questions/what-is-the-z-
score-corresponding-to-the-top-10-percent-of-any-data-set

nearest_value_z_top10_roof <- 1.29 # Z score for 0.9015, Standard normal table

nearest_value_z_top10_floor <- 1.28 # Z score 0.8997, Standard normal table

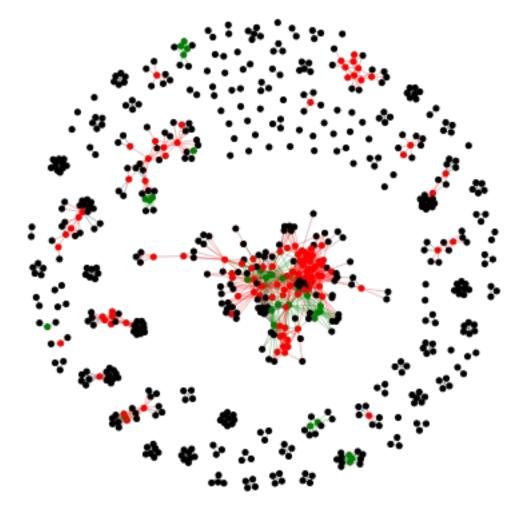
nearest_value_p_top10_roof <- 0.9015

nearest_value_p_top10_floor <- 0.8997
```

- $top10\_way\_0.9 \leftarrow ((0.9 nearest\_value\_p\_top10\_roof) / (nearest\_value\_p\_top10\_floor nearest\_value\_p\_top10\_roof))$
- $\begin{array}{l} \text{raw\_score\_top\_10} \longleftarrow \mathbf{mean}(\mathbf{df\_h1\$Herf\_Index}) \, + \, ((\,\mathbf{z\_score\_top\_10}) \, * \, \mathbf{sd}(\mathbf{df\_h1\$Herf\_Index}) \\ \, \mathbf{Index})) \end{array}$
- $\#\!\#$  Author with a Herf Index over 0.9585829 are evaluated as part of the top 10%.

```
for (i in 1:nrow(df_h1)){
        row <- df_h1[i,]
        sub df gc <- df gc | df gc | Inventors == row | Inventor, |
        # Include the check after the amount of published patents for each inventor,
                          to avoid including inventors that have only published one patent, where
                          no clear IPC classes diversity is observable
         if((row\$Herf Index >= raw score top 10) & (nrow(sub df qc) > 1))
                 df_h1[df_h1$Inventor == row$Inventor, "Diversity_Type"] <- "Specialist"
}
# Evaluate who is a Generalist
# Lowest 10% Herfindhal index distribution
\# For more information, see: https://www.dummies.com/article/academics-the-
               arts/math/statistics/how-to-find-a-percentile-for-a-normal-distribution
               -169600/
# Use linear interpolation to capture edge cases
 nearest_value_z_lowest10_roof \leftarrow -1.28 # Z score for 0.1003, Standard normal
               table
 nearest_value_z_lowest10_floor <- -1.29 # Z score for 0.0985, Standard normal
               table
 nearest_value_p_lowest10_roof <- 0.1003
 nearest_value_p_lowest10_floor <- 0.0985
lowest10\_way\_0.1 \leftarrow ((0.1 - nearest\_value\_p\_lowest10\_roof) / (nearest\_value\_p\_lowest10\_roof)
              lowest10_floor - nearest_value_p_lowest10_roof))
z\_score\_lowest\_10 \leftarrow nearest\_value\_z\_lowest10\_roof + ((nearest\_value\_z\_lowest_10\_roof) + ((nearest\_va
              lowest10_floor - nearest_value_z_lowest10_roof) * (lowest10_way_0.1))
raw_score_lowest_10 \leftarrow mean(df_h1\$Herf_Index) + ((z_score_lowest_10) * sd(df_lowest_10)
              h1$Herf_Index))
\mathbf{cat} ( \text{"Author} \sqcup \mathbf{with} \sqcup \mathbf{a} \sqcup \mathbf{Herf} \sqcup \mathbf{Index} \sqcup \mathbf{under} \text{", raw} \underline{\quad} \mathbf{score} \underline{\quad} \mathbf{lowest} \underline{\quad} \mathbf{10} \,, \text{ "are} \sqcup \mathbf{evaluated} \sqcup \mathbf{as} \sqcup \mathbf{under} \square \mathbf{10} \,, \mathbf{under}
              part_{\square} of_{\square} the_{\square} lowest_{\square} 10\%.")
## Author with a Herf Index under 0.2298311 are evaluated as part of the
              lowest 10%.
for (i in 1:nrow(df_h1)){
        row <- df h1[i,]
        sub\_df\_qc \leftarrow df\_qc[df\_qc$Inventors == row$Inventor,]
        \# Include the check after the amount of published patents for each inventor,
                          to avoid including inventors that have only published one patent, where
                          no clear IPC classes diversity is observable
         if ((row$Herf_Index <= raw_score_lowest_10) & (nrow(sub_df_qc) > 1)){
                 df_h1[df_h1$Inventor == row$Inventor, "Diversity_Type"] <- "Generalist"
        }
 }
\# Connect brokerage and generalist/specialist distribution
broker diversity <- df h1 df h1$IsBroker == "Broker" & df h1$Diversity Type!=
                   "None",
```

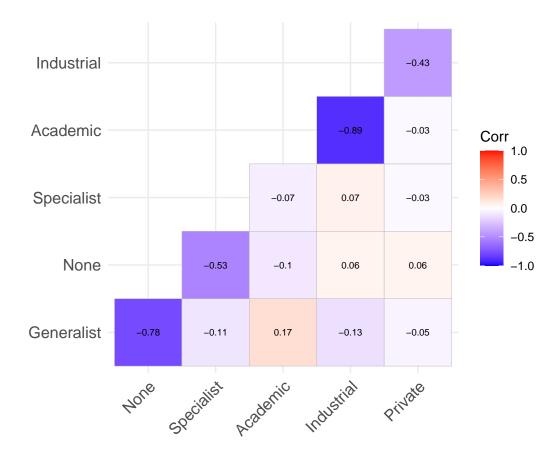
```
cat("Inutotal", nrow(broker_diversity), "brokersuwithugivenudiversityutypesu
          were identified.")
## In total 30 brokers with given diversity types were identified.
print(table(broker_diversity$Diversity_Type))
##
## Generalist Specialist
                                  20
##
\operatorname{\mathbf{cat}}( \operatorname{"From}_{\sqcup}\operatorname{these}_{\sqcup}\operatorname{brokers},_{\sqcup}\operatorname{we}_{\sqcup}\operatorname{identified}_{\sqcup}20_{\sqcup}\operatorname{Generalists},_{\sqcup}\operatorname{which}_{\sqcup}\operatorname{equals}_{\sqcup}\operatorname{to}_{\sqcup}a_{\sqcup}
           distribution \Box of ", (20/\text{nrow}(\text{broker\_diversity})) * 100, "% \n")
## From these brokers, we identified 20 Generalists, which equals to a
           distribution of 66.66667 %
cat("From_{\sqcup}these_{\sqcup}brokers,_{\sqcup}we_{\sqcup}identified_{\sqcup}10_{\sqcup}Specialists,_{\sqcup}which_{\sqcup}equals_{\sqcup}to_{\sqcup}a_{\sqcup}
           distribution of , (10/nrow (broker_diversity)) * 100, "%")
## From these brokers, we identified 10 Specialists, which equals to a
           distribution of 33.33333 %
\mathbf{print} \, (\, \tt "There \sqcup are \sqcup more \sqcup general ists \sqcup than \sqcup special ists \sqcup based \sqcup on \sqcup the \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup the \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup the \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup the \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup the \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup the \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup the \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup the \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup the \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup the \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup the \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup the \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup the \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup the \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup the \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup broker \sqcup special ists \sqcup based \sqcup on \sqcup broker \sqcup special ists \sqcup broker \sqcup special ists \sqcup specia
           distribution.")
## [1] "There are more generalists than specialists based on the broker
           distribution.'
# Visualize key players
 nodes_groups <- vector()</pre>
for (current_node in vis_data$nodes$id){
       if (current_node %in% df_h1$Inventor[df_h1$IsBroker == "Broker"]) {
             if(current_node %in% broker_diversity$Inventor){
                   nodes_groups <- c(nodes_groups, "Green")
             }else{
                   nodes groups <- c(nodes groups, "Red")
      }else{
             nodes_groups <- c(nodes_groups, "Black")
 }
 vis_data$nodes$color <- nodes_groups
 vis_network 2 <- visNetwork (nodes = vis_data$nodes, edges = vis_data$edges,
          width = "100\%")
\# Red Nodes = Broker in general
# Green Nodes = Broker with Diversity Type
\# Black Nodes = Others
 vis network 2 %%
       visPhysics(solver = "forceAtlas2Based", forceAtlas2Based = list(
                 gravitationalConstant = -100, avoidOverlap = 1)) %%
       visIgraphLayout(layout = "layout_nicely", physics = FALSE, smooth=F)
```



<sup>•</sup> H2: We expect that more generalists who adopt the broker role in a network to be of academic origin.

```
# We are continuing using the dataframe from H1.
# Determine origin of each inventor | view & use dataframe "edge_list"
# Selecting of applicant type is based on the majority of type occurrences,
    see function "identify_applicant_type" in 2.1
df_h2 <- data.frame(from=edge_list$from, to=edge_list$to, group=edge_list$
    group)
for (i in 1:nrow(df_h1)) {
  row <- df_h1[i,]
  df_{sub} \leftarrow df_{h2}[df_{h2}f_{rom} = row$Inventor,]
  df_h1[df_h1$Inventor == row$Inventor, "Applicant_Type"] <- names(which.max(
      table(df_sub$group)))
}
table_applicant_type <- table(df_h1$Applicant_Type)
cat("Overall_Distribution_of_applicant_types_through_all_Inventors")
## Overall Distribution of applicant types through all Inventors
print(table_applicant_type)
##
      academic industrial
##
                                private
             65
##
df_applicant_type <- as.data.frame(table_applicant_type)</pre>
df_applicant_type$Distribution <- df_applicant_type$Freq / sum(df_applicant_
    type$Freq)
# Calculate distribution of diversities types of the identified generalist who
     are brokers
generalist\_with\_applicant\_type \leftarrow df_h1[df_h1$IsBroker == "Broker" & df_h1$
    Diversity_Type == "Generalist",
# Output results in numbers
print(table(generalist_with_applicant_type$Applicant_Type))
##
##
      academic industrial
##
              3
                         17
amount_generalists <- nrow(generalist_with_applicant_type)
\mathtt{cat} ("From", amount_generalists, "generalists, \( \tu \mathtt{we} \) identified \( \tu 3 \) of \( \tu \mathtt{academic} \)
    origin, \square which \square equals \square to \square a \square distribution \square of \square, (3/amount_generalists) * 100,
    "%_\n")
## From 20 generalists, we identified 3 of academic origin, which equals to a
    distribution of 15 %
\mathtt{cat} ("From", amount_generalists, "generalists, \( \tu \mathtt{we} \) identified \( \tu 17 \) of \( \tu industrial \)
    origin, || which || equals || to || a || distribution || of ||, (17/amount generalists) * 100,
     "%<sub>□</sub>\n")
```

```
## From 20 generalists, we identified 17 of industrial origin, which equals to
    a distribution of 85 %
# Draw Conclusion from subset on larger distribution by utilizing the
   correlation coefficient based on pearson's method
pairwise\_comp \leftarrow df_h1[c(7,8,9)]
pairwise_comp$IsBroker <- factor(pairwise_comp$IsBroker)</pre>
pairwise_comp$Diversity_Type <- factor(pairwise_comp$Diversity_Type)
pairwise_comp$Applicant_Type <- factor(pairwise_comp$Applicant_Type)
pairwise_comp <- pairwise_comp [pairwise_comp$IsBroker == "Broker",]
# Convert to bivariate binary distribution (Diversity and Applicant Type), as
   the data set is based on only brokers
mm <- model.matrix(~ IsBroker + Diversity_Type + Applicant_Type, data=pairwise
   _comp, contrasts.arg = lapply(pairwise_comp[, sapply(pairwise_comp, is.
   factor), drop = FALSE, contrasts, contrasts = FALSE)
\# pairwise.complete.obs means that the correlation or covariance between each
   pair of variables is computed using all complete pairs of observations on
   those variables
mm_cor <- cor(mm, use="pairwise.complete.obs", method = c("pearson"))
## Warning in cor(mm, use = "pairwise.complete.obs", method = c("pearson")):
## Standardabweichung ist Null
mm_cor %% ggcorrplot (show.diag = F, type = "lower", lab=TRUE, lab_size=2.5)
```



 $\textbf{cat}( \, "\, Correlation \, \bot \, of \, \bot \, Generalist \, \bot \, and \, \bot \, Academic \, \bot \, is \, \bot \, 0.17 \, , \, \bot \, given \, \bot \, that \, \bot \, the \, \bot \, inspected \, \bot \, inventors \, \bot \, are \, \bot \, brokers \, . \, ")$ 

## Correlation of Generalist and Academic is 0.17, given that the inspected inventors are brokers.

 $\begin{array}{l} \textbf{cat} ( \ "Correlation \ \_of \ \_Generalist \ \_and \ \_Industrial \ \_is \ \_-0.13, \ \_given \ \_that \ \_the \ \_inspected \ \_inventors \ \_are \ \_brokers \ . \ ") \end{array}$ 

## Correlation of Generalist and Industrial is -0.13, given that the inspected inventors are brokers.

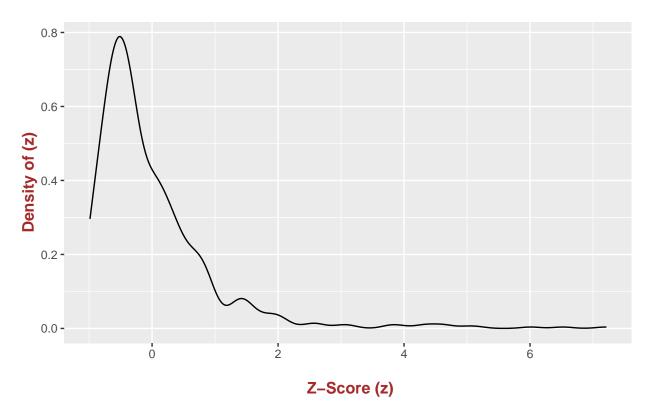
## Despite the measurement of 20 generalists, where 3 inventors are of academic origin, the overall correlation factor of generalist in combination with academic is higher.

• H3: We expect peripheral players to be specialists.

```
# Calculate out-degree centrality for each inventor
degree_centrality <- degree (network_graph, mode = "out", normalized = T)
df degree centr <- data.frame(as.list(degree centrality))
t_df_degree_centr <- transpose(df_degree_centr)
t_df_degree_centr$Inventor <- colnames(df_degree_centr)
\# Add out-degree centrality to df h1
for(i in 1:nrow(t_df_degree_centr)){
  row <- t_df_degree_centr[i,]
  df_h1[df_h1$Inventor == row$Inventor, "Degree_Centr"] <- row$V1
}
# Calculate Z scores for Degree_Centr
df h1 <- df h1 %% mutate(Degree Centr ZScore = (Degree Centr - mean(Degree_
   Centr))/sd(Degree_Centr))
# Adapt approach from H1 towards calculating lowest 10%
# Lowest 30% Herfindhal index distribution, as distribution indicates that
    there are few inventors with way more connections than the majority.
# This is indicated by the fact, that the standard deviation is larger than
    the mean.
# Use linear interpolation to capture edge cases
nearest_value_z_lowest30_roof \leftarrow -0.52 # Z score for 0.30153, Standard normal
nearest_value_z_lowest30_floor \leftarrow -0.53 \# Z \ score \ for \ 0.29806, Standard normal
     table
nearest_value_p_lowest30_roof <- 0.30153
nearest_value_p_lowest30_floor <- 0.29806
lowest30 way 0.3 <- ((0.3 - nearest_value_p_lowest30_roof) / (nearest_value_p_
   lowest30_floor - nearest_value_p_lowest30_roof))
z score lowest 30 <- nearest_value z lowest30 roof + ((nearest_value z
   lowest30_floor - nearest_value_z_lowest30_roof) * (lowest30_way_0.3))
mean_degree_centr <- (mean(df_h1$Degree_Centr))
cat("Mean_of_degree_centrality_distribution:",mean_degree_centr,"\n")
## Mean of degree centrality distribution: 0.008567975
sd_degree_centr <- sd(df_h1$Degree_Centr)
cat("Standard_Deviation_of_degree_centrality_distribution:",sd_degree_centr,"\
   n")
## Standard Deviation of degree centrality distribution: 0.008695654
print ("Standard deviation is larger than mean.")
## [1] "Standard deviation is larger than mean."
raw_score_lowest_30_degree_centr <- mean_degree_centr + (z_score_lowest_30 *
   sd_degree_centr)
\textbf{cat} ( \texttt{"Author} \bot \texttt{with} \bot \texttt{a} \bot \texttt{Degree} \bot \texttt{Centrality} \bot \texttt{of} \bot \texttt{under"}, \texttt{raw\_score\_lowest\_30\_degree\_}
    centr, \ "are \sqcup evaluated \sqcup as \sqcup part \sqcup of \sqcup the \sqcup lowest \sqcup 30\% \sqcup and \sqcup are \sqcup therefore \sqcup
    peripheral_players.")
```

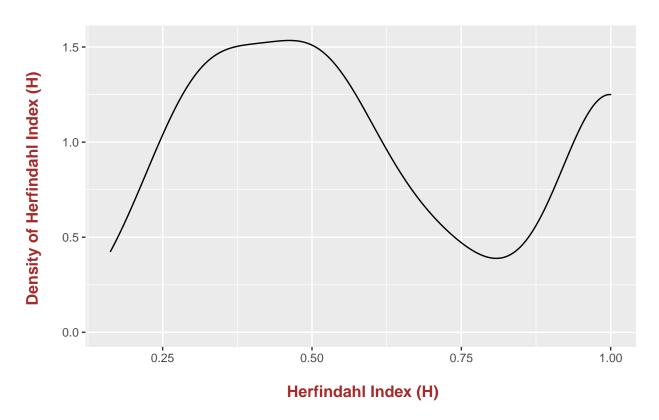
```
## Author with a Degree Centrality of under 0.004007893 are evaluated as part of the lowest 30% and are therefore peripheral players.
```

### Distribution of Degree Centrality Z-Scores



```
## Generalist Specialist
                                 2
amount_relevant_peripheral_p <- nrow(peripheral_diversity)
\mathtt{cat} ("From", amount_relevant_peripheral_p, "peripheral_players, \sqcup \mathtt{we} \sqcup \mathtt{identified} \sqcup 2 \sqcup
          generalists, _which_equals_to_a_distribution_of ", (2/amount_relevant_
          peripheral_p) * 100, "%_\n")
## From 7 peripheral players, we identified 2 generalists, which equals to a
          distribution of 28.57143 \%
\mathtt{cat} ("From", amount_relevant_peripheral_p, "peripheral_players, \sqcupwe\sqcupidentified \sqcup5\sqcup
          specialists, \_which \_equals \_to \_a \_distribution \_of ", (5/amount\_relevant \_
          ## From 7 peripheral players, we identified 5 specialists, which equals to a
          distribution of 71.42857 %
\textbf{print} \ ( \ "Based \ \_on \ \_this \ \_measurement \ \_and \ \_the \ \_awareness \ \_of \ \_the \ \_small \ \_sample \ \_size \ , \ \_awareness \ \_of \ \_the \ \_small \ \_sample \ \_size \ , \ \_awareness \ \_of \ \_the \ \_small \ \_sample \ \_size \ , \ \_awareness \ \_of \ \_the \ \_small \ \_sample \ \_size \ , \ \_awareness \ \_of \ \_the \ \_small \ \_sample \ \_size \ , \ \_awareness \ \_of \ \_the \ \_small \ \_sample \ \_size \ , \ \_awareness \ \_of \ \_the \ \_small \ \_sample \ \_size \ , \ \_awareness \ \_of \ \_the \ \_small \ \_sample \ \_size \ , \ \_awareness \ \_of \ \_the \ \_small \ \_sample \ \_size \ , \ \_awareness \ \_of \ \_the \ \_small \ \_sample \ \_size \ , \ \_awareness \ \_of \ \_the \ \_small \ \_sample \ \_size \ , \ \_awareness \ \_of \ \_the \ \_small \ \_sample \ \_size \ , \ \_awareness \ \_of \ \_the \ \_small \ \_sample \ \_size \ , \ \_awareness \ \_of \ \_of
         _confirmation_for_our_hypothesis_can_be_derived.")
## [1] Based on this measurement and the awareness of the small sample size,
         a confirmation for our hypothesis can be derived."
# Get the distribution of Herf Index based on the peripheral players
 df_{peripheral} \leftarrow df_{h1}[df_{h1}] Is Peripheral Playe = "Peripheral Player",
 ggplot(df\_peripheral, aes(x = Herf\_Index)) +
      geom_density() +
      labs(x = " \setminus n \cup Herfindahl \cup Index \cup (H)",
                   y = "Density \cup of \cup Herfindahl \cup Index \cup (H) \cup \backslash n",
                    title = "Distribution \cup of \cup Herf \cup Index \cup based \cup on \cup peripheral \cup players \setminus n") +
      theme(plot.title = element_text(hjust = 0.5),
                      axis.title.x = element_text(face="bold", colour="brown", size = 12),
                      axis.title.y = element_text(face="bold", colour="brown", size = 12))
```

### Distribution of Herf Index based on peripheral players



 $\begin{aligned} \mathbf{print} \big( \, \text{"Interpretation} \, | \, \text{of} \, | \, \text{Herfindahl} \, | \, \text{Index} \, | \, \text{Distribution} \, | \, \text{based} \, | \, \text{on} \, | \, \text{existing} \, | \, \\ \text{peripheral} \, | \, \text{players} \, : \, \text{"} \, \big) \end{aligned}$ 

```
## [1] "Interpretation of Herfindahl Index Distribution based on existing peripheral players:"
```

```
print ("There, is, a, trends, towards, a, lower, herf, index, value, observable.")
```

## [1] "There is a trends towards a lower herf index value observable."

 $\begin{aligned} \textbf{print} \left( \text{"This} \sqcup \text{allows} \sqcup \text{us} \sqcup \text{to} \sqcup \text{derive} \sqcup \text{an} \sqcup \text{orientation} \sqcup \text{of} \sqcup \text{peripheral} \sqcup \text{players} \sqcup \text{towards} \sqcup \text{the} \sqcup \text{generalists} \sqcup \text{segment.} \sqcup \text{This} \sqcup \text{is} \sqcup \text{contrary} \sqcup \text{to} \sqcup \text{our} \sqcup \text{stated} \sqcup \text{hypothesis.} \end{aligned} \right) \end{aligned}$ 

## [1] "This allows us to derive an orientation of peripheral players towards the generalists segment. This is contrary to our stated hypothesis."

```
# Visualize results
vis_data_h3 <- toVisNetworkData(network_graph)
vis_network_h3 <- visNetwork(nodes = vis_data_h3$nodes, edges = vis_data_h3$
    edges)

nodes_groups_h3 <- vector()

for (current_node in vis_data_h3$nodes$id){
    if (current_node %in% df_h1$Inventor[df_h1$IsPeripheralPlayer == "
        PeripheralPlayer"]){</pre>
```

nodes\_groups\_h3 <- c(nodes\_groups\_h3, "Blue")</pre>

