

a)

$$sY(s) - y(0) - Y(s) = \frac{1}{s-a}$$

$$a=1$$

$$(s-1)Y(s) - 1 = \frac{1}{s-1} + 1$$

$$Y(s) = \frac{1}{(s-1)^2} + \frac{1}{s-1}$$

$$y(t) = te^t + e^t = (t+1)e^t$$

b)

$$sY(s) - 5 + 3Y(s) = -\frac{s}{s^2+1}$$

$$a=1$$

$$sY(s) + 3Y(s) = -\frac{s}{s^2+1} + 5$$

$$(s+3)Y(s) = \dots$$

$$Y(s) = -\frac{s}{(s^2+1) \cdot (s+3)} + \frac{5}{s+3}$$

$$= -\frac{s}{s^3+3s^2+s+3} + \frac{5}{s+3}$$

$$Y(t) = \frac{-3}{10} \left(-e^{-3t} + \cos(t) + \frac{1}{3} \sin(t) \right) + 5e^{-3t}$$

$\phi = 3$
 $a = 3$
 $b = 1$

$$Y(t) = -\frac{3}{10} \left(-e^{-3t} + \cos(t) + \frac{1}{3} \sin(t) \right) + 5e^{-3t}$$