

c)

$$sY(s) - 5Y(s) = 2 \cdot \frac{s}{s^2+1} - \frac{3}{s^2+9}$$

$$(s-5)Y(s) = \frac{2s}{s^2+1} - \frac{3}{s^2+9}$$

$$Y(s) = \frac{2s}{(s^2+1)(s-5)} - \frac{3}{(s^2+9)(s-5)}$$

$$= \frac{2s}{s^3-5s^2+s-5} - \frac{3}{s^3-5s^2+9s-45}$$

$$y(t) = -\frac{10}{26} \cdot (-e^{5t} + \cos(t) + \frac{1}{5} \sin(t)) - \frac{3}{34} \cdot (e^{5t} - \cos(3t) + \frac{5}{3} \sin(3t))$$

$r = 5$
 $a = -5$
 $b = 3$

d)

$$sY(s) - \textcircled{2} + 4Y(s) = \frac{1}{s^2}$$

$$(s+4)Y(s) = \frac{1}{s^2} + \textcircled{2}$$

$$Y(s) = \frac{1}{s^2(s+4)} + \frac{\textcircled{2}}{s+4}$$

$$y(t) = \frac{1}{16} (e^{-4t} + 4t - 1) + \textcircled{2} e^{-4t}$$

$$y(t) = \frac{1}{16} (e^{-4t} + 4t - 1) + \left(\frac{1}{16} (28e^4 - 1) \right) e^{-4t}$$