

IC-252 Lab
Lab Assignment-2
due for submission on Moodle by 26th Feb

1. Suppose that a laboratory test to detect a certain disease has the following statistics.
 A = event that the tested person has the disease
 B = event that the test result is positive
It is known that $P(B|A) = 0.99$ and $P(B|\bar{A}) = 0.005$, and 0.1 of the population actually has the disease. What is the probability that a person has the disease given that the test result is positive?

2. Let there be two unbiased N -sided dice that are thrown once, for instance, a 5-sided dice will have five faces, each having 1, 2, 3, 4, 5 number of dots respectively. Write a general program which takes N as input and give the following outputs,
 - (a) Sample space $S = \{ \cdot \cdot \cdot \}$.
 - (b) Event E_1 that the sum of the dots on the dice equals N .
 - (c) Event E_2 that the dots on the first dice is $\lfloor N/2 \rfloor$, where $\lfloor \cdot \rfloor$ indicates greatest integer function.
 - (d) Event E_3 that the sum of the dots on the dice is greater than $N + \lfloor N/2 \rfloor$, where $\lfloor \cdot \rfloor$ indicates the greatest integer function.
 - (e) Event $E_4 = E_1 \cap E_3$, i.e., when the sum is N and greater than $N + \lfloor N/2 \rfloor$.
 - (f) Probabilities of the events E_1, E_2, E_3 , and E_4 , i.e., $P(E_1), P(E_2), P(E_3)$, and $P(E_4)$.
 - (g) Are events E_1 and E_2 independent? Also, output whether the events E_1 and E_3 independent.

3. Repeat Question 2 to write a general program which takes N as input to output the parts 2f and 2g without using the probability formulas. Hence, run the simulation K times in a program and compute the probabilities by utilizing the counts of the desired outcomes. In your report, prepare the below table, Table 3, for a fixed N and increasing K to state your observations.

Table 1: Table for Question-3.

For a fixed value of $N =$	$K = 10$	$K = 50$	$K = 100$	$K = 1000$	$K = 5000$
$P(E_1)$					
$P(E_2)$					
$P(E_3)$					
$P(E_4)$					
Are E_1 & E_2 seem independent?					
Are E_3 & E_4 seem independent?					