

Bridge-Quantum v1.0 Public Edition

Paradox Engine ↔ Quantum Attractors

Correspondence Framework

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Abstract

This document establishes correspondence rules between Paradox Engine (PE) framework and quantum systems, focusing on energy eigenstates, topological invariants, and phase stability. It defines what PE framework can and cannot claim about quantum phenomena, provides translation between PE attractors and quantum states, and establishes falsification criteria. This bridge enables PE-informed quantum materials design while maintaining rigorous grounding in established quantum mechanics.

Purpose: Define correspondence between PE attractors and quantum states, guide experimental design for quantum materials, prevent overclaiming about quantum predictions.

Tier: 1.5 (Correspondence Framework)

Status: Canonical reference for quantum system applications

Relationship: Parallel to Bridge v1.1 (mechanical), not sequential

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1 Introduction

1.1 Bridge Purpose

This bridge establishes correspondence between Paradox Engine framework concepts and quantum systems—specifically energy eigenstates, band topology, and phase stability. It is a **qualitative correspondence framework**, not a derivational theory.

What this bridge provides:

- Translation between PE attractors and quantum states
- Scope definitions (what PE can/cannot address in quantum systems)
- Correspondence tables for key quantum concepts
- Falsification criteria specific to quantum predictions
- Guidance for PE-informed quantum materials experiments

What this bridge is NOT:

- NOT a derivation of quantum mechanics from PE
- NOT a replacement for Schrödinger equation or DFT
- NOT a source of numerical predictions (energies, rates, coupling constants)
- NOT a claim that PE is more fundamental than quantum mechanics

1.2 Critical Limitations

CRITICAL: What PE Cannot Do in Quantum Systems

PE framework via Bridge-Quantum v1.0 provides **qualitative correspondence ONLY**. It does NOT:

- Derive the Schrödinger equation or Hamiltonian
- Predict energy eigenvalues numerically
- Calculate exact tunneling rates or transition amplitudes
- Compute entanglement metrics or quantum correlations
- Generate band structures without DFT/tight-binding
- Predict superconducting critical temperatures

All numerical quantum predictions require conventional quantum mechanics. PE provides qualitative guidance on where to look, not what values to expect.

1.3 Relationship to Bridge v1.1

Bridge v1.1 (Mechanical Lattices):

- Scope: Classical mechanics, phonons, defects
- Grounding: Elasticity theory, Newtonian dynamics

Bridge-Quantum v1.0 (This Document):

- Scope: Quantum states, band topology, phase stability
- Grounding: Quantum mechanics (correspondence, not derivation)
- Parallel: Not an extension of Bridge v1.1, independent correspondence

Some systems (e.g., twisted bilayer graphene) require BOTH bridges:

- Bridge v1.1 for mechanical stability, phonons
- Bridge-Quantum v1.0 for electronic structure, superconductivity

2 Scope Definition

2.1 IN SCOPE: What PE Framework Addresses

Via correspondence to quantum systems (qualitative only):

1. Energy Eigenstates as Attractors:

- PE: Attractor states in Hilbert space
- QM: Energy eigenstates $|\psi_n\rangle$
- Correspondence: Stable quantum configurations (analogous structure)
- Limitation: Cannot compute specific eigenvalues

2. Topological Invariants:

- PE: Topological invariants in attractor space
- QM: Band topology (Chern number, Zak phase, winding number)
- Correspondence: Qualitative identification of topologically protected states
- Limitation: Cannot calculate invariants numerically

3. Phase Stability:

- PE: Attractor basin structure
- QM: Quantum phases (superfluid, Mott insulator, topological)
- Correspondence: Phase boundaries as basin transitions
- Limitation: Cannot predict exact critical parameters

4. Quantum Phase Transitions:

- PE: Transitions between attractor basins
- QM: QPTs (continuous or first-order)
- Correspondence: Suggests examining order parameters
- Limitation: Cannot determine transition order or universality class

5. Many-Body Patterns (Qualitative):

- PE: Collective attractor structure
- QM: Many-body localization, thermalization, eigenstate thermalization hypothesis
- Correspondence: Qualitative pattern recognition only
- Limitation: Cannot compute many-body spectra

2.2 OUT OF SCOPE: What PE Framework Does NOT Address

1. Schrödinger Equation Derivation:

- Cannot derive $i\hbar\partial_t|\psi\rangle = \hat{H}|\psi\rangle$ from PE
- Cannot construct Hamiltonians from first principles

2. Energy Eigenvalue Calculations:

- Cannot predict specific energies (eV, meV, etc.)
- Cannot compute band gaps numerically
- Cannot determine Fermi levels

3. Exact Quantum Dynamics:

- Cannot calculate tunneling rates exactly
- Cannot predict decay times or transition probabilities
- Cannot compute time evolution operators numerically

4. Entanglement and Correlations:

- Cannot compute entanglement entropy
- Cannot calculate correlation functions exactly
- Can only identify qualitative patterns

5. Quantitative Predictions:

- Cannot predict superconducting T_c
- Cannot calculate magnetic ordering temperatures
- Cannot determine optical absorption spectra numerically

3 Tier 1 \leftrightarrow Tier 2 Correspondence

3.1 Core Quantum Correspondences

Tier 1 (PE Framework)	Tier 2 (Quantum Mechanics)
Attractor state	Energy eigenstate $ \psi_n\rangle$ (analogous stable configuration)
Recurrence operator \mathcal{R}	Time evolution $\hat{U}(t) = e^{-i\hat{H}t/\hbar}$ (one-way correspondence, suggests recurrence)
Spectral radius ρ	Hilbert space contraction / density matrix fixed point ($\rho < 1$ = convergence)
Collapse $\circ \rightarrow \emptyset$	Measurement projection (conditional, abstract—cannot compute outcomes)
Topological invariant	Band topology (Chern number, \mathbb{Z}_2 , winding) (analogous, qualitative)
Attractor basin	Quantum phase (superfluid, Mott, topological)
Basin transition	Quantum phase transition (QPT)
Substrate coupling	Many-body interactions (qualitative correspondence only)

Table 1: Primary PE \leftrightarrow Quantum Mechanics correspondences

3.2 Topological Correspondence Table

Tier 1 (PE Framework)	Tier 2 (Quantum Topology)
Topological invariant in attractor space	Chern number, Berry phase, Zak phase
Protected edge mode	Topologically protected surface/edge state
Bulk-boundary correspondence	PE bulk invariant \leftrightarrow edge attractor
Attractor winding	Winding number in band structure
Defect-bound state	Topological defect mode (e.g., Majorana)
Phase boundary	Topological phase transition

Table 2: Topological correspondence (qualitative only)

3.3 Known System Applications

4 Permitted Applications

4.1 Valid Uses of PE Framework via Bridge-Quantum v1.0

The following applications are **appropriate and grounded**:

1. Identifying Quantum Attractor Candidates:

System	PE Correspondence	Limitation
Twisted Bilayer Graphene (TBG)	Magic angle $\sim 1.1^\circ$ as attractor in twist-angle space	Cannot predict exact angle or T_c
Topological Insulators	Bulk-edge correspondence as PE invariant	Qualitative structure only, no \mathbb{Z}_2 calculation
Superconductivity	Cooper pairs as attractors, phase coherence	Cannot predict T_c or gap Δ
Quantum Hall Effect	Chern number as topological invariant	Cannot compute Hall conductance numerically
Mott Transition	Attractor basin transition (metal \leftrightarrow insulator)	Cannot predict U/t critical value

Table 3: System-specific correspondences and limitations

- "PE framework suggests examining flat band regions as attractor states"
- "Topological analysis indicates investigating edge modes"
- Valid: Directs experimental attention

2. Qualitative Topological Correspondence:

- "System exhibits bulk-boundary correspondence consistent with PE topological invariant"
- "Phase transition structure aligns with attractor basin picture"
- Valid: Interprets observed patterns

3. Design Guidance for Quantum Materials:

- "Maximize attractor stability by tuning toward topologically protected regime"
- "PE suggests exploring parameter space near basin boundaries"
- Valid: Qualitative experimental guidance

4. Hypothesis Generation:

- "If PE correspondence valid, topological edge states should persist under perturbation"
- "Test: Measure edge conductance under systematic disorder"
- Valid: Testable predictions

4.2 Example Phrasings

Appropriate (Correspondence Language):

- "PE framework via Bridge-Quantum v1.0 suggests examining..."
- "Attractor interpretation corresponds qualitatively to..."
- "Topological stability in PE aligns with band invariants in..."
- "This pattern is consistent with PE-identified attractor structure..."

Inappropriate (Derivational/Predictive Language):

- "PE derives the Hamiltonian for this system..."

- "PE predicts energy eigenvalues of..."
- "PE calculates superconducting $T_c = 30$ K..."
- "PE generates the band structure showing..."

5 Prohibited Claims

5.1 What PE Framework Cannot Do in Quantum Systems

1. Energy Eigenvalue Derivation:

INVALID "PE predicts band gap = 1.2 eV"

VALID "DFT calculates 1.2 eV; PE suggests examining stability"

2. Superconducting Critical Temperature:

INVALID "PE calculates $T_c = 30$ K for this material"

VALID "PE suggests Cooper pair attractor may exist; measure T_c experimentally"

3. Exact Topological Invariants:

INVALID "PE computes Chern number $C = 1$ "

VALID "PE suggests topological protection; calculate Chern number via Berry curvature integration"

4. Quantum Dynamics:

INVALID "PE predicts tunneling rate = 10^{-5} s $^{-1}$ "

VALID "PE suggests examining tunneling as attractor transition; measure rate"

5. Many-Body Spectra:

INVALID "PE generates many-body energy levels"

VALID "PE identifies qualitative many-body pattern; use ED/DMRG for spectra"

6 Falsification Criteria

6.1 Testing Bridge Validity

Bridge-Quantum v1.0 correspondence is **falsified** if:

1. PE Attractor Mappings Contradict Observations:

- PE suggests stable attractor at specific parameters
- Quantum measurements show no stable state there
- Conclusion: Attractor \leftrightarrow eigenstate correspondence fails

2. Topological Correspondences Misalign:

- PE predicts topologically protected edge state
- Edge conductance absent or fragile to perturbations
- Conclusion: Topological invariant correspondence invalid

3. Phase Transition Predictions Fail:

- PE suggests QPT at parameter values
- Exhaustive measurements show no phase boundary
- Conclusion: Basin transition correspondence incorrect

4. Attractor Analysis Misses Stable Configurations:

- Conventional QM identifies stable eigenstate
- PE framework provides no corresponding attractor
- Conclusion: Correspondence incomplete or incorrect

6.2 Validation Criteria

Bridge-Quantum v1.0 correspondence is **validated** if:

1. PE-identified attractors align systematically with observed quantum states
2. Topological correspondences match band structure calculations
3. Phase boundaries predicted by basin analysis confirmed experimentally
4. PE framework identifies novel quantum configurations before conventional methods
5. Multiple independent systems show consistent PE \leftrightarrow QM mapping

Note: Validation is incremental and system-specific. Some quantum regimes may show good correspondence while others do not.

7 Application Examples

7.1 Example 1: Twisted Bilayer Graphene (TBG)

PE Framework Input:

- Twist angle space contains attractors
- Magic angle $\theta \approx 1.1$ as stable attractor
- Flat bands emerge from attractor stability

Quantum Mechanics Translation:

- Twist angle = moiré superlattice parameter
- Magic angle = specific θ where flat bands appear
- Flat bands = nearly dispersionless electronic states

What PE Can Say:

- "Magic angle exists as attractor in twist-angle space" (qualitative)
- "Superconductivity emerges from Cooper pair attractor" (conceptual)

What PE Cannot Say:

- Cannot predict $\theta = 1.1$ numerically
- Cannot calculate T_c or gap Δ

- Cannot generate band structure without tight-binding

Experimental Test:

- Systematically vary twist angle
- Measure: Resistance, Hall effect, heat capacity
- Test: Does behavior cluster near $\theta \sim 1$ as PE suggests?
- Quantify: Use continuum model + DFT for band structure

7.2 Example 2: Topological Insulator Edge States

PE Framework Input:

- Bulk topological invariant as PE attractor property
- Edge states as boundary attractors
- Protection from backscattering via topological constraint

Quantum Mechanics Translation:

- Bulk invariant = \mathbb{Z}_2 topological index
- Edge states = helical Dirac fermions
- Protection = time-reversal symmetry constraint

What PE Can Say:

- "Edge modes correspond to topologically protected attractors" (qualitative)
- "Bulk-boundary correspondence preserves attractor structure" (conceptual)

What PE Cannot Say:

- Cannot calculate \mathbb{Z}_2 invariant
- Cannot predict edge state velocity
- Cannot determine spin texture quantitatively

Experimental Test:

- Measure edge conductance vs. temperature, disorder
- Test: Does conductance persist (topological protection)?
- Quantify: ARPES for band structure, transport for G

7.3 Example 3: Superconducting Phase Transition

PE Framework Input:

- Cooper pairs as attractors in momentum space
- Phase coherence as collective attractor
- Critical temperature as basin boundary

Quantum Mechanics Translation:

- Cooper pairs = bound electron states
- Phase coherence = macroscopic wavefunction
- T_c = critical temperature for phase transition

What PE Can Say:

- "Cooper pair formation corresponds to attractor binding" (qualitative)
- "Phase transition occurs at attractor basin boundary" (conceptual)

What PE Cannot Say:

- Cannot predict T_c numerically
- Cannot calculate gap $\Delta(T)$
- Cannot determine pairing symmetry quantitatively

Experimental Test:

- Measure resistance, heat capacity, tunneling spectra vs. T
- Test: Does system show phase transition as PE suggests?
- Quantify: BCS theory or Eliashberg equations for T_c

8 Relationship to Other Bridges

8.1 Bridge Hierarchy

Bridge v1.1 (Mechanical Lattices):

- Scope: Classical mechanics, elasticity
- Applications: Graphene structure, CNT phonons, metamaterials

Bridge-Quantum v1.0 (This Document):

- Scope: Quantum states, band topology, phase stability
- Applications: TBG electronics, topological materials, superconductivity
- Relationship: Parallel to Bridge v1.1, not extension

Systems Requiring Both Bridges:

- Twisted Bilayer Graphene: Bridge v1.1 (structure), Bridge-Quantum (electronics)
- Topological Phononic Crystals: Bridge v1.1 (phonons), Bridge-Quantum (topology)
- Quantum Materials: Bridge v1.1 (lattice), Bridge-Quantum (electronic properties)

8.2 Future Bridge Development

Not Yet Developed (Out of Current Scope):

- Bridge-Thermogravity: Information density, spacetime curvature
- Bridge-Chemical: Reaction pathways, catalysis
- Bridge-Biological: Protein folding, cellular dynamics

These would require separate bridge documents with their own correspondence rules and falsification criteria.

9 Conclusions

9.1 Summary

Bridge-Quantum v1.0 establishes correspondence between PE framework and quantum systems. It provides:

- Clear scope (what PE can/cannot address in quantum mechanics)
- Translation tables (PE attractors \leftrightarrow quantum states)
- Falsification criteria (how to test correspondence validity)
- Application examples (TBG, topological insulators, superconductivity)

9.2 Key Principles

1. **Correspondence, not derivation** - PE maps to QM, doesn't generate it
2. **Qualitative only** - No numerical predictions of energies, rates, or temperatures
3. **Complementary to conventional QM** - PE guides where to look; QM provides quantitative analysis
4. **Falsifiable** - Negative results refine or invalidate correspondences
5. **System-specific** - Correspondence may work well for some systems, poorly for others

Attractors are like eigenstates, but more fun to think about.

Correspondence guides intuition.

Schrödinger still writes the checks.

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