

Stack 2

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Recall

- Concept of Stack
 - Last-in First Out property
 - Operations restricted on one end of the container.
 - $O(1)$
 - Two ways of representation.
 - Demo of Array-based Stack Implementation

Today Class

- Demo of Linked List Stack
- Applications of Stack
 - Reverse List/Array
 - Decimal to Binary Number
 - Parenthesis Matching
 - Infix Expression and Postfix Expression

Demo of Linked List Stack

Demo of Stack Applications

- Reverse List/Array
- Decimal to Binary Number
- Parenthesis Matching

Parentheses Matching

- Each “(”, “{”, or “[” must be paired with a matching “)”, “}”, or “]”
 - correct: ()(()){([())}
 - incorrect: ((())(()){([())}
 - incorrect:)(()){([())}
 - incorrect: ({ []})}
 - incorrect: (

Parentheses Matching

Algorithm ParenMatch(X, n):

Input: An array X of n tokens, each of which is either a grouping symbol, a variable, an arithmetic operator, or a number

Output: **true** if and only if all the grouping symbols in X match

Let S be an empty stack

for $i=0$ to $n-1$ **do**

if $X[i]$ is an opening grouping symbol **then**

$S.push(X[i])$

else if $X[i]$ is a closing grouping symbol **then**

if $S.isEmpty()$ **then**

return false {nothing to match with}

if $S.pop()$ does not match the type of $X[i]$ **then**

return false {wrong type}

if $S.isEmpty()$ **then**

return true {every symbol matched}

else return false {some symbols were never matched}

Concept of Infix and Postfix Expressions

- Infix expressions
 - This is the common expression we use in programing.
 - It is a crucial task in Compiler.
 - Operators are in between operands.
 - You have walk though the whole expression before starting to evaluate.
 - E.g. $3 + 4 * 2$,
 - You cannot do $3 + 4$ first.

Concept of Infix and Postfix Expressions

- Postfix expressions,
 - Precedence and associativity are build-in to the expression.
 - So you can evaluate it from left to right.
 - E.g $3\ 4\ 2\ *\ +$

Concept of Infix and Postfix Expressions

- To Evaluate Infix Expression
 - We can first transfer infix to postfix.
 - Then we evaluate postfix expression.
- Both steps above need Stack structure.

Examples of Infix and Postfix

- Infix: $2 + 3$ infix
 - Postfix: $2\ 3\ +$
- Infix: $2 * 3 + 4$
 - Postfix: $2\ 3\ *\ 4\ +$
- Infix: $2 + 3 * 4$
 - Postfix: $2\ 3\ 4\ *\ +$
- Infix: $(2 + 3) * 4$
 - Postfix: $2\ 3\ +\ 4\ *$

Postfix Evaluation algorithm

```
While there are items in the the postfix expression
{
    if the current item is an operand,
        push it onto stack.
    else
        pop stack and attach operand to right of the operator
        pop stack again and attach operand to the left of the operator
        evaluate and push the results

    advanced to next item in postfix expression,
}
if only one number left in stack,
    pop and this is the final result.
else
    postfix has error in it.(probably the original infix has syntax error)
```

Summary and Next Class

- Many Applications
 - Parens Matching
 - Reverse Array
 - Decimal to Binary Conversion
- Concept of infix and postfix expression
- How to evaluate postfix expression?

Next Class

- How to convert infix into postfix expression?
 - Then we know how to evaluate infix expression in compilers.