CSCI 3104 Fall 2021
Instructors: Profs. Grochow and Waggoner

# Midterm 1- Standard 9

Due Date ..... TODO
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## Contents



## 1 Instructions

- The solutions **should be typed**, using proper mathematical notation. We cannot accept hand-written solutions. Here's a short intro to LaTeX.
- You should submit your work through the **class Canvas page** only. Please submit one PDF file, compiled using this LaTeX template.
- You may not need a full page for your solutions; pagebreaks are there to help Gradescope automatically find where each problem is. Even if you do not attempt every problem, please submit this document with no fewer pages than the blank template (or Gradescope has issues with it).
- You **may not collaborate with other students**. **Copying from any source is an Honor Code violation. Furthermore, all submissions must be in your own words and reflect your understanding of the material.** If there is any confusion about this policy, it is your responsibility to clarify before the due date.
- Posting to **any** service including, but not limited to Chegg, Discord, Reddit, StackExchange, etc., for help on an assignment is a violation of the Honor Code.
- You **must** virtually sign the Honor Code (see Section 2). Failure to do so will result in your assignment not being graded.

## 2 Honor Code (Make Sure to Virtually Sign)

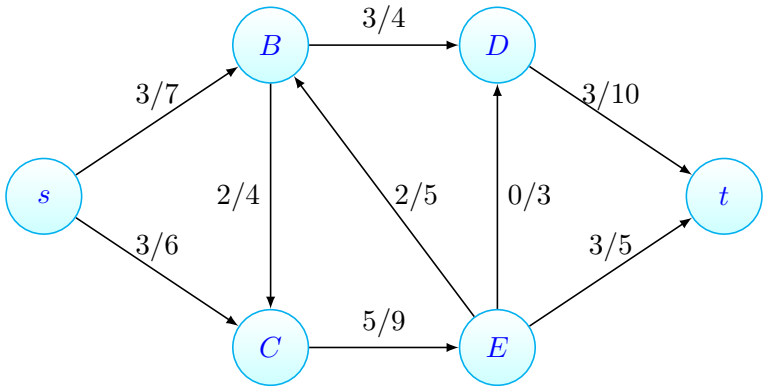
**Problem 1.**

- My submission is in my own words and reflects my understanding of the material.
- I have not collaborated with any other person.
- I have not posted to external services including, but not limited to Chegg, Discord, Reddit, StackExchange, etc.
- I have neither copied nor provided others solutions they can copy.

*Agreed (John Blackburn).* □

## 3 Standard 9- Network Flows: Terminology

**Problem 2.** Consider the following flow network, with the following flow configuration $f$ as indicated below. For each question, use the flow $f$.




Do the following.

(a) What is the maximum *additional* amount of flow that we can push across the edge $(C, E)$ from $C \to E$? Do not consider where this flow would come from nor where it would go to, just how much additional flow $C$ can push to $E$. Justify using 1-2 sentences.

*Answer.* The max flow I can push from $C \to E$ is 4. This is because the edge has a max flow capacity of 9, and already has 5 flowing through it. Therefore, only 4 more units of flow can be pushed through. □

(b) What is the maximum amount of flow that $C$ can push backwards to $B$? Do **not** consider whether $B$ can reroute that flow elsewhere; just whether $C$ can push flow backwards. Justify using 1-2 sentences.

*Answer.* The max flow I can push backwards through $C \to B$ is 2. This is because there is already 2 units of flow going through the edge in the positive direction. The net flow through an edge cannot be less than zero, so when pushing negative flow we cannot push more than is already flowing in the positive direction. Therefore, since 2 is flowing in the positive direction, a max of 2 can be pushed backwards from $C \to B$. □

(c) What is the maximum amount of flow that $D$ can push backwards to $E$? Do **not** consider whether $E$ can reroute that flow elsewhere; just whether $D$ can push flow backwards. Justify using 1-2 sentences.

*Answer.* The max flow that can be pushed from $D \to E$ given the current flow configuration is 0. Net flow cannot be less than zero, and since there currently is zero flow in the edge no flow can be pushed backwards. □

(d) How much flow can be pushed along the flow-augmenting path $s \to B \to C \to E \to D \to t$? Justify using 1-2 sentences.

*Answer.* The max flow available to the path is 2. The constraining edge is $B \to C$ with a max flow available of 2. Therefore, only 2 can be pushed through the entire path. □

(e) Find a second flow-augmenting path and indicate the maximum amount of additional flow that can be pushed along the path. Assume that the flow-augmenting path from part (d) has **not** been applied. Justify using 1-2 sentences.

*Answer.* A flow path I Found is $s \to C \to E \to t$ with a max flow of 2. The constraining edge is $E \to t$ with a max flow available of 2. Therefore only 2 can be pushed along the entire path. □