CSCI 3104 Fall 2021 INSTRUCTORS: PROFS. GROCHOW AND WAGGONER

Quiz-Standard 19

Due Date	TODO
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Contents	
1 Instructions	1
2 Honor Code (Make Sure to V	irtually Sign)
3 Standard 19- Tree Method	3

1 Instructions

- The solutions **should be typed**, using proper mathematical notation. We cannot accept hand-written solutions. Here's a short intro to LATEX.
- You should submit your work through the **class Canvas page** only. Please submit one PDF file, compiled using this LaTeX template.
- You may not need a full page for your solutions; pagebreaks are there to help Gradescope automatically find where each problem is. Even if you do not attempt every problem, please submit this document with no fewer pages than the blank template (or Gradescope has issues with it).
- You may not collaborate with other students. Copying from any source is an Honor Code violation. Furthermore, all submissions must be in your own words and reflect your understanding of the material. If there is any confusion about this policy, it is your responsibility to clarify before the due date.
- Posting to any service including, but not limited to Chegg, Discord, Reddit, StackExchange, etc., for help on an assignment is a violation of the Honor Code.
- You **must** virtually sign the Honor Code (see Section 2). Failure to do so will result in your assignment not being graded.

2 Honor Code (Make Sure to Virtually Sign)

Problem 1.

- My submission is in my own words and reflects my understanding of the material.
- I have not collaborated with any other person.
- I have not posted to external services including, but not limited to Chegg, Discord, Reddit, StackExchange, etc.
- I have neither copied nor provided others solutions they can copy.

Agreed John Blackburn.	
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Standard 19- Tree Method 3

Problem 2. Using the tree method, find a suitable function f(n) such that $T(n) \in \Theta(f(n))$. Show all work. You may without loss of generality assume that n is a power of 5; that is, $n = 5^k$ for some integer $k \ge 0$.

$$T(n) = \begin{cases} 3 & : n < 5, \\ 5T(n/5) + 2n & : n \ge 5. \end{cases}$$

Answer. To determine the total work, we first determine the non-recursive work done at each level, then sum the non-recursive work done across all levels.

At level $i \geq 0$, the recursion tree has 5^i nodes. The non-recursive work done by each node is $\frac{2n}{5^i}$. Thus, the total non-recursive work done at level i is:

$$5^i(\frac{2n}{5^i}) = 2n$$

Now observe we hit a base case when $n = 5^k < 5$. Solving for k, we have that $n/5^h < 5$. Since $n = 5^k$ we hit a base case when h = k. That is, we have k levels to the tree where the levels are indexed 0,1,...,k-1. In particular, we note that $k = \log_5(n)$. Thus:

note that
$$k = \log_5(n)$$
.
 $T(n) = \sum_{i=0}^{k-1} 2n$
 $T(n) = 2n \sum_{i=0}^{\log_5(n)-1} 1$
 $T(n) = 2n \log_7(n)$

$$T(n) = 2n \sum_{i=0}^{\log_5(n)-1} 1$$

$$T(n) = 2n \log_5(n)$$

So,
$$T(n) \in \Theta(n \log(n))$$