

Quiz- Standard 15

Due Date TODO
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1 Instructions

- The solutions **should be typed**, using proper mathematical notation. We cannot accept hand-written solutions. Here's a short intro to L^AT_EX.
- You should submit your work through the **class Canvas page** only. Please submit one PDF file, compiled using this L^AT_EX template.
- You may not need a full page for your solutions; pagebreaks are there to help Gradescope automatically find where each problem is. Even if you do not attempt every problem, please submit this document with no fewer pages than the blank template (or Gradescope has issues with it).
- You **may not collaborate with other students**. **Copying from any source is an Honor Code violation. Furthermore, all submissions must be in your own words and reflect your understanding of the material.** If there is any confusion about this policy, it is your responsibility to clarify before the due date.
- Posting to **any** service including, but not limited to Chegg, Discord, Reddit, StackExchange, etc., for help on an assignment is a violation of the Honor Code.
- You **must** virtually sign the Honor Code (see Section 2). Failure to do so will result in your assignment not being graded.

2 Honor Code (Make Sure to Virtually Sign)

Problem 1.

- My submission is in my own words and reflects my understanding of the material.
- I have not collaborated with any other person.
- I have not posted to external services including, but not limited to Chegg, Discord, Reddit, StackExchange, etc.
- I have neither copied nor provided others solutions they can copy.

Agreed (John Blackburn).

□

3 Standard 15- Analyzing Code II: Nested Dependent Loops

Problem 2. Analyze the *worst-case* runtime of the following algorithm. Clearly derive the runtime complexity function $T(n)$ for this algorithm, and then find a tight asymptotic bound for $T(n)$ (that is, find a function $f(n)$ such that $T(n) \in \Theta(f(n))$). Avoid heuristic arguments from 2270/2824 such as multiplying the complexities of nested loops.

Algorithm 1 Nested Dependent Loops

```
1: procedure FOO1(Integer  $n$ )
2:   for  $i \leftarrow 1; i \leq 2 * n; i \leftarrow i + 1$  do
3:     for  $j \leftarrow 1; j \leq i; j \leftarrow j + 1$  do
4:       print ( $i + j$ )
```

Answer. I start by analyzing the j-loop

The j-loop does the following. the init takes one step. Observe the j loop takes i iterations. At each iteration, the loop does the following: the comparison $j \leq i$ takes one step. The update of j takes 2 steps, and the print statement takes two steps. so the runtime of this loop is:

$$1 + \sum_{j=1}^i (1 + 2 + 2) = 1 + 5i$$

Now for the outer loop i . One step for initialization. The loop does $2n$ iterations. It takes one step to compare i to $2n$, and 2 steps to update the i variable. The body of the loop solely consists of the j-loop. Therefore the runtime of the i -loop is:

$$1 + \sum_{i=1}^{2n} (1 + 2 + 1 + 5i) = 1 + \sum_{i=1}^{2n} (4) + 5 * \sum_{i=1}^{2n} (i) = 1 + 4n + 5(\frac{2n(2n+1)}{2}) = 1 + 9n + 10n^2$$

therefore the function $T(n) = 10n^2 + 9n + 1$. So $T(n) \in \Theta(n^2)$

□