

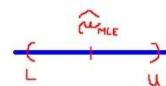
DATA SAMPLE: (x_1, \dots, x_n)
 MODEL: $(X_1, \dots, X_n) = (X_1, \dots, X_n)$, $X \sim N(\mu, \sigma^2)$

$(1-\alpha) \cdot 100\%$ CI: 1) 2-sided: (L, U)
 95 %

$$P(L \leq \mu \leq U) = 1-\alpha$$

$$L = \hat{\mu}_{MLE} - q_{1-\frac{\alpha}{2}} \cdot \frac{\sigma^2}{n}$$

$$U = \hat{\mu}_{MLE} + q_{1-\frac{\alpha}{2}} \cdot \frac{\sigma^2}{n}$$



2) LEFT: (L, ∞)

$$P(L \leq \mu) = 1-\alpha$$

$$L = \hat{\mu}_{MLE} - q_{1-\alpha} \cdot \frac{\sigma^2}{n}$$



3) RIGHT: $(-\infty, U)$

$$P(\mu \leq U) = 1-\alpha$$

$$U = \hat{\mu}_{MLE} + q_{1-\alpha} \cdot \frac{\sigma^2}{n}$$



$q_{1-\frac{\alpha}{2}}$ | $q_{1-\alpha}$ are the QUANTILES of: **NORMAL distribution** (σ^2 is known)
STUDENT t-distribution (is not)
 (with $n - 1$ degrees of freedom)