$$c_i \sim \text{NB}(\xi, p_i)$$

 $\text{logit}(p_i) = \boldsymbol{x}_i^T \boldsymbol{\beta} + \alpha \eta_i^*$