

# Tigger and Winnie-the-Pooh

First of all, we note that the shortest path for moving the Tiggers from point  $A$  to point  $B$  will be the smallest in terms of the number of jumps.

**SUBTASK 1.** Let the Tiggers jump length be  $d$  and greater than the distance  $AB$ . Then the Tigger will be able to get from the point  $A$  to the point  $B$  in two jumps — first it jumps to the point  $C$ , separated from the points  $A$  and  $B$  at a distance of  $d$ , and then from the point  $C$  jumps to the point  $B$ . To calculate the coordinates of the point  $C$ , we first find the middle  $M$  of the segment  $AB$ , compose the vector  $\overrightarrow{MT}$ , perpendicular to the vector  $\overrightarrow{AB}$ . Then, in the direction of the vector  $\overrightarrow{MT}$  from the point  $M$ , we postpone the segment  $MT'$  (vector) of length  $\sqrt{d^2 - \frac{1}{4}AB^2}$ . It remains to add the coordinates of the displacement  $MT'$  to the coordinates of the point  $M$ .

The implementation of this idea allows us to solve the problem by 20 points.

**SUBTASKS 2 AND 3.** Let the points  $A$  and  $B$  be on a horizontal or vertical line. Then the computational formulas for finding the intermediate points that the Tigger need to jump into are quite simple.

First we find the distance  $AB$  and check if  $AB$  is divisible without a remainder by the length of the jump  $d$ . If so, then the number of jumps is equal to the quotient of dividing  $AB$  by  $d$ , and the coordinates of intermediate jumping points are obtained from the coordinates of the point  $A$  by horizontal displacement (subtask 2) or vertical (subtask 3) by  $\frac{i}{q} \cdot AB$ , where  $i$  is the number of the jump,  $q$  is the quotient of dividing  $AB$  by  $d$ .

If  $AB$  is not completely divisible by  $d$ , then the total number of jumps is 2, if  $AB < 2 \cdot d$ , and  $q = \lceil \frac{AB}{d} \rceil$ , if  $AB > 2 \cdot d$ . (Here  $\lceil x \rceil$  is the smallest integer that is not less than  $x$ .) To get from  $A$  to  $B$ , the Tigger first makes  $q - 2$  jumps in a straight line  $AB$ , approaching the point  $B$ , and then, when the remaining distance to the point  $B$  is already less than  $2d$ , make two more jumps, as described in subtask 1, get to the point  $B$ .

The implementation of these ideas allows us to solve the problem by 70 points.

**SUBTASKS 4.** The idea of solving the problem in the general situation is the same as in subtask 2 and 3. The formulas for calculating the coordinates of intermediate jumps are slightly more complicated, since the angle of inclination of the straight line  $AB$  must be taken into account.

The implementation of these ideas in the general case allows us to solve the problem by 100 points.