

Таблица 1: Must-try functions.

| Formula | Output dimension | # of arguments | # of parameters |
|-------------|------------------|----------------|-----------------|
| \sqrt{x} | 1 | 1 | 0 |
| $x\sqrt{x}$ | 1 | 1 | 0 |
| $\arctan x$ | 1 | 1 | 0 |
| $\ln x$ | 1 | 1 | 0 |
| $x \ln x$ | 1 | 1 | 0 |

Таблица 2: List of elementary functions.

| Function name | Formula | Output dimension | # of arguments | # of parameters |
|----------------------|--|------------------|----------------|-----------------|
| Add constant | $x + w$ | 1 | 1 | 1 |
| Quadratic | $w_2x^2 + w_1x + w_0$ | 1 | 1 | 3 |
| Cubic | $w_3x^3 + w_2x^2 + w_1x + w_0$ | 1 | 1 | 4 |
| Logarithmic sigmoid | $1/(w_0 + \exp(-w_1x))$ | 1 | 1 | 2 |
| Exponent | $\exp x$ | 1 | 1 | 0 |
| Normal | $\frac{1}{w_1\sqrt{2\pi}} \exp\left(\frac{(x-w_2)^2}{2w_1^2}\right)$ | 1 | 1 | 2 |
| Multiply by constant | $x \cdot w$ | 1 | 1 | 1 |
| Monomial | $w_1x^{w_2}$ | 1 | 1 | 2 |
| Weibull-2 | $w_1w_2x^{w_2-1} \exp -w_1x^{w_2}$ | 1 | 1 | 2 |
| Weibull-3 | $w_1w_2x^{w_2-1} \exp -w_1(x - w_3)^{w_2}$ | 1 | 1 | 3 |

Таблица 3: Monotone functions.

| By growth rate | | | | | |
|---------------------------|----------------------------|------------------|----------------|-----------------|---------------|
| Function name | Formula | Output dimension | # of arguments | # of parameters | Constraints |
| Linear | $w_1x + w_0$ | 1 | 1 | 2 | |
| Exponential rate | $\exp(w_1x + w_0)$ | 1 | 1 | 2 | $w_1 > 0$ |
| Polynomial rate | $\exp(w_1 \ln x + w_0)$ | 1 | 1 | 2 | $w_1 > 1$ |
| Sublinear polynomial rate | $\exp(w_1 \ln x + w_0)$ | 1 | 1 | 2 | $0 < w_1 < 1$ |
| Logarithmic rate | $w_1 \ln x + w_0$ | 1 | 1 | 2 | $w_1 > 0$ |
| Slow convergence | $w_0 + w_1/x$ | 1 | 1 | 2 | $w_1 \neq 0$ |
| Fast convergence | $w_0 + w_1 \cdot \exp(-x)$ | 1 | 1 | 2 | $w_1 \neq 0$ |
| Other | | | | | |
| Soft ReLu | $\ln(1 + e^x)$ | 1 | 1 | 0 | |
| Sigmoid | $1/(w_0 + \exp(-w_1x))$ | 1 | 1 | 2 | $w_1 > 0$ |
| Nonparametric log-sigmoid | $1/(1 + \exp(-x))$ | 1 | 1 | 0 | |
| Hiberbolic tangent | $\tanh(x)$ | 1 | 1 | 0 | |
| softsign | $\frac{ x }{1+ x }$ | 1 | 1 | 0 | |

Таблица 4: Multivariate.

| Bivariate | | | | |
|------------------------|---|---|------------|-------------|
| Plus | $x_1 + x_2$ | 1 | 2 | 0 |
| Minus | $x_1 - x_2$ | 1 | 2 | 0 |
| Product | $x_1 \cdot x_2$ | 1 | 2 | 0 |
| Division | $\frac{x_1}{x_2}$ | 1 | 2 | 0 |
| | $x_1 \sqrt{x_2}$ | 1 | 2 | 0 |
| | $x_1 \ln x_2$ | 1 | 2 | 0 |
| Multivariate | | | | |
| Sum of products | $\sum_{i,j} x_i x_j$ | 1 | $n \geq 2$ | 0 |
| Sum of products | $\sum_{i,j,k} x_i x_j x_k$ | 1 | $n \geq 3$ | 0 |
| Sum of Gaussians | $\sum_{j=1}^n a_j \exp(-\frac{(x_j - b_j)^2}{c_j})$ | 1 | n | $3n$ |
| Polynomial | $\sum_{j=0}^n a_j x^j$ | 1 | 1 | n |
| Rational polynomial | $\frac{\sum_{j=0}^n a_j x^j}{x^m + \sum_{j=0}^{m-1} b_j x^j}$ | 1 | 1 | $n + m + 1$ |

Таблица 5: Data statistics.

| | | | | |
|------------------|--|-----|-------------|------------|
| sum | $\sum_i x_i$ | 1 | m | 0 |
| mean | $(\sum_i x_i)/m$ | 1 | m | 0 |
| min | $\min_i x_i$ | 1 | m | 0 |
| max | $\max_i x_i$ | 1 | m | 0 |
| std | $\frac{1}{m-1} \sqrt{\sum_i (x_i - \text{mean}(x))^2}$ | 1 | m | 0 |
| hist | $\sum_i [X_{j-1} < x_i \leq X_j]$ | n | m | $n - 1$ |
| conv | $\sum_j x_{i-j} w_j$ | 1 | $m - n + 1$ | $n \leq m$ |
| FFT coefficients | | n | m | 1 |