

Feature generation for multiscale time series forecasting

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Outline

- ▶ Data preprocessing
- ▶ Design matrix
- ▶ Testing procedure
- ▶ Feature generation
- ▶ Feature selection

Problem statement

Multiscale data

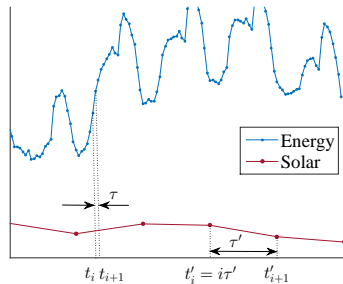
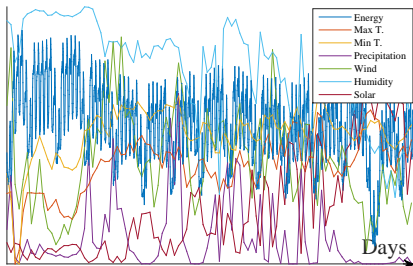
Consider a large set of time series $\mathcal{D} = \{\mathbf{s}^{(q)} \mid q = 1 \dots, Q\}$.

Each real-valued time series \mathbf{s}

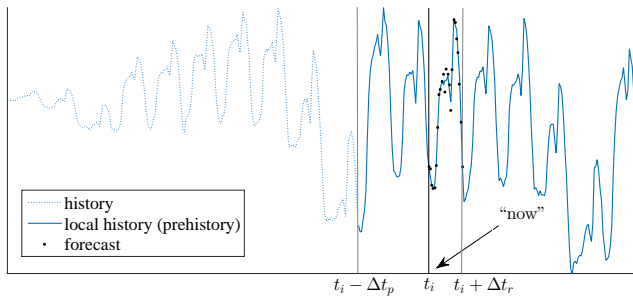
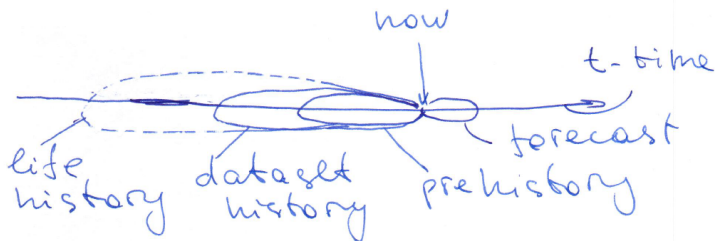
$$\mathbf{s} = [s_1, \dots, s_i, \dots, s_T], \quad s_i = s(t_i), \quad 0 \leq t_i \leq t_{\max}$$

is a sequence of observations of some real-valued signal $s(t)$.

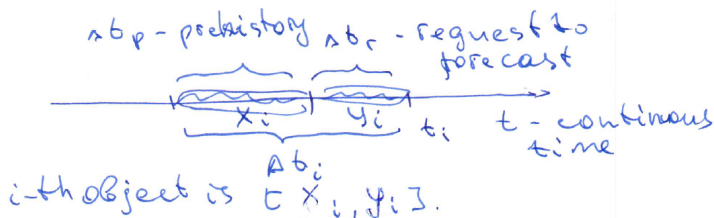
Each time series $\mathbf{s}^{(q)}$ has its own sampling rate $\tau^{(q)}$.



Time series forecasting

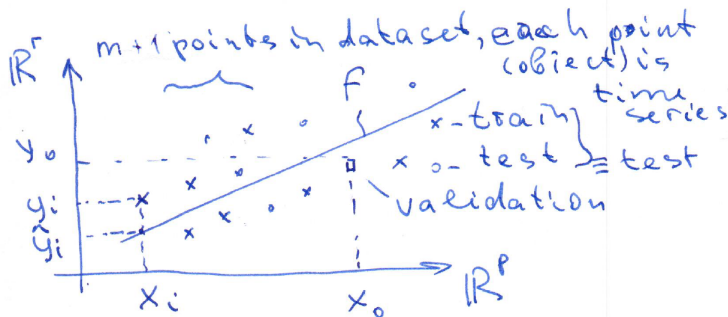


Design matrix



$$[x_i | y_i] = \underbrace{s(t_i - \Delta t_r - \Delta t_p), \dots, s(t_i - \Delta t_r)}_{x_i}, \underbrace{s(t_i), \dots, s(t_i)}_{y_i}.$$

Design matrix



$$\mathbf{X}^* = \left[\begin{array}{c|c} \mathbf{x} & \mathbf{y} \\ \hline \mathbf{X} & \mathbf{Y} \end{array} \right] = \left[\begin{array}{ccc|ccc} \mathbf{x}^{(1)} & \dots & \mathbf{x}^{(Q)} & \mathbf{y}^{(1)} & \dots & \mathbf{y}^{(Q)} \\ \mathbf{x}_m^{(1)} & \dots & \mathbf{x}_m^{(Q)} & \mathbf{y}_m^{(1)} & \dots & \mathbf{y}_m^{(Q)} \\ \vdots & \ddots & \vdots & \vdots & \ddots & \vdots \\ \mathbf{x}_1^{(1)} & \dots & \mathbf{x}_1^{(Q)} & \mathbf{y}_1^{(1)} & \dots & \mathbf{y}_1^{(Q)} \end{array} \right].$$

Regression problem

Now we are able to state the regression problem as follows:

$$\hat{\mathbf{y}} = f(\mathbf{x}, \hat{\mathbf{w}}), \quad \hat{\mathbf{w}} = \arg \min_{\mathbf{w}} S(\mathbf{w} | \mathbf{f}(\mathbf{w}, \mathbf{x}), \mathbf{y}). \quad (1)$$

Here the error function $S(\mathbf{w} | \mathbf{f}(\mathbf{w}, \mathbf{x}), \mathbf{y})$ averages forecasting errors of $[\mathbf{x}_i | \mathbf{y}_i]$ over all segments $i = 1, \dots, m$ in the test set:

$$S(\mathbf{w} | \mathbf{f}(\mathbf{w}, \mathbf{x}), \mathbf{y}) = \frac{r}{m} \sum_{i=1}^m l(\mathbf{y}_i, f(\mathbf{x}_i, \mathbf{w})).$$

Let $\boldsymbol{\varepsilon}$ denote residual vector

$$\boldsymbol{\varepsilon} = [\varepsilon_1, \dots, \varepsilon_r] = \mathbf{y} - \hat{\mathbf{y}}$$

for the forecast $\hat{\mathbf{y}} = \mathbf{f}(\mathbf{w}, \mathbf{x})$ of \mathbf{y} .

Types of forecasting errors

- ▶ scale-dependent metrics: mean absolute error

$$MAE = \frac{1}{r} \sum_{j=1}^r |\varepsilon_j|,$$

- ▶ percentage-error metrics: (symmetric) mean absolute percent error

$$MAPE = \frac{1}{r} \sum_{j=1}^r \frac{|\varepsilon_j|}{|y_j|}, \quad sMAPE = \frac{1}{r} \sum_{j=1}^r \frac{2|\varepsilon_j|}{|\hat{y}_j + y_j|},$$

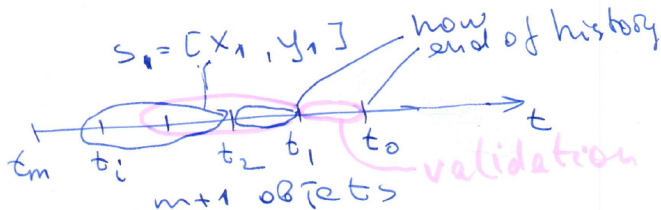
- ▶ relative-error metrics (to residues ε^* of a benchmark method):

$$MRAE = \frac{1}{r} \sum_{j=1}^r \frac{|\varepsilon_j|}{\varepsilon_j^*},$$

- ▶ and scale-free error metrics:

$$MASE = \frac{n-1}{r} \frac{\sum_{i=1}^r |\varepsilon_i|}{\sum_{j=2}^n |x_j - x_{j-1}|}.$$

Rolling validation



Rolling validation

- 1) construct the validation vector $\mathbf{x}_{\text{val},k}^*$ for time series of the length Δt_r as the first row of the design matrix \mathbf{Z} ,
- 2) construct the rest rows of the design matrix \mathbf{Z} for the time after t_k and present it as

$$\mathbf{Z} = \left[\begin{array}{c|c} \dots & \dots \\ \hline \mathbf{x}_{\text{val},k} & \mathbf{y}_{\text{val},k} \\ 1 \times n & 1 \times r \\ \hline \mathbf{X}_{\text{train},k} & \mathbf{Y}_{\text{train},k} \\ m_{\min} \times n & m_{\min} \times r \\ \hline \dots & \dots \end{array} \right], \uparrow_k$$

- 3) optimize model parameters \mathbf{w} using $\mathbf{X}_{\text{train},k}$, $\mathbf{Y}_{\text{train},k}$,
- 4) compute residues $\varepsilon_k = \mathbf{y}_{\text{val},k} - \mathbf{f}(\mathbf{x}_{\text{val},k}, \mathbf{w})$ and MAPE,
- 5) increment k and repeat.

Feature generation

Generating extra features

To augment feature description, consider the following types of features:

- 1) the local history of all time series themselves,
- 2) transformations (non-parametric and parametric) of local history,
- 3) parameters of the local models,
- 4) distances to the centroids of local clusters.

Functional transforms

The procedure of generating new features ϕ requires:

- ▶ the original features $\mathbf{x} = \{\mathbf{x}_1, \dots, \mathbf{x}_Q\}$,
- ▶ the set of primitive functions $G = \{g(\mathbf{b}, \mathbf{x})\}$,

$$g : \mathbf{x} \mapsto \phi;$$

- ▶ the generation rules: $\mathcal{G} \supset G$, where the superposition $g_k \circ g_l \in \mathcal{G}$ w.r.t. numbers and types of the input and output arguments;
- ▶ the simplification rules: g_u is not in \mathcal{G} , if there exist a rule

$$r : g_u \mapsto g_v \in \mathcal{G}.$$

The result is

the set of the features $\mathbf{x} = \{\mathbf{x}_1, \dots, \mathbf{x}_Q, \phi_1, \dots, \phi_N\}$.

Examples of nonparametric transformation functions

► Univariate

Formula	Output dimension
\sqrt{x}	1
$x\sqrt{x}$	1
$\arctan x$	1
$\ln x$	1
$x \ln x$	1

► Bivariate

Plus	$x_1 + x_2$
Minus	$x_1 - x_2$
Product	$x_1 \cdot x_2$
Division	$\frac{x_1}{x_2}$
	$x_1 \sqrt{x_2}$
	$x_1 \ln x_2$

Nonparametric transformations: sample statistics

Nonparametric transformations include basic data statistics:

- Sum or average value of each row \mathbf{x}_i , $i = 1, \dots, m$:

$$\phi_i = \sum_{j=1}^n x_{ij}, \text{ or } \phi'_i = \frac{1}{n} \sum_{j=1}^n x_{ij}.$$

- Min and max values: $\phi_i = \min_j x_{ij}$, $\phi'_i = \max_j x_{ij}$.
- Standard deviation:

$$\phi_i = \frac{1}{n-1} \sqrt{\sum_{j=1}^n (x_{ij} - \text{mean}(\mathbf{x}_i))^2}.$$

- Data quantiles: $\phi_i = [X_1, \dots, X_K]$, where

$$\sum_{j=1}^n [X_{k-1} < x_{ij} \leq X_k] = \frac{1}{K}, \text{ for } k = 1, \dots, K.$$

Nonparametric transformations: Haar's transform

Applying Haar's transform produces multiscale representations of the same data.

Assume that $n = 2^K$ and init $\phi_{i,j}^{(0)} = \phi'_{i,j}{}^{(0)} = x_{ij}$ for $j = 1, \dots, n$.

To obtain coarse-graining and fine-graining of the input feature vector \mathbf{x}_i , for $k = 1, \dots, K$ repeat:

- data averaging step

$$\phi_{i,j}^{(k)} = \frac{\phi_{i,2j-1}^{(k-1)} + \phi_{i,2j}^{(k-1)}}{2}, \quad j = 1, \dots, \frac{n}{2^k},$$

- and data differencing step

$$\phi'_{i,j}{}^{(k)} = \frac{\phi_{i,2j}^{(k-1)} - \phi_{i,2j-1}^{(k-1)}}{2}, \quad j = 1, \dots, \frac{n}{2^k}.$$

The resulting multiscale feature vectors are $\phi_i = [\phi_i^{(1)}, \dots, \phi_i^{(K)}]$ and $\phi'_i = [\phi'_i{}^{(1)}, \dots, \phi'_i{}^{(K)}]$.

Parametric transformations

Optimization of the transformation function parameters \mathbf{b} is iterative:

1. Fix the vector $\hat{\mathbf{b}}$, collected over all the primitive functions $\{g\}$, which generate features ϕ :

$$\hat{\mathbf{w}} = \arg \min S(\mathbf{w} | \mathbf{f}(\mathbf{w}, \mathbf{x}), \mathbf{y}), \quad \text{where} \quad \phi(\hat{\mathbf{b}}, \mathbf{s}) \subseteq \mathbf{x}.$$

2. Optimize transformation parameters $\hat{\mathbf{b}}$ given model parameters $\hat{\mathbf{w}}$

$$\hat{\mathbf{b}} = \arg \min S(\mathbf{b} | \mathbf{f}(\hat{\mathbf{w}}, \mathbf{x}), \mathbf{y}).$$

Repeat these steps until vectors $\hat{\mathbf{w}}, \hat{\mathbf{b}}$ converge.

Examples of parametric transformation functions

Function name	Formula	Output dim.	Num. of args	Num. of pars
Add constant	$x + w$	1	1	1
Quadratic	$w_2 x^2 + w_1 x + w_0$	1	1	3
Cubic	$w_3 x^3 + w_2 x^2 + w_1 x + w_0$	1	1	4
Logarithmic sigmoid	$1/(w_0 + \exp(-w_1 x))$	1	1	2
Exponent	$\exp x$	1	1	0
Normal	$\frac{1}{w_1 \sqrt{2\pi}} \exp\left(\frac{(x-w_2)^2}{2w_1^2}\right)$	1	1	2
Multiply by constant	$x \cdot w$	1	1	1
Monomial	$w_1 x^{w_2}$	1	1	2
Weibull-2	$w_1 w_2 x^{w_2-1} \exp -w_1 x^{w_2}$	1	1	2
Weibull-3	$w_1 w_2 x^{w_2-1} \exp -w_1 (x - w_3)^{w_2}$	1	1	3
...

Monotone functions

► By grow rate

Function name	Formula	Constraints
Linear	$w_1 x + w_0$	
Exponential rate	$\exp(w_1 x + w_0)$	$w_1 > 0$
Polynomial rate	$\exp(w_1 \ln x + w_0)$	$w_1 > 1$
Sublinear polynomial rate	$\exp(w_1 \ln x + w_0)$	$0 < w_1 < 1$
Logarithmic rate	$w_1 \ln x + w_0$	$w_1 > 0$
Slow convergence	$w_0 + w_1/x$	$w_1 \neq 0$
Fast convergence	$w_0 + w_1 \cdot \exp(-x)$	$w_1 \neq 0$

► Other

Soft ReLu	$\ln(1 + e^x)$	
Sigmoid	$1/(w_0 + \exp(-w_1 x))$	$w_1 > 0$
Softmax	$1/(1 + \exp(-x))$	
Hiberbolic tangent	$\tanh(x)$	
softsign	$\frac{ x }{1+ x }$	

Parameters of the local models

Other options:

- ▶ Parameters of SSA approximation of the time series $\mathbf{x}^{(q)}$.
- ▶ Parameters of the FFT of each $\mathbf{x}^{(q)}$.
- ▶ Parameters of polynomial/spline approximation of each $\mathbf{x}^{(q)}$.

Parameters of the local models: SSA

For the time series \mathbf{s} construct the Hankel matrix with a period k and shift p , so that for $\mathbf{s} = [s_1, \dots, s_T]$ the matrix

$$\mathbf{H}^* = \left[\begin{array}{c|cc} s_T & \dots & s_{T-k+1} \\ \vdots & \ddots & \vdots \\ s_{k+p} & \dots & s_{1+p} \\ s_k & \dots & s_1 \end{array} \right], \text{ where } 1 \geq p \geq k.$$

Reconstruct the regression to the first column of the matrix $\mathbf{H}^* = [\mathbf{h}, \mathbf{H}]$ and denote its least square parameters as the feature vector

$$\phi(\mathbf{s}) = \arg \min \|\mathbf{h} - \mathbf{H}\phi\|_2^2.$$

For the original feature vector $\mathbf{x} = [\mathbf{x}^{(1)}, \mathbf{x}^{(Q)}]$ use the parameters $\phi(\mathbf{x}^{(q)})$, $q = 1, \dots, Q$ as the features.

Metric features: distances to the centroids of local clusters

Apply kernel trick to the time series.

1. For given local feature vector $\mathbf{x}_i^{(q)}$, $q = 1, \dots, Q$ compute k -means centroids $\mathbf{c}_p^{(m)}$, $p = 1, \dots, P$.
2. With the selected k -means distance function ρ construct the feature vector

$$\phi_i^{(q)} = [\rho(\mathbf{c}_1^{(q)}, \mathbf{x}_i^{(q)}), \dots, \rho(\mathbf{c}_P^{(q)}, \mathbf{x}_i^{(q)})] \in \mathbb{R}_+^P.$$

The procedure may be applied to each $\mathbf{x}^{(q)}$ or directly to the $\mathbf{x} = [\mathbf{x}^{(1)}, \dots, \mathbf{x}^{(Q)}]$, resulting in only P additional features instead of $Q \cdot P$

Feature selection

Mixture models

Linear mixture models

Assume the target variable \mathbf{y} is generated by one of K linear models $f_k(\mathbf{x}, \mathbf{w}_k)$. Let the distribution of the target variable \mathbf{y} be a mixture of normal distributions

$$p(\mathbf{y}|\mathbf{x}, \boldsymbol{\theta}) = \sum_{k=1}^K \pi_k \mathcal{N}(\mathbf{y}|\mathbf{w}_k^T \mathbf{x}, \beta) =$$

$$\sum_{k=1}^K \frac{1}{(2\pi\beta_k)^{n/2}} \exp \left(\left(-\frac{1}{2\beta_k} (\mathbf{y} - \mathbf{w}_k^T \mathbf{x})^T (\mathbf{y} - \mathbf{w}_k^T \mathbf{x}) \right) \right).$$

Here $\boldsymbol{\theta}$ denotes the concatenated vector of parameters:

$$\boldsymbol{\theta} = [\mathbf{w}_1, \dots, \mathbf{w}_K, \boldsymbol{\pi}, \beta]^T,$$

where $\boldsymbol{\pi} = [\pi_1, \dots, \pi_K]$ are weights of the models, and $\mathbf{B} = \beta \mathbf{I}_m$ is the covariance matrix for \mathbf{y} .

Parameter estimation

To find maximum likelihood estimates of $\hat{\theta}$

$$\hat{\theta} = \arg \max_{\theta} \ln p(\mathbf{y}|\theta),$$

introduce hidden indicator variables $Z = [\mathbf{z}_1, \dots, \mathbf{z}_m]$, $z_{ik} \in \{0, 1\}$, such that

$$z_{ik} = 1 \Leftrightarrow y_i \sim \mathcal{N}(\mathbf{w}_k^T \mathbf{x}_i, \beta).$$

Then the loglikelihood function $p(\mathbf{y}, Z|X, \theta)$ takes the form

$$p(\mathbf{y}|X, Z, \theta) = \sum_{i=1}^m \sum_{k=1}^K z_{ik} (\ln \pi_k + \ln \mathcal{N}(y_i|\mathbf{w}_k^T \mathbf{x}_i, \beta)).$$

EM-algorithm: instead of $p(\mathbf{y}|X, \theta)$ maximize the expected loglikelihood $E_Z[p(\mathbf{y}, Z|X, \theta)]$ of the observed data.

Expectation step

Expectation-Maximization algorithm maximizes $E_Z[p(\mathbf{y}, Z|X, \boldsymbol{\theta})]$, updating parameters estimates $\boldsymbol{\theta}^{(r+1)}$ in two iterative steps with $\boldsymbol{\theta}^{(r)}$ fixed.

E-step: obtain $E(Z) = [\gamma_{ik}]$. Using Bayesian rule, obtain:

$$\gamma_{ik}^{(r+1)} = E(z_{ik}) = p(k|\mathbf{x}_i, \boldsymbol{\theta}^{(r)}) = \frac{\pi_k \mathcal{N}(y_i|\mathbf{x}_i^T \mathbf{w}_k^{(r)}, \beta^{(r)})}{\sum_{k'=1}^K \pi_{k'} \mathcal{N}(y_i|\mathbf{x}_i^T \mathbf{w}_{k'}^{(r)}, \beta^{(r)})}.$$

Define expectations of joint loglikelihood $\ln p(\mathbf{y}, Z|X, \boldsymbol{\theta})$ with respect to the posteriors distribution $p(Z|\mathbf{y}, \boldsymbol{\theta})$

$$Q^{(r)}(\boldsymbol{\theta}) = E_Z(\ln p(\mathbf{y}, Z|\boldsymbol{\theta})) = \sum_{i=1}^m \sum_{k=1}^K \gamma_{ik}^{(r+1)} \left(\ln \pi_k^{(r)} + \ln \mathcal{N}(y_i|\mathbf{x}_i^T \mathbf{w}_k^{(r)}, \beta^{(r)}) \right)$$

Maximization step

Expectation-Maximization algorithm maximizes $E_Z[p(\mathbf{y}, Z|X, \boldsymbol{\theta})]$, updating parameters estimates $\boldsymbol{\theta}^{(r+1)}$ in two iterative steps with $\boldsymbol{\theta}^{(r)}$ fixed.

M-step: update parameters $\boldsymbol{\theta}$, maximizing $Q^{(r)}(\boldsymbol{\theta}) = E_Z(\ln p(\mathbf{y}, Z|\boldsymbol{\theta}))$ with respect to $\boldsymbol{\theta}$ with $\gamma^{(r+1)}$ fixed:

$$\pi_k^{(r+1)} = \frac{1}{n} \sum_{i=1}^m \gamma_{ik}^{(r+1)}.$$

$$\mathbf{w}_k^{(r+1)} = \arg \max_{\mathbf{w}_k} \sum_{i=1}^m -\gamma_{ik}^{(r+1)} (y_i - \mathbf{w}_k^T \mathbf{x}_i)^2,$$

$$\beta_k^{(r+1)} = \arg \max_{\beta} \sum_{i=1}^m \gamma_{ik}^{(r+1)} \left(n \ln \beta - \frac{1}{\beta} (y_i - \mathbf{x}_i^T \mathbf{w}_k^{(r+1)})^2 \right).$$

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Mixture of Experts

Suppose that each model $f(\mathbf{x}, \mathbf{w}_k)$ generates a sample (\mathbf{x}, y) with some probability $p(k|\mathbf{x}, \mathbf{w})$. Then the following factorization holds

$$p(y|\mathbf{x}, \boldsymbol{\theta}) = \sum_{k=1}^K p(y, k|\mathbf{x}, \boldsymbol{\theta}) = \sum_{k=1}^K p(k|\mathbf{x}, \boldsymbol{\theta}) p(y|k, \mathbf{x}, \boldsymbol{\theta})$$

for $p(y|\mathbf{x}, \boldsymbol{\theta})$.

Here $p(k|\mathbf{x}, \boldsymbol{\theta})$ correspond to weight parameters π_k in mixture models dependent on the inputs \mathbf{x} :

$$\pi_k(\mathbf{x}, \mathbf{v}_k) = \frac{\exp(\mathbf{v}_k^T \mathbf{x})}{\sum_{k'=1}^K \exp(\mathbf{v}_{k'}^T \mathbf{x})}.$$

Parameter's estimation via EM differs only in M-step.

EM for Mixture of experts

E-step: compute hidden variables $\gamma_{ik}^{(r+1)}$, the expectation of the indicator variables, as previously shown.

M-step: find new parameter estimates

$$\mathbf{v}_k^{(r+1)} = \arg \max_{\mathbf{v}} \sum_{i=1}^m \gamma_{ik}^{(r+1)} \ln \pi_k(\mathbf{x}_i, \mathbf{v}),$$

$$\mathbf{w}_k^{(r+1)} = \arg \max_{\mathbf{w}_k} \left[- \sum_{i=1}^m \gamma_{ik}^{(r+1)} (y_i - \mathbf{w}_k^T \mathbf{x}_i)^2 \right],$$

$$\beta_k^{(r+1)} = \arg \max_{\beta} \left[n \ln \beta - \frac{1}{\beta} \left(y_i - \mathbf{x}_i^T \mathbf{w}_k^{(r+1)} \right)^2 \right].$$

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$$\beta_k^{(r+1)} = \arg \max_{\beta} \left[n \ln \beta - \frac{1}{\beta} \left(y_i - \mathbf{x}_i^T \mathbf{w}_k^{(r+1)} \right)^2 \right].$$

Resampling time series

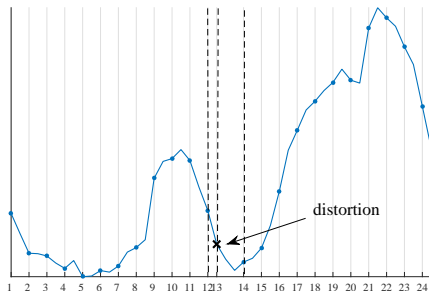
Resampling

The sampling rate might be changing over time, specifically

1. The initial sampling rate is approximately even, but distortions are possible:

$$t_i = i \cdot \tau + \delta_i, |\delta_i| < \frac{\tau}{2}.$$

In this case the number T_s of resampled observations equals the initial number of observations T .

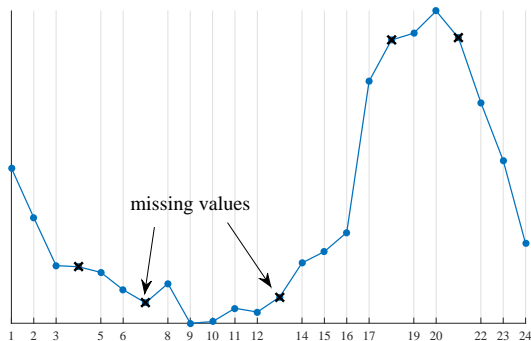


Resampling

2. The sampling rate is even, but some values are missing:

$$|t_{i+1} - t_i| = n\tau, n \in \mathbb{N}.$$

Here $\tau_s = \tau$ and missing values are the only ones that one needs to approximate.

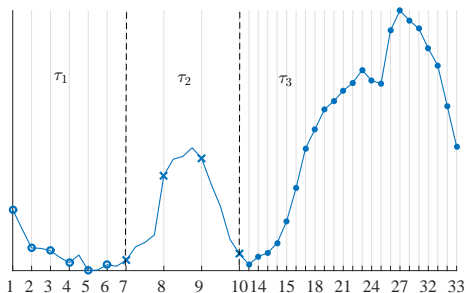


Resampling

3. Time series \mathbf{s} comprises a finite number of intervals \mathbf{s}_k , each sampled from $s(t)$ at fixed sampling rate:

$$\mathbf{s} = \left[s(\tau_1), \dots, s(T_1\tau_1), s(T_1\tau_1 + \tau_2), \dots, s\left(\sum_k T_k\tau_k\right) \right],$$

where $\sum_k T_k = T$. Here we select the maximum sampling rate $f_s = \max_k \frac{1}{\tau_k}$ and upsample the rest time series, using piecewise constant approximation.



Resampling

Piece-wise constant approximation of missing values:

