

8 Puzzle Problem

$$f = g + h$$

Definition 1.

$g(n)$ = number of moves taken in going from S_I to S .

$h_1(n)$ = number of tiles in S in the “wrong position”

S_I :

2	8	3
1	6	4
7		5

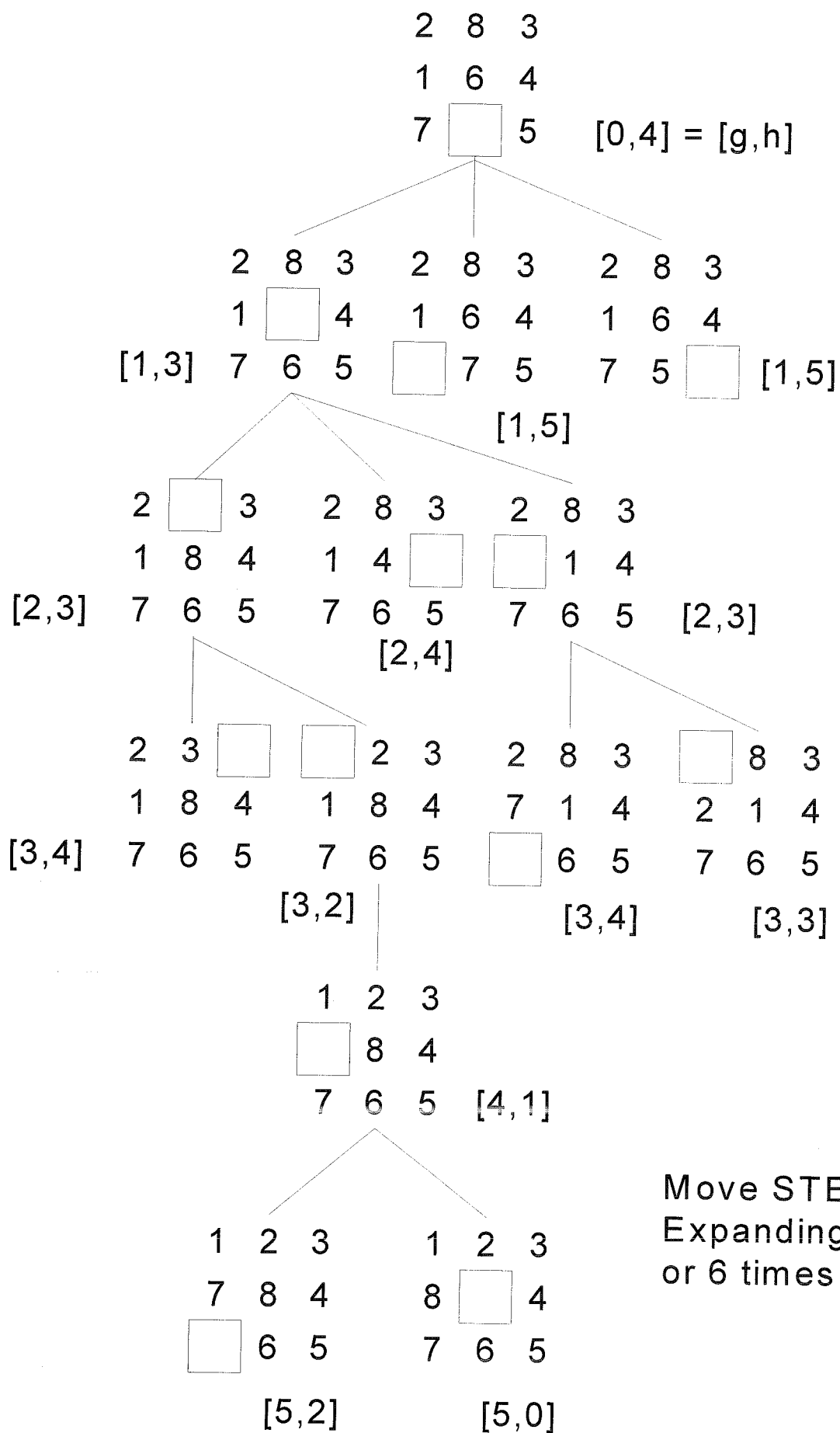
S_F :

1	2	3
8		4
7	6	5

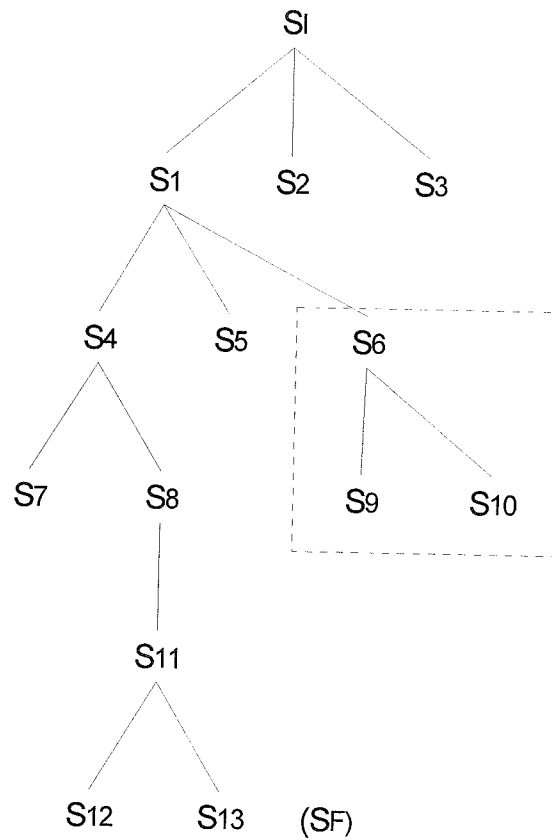
$$S_I \neq S_F$$

Question: Is h_1 admissible?

$$h_1 \leq h^*$$



Move STEPs = 5
Expanding Nodes = 5
or 6 times



Queue:

SI

S1	S2	S3
f=4	f=6	f=6

S4	S6	S5	S2	S3
f=5	f=5	f=6	f=6	f=6

or

S6	S4	S5	S2	S3
f=5	f=5	f=6	f=6	f=6

S8	S6	S5	S2	S3	S7
f=5	f=5	f=6	f=6	f=6	f=7

S4	S5	S2	S3	S10	S9
f=5	f=6	f=6	f=6	f=6	f=7

S11	S6	S5	S2	S3	S7
f=5	f=5	f=6	f=6	f=6	f=7

S8	S5	S2	S3	S10	S9	S7
f=5	f=6	f=6	f=6	f=6	f=7	f=7

S13	S6	S5	S2	S3	S7	S12
f=5	f=5	f=6	f=6	f=6	f=7	f=7

S11	S5	S2	S3	S10	S9	S7
f=5	f=6	f=6	f=6	f=6	f=7	f=7

↑
SF

S13	S5	S2	S3	S10	S9	S7	S12
f=5	f=6	f=6	f=6	f=6	f=7	f=7	f=7

↑
SF

Definition 2.

$$f = g + h_2$$

$g(n)$ = number of moves taken in going from S_I to S .
(node n)

$h_2(n)$ = sum of the distances of the tiles from S_F position.

S_I :

2	8	3
1	6	4
7		5

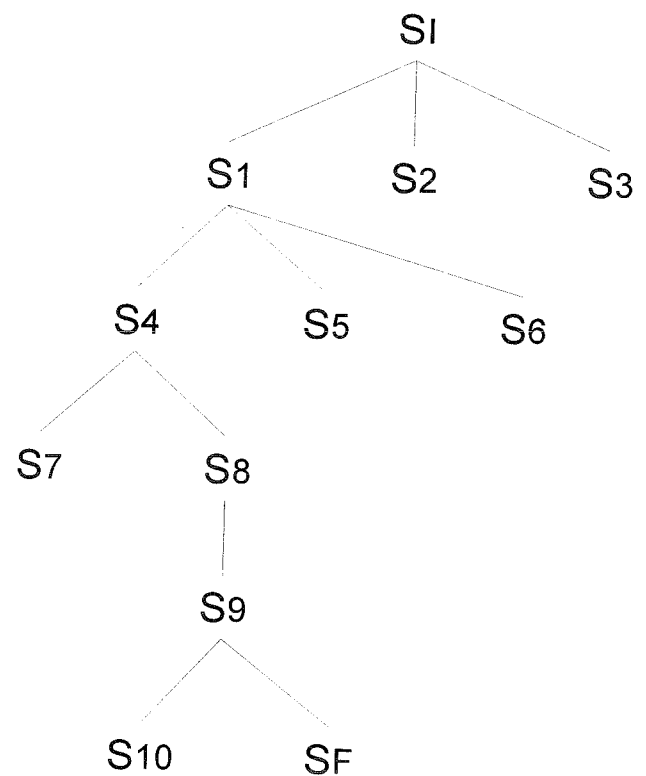
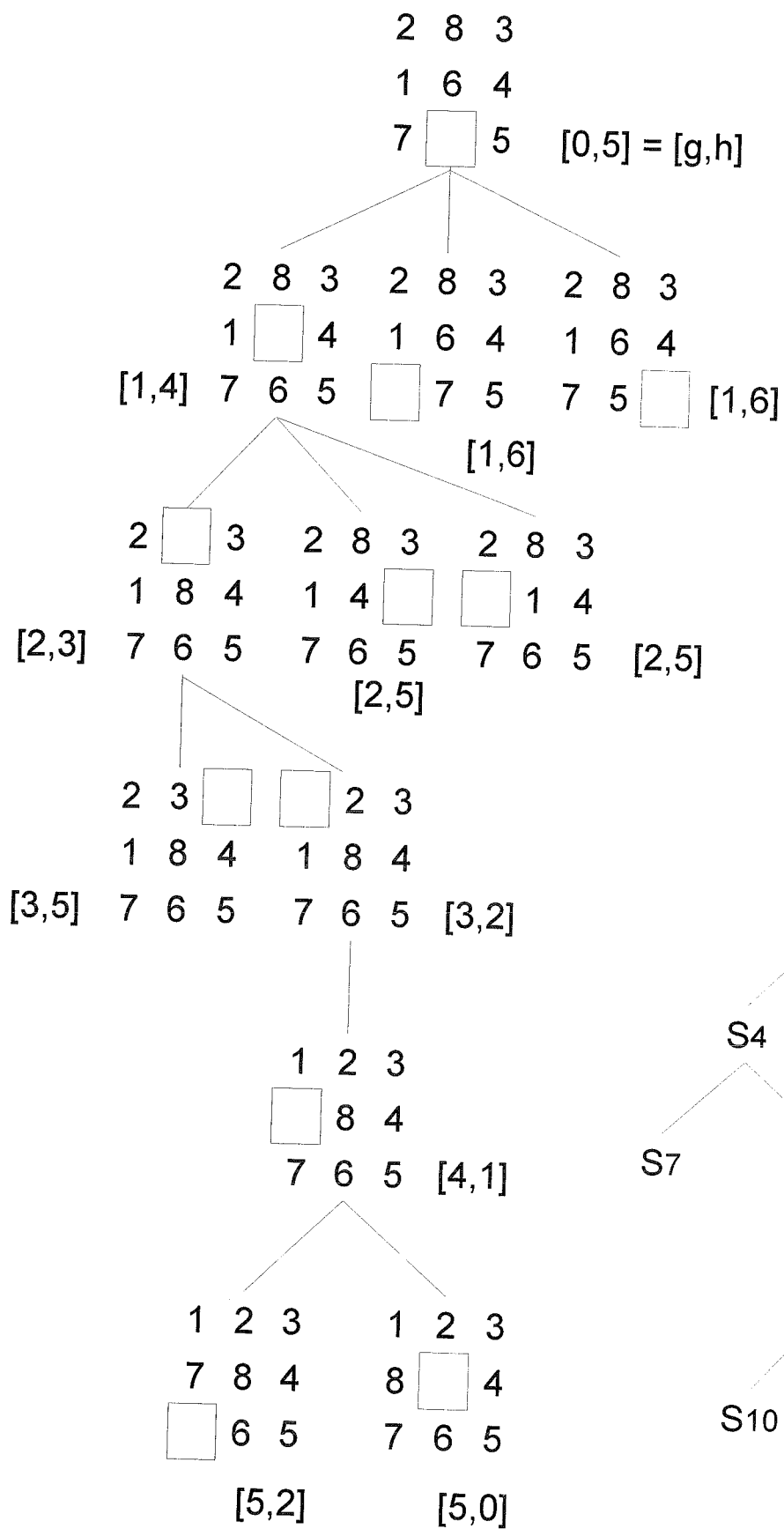
S_F :

1	2	3
8		4
7	6	5

$$S_I \Rightarrow S_F$$

Question: Is h_2 admissible?

$$h_1 \leq h_2 \leq h^*$$



Move STEPs = 5
Expanding Nodes = 5 times

Queue:

S1

S1 f=5	S2 f=7	S3 f=7
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S4 f=5	S5 f=7	S6 f=7	S2 f=7	S3 f=7
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S8 f=5	S5 f=7	S6 f=7	S2 f=7	S3 f=7	S7 f=8
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S9 f=5	S5 f=7	S6 f=7	S2 f=7	S3 f=7	S7 f=8
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S11 f=5	S10 f=7	S5 f=7	S6 f=7	S2 f=7	S3 f=7	S7 f=8
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▲
SF