Code Template for ACM-ICPC

zzuzxy

September 26, 2018

Contents

1	1数	据结构	1
	1.1	二叉树.cpp	1
	1.2	堆.cpp	2
	1.3	字符串	3
		1.3.1 1 Trie(前缀树).cpp	3
		1.3.2 2 KMP.cpp	4
		1.3.3 3 AC 自动机.cpp	5
		1.3.4 4 KMP-KMP 变形.cpp	6
		1.3.5 5 字符串 hash.cpp	8
		1.3.6 6 后缀数组.cpp	9
2			10
	2.1	1 最长上升子序列.cpp	10
9	3 图	∤ &	10
3			10 10
	3.1		10
		3.1.2 2. 无向图的双连通分量.cpp	13
			14
			15
	3.2		16
	5.2		16
		· • • II	18
	3.3		19
	5.5		19
			22
		11	$\frac{22}{25}$
	3.4		$\frac{20}{27}$
	0.4		27
			28
	3.5		29
	0.0		29
			30
		1 211 11	32
			35
	3.6		38
			38
			41
			43
4	4数		44
	4.1	3 FWT 模板.cpp	44
	4.2		44
		11	44
		0 11	45
		4.2.3 lrj.cpp	48
	4.3		49
	4.4		50
			50
			51
			52
			53
		4.4.5 4 除法.cpp	53

		4.4.6	Euler.cpp	54
		4.4.7	lucas ,组合数.cpp	54
		4.4.8	miller-rabin-Pollard-rho.cpp	55
		4.4.9	快速数论变换.cpp	58
		4.4.10	欧拉筛和埃氏筛.cpp	59
		4.4.11	素性检测.cpp	59
		4.4.12	素数筛.cpp	61
			逆元打表.cpp	62
	4.5		tikasa.cpp	62
	4.6		Z辛普森积分.cpp	
		–		
5	5 几	.何		63
	5.1	2D		63
		5.1.1	PSLG.cpp	63
		5.1.2	二维几何模板.cpp	65
		5.1.3	二维凸包.cpp	68
		5.1.4	判断点是否在多边形内.cpp	68
		5.1.5	圆与多边形相交的面积.cpp	69
		5.1.6	求圆与直线的交点.cpp	73
	5.2	3D		73
		5.2.1	三维几何的基本操作.cpp	73
		5.2.2	三维几何的模版.cpp	75
		5.2.3	三维凸包.cpp	77
		5.2.4	维度转换为三维坐标.cpp	79
6	6 其	_		7 9
	6.1			
		6.1.1	fread.cpp	79
		6.1.2	fread2.cpp	80
		6.1.3	保留小数.cpp	82
		6.1.4	读取整数.cpp	83
	6.2	c++ =	中处理 2 进制的一些函数.cpp	83
	6.3	测量程	是序的运行时间.cpp	84

1 1数据结构

1.1 二叉树.cpp

```
// 通过中序遍历和后序遍历建立二叉树
//https://vjudge.net/problem/UVA-548
#include<bits/stdc++.h>
using namespace std;
const int maxn = 1e5+10;
const int INF = 1e8;
int in_order[maxn],post_order[maxn],l[maxn],r[maxn];
int read_order(int *a)
    string s;
    if(!getline(cin,s)) return false;
    stringstream ss(s);
    n = 0;
    int v;
    while(ss >> v)
       a[n++] = v;
    return n > 0;
}
int build_tree(int L1,int R1,int L2,int R2)
{
    if(L1 > R1)
       return 0;
    int root = post_order[R2];
    int p = L1;
    while(in_order[p] != root)
        p++;
    int cnt = p-L1;
    l[root] = build_tree(L1,p-1,L2,L2+cnt-1);
    r[root] = build_tree(p+1,R1,L2+cnt,R2-1);
    return root;
}
int best, bestsum;
void dfs(int a,int b)
{
    if(!l[a] && !r[a])
    {
       b += a;
        if(bestsum > b||(bestsum == b&&best > a))
            best = a;
            bestsum = b;
        }
    }
    if(l[a]) dfs(l[a],b+a);
    if(r[a]) dfs(r[a],b+a);
}
```

```
int main(void)
    while(read_order(in_order))
        read_order(post_order);
        build_tree(0,n-1,0,n-1);
          cout << 0 << end l;
        bestsum = INF;
        dfs(post_order[n-1],0);
        cout<<best<<endl;</pre>
    return 0;
}
1.2 堆.cpp
// 堆的插入和删除操作
void Insert(int vv)
    int t = sz++;
    h[t] = vv;
    while(t > 1)
        if(h[t] < h[t/2])
            swap(h[t],h[t/2]);
            t /= 2;
        }
        else break;
    }
}
int Down(int i)
{
    int t;
    while(i * 2 <= n)
        if(h[i] > h[2*i])
            t = 2*i;
        else
            t = i;
        if(i*2+1 \le n\&\&h[i*2+1] < h[t])
          t = i*2+1;
        if(i == t)
            break;
        swap(h[t],h[i]);
        i = t;
    }
}
```

1.3 字符串

1.3.1 1 Trie(前缀树).cpp

```
const int maxnode = 4e5+100;
const int sigma_size = 26;
struct Trie
    int ch[maxnode][sigma_size];
    int val[maxnode];
    int sz;
    Trie()
        sz = 1;
        memset(ch[0],0,sizeof(ch[0]));
    }
    int idx(char c)
    {
        return c-'a';
    }
    void init(void)
        memset(ch,0,sizeof(ch));
        memset(val,0,sizeof(val));
    }
    void insert(char *s,int v)
        int u = 0, n = strlen(s);
        for(int i = 0; i < n; ++i)</pre>
            int c = idx(s[i]);
            if(!ch[u][c])
            {
                memset(ch[sz],0,sizeof(ch[sz]));
                val[sz] = 0;
                ch[u][c] = sz++;
            }
            u = ch[u][c];
        val[u] = v;
    }
    int query(char *s,int t)
        int sum = 0;
        int u = 0,n = strlen(s);
        for(int i = 0; i < n; ++i)</pre>
            int c = idx(s[i]);
            if(ch[u][c])
            {
                if(val[ch[u][c]])
                    sum = (sum + ans[i+t+1]) \% mod;
            }
            else
                return sum;
```

```
u = ch[u][c];
        return sum;
    }
};
1.3.2 2 KMP.cpp
#include <bits/stdc++.h>
#define mem(ar, num) memset(ar, num, sizeof(ar))
#define me(ar) memset(ar,0,sizeof(ar))
\#define\ lowbit(x)\ (x \& (-x))
using namespace std;
typedef long long LL;
typedef unsigned long long ULL;
const int
             prime = 999983;
const int
             INF = Ox7FFFFFFF;
const LL
             INFF =0x7FFFFFFFFFFFF;
const double pi = acos(-1.0);
const double inf = 1e18;
const double eps = 1e-6;
const LL mod = 20071027;
int f[1100];
char ch[100];
void getFail(char *P,int *f)
{
    int m = strlen(P);
    f[0] = 0, f[1] = 0;
    for(int i = 1;i < m; ++i)</pre>
        int j = f[i];
        while(j && P[i] != P[j]) j = f[j];
        f[i+1] = P[i] == P[j] ? j + 1: 0;
    }
void find(char * T,char * P,int* f)
    int n = strlen(T),m = strlen(P);
    getFail(P,f);
    int j = 0;
    for(int i = 0; i < n; ++i)
        while(j\&\&P[j] != T[i]) j = f[j];
        if(P[j] == T[i]) j++;
        if(j == m) printf("d\n",i-m+1);
    }
}
int main(void)
    cin>>ch;
```

```
getFail(ch,f);
   printf("%d",f[strlen(ch)-1]);
   return 0;
}
1.3.3 3 AC 自动机.cpp
const int SIGMA_SIZE = 26;
const int MAXNODE = 11000;
const int MAXS = 150 + 10;
struct AhoCorasickAutomata {
  int ch[MAXNODE][SIGMA_SIZE];
                   // fail 函数
  int f[MAXNODE];
  int val[MAXNODE]; // 每个字符串的结尾结点都有一个非 O 的 val
  int last[MAXNODE]; // 输出链表的下一个结点
  int sz;
 void init() {
   sz = 1;
   memset(ch[0], 0, sizeof(ch[0]));
 // 字符 c 的编号
  int idx(char c) {
   return c-'a';
 }
  // 插入字符串。v 必须非 O
  void insert(char *s, int v) {
   int u = 0, n = strlen(s);
   for(int i = 0; i < n; i++) {</pre>
     int c = idx(s[i]);
     if(!ch[u][c]) {
       memset(ch[sz], 0, sizeof(ch[sz]));
       val[sz] = 0;
       ch[u][c] = sz++;
     u = ch[u][c];
   val[u] = v;
  // 递归打印以结点 j 结尾的所有字符串
  void print(int j) {
   if(j) {
     print(last[j]);
 }
  // 在 T 中找模板
  int find(char* T) {
```

```
int n = strlen(T);
   int j = 0; // 当前结点编号, 初始为根结点
   for(int i = 0; i < n; i++) { // 文本串当前指针
      int c = idx(T[i]);
     while(j && !ch[j][c]) j = f[j]; // 顺着细边走, 直到可以匹配
      j = ch[j][c];
     if(val[j]) print(j);
      else if(last[j]) print(last[j]); // 找到了!
   }
  }
  // 计算 fail 函数
  void getFail() {
   queue<int> q;
   f[0] = 0;
    // 初始化队列
   for(int c = 0; c < SIGMA_SIZE; c++) {</pre>
      int u = ch[0][c];
      if(u) { f[u] = 0; q.push(u); last[u] = 0; }
   // 按 BFS 顺序计算 fail
   while(!q.empty()) {
      int r = q.front(); q.pop();
     for(int c = 0; c < SIGMA_SIZE; c++) {</pre>
        int u = ch[r][c];
       if(!u) continue;
       q.push(u);
        int v = f[r];
       while(v \&\& !ch[v][c]) v = f[v];
       f[u] = ch[v][c];
       last[u] = val[f[u]] ? f[u] : last[f[u]];
     }
   }
 }
};
1.3.4 4 KMP-KMP 变形.cpp
//https://www.nowcoder.com/acm/contest/119/E
#include <bits/stdc++.h>
using namespace std;
const int N=200010;
int a[N],b[N];
int x[N],y[N],nxt[N];
void kmp_pre(int x[],int m,int nxt[])
   int i,j;
    j=nxt[0]=-1;
    i=0;
   while(i<m) {</pre>
```

{

```
while (-1!=j \&\& (x[i]!=x[j]\&\&x[j]!=-1)) j=nxt[j];
        nxt[++i]=++j;
    }
}
int KMP_Count(int x[],int m,int y[],int n)
{
//
      for (int i=0; i<n; i++) {
//
          printf("%d ",y[i]);
//
      puts("");
//
//
      for (int i=0; i < m; i++) {
          printf("%d ",x[i]);
//
      puts("");
    int i,j;
    int ans=0;
    kmp_pre(x,m,nxt);
    i=j=0;
    while(i<n) {</pre>
         while (-1!=j \&\& !(y[i]==x[j]||(x[j]==-1\&\&(y[i]==-1||j-y[i]<0)))) \ j=nxt[j]; \\
        j++;
        if(j>=m) {
             ans++;
             j=nxt[j];
        }
    }
    return ans;
}
int main()
{
    int n,m,k;
    scanf("%d%d",&n,&k);
    memset(x,-1,sizeof(x));
    memset(y,-1,sizeof(y));
    map<int,int> pre;
    for (int i=0;i<n;i++) {</pre>
        scanf("%d",&a[i]);
        auto pos=pre.find(a[i]);
        if (pos!=pre.end()) {
            y[i]=i-pos->second;
        pre[a[i]]=i;
    }
    scanf("%d",&m);
    pre.clear();
    for (int i=0;i<m;i++) {</pre>
        scanf("%d",&b[i]);
        auto pos=pre.find(b[i]);
        if (pos!=pre.end()) {
             x[i]=i-pos->second;
        }
```

```
pre[b[i]]=i;
   printf("%d\n",KMP_Count(x,m,y,n));
   return 0;
}
1.3.5 5 字符串 hash.cpp
// 字符串 hash, 查找在字符串中至少出现 k 次的最长字符串
#include<cstdio>
#include<cstring>
#include<algorithm>
using namespace std;
const int maxn = 40000+10;
const int x = 123;
int n,m,pos;
unsigned long long H[maxn],xp[maxn];
unsigned long long Hash[maxn];
int Rank[maxn];
int cmp(const int &a,const int &b){
        return Hash[a] < Hash[b] ||(Hash[a] == Hash[b] &&a <b );
}
int possible(int L){
        int c = 0;
       pos = -1;
        for(int i = 0;i < n-L+1; ++i){</pre>
                Rank[i] = i;
                Hash[i] = H[i]-H[i+L]*xp[L];
        }
        sort(Rank,Rank+n-L+1,cmp);
        for(int i = 0;i < n-L+1; ++i){</pre>
                if(i == 0 | | Hash[Rank[i]] != Hash[Rank[i-1]]) c = 0;
                if(++c >= m) pos = max(pos,Rank[i]);
        return pos >= 0;
}
char s[maxn];
int main(void)
    while((scanf("%d",&m)) == 1\&\&m){
        scanf("%s",s);
       n = strlen(s);
       H[n] = 0;
        for(int i = n-1; i \ge 0; i--) H[i] = H[i+1]*x+(s[i]-'a');
        xp[0] = 1;
        for(int i = 1; i \le n; ++i) xp[i] = xp[i-1]*x;
        if(!possible(1)) printf("none\n");
```

```
else{
           int L = 1,R = n;
       while (R >= L) {
               int M = (R+L)/2;
               if(possible(M)) L = M+1;
               else R = M-1;
       possible(R);
       printf("%d %d\n",R,pos);
   }
  return 0;
}
1.3.6 6 后缀数组.cpp
const int maxn = 1e6 + 10;
struct SuffixArray {
                   // 原始字符数组(最后一个字符应必须是 O, 而前面的字符必须非 O)
 int s[maxn];
 int sa[maxn];
                   // 后缀数组
                  // 名次数组. rank[0] 一定是 n-1, 即最后一个字符
 int rank[maxn];
 int height[maxn]; // height 数组
 int t[maxn], t2[maxn], c[maxn]; // 辅助数组
 int n; // 字符个数
 void clear() { n = 0; memset(sa, 0, sizeof(sa)); }
 // m 为最大字符值加 1。调用之前需设置好 s 和 n
 void build_sa(int m) {
   int i, *x = t, *y = t2;
   for(i = 0; i < m; i++) c[i] = 0;
   for(i = 0; i < n; i++) c[x[i] = s[i]]++;
   for(i = 1; i < m; i++) c[i] += c[i-1];
   for(i = n-1; i >= 0; i--) sa[--c[x[i]]] = i;
   for(int k = 1; k <= n; k <<= 1) {</pre>
     int p = 0;
     for(i = n-k; i < n; i++) y[p++] = i;
     for(i = 0; i < n; i++) if(sa[i] >= k) y[p++] = sa[i]-k;
     for(i = 0; i < m; i++) c[i] = 0;
     for(i = 0; i < n; i++) c[x[y[i]]]++;
     for(i = 0; i < m; i++) c[i] += c[i-1];
     for(i = n-1; i >= 0; i--) sa[--c[x[y[i]]]] = y[i];
     swap(x, y);
     p = 1; x[sa[0]] = 0;
     for(i = 1; i < n; i++)
       x[sa[i]] = y[sa[i-1]] = y[sa[i]] &  y[sa[i-1]+k] = y[sa[i]+k] ? p-1 : p++;
     if(p >= n) break;
     m = p;
   }
 }
 void build_height() {
```

```
int i, j, k = 0;
for(i = 0; i < n; i++) rank[sa[i]] = i;
for(i = 0; i < n; i++) {
   if(k) k--;
   int j = sa[rank[i]-1];
   while(s[i+k] == s[j+k]) k++;
   height[rank[i]] = k;
}
};</pre>
```

//最长上升子序列 The longest increasing sequence

2 2 动态规划

2.1 1 最长上升子序列.cpp

```
template <class It>
int n_lisLength(It begin,It end)
{
   typedef typename iterator_traits<It>::value_type T;
   T inf = 1<<30;
   vector<T> best(end-begin,inf);
   for(It i = begin; i != end; ++i)
        *lower_bound(best.begin(),best.end(),*i) = *i;
   return lower_bound(best.begin(),best.end(),inf) - best.begin();
```

3 3 图论

}

3.1 DFS

3.1.1 1. 无向图的割点和桥.cpp

```
SPF POJ - 1523
// 如果有割点, 那么割点与子节点边就是割边
int dfs(int u,int fa){
   int lowu = pre[u] = ++dfs_clock;
   int child = 0;
   for(int i = 0;i < G[u].size(); ++i){</pre>
        int v = G[u][i];
        if(!pre[v]){
            child++;
            int lowv = dfs(v,u);
            lowu = min(lowu,lowv);
            if(lowv >= pre[u]){
                iscut[u]++;
            }
        else if(pre[v] < pre[u] && v != fa){</pre>
            lowu = min(lowu,pre[v]);
        }
   }
```

```
if(fa < 0 \&\& child == 1) iscut[u] = 0;
    else if(fa < 0&&child >= 2) iscut[u] = child-1;
    return low[u] = lowu;
}
如果要输出去掉割点之后的联通分量的个数,需要谈判根的情况
#include<iostream>
#include<cstdio>
#include < cctype >
#include<cstring>
#include<algorithm>
#include<vector>
#include<stack>
#include<map>
#include<queue>
#include<cmath>
#define mem(ar, num) memset(ar, num, sizeof(ar))
#define me(ar) memset(ar,0,sizeof(ar))
#define lowbit(x) (x \mathcal{E}(-x))
#define Pb push_back
#define FI first
#define SE second
#define rep(i,a,n) for (int i=a; i < n; i++)
#define per(i,a,n) for (int i=n-1;i>=a;i--)
#define IOS ios::sync with stdio(false)
#define DEBUG cout<<endl<<"DEBUG"<<endl;</pre>
using namespace std;
typedef long long LL;
typedef unsigned long long ULL;
           prime = 999983;
const int
const int
           INF = Ox7FFFFFFF;
            INFF =0x7FFFFFFFFFFFF;
const LL
const double pi = acos(-1.0);
const double inf = 1e18;
const double eps = 1e-6;
            mod = 1e9 + 7;
const LL
 \label{local_local_local_local}       LL \ qpow(LL \ a, LL \ b) \\ \{LL \ s=1; while(b>0) \{if(b\&1)s=s*a\%mod; a=a*a\%mod; b>>=1; \} \\ return \ s; \} 
LL gcd(LL a, LL b) {return b?gcd(b, a%b):a;}
int dr[2][4] = \{1,-1,0,0,0,0,-1,1\};
typedef pair<int,int> P;
const int maxn = 1000+100;
// cosnt int maxm = 1e6+100
int pre[maxn];
int dfs clock = 0;
vector<int> G[maxn];
int iscut[maxn];
int low[maxn];
void init(){
    dfs_clock = 1;
    rep(i,1,maxn) G[i].clear();
    me(iscut);
    me(low);
    me(pre);
}
```

```
int dfs(int u,int fa){
    int lowu = pre[u] = ++dfs_clock;
    int child = 0;
    for(int i = 0;i < G[u].size(); ++i){</pre>
        int v = G[u][i];
        if(!pre[v]){
            child++;
            int lowv = dfs(v,u);
            lowu = min(lowu,lowv);
            if(lowv >= pre[u]){
                iscut[u]++;
        }
        else if(pre[v] < pre[u] && v != fa){
            lowu = min(lowu,pre[v]);
        }
    }
    if(fa < 0&&child == 1) iscut[u] = 0;
    else if(fa < 0&&child >= 2) iscut[u] = child-1;
    return low[u] = lowu;
}
// #define Debug
int main(void)
    #ifdef Debug
    freopen("input.txt", "r", stdin);
    freopen("output.txt","w+",stdout);
    #endif
    int kase = 0;
    while(1){
        init();
        int u,v;
        int t = 0;
        while (scanf("%d", &u) == 1 & &u != 0){
          scanf("%d",&v);
          G[u].Pb(v);
          G[v].Pb(u);
        if(t==0)break;
        // rep(i,1,maxn) if(!G[i].empty()){
        // dfs(i,-1);
        // break;
        // }
        dfs(1,-1);
        int num = 0;
        rep(i,1,1001) if(iscut[i]) num++;
        printf("Network #%d\n",++kase);
        if(num > 0)
            rep(i,1,1001) if(iscut[i]){
            printf(" SPF node %d leaves %d subnets\n",i,iscut[i]+1);
```

```
}
       }
        else
            printf(" No SPF nodes\n");
        if(kase) puts("");
   }
   return 0;
}
3.1.2 2. 无向图的双连通分量.cpp
// 无向图的点联通分量
const int maxn= 1000+10;
int pre[maxn],iscut[maxn],bccno[maxn],dfs_clock,bcc_cnt;
vector<int> G[maxn],bcc[maxn];
stack<Edge> S;
int dfs(int u,int fa){
  int lowu = pre[u] = ++dfs_clock;
  int child = 0;
  for(int i = 0;i < G[u].size(); ++i){</pre>
   int v = G[u][i];
   Edge e = (Edge) \{u,v\};
   if(!pre[v]){
      S.push(e);
      child++;
      int lowv = dfs(v,u);
      lowu = min(lowu,lowv);
      if(lowv >= pre[u]){
        iscut[u] = true;
        bcc_cnt++;
       bcc[bcc_cnt].clear();
        for(;;){
          Edge x = S.top(); S.pop();
          if(bccno[x.u] != bcc_cnt) {bcc[bcc_cnt].push_back(x.u); bccno[x.u] = bcc_cnt;}
          if(bccno[x.v] != bcc_cnt) {bcc[bcc_cnt].push_back(x.v); bccno[x.v] = bcc_cnt;}
          if(x.u == u\&\&x.v == v) break;
       }
      }
   }
   else if(pre[v] < pre[u]&&v != fa){</pre>
      S.push(e);lowu = min(pre[v],lowu);
   }
  }
  if(fa < 0&& child == 1) iscut[u] = 0;</pre>
  return lowu;
}
void find_bcc(int n){
  memset(pre,0,sizeof(pre));
  memset(iscut,0,sizeof(iscut));
  memset(bccno,0,sizeof(bccno));
```

```
dfs_clock = bcc_cnt = 0;
 for(int i = 0;i < n; ++i) if(!pre[i]) dfs(i,-1);</pre>
}
//无向图的边-双联通分量
// 第一边 dfs 求出所有的割边, 然后第二边 dfs 求出所有边——双连通分量(不经过割边)
3.1.3 3 有向图的强联通分量.cpp
// tarjan 算法
const int maxn = 2e4+100;
vector<int> G[maxn];
int pre[maxn],lowlink[maxn],sccno[maxn],dfs_clock,scc_cnt;
stack<int> S;
void dfs(int u){
   pre[u] = lowlink[u] = ++dfs_clock;
   S.push(u);
   for(int i = 0;i < G[u].size(); ++i){</pre>
        int v = G[u][i];
        if(!pre[v]){
           dfs(v);
           lowlink[u] = min(lowlink[u],lowlink[v]);
   else if(!sccno[v]){
       lowlink[u] = min(lowlink[u],pre[v]);
    if(lowlink[u] == pre[u]){
       scc_cnt++;
       for(;;){
           int x = S.top(); S.pop();
           sccno[x] = scc_cnt;
           if(x == u) break;
       }
   }
void find_scc(int n){
   dfs_clock= scc_cnt = 0;
   me(sccno),me(pre);
   rep(i,0,n) if(!pre[i]) dfs(i);
// kosaraju
const int maxn = 2e4+100;
vector<int> G[maxn],G2[maxn];
vector<int> S;
int vis[maxn],sccno[maxn],scc_cnt;
void dfs1(int u){
```

```
if(vis[u]) return ;
        vis[u] = 1;
        for(int i = 0;i < G[u].size(); ++i) dfs1(G[u][i]);</pre>
        S.push_back(u);
void dfs2(int u){
        if(sccno[u]) return ;
        sccno[u] = scc_cnt;
          for(int i = 0;i < G2[u].size(); ++i) dfs2(G2[u][i]);</pre>
}
void find_scc(int n){
        scc_cnt = 0;
        S.clear();
        memset(sccno,0,sizeof(sccno));
        memset(vis,0,sizeof(vis));
        for(int i = 0;i < n; ++i) dfs1(i);</pre>
    for(int i = n-1; i >= 0; --i){
            if(!sccno[S[i]]) {
                     scc_cnt++;
                     dfs2(S[i]);
            }
    }
}
3.1.4 4 2-sat 问题.cpp
// O(n*m) 复杂度不确定
const int maxn = 2000 + 10;
struct TwoSAT {
  int n;
  vector<int> G[maxn*2];
  bool mark[maxn*2];
  int S[maxn*2], c;
  bool dfs(int x) {
    if (mark[x^1]) return false;
    if (mark[x]) return true;
    mark[x] = true;
    S[c++] = x;
    for (int i = 0; i < G[x].size(); i++)</pre>
      if (!dfs(G[x][i])) return false;
    return true;
  }
  void init(int n) {
    this->n = n;
    for (int i = 0; i < n*2; i++) G[i].clear();</pre>
    memset(mark, 0, sizeof(mark));
  }
  // x = xval \ or \ y = yval
  void add_clause(int x, int xval, int y, int yval) {
```

```
x = x * 2 + xval;
    y = y * 2 + yval;
    G[x].push_back(y^1); // G[0].Pb(1)
    G[y].push_back(x^1); // G[1].Pb(0);
  bool solve() {
    for(int i = 0; i < n*2; i += 2)
      if(!mark[i] && !mark[i+1]) {
        c = 0;
        if(!dfs(i)) {
          while(c > 0) mark[S[--c]] = false;
          if(!dfs(i+1)) return false;
        }
      }
    return true;
};
3.2 LCA
3.2.1 1 DFS+RMQ.cpp
#include<cstdio>
#include<cstring>
#include<vector>
#include<cmath>
#include<iostream>
using namespace std;
const int maxn = 40000+100;
const int maxlogv = 17;
struct Edge{
        int to,weight;
        Edge(int t,int w):to(t),weight(w){};
};
vector<Edge> G[maxn];
int id[maxn],dis[maxn];
int vs[maxn*2],depth[maxn*2];
int dp[maxn*2][maxlogv];
void dfs(int node,int fa,int d,int &k){
           id[node] = k;
           vs[k] = node;
         depth[k++] = d;
         // dis[node] = distance;
         for(int i = 0;i < G[node].size(); ++i){</pre>
                 Edge &t = G[node][i];
                 if(t.to == fa) continue;
                 dis[t.to] = dis[node]+t.weight;
                 dfs(t.to,node,d+1,k);
        vs[k] = node;
        depth[k++] = d;
         }
}
```

```
void init_rmq(int n){
        for(int i = 0;i < n ; ++i) dp[i][0] = i;</pre>
    for(int j = 1;(1<<j) <= n; ++j){</pre>
             for(int i = 0; i + (1 << j) - 1 < n; ++i){
                     if(depth[dp[i][j-1]] < depth[dp[i+(1<<(j-1))][j-1]])
                              dp[i][j] = dp[i][j-1];
                     else
                              dp[i][j] = dp[i+(1<<(j-1))][j-1];
             }
    }
}
int query(int 1,int r){
        int k = 0;
        while((1 << (k+1)) <= r-l+1) k++;
         if(depth[dp[l][k]] < depth[dp[r-(1<<k)+1][k]])
                  return dp[l][k];
         else
                  return dp[r-(1<<k)+1][k];
}
int lca(int u,int v){
        return vs[query(min(id[u],id[v]),max(id[u],id[v]))];
}
void init(int n){
        int k = 0;
        dfs(0,-1,0,k);
        init_rmq(2*n-1);
}
int main(void){
    int n,m,q;
    while(~scanf("%d%d",&n,&m)){
            for(int i = 0;i < n; ++i) G[i].clear();</pre>
             int u,v,w;
             for(int i = 0;i < m; ++i){</pre>
                     scanf("%d%d%d",&u,&v,&w);
                     u--, v--;
                     G[u].push_back(Edge(v,w));
                     G[v].push_back(Edge(u,w));
             }
             init(n);
             scanf("%d",&q);
             while(q--){
                     int u,v;
                     scanf("%d %d",&u,&v);
                     u--, v--;
                     int f = lca(u,v);
                     printf("%d\n",dis[u]+dis[v]-2*dis[f]);
             }
    }
        return 0;
}
```

3.2.2 2 倍增算法.cpp

```
// POJ1330
// LCA 的倍增算法
#include<vector>
#include<cstdio>
#include<cstring>
using namespace std;
const int maxn = 1e4+100;
const int maxlogv = 14;
vector<int> G[maxn];
int root;
int parent[maxlogv][maxn];
int depth[maxn];
void dfs(int v,int p,int d){
        parent[0][v] = p;
        depth[v] = d;
        for(int i = 0;i < G[v].size(); ++i){</pre>
                if(G[v][i] != p){
                        dfs(G[v][i],v,d+1);
                }
        }
}
void init(int V){
        dfs(root,-1,0);
        for(int k = 0; k+1 < maxlogv; ++k){
                for(int v = 0; v < V; ++v){
                         if(parent[k][v] < 0) parent[k+1][v] = -1;
                         else parent[k+1][v] = parent[k][parent[k][v]];
                }
        }
}
int lca(int u,int v){
        if(depth[u] > depth[v]) swap(u,v);
        for(int k = 0;k < maxlogv; ++k){</pre>
                if(((depth[v] - depth[u]) >> k)& 1){
                        v = parent[k][v];
                }
        if(u == v) return u;
        for(int k = maxlogv-1; k \ge 0; --k){
                if(parent[k][u] != parent[k][v]){
                        u = parent[k][u];
                        v = parent[k][v];
                }
        return parent[0][u];
```

```
}
bool OUT[maxn];
int main(void)
        int T;
    scanf("%d",&T);
    while(T--){
            int n;
            for(int i = 0;i < n; ++i) G[i].clear();</pre>
            memset(OUT,0,sizeof(OUT));
            scanf("%d",&n);
            for(int i = 1;i < n; ++i) {
                    int u,v;
                    scanf("%d %d",&u,&v);
                    u--, v--;
                    G[u].push_back(v);
            OUT[v] = 1;
            for(int i = 0;i < n; ++i) if(!OUT[i]){</pre>
            root = i;
            break;
            }
            init(n);
            int u,v;
            scanf("%d %d",&u,&v);
            u--, v--;
        printf("%d\n",lca(u,v)+1);
    }
   return 0;
}
3.3 Maxflow
3.3.1 1 Dinic.cpp
// dinic
#include <cstdio>//C 语言 io
#include <cstring>//以下是 c 语言常用头文件
#include <cmath>
#include <cstdlib>
#include <ctime>
#include <cctype>
#include <cstring>
#include <cmath>
#include <iostream>//c++IO
#include <sstream>
#include <string>
#include <list>//c++ 常用容器
#include <vector>
#include <set>
#include <map>
#include <queue>
#include <stack>
```

```
#include <algorithm>//c++ 泛型的一些函数
#include <functional>//用来提供一些模版
#define fo0(i,n) for(int i = 0; i < n; ++i)
#define fol(i,n) for(int i = 1; i \le n; ++i)
#define mem(ar,num) memset(ar,num,sizeof(ar))
#define me(ar) memset(ar,0,sizeof(ar))
#define lowbit(x) (x\Im(-x))
using namespace std;
typedef long long LL;
typedef unsigned long long ULL;
const int
            prime = 999983;
            INF = 0x7FFFFFFF;
const int
            INFF =Ox7FFFFFFFFFFFF;
const LL
const double pi = acos(-1.0);
const double inf = 1e18;
const double eps = 1e-6;
const LL
            mod = 1e9 + 7;
const int LEN = 20000+1000;
const int maxn = 1e8;
struct Edge{
 int from, to, cap, flow;
 Edge(int u,int v,int w,int f): from(u),to(v),cap(w),flow(f){}
};
struct Dinic{
  int n,m,s,t;
  vector<Edge> edges;
  vector<int> G[LEN];
  int a[LEN];
  int vis[LEN];
  int d[LEN];
   int cur[LEN];//好吧就是点,代表该点在一次求增广的过程中搜索到了那条边,意思就是从这条边往下肯定搜索不到约
  void init(int n)
  {
      this->n = n;
      for(int i = 0; i < n; ++i)
       G[i].clear();
      edges.clear();
  }
  void Add(int u,int v,int w)
  {
      edges.push_back(Edge(u,v,w,0));
      edges.push_back(Edge(v,u,0,0));
      m = edges.size();
      G[u].push_back(m-2);
      G[v].push_back(m-1);
  }
  bool Bfs(void)//分层
     me(d);
     me(vis);
     d[s] = 0;
     vis[s] = 1;
     queue<int> Q;
```

```
Q.push(s);
   while(!Q.empty())
       int q = Q.front();Q.pop();
       for(size_t i = 0;i < G[q].size();++i)</pre>
           Edge &tmp = edges[G[q][i]];
           if(!vis[tmp.to]&&tmp.cap>tmp.flow)
           {
                vis[tmp.to] = 1;
                d[tmp.to] = d[q] + 1;
                Q.push(tmp.to);
       }
   }
   return vis[t];
}
int Dfs(int node,int a)
{
    if(node == t | |a == 0)
     return a;
    int flow = 0,f;
    for(int &i = cur[node];i < G[node].size();++i)</pre>
       Edge &tmp = edges[G[node][i]];
       if(d[tmp.to] == d[node] + 1 \&\& (f = Dfs(tmp.to,min(a,tmp.cap-tmp.flow))) > 0)
           flow += f;
           tmp.flow += f;
           edges[G[node][i]^1].flow -= f;
           a -= f;
           if(a==0)
             break;
       }
    }
    return flow;
}
int MaxFlow(int s,int t)
{
    this->s = s;
    this->t = t;
    int flow = 0;
    while(Bfs())
    {
        me(cur);
        flow += Dfs(s,maxn);
    }
    return flow;
}
```

```
};
Dinic dinic;
int main()
{
   int N,M,S,T;
   while(cin>>N>>M)
       S = 1, T = N;
       dinic.init(N);
       int u, v, w;
       for(int i = 0; i < M; ++i)
           scanf("%d %d %d",&u,&v,&w);
           dinic.Add(u,v,w);
       }
       int ans = 0;
       ans = dinic.MaxFlow(S,T);
       printf("%d\n",ans);
   }
   return 0;
}
3.3.2 2 ISAP.cpp
// 点的下标从零开始, 注意初始化
#include<cstdio>
#include<cstring>
#include<queue>
#include<vector>
#include<algorithm>
using namespace std;
const int maxn = 10000 + 10;
const int INF = 1000000000;
struct Edge {
  int from, to, cap, flow;
};
bool operator < (const Edge& a, const Edge& b) {</pre>
 return a.from < b.from || (a.from == b.from && a.to < b.to);
}
struct ISAP {
  int n, m, s, t;
 vector<Edge> edges;
 vector<int> G[maxn]; // 邻接表, G[i][j] 表示结点 i 的第 j 条边在 e 数组中的序号
                        // BFS 使用
 bool vis[maxn];
                        // 从起点到 i 的距离
  int d[maxn];
  int cur[maxn];
                       // 当前弧指针
```

```
// 可增广路上的上一条弧
int p[maxn];
int num[maxn];
                      // 距离标号计数
void AddEdge(int from, int to, int cap) {
  edges.push_back((Edge){from, to, cap, 0});
  edges.push_back((Edge){to, from, 0, 0});
  m = edges.size();
  G[from].push_back(m-2);
  G[to].push_back(m-1);
bool BFS() {
  memset(vis, 0, sizeof(vis));
  queue<int> Q;
  Q.push(t);
  vis[t] = 1;
  d[t] = 0;
  while(!Q.empty()) {
    int x = Q.front(); Q.pop();
    for(int i = 0; i < G[x].size(); i++) {</pre>
      Edge& e = edges[G[x][i]^1];
      if(!vis[e.from] && e.cap > e.flow) {
        vis[e.from] = 1;
        d[e.from] = d[x] + 1;
        Q.push(e.from);
      }
   }
  }
  return vis[s];
void init(int n) {
  this->n = n;
  for(int i = 0; i < n; i++) G[i].clear();</pre>
  edges.clear();
int Augment() {
  int x = t, a = INF;
  while(x != s) {
    Edge& e = edges[p[x]];
    a = min(a, e.cap-e.flow);
    x = edges[p[x]].from;
  }
  x = t;
  while(x != s) {
    edges[p[x]].flow += a;
    edges[p[x]^1].flow -= a;
    x = edges[p[x]].from;
  }
  return a;
}
```

```
int Maxflow(int s, int t) {
    this->s = s; this->t = t;
    int flow = 0;
    BFS();
    memset(num, 0, sizeof(num));
    for(int i = 0; i < n; i++) num[d[i]]++;</pre>
    int x = s;
    memset(cur, 0, sizeof(cur));
    while(d[s] < n) {
      if(x == t) {
        flow += Augment();
        x = s;
      }
      int ok = 0;
      for(int i = cur[x]; i < G[x].size(); i++) {</pre>
        Edge& e = edges[G[x][i]];
        if(e.cap > e.flow && d[x] == d[e.to] + 1) { // Advance}
          ok = 1;
          p[e.to] = G[x][i];
          cur[x] = i; // 注意
          x = e.to;
          break;
      }
      if(!ok) { // Retreat
        int m = n-1; // 初值注意
        for(int i = 0; i < G[x].size(); i++) {</pre>
          Edge& e = edges[G[x][i]];
          if(e.cap > e.flow) m = min(m, d[e.to]);
        if(--num[d[x]] == 0) break;
        num[d[x] = m+1]++;
        cur[x] = 0; // 注意
        if(x != s) x = edges[p[x]].from;
      }
    }
    return flow;
};
ISAP g;
int main() {
int N,M;
int S,T;
 scanf("%d %d",&N,&M);
 scanf("%d %d",&S,&T);
 int u,v,w;
 g.init(N);
 while(M--){
         scanf("%d %d %d",&u,&v,&w);
```

```
u--, v--;
   g.AddEdge(u,v,w);
}
printf("%d",g.Maxflow(S-1,T-1));
 return 0;
}
3.3.3 3 MCMF.cpp
// 最小费用最大流, 下标从 1 开始
#include <bits/stdc++.h>
#define mem(ar,num) memset(ar,num,sizeof(ar))
#define me(ar) memset(ar,0,sizeof(ar))
#define lowbit(x) (x \otimes (-x))
#define Pb push_back
#define FI first
#define SE second
#define For(i,a,b) for(int i = a; i < b; ++i)
#define IOS ios::sync_with_stdio(false)
using namespace std;
typedef long long LL;
typedef unsigned long long ULL;
const int
            prime = 999983;
const int
            INF = 1e8;
           INFF =0x7FFFFFFFFFFFF;
const LL
const double pi = acos(-1.0);
const double inf = 1e18;
const double eps = 1e-6;
const LL
           mod = 1e9 + 7;
LL qpow(LL a,LL b){LL s=1; while(b>0){if(b&1)s=s*a%mod;a=a*a%mod;b>>=1;}return s;}
LL gcd(LL a,LL b) {return b?gcd(b,a%b):a;}
int dr[2][4] = \{1,-1,0,0,0,0,-1,1\};
typedef pair<int,int> P;
struct Edge{
   int from, to, cap, flow, cost;
};
const int maxn = 5000+100;
struct MCMF{
        int n,m,s,t;
        vector<Edge> edges;
        vector<int> G[maxn];
        int inq[maxn];
        int d[maxn];
        int p[maxn];
        int a[maxn];
        void init(int n){
                this->n = n;
                for(int i = 0;i < n; ++i) G[i].clear();</pre>
                edges.clear();
        void AddEdge(int from,int to,int cap,int cost){
```

```
edges.push_back((Edge){to,from,0,0,-cost});
                int m = edges.size();
                G[from].push_back(m-2);
                G[to].push_back(m-1);
        bool BellmanFord(int s,int t,int &flow,int &cost){
                for(int i = 0;i < n; ++i) d[i] = INF;</pre>
                memset(inq,0,sizeof(inq));
                d[s] = 0, inq[s] = 1; p[s] = 0, a[s] = INF;
                queue<int> Q;
                Q.push(s);
                while(!Q.empty()){
                         int u = Q.front(); Q.pop();
                         inq[u] = 0;
                         for(int i = 0;i < G[u].size(); ++i){</pre>
                                 Edge& e = edges[G[u][i]];
                                 if(e.cap > e.flow \&\&d[e.to] > d[u]+e.cost){
                                         d[e.to] = d[u]+e.cost;
                                         p[e.to] = G[u][i];
                                         a[e.to] = min(a[u],e.cap-e.flow);
                                         if(!inq[e.to]) {
                                                  Q.push(e.to); inq[e.to] = 1;
                                         }
                                 }
                         }
                }
                if(d[t] == INF) return false;
                flow += a[t];
                cost += d[t]*a[t];
                int u = t;
                while(u != s){
                         edges[p[u]].flow += a[t];
                         edges[p[u]^1].flow -= a[t];
                         u = edges[p[u]].from;
                }
                return true;
        int Mincost(int s,int t,int &flow,int &cost){
                 flow = 0, cost = 0;
                while(BellmanFord(s,t,flow,cost));
                return cost;
        }
};
MCMF mcmf;
int main(void)
{
```

edges.push_back((Edge){from,to,cap,0,cost});

```
int n,m,s,t;
        scanf("%d %d %d",&n,&m,&s,&t);
        int u,v,w,c;
        mcmf.init(n+1);
        while(m--){
                scanf("%d %d %d",&u,&v,&w,&c);
                mcmf.AddEdge(u,v,w,c);
        }
    int flow,cost;
    flow = 0, cost = 0;
    mcmf.Mincost(s,t,flow,cost);
        printf("%d %d\n",flow,cost);
   return 0;
}
3.4 二分图
3.4.1 KM.cpp
const int maxn = 500+5;
struct KM{
        int n;
        vector<int> G[maxn];
        int W[maxn][maxn];
        int Lx[maxn];
        int Ly[maxn];
        int Left[maxn];
        bool S[maxn],T[maxn];
        void init(int n){
                this->n = n;
                for(int i = 1;i <= n; ++i) G[i].clear();</pre>
                memset(W,0,sizeof(W));
        }
        void AddEdge(int u,int v,int w){
                G[u].push_back(v);
                W[u][v] = w;
        bool match(int u){
                S[u] = true;
                for(int i =0;i < G[u].size(); ++i){</pre>
                        int v = G[u][i];
                        if(Lx[u]+Ly[v] == W[u][v]&&!T[v]){
                                T[v] = true;
                                 if(Left[v] == -1||match(Left[v])){
                                    Left[v] = u;
                                    return true;
                                }
                        }
                }
                return false;
        void update(){
                int a = INF;
```

```
for(int u = 0; u < n; ++u)
                 if(S[u])
                   for(int i = 0;i < G[u].size(); ++i){</pre>
                           int v = G[u][i];
                           if(!T[v])
                             a = min(a,Lx[u]+Ly[v]-W[u][v]);
                for(int i = 0; i < n; ++i){
                        if(S[i]) Lx[i] -= a;
                        if(T[i]) Ly[i] += a;
                }
        }
        void solve(){
                for(int i = 0; i < n; ++i){
                        Lx[i] = *max_element(W[i],W[i]+n);
                        Left[i] = -1;
                        Ly[i] = 0;
                }
                for(int u = 0; u < n; ++u){
                        for(;;){
                                for(int i = 0; i < n; ++i) S[i] = T[i] = 0;
                                if(match(u)) break;
                                else update();
                        }
                }
        }
};
3.4.2 匈牙利算法.cpp
#include <bits/stdc++.h>
#define mem(ar, num) memset(ar, num, sizeof(ar))
#define me(ar) memset(ar,0,sizeof(ar))
#define lowbit(x) (x \otimes (-x))
#define Pb push_back
#define FI first
#define SE second
#define For(i,a,b) for(int i = a; i < b; ++i)
#define IOS ios::sync_with_stdio(false)
using namespace std;
typedef long long LL;
typedef unsigned long long ULL;
const int
            prime = 999983;
            INF = Ox7FFFFFF;
const int
           INFF =0x7FFFFFFFFFFFF;
const LL
const double pi = acos(-1.0);
const double inf = 1e18;
const double eps = 1e-6;
             mod = 1e9 + 7;
const LL
LL qpow(LL a,LL b){LL s=1; while(b>0){if(b&1)s=s*a%mod;a=a*a%mod;b>>=1;}return s;}
LL gcd(LL a, LL b) {return b?gcd(b, a%b):a;}
int dr[2][4] = \{1,-1,0,0,0,0,-1,1\};
typedef pair<int,int> P;
const int maxn = 1000+10;
```

```
vector<int> G[maxn];
int match[maxn];
bool used[maxn];
int N,M;
bool dfs(int v){
        used[v] = true;
        for(int i = 0;i < G[v].size(); ++i){</pre>
                int u = G[v][i],w = match[u];
                if(w < 0 | | !used[w] \&\&dfs(w)) {
                        match[v] = u;
                        match[u] = v;
                        return true;
                }
        }
        return false;
int main(void)
    scanf("%d %d",&N,&M);
    while(M--){
            int u,v;
            scanf("%d %d",&u,&v);
            G[u].Pb(v);
            G[v].Pb(u);
        }
        int ans = 0;
        memset(match,-1,sizeof(match));
        for(int i = 1;i <= N; ++i){</pre>
                if(match[i] < 0){</pre>
                        memset(used,0,sizeof(used));
                         if(dfs(i)){
                                 ans++;
                         }
                }
        }
   cout<<ans<<endl;</pre>
   return 0;
}
3.5 最小生成树
3.5.1 1 Krustral 卡鲁斯卡尔算法.cpp
复杂度 E*log(E), 适用于稀疏图
https://vjudge.net/problem/HDU-1863
#include<bits/stdc++.h>
using namespace std;
const int maxn = 100+100;
```

```
struct Edge//边
{
   int from, to, cost;
   bool operator< ( const Edge & a)</pre>
       return cost < a.cost;</pre>
   }
};
Edge edge[maxn];
int F[maxn];
int Find(int x)//并查集算法
   return x == F[x] ? x:F[x] = Find(F[x]);
}
int main(void)
   int N,M;
   while(cin>>N>>M&&N)// N 代表的是道路数量, M 代表村庄的数量
       for(int i = 0; i <= M; ++i)</pre>
           F[i] = i;
       for(int i = 0; i < N; ++i)</pre>
            Edge &t = edge[i];
           scanf("%d %d %d",&t.from,&t.to,&t.cost);
       sort(edge,edge+N);// 对边进行排序
        int sum = 0;
        int num = M;
       for(int i = 0;i < N; ++i)// 一个个将边加进去
           Edge t = edge[i];
            if(Find(t.from) == Find(t.to))
               continue;
           F[Find(t.from)] = F[Find(t.to)];
           sum += t.cost;
           num--;
       }
        if(num == 1)
            cout<<sum<<endl;</pre>
            cout<<"?"<<endl;</pre>
   }
   return 0;
}
3.5.2 2 prim 算法.cpp
prim 算法是进行加点,使用于稠密图,可以选择用堆或者不用
不用堆 O(V*V);
用堆 O(E * log(V));
```

```
https://vjudge.net/problem/HDU-1863
*/
typedef pair<int,int> P;
const int LEN = 2e6+100;
int Away [LEN];//记录从当前已选结点到 j 节点的路径的最小值
bool vis[LEN];
int N,M;//N 道路数目, M 村庄个数
vector<vector<P> > vec(LEN);
int main()
       cin>>M>>N;
       int from, to, weight;
       while(N--)
       {
           scanf("%d %d %d",&from,&to,&weight);
           vec[from].push_back(P(weight,to));
           vec[to].push_back(P(weight,from));
       }// 添加边
       for(int i = 2; i \le M; ++i)
           Away[i] = INF;//初始化 Away 数组
       Away[1] = 0;
       int Left = M;
       int All_cost = 0;
       priority_queue<P,vector<P>,greater<P> > q;// 小顶堆
       q.push(P(0,1));
       while(!q.empty()&&Left>0)
       {
           P tmp = q.top();q.pop();
           int To = tmp.second;
           if(vis[To])
               continue;
           vis[To] = 1;
           Left--;
           All_cost += tmp.first;
           for(int i = 0; i < vec[To].size(); ++i)// 更新 Away 数组
               P \&t = vec[To][i];
               if(!vis[t.second] && Away[t.second] > t.first)
                   Away[t.second] = t.first;
                   q.push(t);
               }
           }
       }
           cout<<All_cost<<endl;</pre>
```

```
return 0;
}
3.5.3 3 最小限制生成树.cpp
// 限制某一点的度数不能超过 K
#include<cstring>
#include<map>
#include<cstdio>
#include<iostream>
#include < algorithm>
#include<set>
using namespace std;
\#define\ me(ar)\ memset(ar,0,sizeof(ar))
const int INF = 1e8;
//......
const int LEN = 30;
int K;
int n,m;
struct Edge
   int x,y;
   int weight;
   bool operator <(const Edge &a) const</pre>
       return weight < a.weight;</pre>
   }
} edge[LEN*LEN+10];//邻接表存边,Kruskal 算法要用
int dis[LEN][LEN];//邻接矩阵
int sign[LEN][LEN];//记录那些边已经在生成树里面了
int vis[LEN];//记录是否相连
int F[LEN];//并查集所用
int Father [LEN]; //由 i 到 i+1 度限制生成树需要用动态规划求解, 用来状态转移
int Best[LEN];//Best[i] 指的是由当前节点到 park 这些边中最长边是多少
int Find(int x)//并查集所用 Find 函数
{
   return x == F[x]?x:F[x] = Find(F[x]);
}
void Dfs(int x)//Dfs 动态规划记忆化搜索
{
    vis[x] = 1;
   for(int i = 1;i <= n; ++i )
       if(sign[i][x]&!vis[i])//如果有边相连并且下一个节点没有被访问
          if(x==0)
                 Best[i] = -INF;//与 park 直接相连的边不能删除
          else
                   Best[i] = max(Best[x],dis[x][i]);//状态转移方程
          Father[i] = x;
          vis[i] = 1;
          Dfs(i);
       }
```

```
}
}
void init(){
         for(int i = 0;i < LEN; ++i)</pre>
           F[i] = i;
       me(sign);//初始化标记数组
       me(vis);
       //初始化邻接矩阵
       for(int i = 0; i < LEN; ++i)
           for(int j = 0; j < LEN; ++j)
            dis[i][j] = INF;
}
int main(void)
   while(cin>>m)
    {
       //初始化并查集数组
       init();
       n = 0;//用来记录共有多少个节点
       // set<string> se;
       map<string,int> ma;//将地点编号
       ma["Park"] = 0;//将 park 加入节点
       string s1,s2;
       int a,b;
       int weight = 0;
       for(int i = 0; i < m; ++i)
           cin>>s1>>s2>>weight;
           if(s1 == "Park" | |ma[s1] != 0)
               a = ma[s1];//如果节点已编号,则直接使用
           else
               a = ma[s1] = ++n;//如果没有编号,编号
           if(s2 =="Park" | |ma[s2]!=0)
               b = ma[s2];
           else
               b = ma[s2] = ++n;
           dis[a][b] = dis[b][a] = weight;
           edge[i].x = a;
           edge[i].y = b;
           edge[i].weight = weight;
       //求最小生成树
       int ans = 0;//kruskal 算法求最小生成树
       sort(edge,edge+m);
       for(int i = 0;i < m; ++i)</pre>
       {
           int x = edge[i].x;
           int y = edge[i].y;
            weight = edge[i].weight;
           if(x==0||y==0)//去除掉 park 这个点
               continue;
           int xx = Find(x);
           int yy = Find(y);
           if(xx!=yy)
```

```
{
              F[xx] = F[yy];
               ans += weight;
               sign[x][y] = sign[y][x] = 1;
           }
       }
       cin>>K;//最小 k 度生成树
       int Min[LEN];//用来记录每一个最小生成树到 park 点的最小路径
       for(int i = 0; i < LEN; ++i)
           Min[i] = INF;//初始化
       int index[LEN];//用来记录最小路径的点
       for(int i = 1;i <= n; ++i)
       {
           if(dis[i][0]<Min[Find(i)])</pre>
               Min[Find(i)] = dis[i][0];
               index[Find(i)] = i;
           }
       }
////
           cout << se. size() << endl;</pre>
       int m = 0;//用来记录除去 park 点即 o 点之后共有多少个连通分量
       for(int i = 1;i <= n; ++i)
       {
           if(Min[i] != INF)
               ans += Min[i];
               sign[index[i]][0] = sign[0][index[i]] = 1;//将这个最小路径的点与 park 相连
               m++;
           }
       }
       int MMin = ans;
       for(int i = m + 1; i <= K; ++i)//从 m+1 到 K 求最小 i 度生成树
           me(vis);
           vis[0] = 1;
           Dfs(0);
           int select = -1;//select 用来记录选择哪个与 park 点相连是最小的
           int sum = INF;
           for(int i = 1;i <= n; ++i)
           {
               if(!sign[0][i] && dis[0][i] != INF)
               {
                  if(dis[i][0]-Best[i]<sum)</pre>
                  {
                      select = i;
                      sum = dis[i][0]-Best[i];
                  }
               }
           if(select == -1)//如果找不到, 就跳出循环
               break:
           ans += sum;
```

```
sign[select][0] = sign[0][select] = 1;
            MMin = min(MMin,ans);
             for(int i = select; i != 0; i = Father[i])
                 if(dis[Father[i]][i] == Best[select])
                     sign[i][Father[i]] = sign[Father[i]][i] = 0;
                     break;
             }
             cout<<ans<<endl;</pre>
        printf("Total miles driven: %d\n", MMin);
       // cout<<MMin<<endl;</pre>
    }
    return 0;
}
3.5.4 4 次小生成树.cpp
#include<iostream>
#include<cstdio>
#include<cstring>
#include<string>
#include<algorithm>
#include<cmath>
#include<vector>
#include<queue>
#define ll long long
using namespace std;
int getint()
    int i=0,f=1;char c;
    for(c=getchar();(c<'0'||c>'9')&&c!='-';c=getchar());
    if(c=='-')f=-1,c=getchar();
    for(;c \ge 0' \& c \le 9';c = getchar())i = (i < 3) + (i < 1) + c - 0';
    return i*f;
}
const int N=100005,M=300005;
struct node
{
    int x,y,w;
    inline friend bool operator < (const node &a,const node &b)
        return a.w<b.w;</pre>
    }
}bian[M];
int id[N],fa[N][20],mx1[N][20],mx2[N][20],dep[N];
int tot,first[N],nxt[N<<1],to[N<<1],w[N<<1];</pre>
11 totlen,ans;
```

```
bool chs[M];
void add(int x,int y,int z)
   nxt[++tot]=first[x],first[x]=tot,to[tot]=y,w[tot]=z;
}
int find(int x)
   return id[x] == x?x:id[x] = find(id[x]);
}
void kruskal()
   for(int i=1;i<=n;i++)id[i]=i;</pre>
    sort(bian+1,bian+m+1);
    int cnt=0;
   for(int i=1;i<=m;i++)</pre>
        int x=find(bian[i].x),y=find(bian[i].y);
       if(x!=y)
        {
            cnt++;
            totlen+=bian[i].w;
            chs[i]=true;
            add(bian[i].x,bian[i].y,bian[i].w);
            add(bian[i].y,bian[i].x,bian[i].w);
            id[y]=x;
            if(cnt==n-1)break;
       }
   }
}
void dfs(int u)
   for(int i=1;i<20;i++)fa[u][i]=fa[fa[u][i-1]][i-1];</pre>
   for(int i=1;i<20;i++)mx1[u][i]=max(mx1[u][i-1],mx1[fa[u][i-1])[i-1]);
   for(int i=1;i<20;i++)</pre>
       mx2[u][i]=max(mx2[u][i-1],mx2[fa[u][i-1]][i-1]);
        if(mx1[u][i-1] < mx1[fa[u][i-1]][i-1] \&\&mx2[u][i] < mx1[u][i-1])
            mx2[u][i]=mx1[u][i-1];
        mx2[u][i]=mx1[fa[u][i-1]][i-1];
   }
   for(int e=first[u];e;e=nxt[e])
        int v=to[e];
        if(v==fa[u][0])continue;
       fa[v][0]=u;mx1[v][0]=w[e];
        dep[v]=dep[u]+1;
       dfs(v);
   }
}
```

```
int Find(int x,int y,int len)
    int Mx1=0,Mx2=0;
    if(dep[x] < dep[y]) swap(x,y);</pre>
    int delta=dep[x]-dep[y];
    for(int i=19;i>=0;i--)
        if(delta&(1<<i))
            if(Mx1>mx1[x][i]&&mx1[x][i]>Mx2)Mx2=mx1[x][i];
            if(Mx1<mx1[x][i])Mx2=max(Mx1,mx2[x][i]),Mx1=mx1[x][i];
            x=fa[x][i];
        }
    if(x==y)return Mx1==len?Mx2:Mx1;
    for(int i=19;i>=0;i--)
        if(fa[x][i]!=fa[y][i])
        {
            if (Mx1>mx1[x][i]&&mx1[x][i]>Mx2)Mx2=mx1[x][i];
            if(Mx1<mx1[x][i])Mx2=max(Mx1,mx2[x][i]),Mx1=mx1[x][i];</pre>
            x=fa[x][i];
            if (Mx1>mx1[y][i]&&mx1[y][i]>Mx2)Mx2=mx1[y][i];
            if(Mx1<mx1[y][i])Mx2=max(Mx1,mx2[y][i]),Mx1=mx1[y][i];</pre>
            y=fa[y][i];
    if(Mx1>mx1[x][0]\&\&mx1[x][0]>Mx2)Mx2=mx1[x][0];
    if(Mx1<mx1[x][0])Mx2=max(Mx1,mx2[x][0]),Mx1=mx1[x][0];
    x=fa[x][0];
    if(Mx1>mx1[y][0]\&\&mx1[y][0]>Mx2)Mx2=mx1[y][0];
    if(Mx1<mx1[y][0])Mx2=max(Mx1,mx2[y][0]),Mx1=mx1[y][0];</pre>
    y=fa[y][0];
    return Mx1==len?Mx2:Mx1;
}
void solve(int e)
    int x=bian[e].x,y=bian[e].y,len=bian[e].w;
    int tmp=Find(x,y,len);
    ans=min(ans,totlen-tmp+len);
}
int main()
    //freopen("lx.in", "r", stdin);
    n=getint(),m=getint();
    for(int i=1;i<=m;i++)</pre>
    {
        bian[i].x=getint();
        bian[i].y=getint();
        bian[i].w=getint();
    }
    kruskal();
    dfs(1);
    ans=1e18;
    for(int i=1;i<=m;i++)</pre>
```

```
if(!chs[i])solve(i);
    printf("%lld",ans);
}
     最短路
3.6
3.6.1 1 Dijkstra.cpp
#include <bits/stdc++.h>
#define mem(ar, num) memset(ar, num, sizeof(ar))
#define me(ar) memset(ar,0,sizeof(ar))
#define lowbit(x) (x\mathcal{E}(-x))
#define Pb push_back
#define FI first
#define SE second
#define For(i,a,b) for(int i = a; i < b; ++i)
{\it \#define\ IOS\ ios::sync\_with\_stdio(false)}
using namespace std;
typedef long long LL;
//typedef unsigned long long ULL;
//const int
              prime = 999983;
//const int
               INF = Ox7FFFFFFF;
              INFF = 0x7FFFFFFFFFFFFF;
//const LL
//const double pi = acos(-1.0);
//const double inf = 1e18;
//const double eps = 1e-6;
//const LL
              mod = 1e9 + 7;
/\!/\!LL \ qpow(LL \ a, LL \ b) \{LL \ s=1; while(b>0) \{if(b\&1)s=s*a\%mod; a=a*a\%mod; b>>=1; \} return \ s; \}
//LL gcd(LL a, LL b) {return b?qcd(b, a%b):a;}
//int dr[2][4] = \{1,-1,0,0,0,0,-1,1\};
//typedef pair<int, int> P;
struct Dijkstra{
     #define maxn 1234
     #define INF 123456789
     int n,m;
     int s,t;
     int dis[maxn],M[maxn][maxn];
     bool vis[maxn]:
     void init(){
             scanf("%d %d %d %d",&n,&m,&s,&t);
             int u,v,c;
        for(int i = 1;i <= n; ++i)</pre>
          for(int j = 1; j \le n; ++j)
            if(i != j)
               M[i][j] = INF;
             for(int i = 0;i < m; ++i){</pre>
                      scanf("%d %d %d",&u,&v,&c);
                      M[u][v] = M[v][u] = min(M[u][v],c);
                  }
         }
        void solve(){
            memset(vis,0,sizeof(vis));
                fill(dis+1,dis+n+1,INF);
                 dis[s] = 0;
```

```
for(int i = 1;i <= n; ++i){
                         int x,Min = INF;
                         for(int j = 1; j <= n; ++j){
                                 if(!vis[j]&&dis[j] <= Min)</pre>
                                   Min = dis[x=j];
                         vis[x] = 1;
                    for(int j = 1; j \le n; ++j){
                             if(!vis[j]\&\&dis[j] > dis[x]+M[x][j])
                               dis[j] = dis[x]+M[x][j];
                         }
                }
                        printf("%d\n",dis[t]);
        }
};
Dijkstra Dij;
int main(void)
 Dij.init();
  Dij.solve();
   return 0;
}
// 加了堆优化的 dij
#include <bits/stdc++.h>
#define mem(ar, num) memset(ar, num, sizeof(ar))
#define me(ar) memset(ar,0,sizeof(ar))
#define lowbit(x) (x\mathcal{E}(-x))
#define Pb push_back
#define FI first
#define SE second
#define For(i,a,b) for(int i = a; i < b; ++i)
#define IOS ios::sync_with_stdio(false)
using namespace std;
typedef long long LL;
typedef unsigned long long ULL;
int dr[2][4] = \{1,-1,0,0,0,0,-1,1\};
typedef pair<int,int> P;
struct Edge{
        Edge(int uu,int vv,int dd):u(uu),v(vv),d(dd){
};
struct Dijstra{
        #define maxn 123456
        #define INF 123456789
        int N,M,S,T;
        typedef pair<int,int> P;
```

```
vector<int> G[maxn];
        bool done[maxn];
        int d[maxn];
        int p[maxn];
        void init(){
                 for(int i = 1;i <= N; ++i) G[i].clear();</pre>
                edges.clear();
                 scanf("%d %d %d",&N,&M,&S,&T);
        //
                   cout << N << N << T << endl;
                 int u,v,w;
                 for(int i = 1;i <= M; ++i){</pre>
                         scanf("%d %d %d",&u,&v,&w);
                         AddEdge(u,v,w);
                         AddEdge(v,u,w);
                }
        }
        void AddEdge(int u,int v,int d){
                 edges.push_back(Edge(u,v,d));
                 int m = edges.size();
                G[u].push_back(m-1);
        }
        void solve(){
                priority_queue<P,vector<P>,greater<P>> Q;
                 for(int i = 1;i <= N; ++i) d[i] = INF;</pre>
                d[S] = 0;
                 memset(done,0,sizeof(done));
                 Q.push(P(0,S));
                 while(!Q.empty()){
                         P x = Q.top(); Q.pop();
                         int u = x.second;
                         if(done[u]) continue;
                         done[u] = true;
                         for(int i = 0;i <G[u].size(); ++i){</pre>
                                 Edge &e = edges[G[u][i]];
                                 if(!done[e.v]\&\&d[e.v] > d[u]+e.d){
                                          d[e.v] = d[u]+e.d;
                                          p[e.v] = G[u][i];
                                          Q.push(P(d[e.v],e.v));
                                 }
                         }
                printf("%d\n",d[T]);
        }
};
Dijstra Dij;
int main(void)
 Dij.init();
 Dij.solve();
   return 0;
```

vector<Edge> edges;

```
}
```

3.6.2 2 Bellman-ford.cpp

```
#include <bits/stdc++.h>
#define mem(ar,num) memset(ar,num,sizeof(ar))
#define me(ar) memset(ar,0,sizeof(ar))
#define lowbit(x) (x \mathcal{C}(-x))
#define Pb push_back
#define FI first
#define SE second
#define For(i,a,b) for(int i = a; i < b; ++i)
#define IOS ios::sync_with_stdio(false)
using namespace std;
typedef long long LL;
typedef unsigned long long ULL;
const int
            prime = 999983;
const int
            INF = Ox7FFFFFFF;
const LL
            INFF =Ox7FFFFFFFFFFFF;
const double pi = acos(-1.0);
const double inf = 1e18;
const double eps = 1e-6;
const LL
            mod = 1e9 + 7;
LL qpow(LL a,LL b) {
   LL s=1;
   while(b>0) {
        if(b&1)
           s=s*a\mod;
       a=a*a\%mod;
       b >> = 1;
   }
   return s;
}
LL gcd(LL a, LL b) {
   return b?gcd(b,a%b):a;
}
int dr[2][4] = \{1,-1,0,0,0,0,-1,1\};
typedef pair<int,int> P;
struct Edge{
        int from, to, dist;
       Edge(int u,int v,int d):from(u),to(v),dist(d){
};
struct Bellman_ford {
    #define maxn 1234567
   bool inq[maxn];// 用来记录入队次数
    int cnt[maxn], d[maxn], p[maxn];
    // cnt 来记录入队次数, 大于 n 就退出, d 用来记录最短距离, p 用来记录路径
        int n,m;
        int s,t;
       vector<Edge> edges;
        vector<int> G[maxn];
        void AddEdge(int from,int to,int dist){
                edges.push_back(Edge(from, to, dist));
```

```
edges.push_back(Edge(to,from,dist));
            int
                        m = edges.size();
                G[from].push_back(m-2);
                G[to].push_back(m-1);
        }
    void init(){
            scanf("%d %d %d",&n,&m,&s,&t);
            int u,v,c;
            for(int i = 0;i < m; ++i){</pre>
              scanf("%d %d %d",&u,&v,&c);
                  AddEdge(u,v,c);
                }
        ///
                    cout<<"test"<<endl;</pre>
        }
    bool bellman_ford() {
        queue<int> Q;
        memset(inq,0,sizeof(inq));
        memset(cnt,0,sizeof(cnt));
        for(int i = 1; i <= n; ++i)
            d[i] = INF;
        d[s] = 0;
        inq[s] = true;
        Q.push(s);
        while(!Q.empty()) {
            int u = Q.front();
            Q.pop();
            inq[u] = false;
            for(int i = 0; i < G[u].size(); ++i) {</pre>
                Edge &e = edges[G[u][i]];
                if(d[u] < INF\&\& d[e.to] > d[u]+e.dist) {
                    d[e.to] = d[u]+e.dist;
                    p[e.to] = G[u][i];
                    if(!inq[e.to]) {
                         Q.push(e.to);
                         inq[e.to] = true;
                         if(++cnt[e.to] > n)
                             return false;
                    }
                }
            }
        printf("%d\n",d[t]);
       }
Bellman_ford bell;
int main(void) {
   bell.init();
   bell.bellman_ford();
    return 0;
```

};

}

3.6.3 3 floyed.cpp

```
// https://hihocoder.com/problemset/problem/1089?sid=1348128
#include <bits/stdc++.h>
#define mem(ar, num) memset(ar, num, sizeof(ar))
#define me(ar) memset(ar,0,sizeof(ar))
#define lowbit(x) (x \otimes (-x))
#define Pb push_back
#define FI first
#define SE second
#define For(i,a,b) for(int i = a; i < b; ++i)
#define IOS ios::sync_with_stdio(false)
using namespace std;
typedef long long LL;
typedef unsigned long long ULL;
const int prime = 999983;
const LL
           INFF =0x7FFFFFFFFFFFF;
const double pi = acos(-1.0);
const double inf = 1e18;
const double eps = 1e-6;
const LL
            mod = 1e9 + 7;
LL qpow(LL a,LL b){LL s=1; while(b>0){if(b&1)s=s*a\mod;a=a*a\mod;b>>=1;}return s;}
LL gcd(LL a, LL b) {return b?gcd(b, a%b):a;}
int dr[2][4] = {1,-1,0,0,0,0,-1,1};
typedef pair<int,int> P;
struct Floyd{
        // 复杂度 O(n^3)
        #define maxn 300
        int d[maxn] [maxn];
        int n,m;
        void init(void){
                scanf("%d %d",&n,&m);
                for(int i = 1;i <= n ;++i)
                 for(int j = 1; j \le n; ++j)
                    if(i != j)
                       d[i][j] = INF;
                int u,v,c;
                for(int i = 0;i < m; ++i){</pre>
                        scanf("%d %d %d",&u,&v,&c);
                        d[u][v] = d[v][u] = min(d[v][u],c);
                }
        void floyd(void){
                for(int k = 1; k \le n; ++k)
                 for(int i = 1;i <= n ;++i)</pre>
                   for(int j = 1; j \le n; ++j)
                     if(d[i][k] < INF\&\&d[j][k] < INF)
                        d[i][j] = min(d[i][j],d[i][k]+d[j][k]);
        }
        void print(void){
                for(int i = 1;i <= n; ++i){
                        for(int j = 1; j \le n; ++j)
                          printf("%d%c",d[i][j]," \n"[j==n]);
```

```
}
        }
};
Floyd floyd;
int main(void)
{
         floyd.init();
         floyd.floyd();
         floyd.print();
   return 0;
}
    4 数学
4.1 3 FWT 模板.cpp
// 异或
void FWT(int *a,int N,int opt){
        const int inv2 = qpow(2,mod-2);
        // j 是区间开始点, i 是区间距离, k 是具体位置, j+k,i+j+k 就是在 a 数组中的坐标
        for(int i = 1;i < N; i <<= 1){</pre>
                for(int p = i << 1, j = 0; j < N; j += p){
                        for(int k = 0; k < i; ++k){
                int X = a[j+k], Y = a[i+j+k];
                a[j+k] = (X+Y) \% mod;
                a[i+j+k] = (X+mod-Y)\%mod;
                if(opt == -1) a[j+k] = 111*a[j+k]*inv2\%mod,a[i+j+k] = 111*a[i+j+k]*inv2\%mod;
                         }
                }
        }
}
if(opt == 1) F[i+j+k] = (F[i+j+k]+F[j+k]) \%mod;
else
             F[i+j+k] = (F[i+j+k+mod-F[j+k]) \mbox{%mod};
\overline{if}(\text{opt} == 1) F[j+k] = (F[j+k]+F[i+j+k]) \% \text{mod};
else
             F[j+k] = (F[j+k] + mod - F[i+j+k]) \mod;
4.2 FFT
4.2.1 FFT.cpp
const double PI = acos(-1.0);
struct Complex
{
    double r,i;
    Complex(double _r = 0,double _i = 0){
        r = _r; i = _i;
```

```
}
    Complex operator +(const Complex &b) {
        return Complex(r+b.r,i+b.i);
    Complex operator -(const Complex &b) {
        return Complex(r-b.r,i-b.i);
    Complex operator *(const Complex &b){
        return Complex(r*b.r-i*b.i,r*b.i+i*b.r);
};
void FFT(Complex y[],int n ,int on)
    for(int i = 0, j = 0; i < n; i++) {
        if(j > i) swap(y[i], y[j]);
        int k = n;
        while(j & (k >>= 1)) j &= ~k;
            j |= k;
     }
    for(int h = 2;h <= n;h <<= 1){
        Complex wn(cos(-on*2*PI/h),sin(-on*2*PI/h));
        for(int j = 0; j < n; j += h){
            Complex w(1,0);
            for(int k = j;k < j+h/2;k++){
                Complex u = y[k];
                Complex t = w*y[k+h/2];
                y[k] = u+t;
                y[k+h/2] = u-t;
                w = w*wn;
        }
    }
    if(on == -1)
        for(int i = 0; i < n; i++)
            y[i].r /= n;
}
4.2.2 kuangbin.cpp
#include <stdio.h>
#include <iostream>
#include <string.h>
#include <algorithm>
#include <math.h>
using namespace std;
const double PI = acos(-1.0);
struct complex
{
    double r,i;
    complex(double _r = 0,double _i = 0)
        r = _r; i = _i;
```

```
}
    complex operator +(const complex &b)
        return complex(r+b.r,i+b.i);
    complex operator -(const complex &b)
        return complex(r-b.r,i-b.i);
    }
    complex operator *(const complex &b)
        return complex(r*b.r-i*b.i,r*b.i+i*b.r);
    }
};
void change(complex y[],int len)
    int i,j,k;
    for(i = 1, j = len/2;i < len-1;i++)
        if(i < j)swap(y[i],y[j]);</pre>
        k = len/2;
        while(j \ge k)
            j -= k;
            k /= 2;
        if(j < k)j += k;
    }
}
void fft(complex y[],int len,int on)
    change(y,len);
    for(int h = 2;h <= len;h <<= 1)</pre>
        complex wn(cos(-on*2*PI/h),sin(-on*2*PI/h));
        for(int j = 0; j < len; j += h)
            complex w(1,0);
            for(int k = j;k < j+h/2;k++)
            {
                complex u = y[k];
                complex t = w*y[k+h/2];
                y[k] = u+t;
                y[k+h/2] = u-t;
                w = w*wn;
            }
        }
    }
    if(on == -1)
        for(int i = 0;i < len;i++)</pre>
            y[i].r /= len;
}
const int MAXN = 400040;
```

```
complex x1[MAXN];
int a[MAXN/4];
long long num[MAXN];//100000*100000 会超 int
long long sum[MAXN];
int main()
   int T;
    int n;
    scanf("%d",&T);
   while(T--)
    {
        scanf("%d",&n);
        memset(num,0,sizeof(num));
        for(int i = 0;i < n;i++)</pre>
            scanf("%d",&a[i]);
            num[a[i]]++;
        }
        sort(a,a+n);
        int len1 = a[n-1]+1;
        int len = 1;
        while( len < 2*len1 )len <<= 1;</pre>
        for(int i = 0; i < len1; i++)
            x1[i] = complex(num[i],0);
        for(int i = len1;i < len;i++)</pre>
            x1[i] = complex(0,0);
        fft(x1,len,1);
        for(int i = 0; i < len; i++)
            x1[i] = x1[i]*x1[i];
        fft(x1,len,-1);
        for(int i = 0;i < len;i++)</pre>
            num[i] = (long long)(x1[i].r+0.5);
        len = 2*a[n-1];
        //减掉取两个相同的组合
        for(int i = 0;i < n;i++)</pre>
            num[a[i]+a[i]]--;
        //选择的无序, 除以 2
        for(int i = 1;i <= len;i++)</pre>
        {
            num[i]/=2;
        }
        sum[0] = 0;
        for(int i = 1;i <= len;i++)</pre>
            sum[i] = sum[i-1]+num[i];
        long long cnt = 0;
        for(int i = 0;i < n;i++)</pre>
        {
            cnt += sum[len]-sum[a[i]];
            //减掉一个取大,一个取小的
            cnt -= (long long)(n-1-i)*i;
            //减掉一个取本身, 另外一个取其它
            cnt -= (n-1);
            //减掉大于它的取两个的组合
```

```
cnt -= (long long)(n-1-i)*(n-i-2)/2;
       }
       //总数
       long long tot = (long long)n*(n-1)*(n-2)/6;
       printf("%.71f\n",(double)cnt/tot);
   return 0;
}
4.2.3 lrj.cpp
#include <bits/stdc++.h>
#define mem(ar, num) memset(ar, num, sizeof(ar))
#define me(ar) memset(ar,0,sizeof(ar))
#define lowbit(x) (x\Im(-x))
using namespace std;
typedef long long LL;
typedef unsigned long long ULL;
const int
           prime = 999983;
           INF = Ox7FFFFFFF;
const int
const LL
          INFF =0x7FFFFFFFFFFFF;
//const double pi = acos(-1.0);
const double inf = 1e18;
const double eps = 1e-6;
const LL
          mod = 1e9 + 7;
int dr[2][4] = \{1,-1,0,0,0,0,-1,1\};
// UVa12298 Super Poker II
// Rujia Liu
const long double PI = acos(0.0) * 2.0;
typedef complex<double> CD;
// Cooley-Tukey 的 FFT 算法, 迭代实现。inverse = false 时计算逆 FFT
inline void FFT(vector<CD> &a, bool inverse) {
 int n = a.size();
 // 原地快速 bit reversal
 for(int i = 0, j = 0; i < n; i++) {
   if(j > i) swap(a[i], a[j]);
   int k = n;
   while(j & (k >>= 1)) j &= ~k;
   j |= k;
 }
 double pi = inverse ? -PI : PI;
 for(int step = 1; step < n; step <<= 1) {</pre>
   // 把每相邻两个 "step 点 DFT" 通过一系列蝴蝶操作合并为一个 "2*step 点 DFT"
   double alpha = pi / step;
   // 为求高效, 我们并不是依次执行各个完整的 DFT 合并, 而是枚举下标 k
   // 对于一个下标 k, 执行所有 DFT 合并中该下标对应的蝴蝶操作, 即通过 E[k] 和 O[k] 计算 X[k]
   // 蝴蝶操作参考:http://en.wikipedia.org/wiki/Butterfly_diagram
   for(int k = 0; k < step; k++) {
     // 计算 omega~k. 这个方法效率低, 但如果用每次乘 omega 的方法递推会有精度问题。
     // 有更快更精确的递推方法, 为了清晰起见这里略去
```

```
CD omegak = exp(CD(0, alpha*k));
     for(int Ek = k; Ek < n; Ek += step << 1) { // Ek 是某次 DFT 合并中 E[k] 在原始序列中的下标
       int Ok = Ek + step; // Ok 是该 DFT 合并中 O[k] 在原始序列中的下标
       CD t = omegak * a[Ok]; // 蝴蝶操作: x1 * omega~k
       a[Ok] = a[Ek] - t; // 蝴蝶操作: y1 = x0 - t
       a[Ek] += t;
                         // 蝴蝶操作:y0 = x0 + t
   }
 }
 if(inverse)
   for(int i = 0; i < n; i++) a[i] /= n;
// 用 FFT 实现的快速多项式乘法
inline vector<double> operator * (const vector<double>& v1, const vector<double>& v2) {
 int s1 = v1.size(), s2 = v2.size(), S = 2;
 while(S < s1 + s2) S <<= 1;
 vector<CD> a(S,0), b(S,0); // 把 FFT 的输入长度补成 2 的幂, 不小于 v1 和 v2 的长度之和
 for(int i = 0; i < s1; i++) a[i] = v1[i];
 FFT(a, false);
 for(int i = 0; i < s2; i++) b[i] = v2[i];
 FFT(b, false);
 for(int i = 0; i < S; i++) a[i] *= b[i];
 FFT(a, true);
 vector<double> res(s1 + s2 - 1);
 for(int i = 0; i < s1 + s2 - 1; i++) res[i] = a[i].real(); // 虚部均为 0
 return res;
}
4.3 template.cpp
// 适用范围, 求 n 次多项式第 x 项的值
namespace polysum {
   #define rep(i,a,n) for (int i=a;i < n;i++)
   #define per(i,a,n) for (int i=n-1;i>=a;i--)
   const int D=1e6+10;
   11 a[D],f[D],g[D],p[D],p1[D],p2[D],b[D],h[D][2],C[D];
   ll powmod(ll a,ll b){ll res=1;a%=mod;assert(b>=0);for(;b;b>>=1){if(b&1)res=res*a%mod;a=a*a%mod;}ret
   //......
  // 已知 a_i 的 d 次多项式, 求第 n 项
   ll calcn(int d,ll *a,ll n) { // a[0].. a[d] a[n]
       if (n<=d) return a[n];</pre>
       p1[0]=p2[0]=1;
       rep(i,0,d+1) {
           11 t=(n-i+mod)\%mod;
           p1[i+1]=p1[i]*t%mod;
       rep(i,0,d+1) {
           11 t=(n-d+i+mod)\%mod;
           p2[i+1]=p2[i]*t%mod;
       }
```

```
11 ans=0;
        rep(i,0,d+1) {
            11 t=g[i]*g[d-i]%mod*p1[i]%mod*p2[d-i]%mod*a[i]%mod;
            if ((d-i)\&1) ans=(ans-t+mod)\%mod;
            else ans=(ans+t)%mod;
        }
        return ans;
    // 初始化, 初始化的时候记得将 D 的值
    void init(int M) {
        f[0]=f[1]=g[0]=g[1]=1;
        rep(i,2,M+5) f[i]=f[i-1]*i\%mod;
        g[M+4] = powmod(f[M+4], mod-2);
        per(i,1,M+4) g[i]=g[i+1]*(i+1)%mod;
// 已知 a_i, 并且知道 a_i 是 m 次多项式
   ll polysum(ll m,ll *a,ll n) { // a[0] .. a[m] \setminus sum_{i=0}^{n} a[i]
        11 b[D];
        11 b[D]:
        for(int i=0;i<=m;i++) b[i]=a[i];</pre>
        b[m+1]=calcn(m,b,m+1);
        rep(i,1,m+2) b[i]=(b[i-1]+b[i])%mod;
        return calcn(m+1,b,n);// m 次多项式的和是 m+1 次多项式
    }
    11 qpolysum(11 R,11 n,11 *a,11 m) {
     // a[0].. a[m] \setminus sum_{i=0}^{n-1} a[i]*R^i
        if (R==1) return polysum(n,a,m);
        a[m+1]=calcn(m,a,m+1);
        11 r=powmod(R,mod-2),p3=0,p4=0,c,ans;
        h[0][0]=0;h[0][1]=1;
        rep(i,1,m+2) {
            h[i][0]=(h[i-1][0]+a[i-1])*r\mbox{mod};
            h[i][1]=h[i-1][1]*r\mbox{mod};
        }
        rep(i,0,m+2) {
            11 t=g[i]*g[m+1-i]\%mod;
            if (i&1) p3=((p3-h[i][0]*t)%mod+mod)%mod,p4=((p4-h[i][1]*t)%mod+mod)%mod;
            else p3=(p3+h[i][0]*t)\mbox{mod}, p4=(p4+h[i][1]*t)\mbox{mod};
        c=powmod(p4,mod-2)*(mod-p3)%mod;
        rep(i,0,m+2) h[i][0]=(h[i][0]+h[i][1]*c)%mod;
        rep(i,0,m+2) C[i]=h[i][0];
        ans=(calcn(m,C,n)*powmod(R,n)-c)%mod;
        if (ans<0) ans+=mod;</pre>
        return ans;
} // polysum::init();
4.4 数论
4.4.1 1 加法.cpp
string add(string a,string b)
```

```
string c;
    int len1=a.length();
    int len2=b.length();
    int len=max(len1,len2);
    for(int i=len1;i<len;i++)</pre>
        a="0"+a;
    for(int i=len2;i<len;i++)</pre>
        b="0"+b;
    int ok=0;
    for(int i=len-1;i>=0;i--)
        char temp=a[i]+b[i]-'0'+ok;
        if(temp>'9')
            ok=1;
            temp-=10;
        else ok=0;
        c=temp+c;
    }
    if(ok) c="1"+c;
    return c;
}
4.4.2 1 逆元.cpp
// 欧几里得扩展
long long ex_gcd(long long a,long long b,long long &x,long long &y)
    if(b == 0)
    {
        x = 1;
        y = 0;
        return a;
    long long m = ex_gcd(b,a%b,y,x);
     y = a/b * x;
    return m;
}
int main()
    long long a,b,x,y;
    cin>>a>>b; //求 a 关于 b 的逆元
    if(ex_gcd(a,b,x,y)==1)
        cout << (x\%b+b)\%b << endl;
    else
        cout<<"None"<<endl;</pre>
    return 0;
// 费马小定理求逆元
qpow(a,p-2,p);
// 逆元打表
   int inv[10000];
```

```
int p;
    cin>>p;
    inv[1] = 1;
    for(int i = 2;i < p; ++i)</pre>
        inv[i] = (p - p/i*inv[p%i]%p)%p;
    for(int i = 1; i < p; ++i)
        cout << inv[i] << " ";
    cout<<endl;</pre>
    for(int i = 1;i < p; ++i)</pre>
        cout<<i * inv[i] % p<<" ";
 // 快速阶乘逆元
 const int maxn = 1e5+10;
long long fac[maxn],invfac[maxn];
void init(int n){
    fac[0] = 1;
    for(int i = 1;i <= n; ++i) fac[i] = fac[i-1]*i\( \)mod;</pre>
    invfac[n] = qpow(fac[n],mod-2);
    for(int i = n-1; i \ge 0; --i) invfac[i] = invfac[i+1]*(i+1)%mod;
}
4.4.3 2 减法.cpp
string sub(string a,string b)
    string c;
    bool ok=0;
    int len1=a.length();
    int len2=b.length();
    int len=max(len1,len2);
    for(int i=len1;i<len;i++)</pre>
        a="0"+a;
    for(int i=len2;i<len;i++)</pre>
        b="0"+b;
    if(a<b)
    {
        string temp=a;
        a=b;
        b=temp;
        ok=1;
    for(int i=len-1;i>=0;i--)
    {
        if(a[i]<b[i])
             a[i-1]-=1;
            a[i]+=10;
        char temp=a[i]-b[i]+'0';
        c=temp+c;
    }
```

```
int pos=0;
    while(c[pos] == '0' && pos<len) pos++;
    if(pos==len) return "0";
    if(ok) return "-"+c.substr(pos);
    return c.substr(pos);
}
4.4.4 3 乘法.cpp
string mul(string a,int b)
    string c;
    char s;
    int len=a.length();
    int ok=0;
    for(int i=len-1;i>=0;i--)
        int temp=(a[i]-'0')*b+ok;
        ok=temp/10;
        s=temp\%10+'0';
        c=s+c;
    }
    while(ok)
        s=ok\%10+101;
        c=s+c;
        ok/=10;
    }
    return c;
}
4.4.5 4 除法.cpp
string div(string a,int b)
    string c;
    int len=a.length();
    int ans=0;
    char s;
    for(int i=0;i<len;i++)</pre>
        ans=ans*10+a[i]-'0';
        s=ans/b+'0';
        ans%=b;
        c+=s;
    }
    int pos=0;
    while(pos<len && c[pos]=='0') pos++;
    if(pos==len) return "0";
    return c.substr(pos);
}
```

4.4.6 Euler.cpp

```
#### 欧拉函数打表
O(nlog(n))
const int maxn = 1e6+100;
int phi[maxn],Prime[maxn];
void init2(int n){
        for(int i = 1;i <= n; ++i) phi[i] = i;</pre>
    for(int i = 2;i <= n; ++i){</pre>
            if(i == phi[i]){
               for(int j = i; j <= n; j += i) phi[j] = phi[j]/i*(i-1);</pre>
    }
 线性筛 O(n)
const int maxn = 1e6+100;
bool check[maxn];
int phi[maxn],Prime[maxn];
void init(int MAXN){
        int N = maxn-1;
    memset(check,false,sizeof(check));
    phi[1] = 1;
    int tot = 0;
    for(int i = 2;i <= N; ++i){</pre>
            if(!check[i]){
                    Prime[tot++] = i;
                    phi[i] = i-1;
            for(int j = 0; j < tot; ++j){
                    if(i*Prime[j] > N) break;
                    check[i*Prime[j]] = true;
                    if(i\%Prime[j] == 0){
                             phi[i*Prime[j]] = phi[i]*Prime[j];
                             break;
                    }
                    else{
                             phi[i*Prime[j]] = phi[i]*(Prime[j]-1);
                    }
            }
    }
4.4.7 lucas, 组合数.cpp
LL qpow(LL a,LL b,LL m){
        LL ans = 1;
        a \%= m;
```

```
while(b > 0){
                if(b&1)
                  ans = ans*am;
                   a = a*a\%m;
                  b >>= 1;
       }
       return ans;
}
LL C(LL n, LL m, LL p) {
        if(m > n) return 0;
       LL tmp1 = 1,tmp2 = 1;
       m = min(n-m,m);
       for(LL i = 1;i <= m; ++i){
                tmp1 = tmp1*(n-m+i)\%p;
                tmp2 = tmp2*i\%p;
        }
       return tmp1*qpow(tmp2,p-2,p)%p;
LL lucas(LL n, LL m, LL p){
        if(m == 0)
          return 1;
        return lucas(n/p,m/p,p)*C(n%p,m%p,p)%p;
}
4.4.8 miller-rabin-Pollard-rho.cpp
// 可以对一个 2~63 的素数进行判断。
可以分解比较大的数的因子。
#include<stdio.h>
#include<string.h>
#include<iostream>
#include<math.h>
#include<stdlib.h>
#include<time.h>
using namespace std;
typedef long long LL;
#define maxn 10000
LL factor[maxn];
int tot;
const int S=20;
LL muti_mod(LL a,LL b,LL c){ //返回 (a*b) mod c,a,b,c<2^63
    a%=c;
    b%=c;
    LL ret=0;
    while (b){
        if (b&1){
           ret+=a;
            if (ret>=c) ret-=c;
        }
```

```
a <<=1;
        if (a>=c) a-=c;
        b>>=1;
    }
    return ret;
}
LL pow_mod(LL x,LL n,LL mod){ //返回 x^n mod c , 非递归版
    if (n==1) return x%mod;
    int bit[90],k=0;
    while (n){
        bit [k++]=n\&1;
        n >> = 1;
    }
    LL ret=1;
    for (k=k-1;k>=0;k--){
        ret=muti_mod(ret,ret,mod);
        if (bit[k]==1) ret=muti_mod(ret,x,mod);
    }
    return ret;
}
bool check(LL a,LL n,LL x,LL t){ //以 a 为基, n-1=x*2^t, 检验 n 是不是合数
    LL ret=pow_mod(a,x,n),last=ret;
    for (int i=1;i<=t;i++){</pre>
        ret=muti_mod(ret,ret,n);
        if (ret==1 && last!=1 && last!=n-1) return 1;
        last=ret;
    }
    if (ret!=1) return 1;
    return 0;
}
bool Miller_Rabin(LL n){
    LL x=n-1, t=0;
    while ((x\&1)==0) x>>=1,t++;
    bool flag=1;
    if (t>=1 && (x&1)==1){
        for (int k=0;k<S;k++){</pre>
            LL a=rand()\%(n-1)+1;
            if (check(a,n,x,t)) {flag=1;break;}
            flag=0;
    }
    if (!flag || n==2) return 0;
    return 1;
}
LL gcd(LL a,LL b){
    if (a==0) return 1;
    if (a<0) return gcd(-a,b);</pre>
    while (b){
        LL t=a\%b; a=b; b=t;
    }
```

```
return a;
}
LL Pollard_rho(LL x,LL c){
    LL i=1,x0=rand()%x,y=x0,k=2;
    while (1){
        i++;
        x0=(muti_mod(x0,x0,x)+c)%x;
        LL d=gcd(y-x0,x);
        if (d!=1 && d!=x){
            return d;
        }
        if (y==x0) return x;
        if (i==k){
            y=x0;
            k+=k;
        }
    }
                              //递归进行质因数分解 N
void findfac(LL n){
    if (!Miller_Rabin(n)){
        factor[tot++] = n;
        return:
    }
    LL p=n;
    while (p>=n) p=Pollard_rho(p,rand() % (n-1) +1);
    findfac(p);
    findfac(n/p);
}
int main()
   // srand(time(NULL));//POJ 上 G++ 要去掉这句话
    int T;
    scanf("%d",&T);
    long long n;
    while(T--)
    {
        scanf("%I64d",&n);
        if (!Miller_Rabin(n)) {printf("Prime\n"); continue; }
        tot = 0;
        findfac(n);
        long long ans=factor[0];
        for(int i=1;i<tot;i++)</pre>
          if(factor[i] < ans) ans = factor[i];</pre>
        printf("%I64d\n",ans);
    }
    return 0;
}
```

4.4.9 快速数论变换.cpp

```
const int mod = 998244353;
LL qpow(LL a,LL b){LL s=1; while(b>0){if(b&1)s=s*a\mod;a=a*a\mod;b>>=1;}return s;}
const int g = 3; //原根
LL quick_mod(LL a,LL b)
    LL ans=1;
    for(;b;b/=2)
         if(b&1)
             ans=ans*a%mod;
        a=a*a%mod;
    }
    return ans;
}
int rev(int x,int r) //蝴蝶操作
{
    int ans=0;
    for(int i=0; i<r; i++)</pre>
    {
         if(x&(1<<i))
             ans+=1<<(r-i-1);
    }
    return ans;
void NTT(int n, LL A[],int on) // 长度为 N (2 的次数)
    int r=0;
    for(;; r++)
         if((1 << r) == n)
             break;
    }
    for(int i=0; i<n; i++)</pre>
         int tmp=rev(i,r);
         if(i<tmp)</pre>
             swap(A[i],A[tmp]);
    for(int s=1; s<=r; s++)</pre>
    {
        int m=1<<s;</pre>
        LL wn=quick_mod(g,(mod-1)/m);
        for(int k=0; k<n; k+=m)</pre>
        {
             LL w=1;
             for(int j=0; j<m/2; j++)</pre>
                 LL t,u;
                 t=w*(A[k+j+m/2]\mbox{\em mod})\mbox{\em mod};
                 u=A[k+j]\%mod;
```

```
A[k+j]=(u+t)\%mod;
                 A[k+j+m/2] = ((u-t)\%mod+mod)\%mod;
                 w=w*wn\%mod;
            }
        }
    }
    if(on==-1)
        for(int i=1;i<n/2;i++)</pre>
            swap(A[i],A[n-i]);
        LL inv=quick_mod(n,mod-2);
        for(int i=0;i<n;i++)</pre>
             A[i]=A[i]\mbox{mod}*inv\mbox{mod};
    }
}
4.4.10 欧拉筛和埃氏筛.cpp
void Era_s(void){
    check[1] = 1;
    tot = 1;
    for(int i = 2;i < maxn; ++i){</pre>
        if(!check[i]){
        Prime[tot++] = i;
        for(int j = i+i; j < maxn; ++j) check[j] = 1;</pre>
    }
}
void Euler_s(void){
    check[1] = 1;
    tot = 1;
    int n = 1e6;
    for(int i = 2;i <= n; ++i){
         if(!check[i]) Prime[tot++] = i;
         for(int j = 1; j < tot; ++j){</pre>
             if(i*Prime[j] > n) break;
             check[i*Prime[j]] = 1;
             if(i % Prime[j] == 0) break;
    }
}
4.4.11 素性检测.cpp
#include<bits/stdc++.h>
using namespace std;
//typedef long long LL;
const int LEN = 1e6+1;
bool vis[LEN];
//int prime[LEN];
int Prime[LEN];
int cnt = 1;
typedef unsigned long long LL;
```

```
LL modular_multi(LL x,LL y,LL mo) {
       LL t;
       x\%=mo;
       for(t=0;y;x=(x<<1)mo,y>>=1)
               if (y&1)
                       t=(t+x)\%mo;
       return t;
}
LL modular_exp(LL num,LL t,LL mo) {
       LL ret=1,temp=num%mo;
       for(;t;t>>=1,temp=modular_multi(temp,temp,mo))
               if (t&1)
                       ret=modular_multi(ret,temp,mo);
       return ret;
}
bool miller_rabin(LL n) {
       if (n==2 | n==7 | n==61)
       return true;
       if (n==1 | (n\&1)==0)
       return false;
       int t=0,num[3]={2,7,61};//2,7,61 对 unsigned int 内的所有数够用了, 最小不能判断的数为 4 759 123 1
       LL a,x,y,u=n-1;
       while ((u\&1)==0)
       t++,u>>=1;
       for(int i=0;i<3;i++) {</pre>
               a=num[i];
               x=modular_exp(a,u,n);
               for(int j=0;j<t;j++) {</pre>
                       y=modular_multi(x,x,n);
                       if (y==1\&\&x!=1\&\&x!=n-1)
                               return false;
           //其中用到定理, 如果对模 n 存在 1 的非平凡平方根, 则 n 是合数。
           //如果一个数 x 满足方程 x^21 (mod n), 但 x 不等于对模 n 来说 1 的两个 '平凡'平方根:1 或-1,
                       x=y;
               if (x!=1)//根据费马小定理, 若 n 是素数, 有 a^(n-1)1(mod n). 因此 n 不可能是素数
                       return false;
       return true;
}
void init(void)
    int n = LEN -1;
   for(int i = 2; i <= n; ++i)
    {
       if(!vis[i])
           Prime[cnt++] = i;
           for(LL j = (LL)i * i; j <= n; j += i)
               vis[j] = 1;
       }
```

```
}
}
bool isPrime(LL n)
        if(n < 1e6)
                for(LL i = 1;i < cnt&&Prime[i] < n; ++i)</pre>
        {
                if(n % Prime[i] == 0)
                 return false;
        }
        return true;
        }
        else
         return miller_rabin(n);
}
int main(void)
        init();
        int T;
        cin>>T;
        while(T--)
        {
           LL n;
           cin>>n;
           if(isPrime(n))
              cout<<"Yes"<<endl;</pre>
           else
              cout<<"No"<<endl;</pre>
        }
        return 0;
}
4.4.12 素数筛.cpp
Eratosthenes筛法(埃拉托斯特尼筛法)
onst int maxn = 1e6+10;
bool check[maxn];
int Prime[maxn];
int tot = 1;
void Eratosthenes(void){
        const int n = maxn -1;
        memset(check,0,sizeof(check));
        for(int i = 2;i < n; ++i){
                if(!check[i]){
                        Prime[tot++] = i;
                         for(int j = i+i; j < n; j += i) check[j] = 1;
                }
        }
}
```

```
欧拉筛
\overline{\text{const}} int \max = 1e6+10;
bool check[maxn];
int Prime[maxn];
int tot = 1;
void Euler shai(void){
        int n = maxn-1;
        memset(check,0,sizeof(check));
        for(int i = 2;i <= n; ++i){</pre>
                 if(!check[i]){
                         Prime[tot++] = i;
                 }
                         for(int j = 1; j < tot; ++j){
                                  if(i*Prime[j] > n) break;
                                      check[i*Prime[j]] =1;
                              if(i % Prime[j]==0) break;
                         }
        }
}
4.4.13 逆元打表.cpp
 int inv[10000];
    int p;
    cin>>p;
    inv[1] = 1;
    for(int i = 2;i < p; ++i)</pre>
        inv[i] = (p - p/i*inv[p\%i]\%p)\%p;
    }
    for(int i = 1; i < p; ++i)
        cout << inv[i] << " ";
    cout<<endl;</pre>
    for(int i = 1;i < p; ++i)</pre>
        cout<<i * inv[i] % p<<" ";
4.5 矩阵快速幂.cpp
// 注意修改 maxn 的值, 要不然容易 T
const int maxn = 100;
int n;
struct Matrix{
        int n,m;
        Matrix(int nn = 1,int mm = 1):n(nn),m(mm){ memset(a,0,sizeof(a));};
        long long a[maxn] [maxn];
};
// void print(const Matrix &a)
// {
           for(int \ i = 1; i \le a.n; ++i, cout \le endl)
```

```
//
           for(int j=1;j \le a.m; ++j)
              cout << a.a[i][j] << " ";
//
1/ }
Matrix operator*(Matrix a, Matrix b)
       Matrix c(a.n,b.m);
       for(int i = 1;i <= a.n; ++i)
               for(int j = 1; j \le b.m; ++j)
                       for(int k = 1; k \le a.m; ++k)
                               c.a[i][j] += a.a[i][k] * b.a[k][j];
                               c.a[i][j] %= mod;
                       }
               }
       }
         print(c);
       return c;
}
     自适应辛普森积分.cpp
4.6
double F(double x)
{
       //Simpson 公式用到的函数
}
double simpson(double a, double b) //三点 Simpson 法, 这里要求 F 是一个全局函数
       double c = a + (b - a) / 2;
       return (F(a) + 4 * F(c) + F(b))*(b - a) / 6;
double asr(double a, double b, double eps, double A)//自适应 Simpson 公式 (递归过程)。已知整个区间 [a,b]
       double c = a + (b - a) / 2;
       double L = simpson(a, c), R = simpson(c, b);
       if (fabs(L + R - A) \le 15 * eps)return L + R + (L + R - A) / 15.0;
       return asr(a, c, eps / 2, L) + asr(c, b, eps / 2, R);
}
double asr(double a, double b, double eps)//自适应 Simpson 公式 (主过程)
{
       return asr(a, b, eps, simpson(a, b));
}
    5 几何
5
5.1 2D
5.1.1 PSLG.cpp
typedef vector<Point> Polygon;
double PolygonArea(Polygon poly)
   double area = 0;
```

```
int n = poly.size();
   for(int i = 1; i < n-1; i++)
       area += Cross(poly[i]-poly[0], poly[(i+1)%n]-poly[0]);
   return area/2;
}
struct Edge
   int from, to; // 起点, 终点, 左边的面编号
   double ang;
   Edge(int f,int t,double a):from(f),to(t),ang(a) {}
};
const int maxn = 10000 + 10; // 最大边数
// 平面直线图 (PSGL) 实现
struct PSLG
{
   int n, m, face_cnt;//face_cnt 面数
   double x[maxn], y[maxn];
   vector<Edge> edges;//储存边
   vector<int> G[maxn];//指向边
   int vis[maxn*2]; // 每条边是否已经访问过
   int left[maxn*2]; // 左面的编号
   int prev[maxn*2]; // 相同起点的上一条边 (即顺时针旋转碰到的下一条边) 的编号
   vector<Polygon> faces;//faces 储存面
   double area[maxn]; // 每个 polygon 的面积
   void init(int n)
       this->n = n;
       for(int i = 0; i < n; i++)</pre>
           G[i].clear();
       edges.clear();
       faces.clear();
   }
   // 有向线段 from->to 的极角
   double getAngle(int from, int to)
   {
       return atan2(y[to]-y[from], x[to]-x[from]);
   }
   void AddEdge(int from, int to)
   {
       edges.push_back((Edge){ from, to, getAngle(from, to)});
       edges.push_back((Edge){ to, from, getAngle(to, from)});
       m = edges.size();
       G[from].push_back(m-2);
       G[to].push_back(m-1);
   }
   // 找出 faces 并计算面积
```

```
void Build()
   {
       for(int u = 0; u < n; u++)
            // 给从 u 出发的各条边按极角排序
            int d = G[u].size();
            for(int i = 0; i < d; i++)
                for(int j = i+1; j < d; j++) // 这里偷个懒, 假设从每个点出发的线段不会太多
                    if(edges[G[u][i]].ang > edges[G[u][j]].ang)
                        swap(G[u][i], G[u][j]);
            for(int i = 0; i < d; i++)</pre>
               prev[G[u][(i+1)%d]] = G[u][i];
       }
       memset(vis, 0, sizeof(vis));
       face_cnt = 0;
        for(int u = 0; u < n; u++)
           for(int i = 0; i < G[u].size(); i++)</pre>
            {
                int e = G[u][i];
                if(!vis[e]) // 逆时针找圈
                    face_cnt++;
                    Polygon poly;
                    for(;;)
                    {
                        vis[e] = 1;
                        left[e] = face_cnt;
                        int from = edges[e].from;
                       poly.push_back(Point(x[from], y[from]));
                        e = prev[e^1];
                        if(e == G[u][i])
                            break;
                        assert(vis[e] == 0);
                    faces.push_back(poly);
               }
            }
       for(int i = 0; i < faces.size(); i++)</pre>
            area[i] = PolygonArea(faces[i]);
   }
};
5.1.2 二维几何模板.cpp
#include <bits/stdc++.h>
#define mem(ar, num) memset(ar, num, sizeof(ar))
#define me(ar) memset(ar,0,sizeof(ar))
#define lowbit(x) (x&(-x))
#define forn(i,n) for(int i = 0; i < n; ++i)
using namespace std;
```

```
typedef long long LL;
typedef unsigned long long ULL;
const int
            prime = 999983;
             INF = 0x7FFFFFFF;
const int
const LL
             INFF =0x7FFFFFFFFFFFF;
const double pi = acos(-1.0);
const double inf = 1e18;
const double eps = 1e-10;
const LL
             mod = 1e9 + 7;
struct Point
    double x,y;
    Point(double x = 0, double y = 0):x(x),y(y) {}
};
typedef Point Vector;
Vector operator + (Vector A, Vector B)
    return Vector(A.x + B.x, A.y + B.y);
}
Vector operator - (Vector A, Vector B)
    return Vector(A.x-B.x,A.y-B.y);
}
Vector operator / (Vector A,double p)
    return Vector(A.x/p,A.y/p);
}
Vector operator * (Vector A,double p)
    return Vector(A.x*p,A.y*p);
}
double angle(Vector v)//求向量的角度从 0 到 2*pi
    return atan2(v.y,v.x);
int dcmp(double x)
    if(fabs(x)<eps)
        return 0;
    else
        return x < 0?-1:1;
bool operator < (const Point &a,const Point &b)</pre>
    if(dcmp(a.x-b.x)==0)
        return a.y<b.y;</pre>
    else
        return a.x<b.x;
}
bool operator == (const Point &a,const Point &b)
```

```
{
   return !dcmp(a.x-b.x)&&!dcmp(a.y-b.y);
}
double Dot(Vector A, Vector B)
   return A.x*B.x+A.y*B.y;
}
double Length(Vector A)
{
   return sqrt(A.x*A.x+A.y*A.y);
}
double Angle(Vector A, Vector B)
   return acos(Dot(A,B)/Length(A)/Length(B));
}
double Cross(Vector A, Vector B)
{
   return A.x*B.y - A.y*B.x;
}
double Area2(Point A,Point B,Point C)
   return Cross(B-A,C-A);
}
Vector Rotate(Vector A, double rad)
{
   return Vector (A.x*cos(rad)-A.y*sin(rad), A.x*sin(rad)+A.y*cos(rad));
}
Vector Normal(Vector A) //单位法线
   double L = Length(A);
   return Vector(-A.y/L,A.x/L);
//调用前确保直线有唯一交点, 当且仅当 Cross(v,w) 非 O
Point Get_Line_Intersection(Point P, Vector v, Point Q, Vector w)
   Vector u = P - Q;
   double t = Cross(w,u)/Cross(v,w);
   return P+v*t;
double Distance_To_Line(Point P,Point A,Point B)//点到直线的距离
   Vector v1 = B-A, v2 = P-A;
   return fabs(Cross(v1,v2)/Length(v1));
double Distance_To_Segment(Point P,Point A,Point B)
   if(A==B)
        return Length (P-A);
   Vector v1 = B-A, v2 = P-A, v3 = P-B;
    if(dcmp(Dot(v1,v2))<0)</pre>
        return Length(v1);
    else if(dcmp(Dot(v1,v3))>0)
        return Length(v3);
    else
```

```
return fabs(Cross(v1,v2))/Length(v1);
}
Point Get_Line_Projection(Point P,Point A,Point B)//求投影点
   Vector v = B - A;
   return A + v*(Dot(v,P-A)/Dot(v,v));
//线段相交判定 相交不在线段的端点
bool Segment_Proper_Intersection(Point a1,Point a2,Point b1,Point b2)
{
   double c1 = Cross(a2-a1,b1-a1), c2 = Cross(a2-a1,b2-a1),
          c3 = Cross(b2-b1,a2-b1), c4 = Cross(b2-b1,a1-b1);
   return dcmp(c1)*dcmp(c2)<0&&dcmp(c3)*dcmp(c4)<0;
}
//判断点是否在线段上 (不包括端点)
bool Onsegment(Point p,Point a1,Point a2)
{
   return dcmp(Cross(a1-p,a2-p))==0&&dcmp(Dot(a1-p,a2-p))<0;
}
5.1.3 二维凸包.cpp
//计算凸包,输入点数组 p,个数为 p,输出点数组为 ch。函数返回凸包顶点数
//输入不能有重复节点
//如果精度要求搞需要用 dcmp 判断
//如果不希望在边上右点,需要将 <= 改为 <
int ConvexHull(Point *p,int n ,Point *ch)
{
   sort(p,p+n);
   int m = 0;
   for(int i = 0; i < n; ++i)
       while (m>1\&\& Cross(ch[m-1]-ch[m-2],p[i]-ch[m-2])<=0) m--;
       ch[m++] = p[i];
   }
   int k = m;
   for(int i = n-2; i >= 0; --i)
       while (m > k \& \& \operatorname{Cross}(\operatorname{ch}[m-1] - \operatorname{ch}[m-2], p[i] - \operatorname{ch}[m-2]) <= 0) m--;
       ch[m++] = p[i];
   if(n > 1) m--;
   return m;
}
5.1.4 判断点是否在多边形内.cpp
typedef vector<Point> Polygon;
int isPointInPolygon(Point p,Polygon poly)
   int n = poly.size();
   int wn = 0;
   for(int i = 0; i < n; ++i)
   {
```

```
if(Onsegment(p,poly[i],poly[(i+1)%n])) return -1;
        int k = dcmp(Cross(poly[(i+1)%n]-poly[i],p-poly[i]));
        int d1 = dcmp(poly[i].y-p.y);
        int d2 = dcmp(poly[(i+1)%n].y-p.y);
        if(k>0\&\&d1 \le 0\&\&d2 > 0) wn ++;
        if (k<0\&\&d2 <= 0\&\&d1 > 0) wn --;
    if(wn != 0) return 1;
    return 0;
}
5.1.5 圆与多边形相交的面积.cpp
#include <iostream>
#include <cstdio>
#include <string>
#include <cmath>
#include <iomanip>
#include <ctime>
#include <climits>
#include <cstdlib>
#include <cstring>
#include <algorithm>
#include <queue>
#include <vector>
#include <set>
#include <map>
using namespace std;
typedef unsigned int UI;
typedef long long LL;
typedef unsigned long long ULL;
typedef long double LD;
const double pi = acos(-1.0);
const double e = exp(1.0);
const double eps = 1e-8;
const int maxn = 400;
double x, y, h;
double vx, vy;
double R;
int n;
struct point
{
    double x, y;
    point(double _x=0.0, double _y=0.0)
        : x(_x), y(_y) {}
    point operator - (const point & p)
        return point(x-p.x, y-p.y);
    }
    double sqrx()
        return sqrt(x*x+y*y);
} p[maxn];
```

```
double xmult(point & p1, point & p2, point & p0);
double distancex(point & p1, point & p2);
point intersection(point u1, point u2, point v1, point v2);
void intersection_line_circle(point c, double r, point 11, point 12, point & p1, point & p2);
point ptoseg(point p, point 11, point 12);
double distp(point & a, point & b);
double Direct_Triangle_Circle_Area(point a, point b, point o, double r);
double xmult(point & p1, point & p2, point & p0)
   return (p1.x-p0.x)*(p2.y-p0.y)-(p1.y-p0.y)*(p2.x-p0.x);
}
double distancex(point & p1, point & p2)
{
   return sqrt((p1.x-p2.x)*(p1.x-p2.x)+(p1.y-p2.y)*(p1.y-p2.y));
}
point intersection(point u1, point u2, point v1, point v2)
   point ret = u1;
   double t = ((u1.x-v1.x)*(v1.y-v2.y)-(u1.y-v1.y)*(v1.x-v2.x))
             / ((u1.x-u2.x)*(v1.y-v2.y)-(u1.y-u2.y)*(v1.x-v2.x));
   ret.x += (u2.x-u1.x)*t;
   ret.y += (u2.y-u1.y)*t;
   return ret;
}
void intersection_line_circle(point c, double r, point 11, point 12, point & p1, point & p2)
{
   point p = c;
   double t;
   p.x += 11.y-12.y;
   p.y += 12.x-11.x;
   p = intersection(p, c, 11, 12);
   t = sqrt(r*r-distancex(p, c)*distancex(p, c))/distancex(11, 12);
   p1.x = p.x+(12.x-11.x)*t;
   p1.y = p.y+(12.y-11.y)*t;
   p2.x = p.x-(12.x-11.x)*t;
   p2.y = p.y-(12.y-11.y)*t;
}
point ptoseg(point p, point 11, point 12)
   point t = p;
   t.x += 11.y-12.y;
   t.y += 12.x-11.x;
   if (xmult(11, t, p)*xmult(12, t, p)>eps)
        return distancex(p, 11) < distancex(p, 12) ? 11 : 12;</pre>
   return intersection(p, t, 11, 12);
}
```

```
double distp(point & a, point & b)
{
   return (a.x-b.x)*(a.x-b.x)+(a.y-b.y)*(a.y-b.y);
}
double Direct_Triangle_Circle_Area(point a, point b, point o, double r)
   double sign = 1.0;
   a = a-o;
   b = b-o;
   o = point(0.0, 0.0);
    if (fabs(xmult(a, b, o)) < eps)</pre>
        return 0.0;
    if (distp(a, o) > distp(b, o))
        swap(a, b);
       sign = -1.0;
   }
   if (distp(a, o) < r*r+eps)</pre>
        if (distp(b, o) < r*r+eps)</pre>
            return xmult(a, b, o)/2.0*sign;
       point p1, p2;
        intersection_line_circle(o, r, a, b, p1, p2);
        if (distancex(p1, b) > distancex(p2, b))
            swap(p1, p2);
        double ret1 = fabs(xmult(a, p1, o));
        double ret2 = acos((p1.x*b.x+p1.y*b.y)/p1.sqrx()/b.sqrx())*r*r;
        double ret = (ret1+ret2)/2.0;
        if (xmult(a, b, o)<eps && sign>0.0 || xmult(a, b, o)>eps && sign<0.0)
            ret = -ret;
       return ret;
   }
   point ins = ptoseg(o, a, b);
    if (distp(o, ins)>r*r-eps)
        double ret = acos((a.x*b.x+a.y*b.y)/a.sqrx()/b.sqrx())*r*r/2.0;
        if (xmult(a, b, o)<eps && sign>0.0 || xmult(a, b, o)>eps && sign<0.0)
            ret = -ret;
       return ret;
   }
   point p1, p2;
    intersection_line_circle(o, r, a, b, p1, p2);
   double cm = r/(distancex(o, a)-r);
   point m = point((o.x+cm*a.x)/(1+cm), (o.y+cm*a.y)/(1+cm));
   double cn = r/(distancex(o, b)-r);
   point n = point((o.x+cn*b.x)/(1+cn), (o.y+cn*b.y)/(1+cn));
    double ret1 = acos((m.x*n.x+m.y*n.y)/m.sqrx()/n.sqrx())*r*r;
   double ret2 = acos((p1.x*p2.x+p1.y*p2.y)/p1.sqrx()/p2.sqrx())*r*r-fabs(xmult(p1, p2, o));
    double ret = (ret1-ret2)/2.0;
    if (xmult(a, b, o)<eps && sign>0.0 || xmult(a, b, o)>eps && sign<0.0)
       ret = -ret;
   return ret;
}
```

```
double Inter(double x,double y,double R,int n,point *area){
        area[n] = area[0];
        point temp = point(x, y);
        double sum = 0;
        for (int i=0; i<n-1; i++)</pre>
            sum += Direct_Triangle_Circle_Area(area[i], area[i+1], temp, R);
        sum += Direct_Triangle_Circle_Area(area[n-1], area[0], temp, R);
        return fabs(sum);
double Cross(point A,point B)
    return A.x*B.y - A.y*B.x;
}
int N,M;
double PolygonArea (point * p,int n)
    double area = 0;
    for(int i = 1; i < n - 1; ++i)
        area += Cross(p[i]-p[0],p[i+1]-p[0]);
    return fabs(area/2);
}
int dcmp(double x)
    if(fabs(x)<eps)</pre>
        return 0;
    else
        return x < 0?-1:1;
}
double S ;
double xi,yi,P,Q;
bool check(double R){
                  cout<<xi<" "<<yi<" "<<P<<" "<<Q<<endl;
//
          printf("r = %lf Intersect = %lf \ n", R, Inter(xi, yi, R, N, p));
//
          printf("%lf\n",(1-P/Q)*S);
        return dcmp(Inter(xi,yi,R,N,p) - (1-P/Q)*S) > 0;
int main()
{
        cin>>N;
        for(int i=0;i< N;i++)</pre>
            scanf("%lf%lf",&p[i].x,&p[i].y);
        }
    S= PolygonArea(p,N);
    //cout<<S<<endl;
    cin>>M;
        for(int i = 0;i < M; ++i){</pre>
```

```
scanf("%lf %lf %lf",&xi,&yi,&P,&Q);
               double l = 0, r = 1e6;
               for(int j = 0; j < 100; ++j){
                       double mid = 1+(r-1)/2;
                       if(check(mid))
                            r = mid:
                       else
                            1 = mid;
                // printf("%lf %lf\n",l,r);
               printf("%.81f\n",r);
       }
   return 0;
}
5.1.6 求圆与直线的交点.cpp
int getLineCircleIntersection(Point A, Point B, Point C, double r, double& t1, double& t2, vector<Point>
  // 初始方程:(A.x + t(B.x - A.x) - C.x)^2 + (A.y + t(B.y - A.y) - C.y)^2 = r^2
  // 整理得:(at + b)^2 + (ct + d)^2 = r^2
  double a = B.x - A.x;
  double b = A.x - C.x;
  double c = B.y - A.y;
  double d = A.y - C.y;
  // 展开得:(a~+c~)t~+2(ab+cd)t+b~+d~-r~=0,即 et~+ft+g=0
  double e = a * a + c * c;
  double f = 2 * (a * b + c * d);
  double g = b * b + d * d - r * r;
  double delta = f * f - 4 * e * g; // 判别式
  if(dcmp(delta) < 0) return 0; // 相离
  if(dcmp(delta) == 0){ // 相切
   t1 = t2 = -f / (2 * e);
   sol.push_back(A+(B-A)*t1);
   return 1;
  }
 t1 = (-f - sqrt(delta)) / (2 * e);
  t2 = (-f + sqrt(delta)) / (2 * e);
  sol.push_back(A+(B-A)*t1);
  sol.push_back(A+(B-A)*t2);
 return 2;
}
5.2
     3D
5.2.1 三维几何的基本操作.cpp
#include <bits/stdc++.h>
using namespace std;
struct Point3
    double x,y,z;
   Point3(double x = 0, double y = 0, double z = 0):x(x),y(y),z(z) {}
```

```
};
typedef Point3 Vector3;
Vector3 operator +(Vector3 v1, Vector3 v2)
    return Vector3(v1.x+v2.x,v1.y+v2.y,v1.z+v2.z);
Vector3 operator -(Vector3 v1, Vector3 v2)
    return Vector3(v1.x-v2.x,v1.y-v2.y,v1.z-v2.z);
}
Vector3 operator *(Vector3 v,double c)
    return Vector3(v.x*c,v.y*c,v.z*c);
}
Vector3 operator /(Vector3 v,double c)
    return Vector3(v.x/c,v.y/c,v.z/c);
}
double Dot(Vector3 A, Vector3 B)
    return A.x*B.x+A.y*B.y+A.z*B.z;
}
double Length(Vector3 A)
{
    return sqrt(Dot(A,A));
}
double Angle(Vector3 A, Vector3 B)
   return acos(Dot(A,B)/(2*Length(A)*Length(B)));
}
double DistanceToplane(const Point3 &p,const Point3 &p0,const Vector3& n)
    return fabs(Dot(p-p0,n))/Length(n);
Point3 GetPlaneProjection(const Point3&p,const Point3&p0,const Vector3&n)
    return p-n*Dot(p-p0,n);
//直线 p1-p2 到平面 p0-n 的交点。 假定交点唯一存在
Point3 LinePlaneIntetsection(Point3 p1,Point3 p2,Point3 p0,Vector3 n)
{
    Vector3 v= p2 - p1;
     /*if(dcmp(Dot(v,n))==0)
//
//
//
          if(dcmp(Dot(p1-p0,n))==0)
              直线在平面上
//
//
          else
              直线与平面平行
//
      }
    double t = Dot(n,p0-p1)/Dot(n,p2-p1);
    return p1 + v*t;
}
```

5.2.2 三维几何的模版.cpp

```
#include <bits/stdc++.h>
const double eps = 1e-6;
using namespace std;
struct Point3
    double x,y,z;
   Point3(double x = 0, double y = 0, double z = 0):x(x),y(y),z(z) {}
typedef Point3 Vector3;
int dcmp(double d)
{
    if(fabs(d) < eps)
        return 0;
   else
       return d < 0?-1:1;
}
Vector3 operator +(Vector3 v1, Vector3 v2)
   return Vector3(v1.x+v2.x,v1.y+v2.y,v1.z+v2.z);
}
Vector3 operator -(Vector3 v1, Vector3 v2)
   return Vector3(v1.x-v2.x,v1.y-v2.y,v1.z-v2.z);
Vector3 operator *(Vector3 v,double c)
   return Vector3(v.x*c,v.y*c,v.z*c);
}
Vector3 operator /(Vector3 v,double c)
   return Vector3(v.x/c,v.y/c,v.z/c);
}
bool operator ==(Point3 A,Point3 B)
  return !dcmp(A.x-B.x)&&!dcmp(A.y-B.y)&&!dcmp(A.z-B.z);
}
double Dot(Vector3 A, Vector3 B)
{
   return A.x*B.x+A.y*B.y+A.z*B.z;
double Length(Vector3 A)
   return sqrt(Dot(A,A));
double Angle(Vector3 A, Vector3 B) //求两向量的夹角
   return acos(Dot(A,B)/(2*Length(A)*Length(B)));
double DistanceToplane(const Point3 &p,const Point3 &p0,const Vector3& n)//
   return fabs(Dot(p-p0,n))/Length(n);
```

```
Point3 GetPlaneProjection(const Point3&p,const Point3&p0,const Vector3&n)
   return p-n*Dot(p-p0,n);
//直线 p1-p2 到平面 p0-n 的交点。 假定交点唯一存在
Point3 LinePlaneIntetsection(Point3 p1, Point3 p2, Point3 p0, Vector3 n)
   Vector3 v= p2 - p1;
     /*if(dcmp(Dot(v,n))==0)
//
//
//
          if(dcmp(Dot(p1-p0,n))==0)
             直线在平面上
//
//
         else
             直线与平面平行
//
//
     */
   double t = Dot(n,p0-p1)/Dot(n,p2-p1);
   return p1 + v*t;
Point3 LinePlaneIntetsection(Point3 p1,Point3 p2,double A,double B,double C,double D)
   Vector3 v = p2-p1;
   double t = (A*p1.x+B*p1.y+C*p1.z+D)/(A*(p1.x-p2.x)+B*(p1.y-p2.y)+C*(p1.z-p2.z));
   return p1 + v*t;
Vector3 Cross(Vector3 A, Vector3 B)
   return Vector3(A.y*B.z-A.z*B.y, A.z*B.x-A.x*B.z, A.x*B.y-A.y*B.x);
double Area2(Point3 A, Point3 B, Point3 C)
   return Length(Cross(B-A,C-A));
}
////已知平面的三点, 求出点法式
//Vector3 Solven(Point3 A, Point3 B, Point3 C)
1/5
//
     return Cross(B-A,C-A);
//判断一个点是否在三角形内, 可以用面积法
bool PointInTri(Point3 P,Point3 A,Point3 B,Point3 C)
   double area1 = Area2(P,A,B);
   double area2 = Area2(P,A,C);
   double area3 = Area2(P,B,C);
   double area4 = Area2(A,B,C);
   return dcmp(area1+area2+area3-area4)==0;
}
//判断线段是否与三角形相交
bool TriSegIntersection(Point3 P0, Point3 P1, Point3 P2, Point3 A, Point3 B, Point3 &P)
{
   Vector3 n = Cross(P1-P0, P2-P0);
    if(dcmp(Dot(n,B-A))==0)
```

```
return false;
    double t = Dot(n, PO-A)/Dot(n, B-A);
    if(dcmp(t) < 0 \mid \mid dcmp(t-1) > 0)
        return false;
    P = A + (B-A) * t;
    return PointInTri(P,P0,P1,P2);
double DitantceToLine(Point3 P,Point3 A,Point3 B)
{
    return Length(Cross(A-P,B-P))/Length(A-B);
}
double DistanceToSegment(Point3 P,Point3 A,Point3 B)
   if(A==B) return Length(P-A);
   Vector3 v1 = B - A, v2 = P - A, v3 = P-B;
   if(dcmp(Dot(v1,v2)) == 0) return Length(v2);
   if(dcmp(Dot(v1,v3)) > 0) return Length(v3);
   return Length(Cross(v1,v2))/Length(v1);
}
double Volume6(Point3 A,Point3 B,Point3 C,Point3 D)
    return Dot(D-A,Cross(B-A,C-A));
}
//
int main(void)
    Point3 A(0,0,0),B(0,100,0),C(100,0,0),D(25,25,0);
    cout<<PointInTri(D,A,B,C)<<endl;</pre>
    return 0;
}
5.2.3 三维凸包.cpp
struct Face{
    int v[3];
    Vector3 normal(Vector *P)
        return Cross(P[v[1]]-P[v[0]],P[v[2]]-P[v[0]]);
    int cansee(Point *P,int i)const
    {
        return Dot(P[i]-P[v[0]],normal(P)) > 0?1 : 0;
    }
};
vector <Face> CH3D(Point3* P,int n)
    vector <Face> cur;
    \operatorname{cur.push\_back}((\operatorname{Face})\{\{0,1,2\}\});
    cur.push_back((Face)\{\{2,1,0\}\});
    for(int i = 3;i < n; ++i)
    {
        vector<Face> next;
```

```
//计算每条边"左面"的可见性
        for(int j= 0; j < cur.size(); ++j)</pre>
           Face &f = cur[j];
            int res = f.cansee(P,i);
            if(!res) next.push_back(f);
            for(int k = 0; k < 3; ++k)
                vis[f.v[k]][f.v[(k+1)%3]] = res;
        }
        for(int j = 0; j < cur.size(); ++j)</pre>
            for(int k = 0; k < 3; ++k)
                int a = cur[j].v[k],b = cur[j].v[(k+1)%3];
                if(vis[a][b]!= vis[b][a]&&vis[a][b])//(a,b) 是分界线, 左边对 P[i] 可见
                 next.push_back((Face){{a,b,i}});
            }
        }
        cnr = next;
   }
   return cur;
double randO1() {return rand() / (double) RAND_MAX;}//O-1 的随机数
double randeps() {return (rand01()-0.5) * eps;}
Point3 add_noise(Point3 p)
   return Point3(p.x + randeps(),p.y+randeps(),p.z+randeps());
}
struct Face{
    int v[3];
   Vector3 normal(Vector *P)
        return Cross(P[v[1]]-P[v[0]],P[v[2]]-P[v[0]]);
   }
   int cansee(Point *P,int i)const
        return Dot(P[i]-P[v[0]],normal(P)) > 0?1 : 0;
   }
};
vector <Face> CH3D(Point3* P,int n)
   vector <Face> cur;
    cur.push_back((Face){{0,1,2}});
    cur.push_back((Face)\{\{2,1,0\}\});
   for(int i = 3;i < n; ++i)</pre>
    {
        vector<Face> next;
        //计算每条边"左面"的可见性
        for(int j= 0; j < cur.size(); ++j)</pre>
            Face &f = cur[j];
            int res = f.cansee(P,i);
```

```
if(!res) next.push_back(f);
            for(int k = 0; k < 3; ++k)
                vis[f.v[k]][f.v[(k+1)%3]] = res;
       }
       for(int j = 0; j < cur.size(); ++j)</pre>
            for(int k = 0; k < 3; ++k)
            {
                int a = cur[j].v[k],b = cur[j].v[(k+1)%3];
                if(vis[a][b]!= vis[b][a]&&vis[a][b])//(a,b) 是分界线, 左边对 P[i] 可见
                 next.push_back((Face){{a,b,i}});
            }
        }
        cnr = next;
   }
   return cur;
}
double randO1() {return rand() / (double) RAND_MAX;}//O-1 的随机数
double randeps() {return (rand01()-0.5) * eps;}
Point3 add noise(Point3 p)
   return Point3(p.x + randeps(),p.y+randeps(),p.z+randeps());
}
5.2.4 维度转换为三维坐标.cpp
// 经纬度转换为球坐标
double torad(double deg)
   return deg/180*acos(-1);
}
void get_coordinate(double R,double lat,double lng,double &x,double &y,double &z)
   lat = torad(lat);
   lng = torad(lng);
   x = R*cos(lat)*cos(lng);
   y = R*cos(lat)*sin(lng);
   z = R*sin(lat);
}
    6 其它
6
6.1 IO
6.1.1 fread.cpp
namespace io {
    const int L = 1 << 20 | 1;</pre>
    char ibuf[L], *iS, *iT, c, obuf[L], *oS = obuf, *oT = obuf + L - 1, qu[55]; int f, qr;
#ifdef whzzt
    #define gc() getchar()
    #define qc() (iS == iT ? (iT = (iS = ibuf) + fread (ibuf, 1, L, stdin), <math>iS == iT ? EOF : *iS ++) :
#endif
```

```
template <class I>
    inline void gi (I &x) {
        for (f = 1, c = gc(); c < 0' | c > 9'; c = gc()) if (c == -1) f = -1;
        for (x = 0; c \le 9' \&\& c \ge 0'; c = gc()) x = x * 10 + (c \& 15); x *= f;
   inline void flush () {
       fwrite (obuf, 1, oS - obuf, stdout);
   }
    inline void putc (char x) {
        *oS ++ = x;
        if (oS == oT) flush (), oS = obuf;
   }
   template <class I>
   void print (I x) {
        if (!x) putc ('0'); if (x < 0) putc ('-'), x = -x;
        while (x) qu[++ qr] = x \% 10 + '0', x /= 10;
       while (qr) putc (qu[qr --]);
   }
   struct io_ff { ~io_ff() { flush(); } } _io_ff_;
}
using io :: gi;
using io :: putc;
using io :: print;
6.1.2 fread 2. cpp
namespace IO{
    #define BUF_SIZE 100000
    #define OUT_SIZE 100000
    #define ll long long
    //fread->read
   bool IOerror=0;
    inline char nc(){
        static char buf[BUF_SIZE],*p1=buf+BUF_SIZE,*pend=buf+BUF_SIZE;
        if (p1==pend){
            p1=buf; pend=buf+fread(buf,1,BUF SIZE,stdin);
            if (pend==p1){IOerror=1;return -1;}
            //{printf("IO error!\n"); system("pause"); for (;;); exit(0);}
        }
       return *p1++;
   }
    inline bool blank(char ch){return ch==' '||ch=='\n'||ch=='\r'||ch=='\t';}
    inline void read(int &x){
        bool sign=0; char ch=nc(); x=0;
        for (;blank(ch);ch=nc());
        if (IOerror)return;
        if (ch=='-')sign=1,ch=nc();
        for (;ch>='0'&&ch<='9';ch=nc())x=x*10+ch-'0';
        if (sign)x=-x;
   }
    inline void read(ll &x){
        bool sign=0; char ch=nc(); x=0;
        for (;blank(ch);ch=nc());
```

```
if (IOerror)return;
    if (ch=='-')sign=1,ch=nc();
    for (;ch>='0'\&\&ch<='9';ch=nc())x=x*10+ch-'0';
    if (sign)x=-x;
}
inline void read(double &x){
    bool sign=0; char ch=nc(); x=0;
    for (;blank(ch);ch=nc());
    if (IOerror)return;
    if (ch=='-')sign=1,ch=nc();
    for (;ch>='0'\&\&ch<='9';ch=nc())x=x*10+ch-'0';
    if (ch=='.'){
        double tmp=1; ch=nc();
        for (;ch>='0'\&\&ch<='9';ch=nc())tmp/=10.0,x+=tmp*(ch-'0');
    }
    if (sign)x=-x;
}
inline void read(char *s){
    char ch=nc();
    for (;blank(ch);ch=nc());
    if (IOerror)return;
    for (;!blank(ch)&&!IOerror;ch=nc())*s++=ch;
    *s=0;
inline void read(char &c){
    for (c=nc();blank(c);c=nc());
    if (IOerror){c=-1;return;}
//fwrite->write
struct Ostream_fwrite{
    char *buf,*p1,*pend;
    Ostream_fwrite(){buf=new char[BUF_SIZE];p1=buf;pend=buf+BUF_SIZE;}
    void out(char ch){
        if (p1==pend){
            fwrite(buf,1,BUF_SIZE,stdout);p1=buf;
        *p1++=ch;
    }
    void print(int x){
        static char s[15],*s1;s1=s;
        if (!x)*s1++='0'; if (x<0)out('-'), x=-x;
        while (x)*s1++=x\%10+'0', x/=10;
        while (s1--!=s) out (*s1);
    }
    void println(int x){
        static char s[15],*s1;s1=s;
        if (!x)*s1++='0'; if (x<0)out('-'), x=-x;
        while(x)*s1++=x\frac{10+0}{x},x/=10;
        while (s1--!=s) out (*s1); out ('\n');
    }
    void print(ll x){
        static char s[25],*s1;s1=s;
        if (!x)*s1++='0'; if (x<0)out('-'), x=-x;
        while (x)*s1++=x\%10+'0', x/=10;
```

```
while (s1--!=s) out (*s1);
       }
       void println(ll x){
          static char s[25],*s1;s1=s;
          if (!x)*s1++='0'; if (x<0)out('-'), x=-x;
          while (x)*s1++=x\%10+'0', x/=10;
          while (s1--!=s) out (*s1); out ('\n');
       }
       void print(double x,int y){
          if (x<-1e-12)out('-'), x=-x; x*=mul[y];
          11 x1=(11)floor(x); if (x-floor(x)>=0.5)++x1;
          11 x2=x1/mul[y],x3=x1-x2*mul[y]; print(x2);
          if (y>0){out('.'); for (size_t i=1;i<y&&x3*mul[i]<mul[y];out('0'),++i); print(x3);}
       }
       void println(double x,int y){print(x,y);out('\n');}
       void print(char *s){while (*s)out(*s++);}
       void println(char *s){while (*s)out(*s++);out('\n');}
       void flush(){if (p1!=buf){fwrite(buf,1,p1-buf,stdout);p1=buf;}}
       ~Ostream fwrite(){flush();}
   }Ostream;
   inline void print(int x){Ostream.print(x);}
   inline void println(int x){Ostream.println(x);}
   inline void print(char x){Ostream.out(x);}
   inline void println(char x){Ostream.out(x);Ostream.out('\n');}
   inline void print(ll x){Ostream.print(x);}
   inline void println(ll x){Ostream.println(x);}
   inline void print(double x,int y){Ostream.print(x,y);}
   inline void println(double x,int y){Ostream.println(x,y);}
   inline void print(char *s){Ostream.print(s);}
   inline void println(char *s){Ostream.println(s);}
   inline void println(){Ostream.out('\n');}
   inline void flush(){Ostream.flush();}
   #undef ll
   #undef OUT SIZE
   #undef BUF_SIZE
};
6.1.3 保留小数.cpp
#include <bits/stdc++.h>
using namespace std;
const double pi = acos(-1.0);
int main(void)
{
   for(int i = 0; i < 5; ++i)
   printf("%.*f\n",i,pi);
   for(int i = 0; i < 5; ++i)
       cout<<setiosflags(ios::fixed)<<setprecision(i)<<pi<<endl;</pre>
   return 0;
}
```

```
6.1.4 读取整数.cpp
```

```
//读取正负整数
inline int input(void)
   int num = 0;
   char c;
   int flag = 0;
   while((c = getchar()) < '0' \mid \mid c > '9') flag = c=='-' ? 1:flag;
   while(c >= '0' \&\& c <= '9')
       num = num * 10 + c - '0', c = getchar();
   if(flag) num = -num;
   return num:
}
6.2 c++ 中处理 2 进制的一些函数.cpp
Built-in Function: int __builtin_ffs (unsigned int x)
Returns one plus the index of the least significant 1-bit of x, or if x is zero, returns zero.
返回右起第一个'1'的位置。
Built-in Function: int __builtin_clz (unsigned int x)
Returns the number of leading 0-bits in x, starting at the most significant bit position. If x is 0, th
返回左起第一个'11'之前0的个数。
Built-in Function: int __builtin_ctz (unsigned int x)
Returns the number of trailing 0-bits in x, starting at the least significant bit position. If x is 0,
返回右起第一个'1'之后的0的个数。
Built-in Function: int __builtin_popcount (unsigned int x)
Returns the number of 1-bits in x.
返回'1'的个数。
Built-in Function: int __builtin_parity (unsigned int x)
Returns the parity of x, i.e. the number of 1-bits in x modulo 2.
返回'1'的个数的奇偶性。
Built-in Function: int __builtin_ffsl (unsigned long)
Similar to __builtin_ffs, except the argument type is unsigned long.
Built-in Function: int __builtin_clzl (unsigned long)
Similar to __builtin_clz, except the argument type is unsigned long.
Built-in Function: int __builtin_ctzl (unsigned long)
Similar to __builtin_ctz, except the argument type is unsigned long.
  Built-in Function: int __builtin_popcountl (unsigned long)
```

```
Similar to __builtin_popcount, except the argument type is unsigned long.

Built-in Function: int __builtin_parityl (unsigned long)

Similar to __builtin_parity, except the argument type is unsigned long.

Built-in Function: int __builtin_ffsll (unsigned long long)

Similar to __builtin_ffs, except the argument type is unsigned long long.

Built-in Function: int __builtin_clzll (unsigned long long)

Similar to __builtin_clz, except the argument type is unsigned long long.

Built-in Function: int __builtin_ctzll (unsigned long long)

Similar to __builtin_ctz, except the argument type is unsigned long long.

Built-in Function: int __builtin_popcountll (unsigned long long)

Similar to __builtin_popcount, except the argument type is unsigned long long.

Built-in Function: int __builtin_parityll (unsigned long long)

Similar to __builtin_parity, except the argument type is unsigned long long.
```

6.3 测量程序的运行时间.cpp