

(12) **United States Patent**
Zhang et al.

(10) **Patent No.:** **US 12,384,410 B2**
(45) **Date of Patent:** **Aug. 12, 2025**

(54) **TASK-MOTION PLANNING FOR SAFE AND EFFICIENT URBAN DRIVING**

(71) Applicant: **The Research Foundation for The State University of New York,**
Binghamton, NY (US)

(72) Inventors: **Shiqi Zhang,** Vestal, NY (US); **Yan Ding,** Shanghai (CN)

(73) Assignee: **The Research Foundation for The State University of New York,**
Binghamton, NY (US)

(*) Notice: Subject to any disclaimer, the term of this patent is extended or adjusted under 35 U.S.C. 154(b) by 323 days.

(21) Appl. No.: **17/687,636**

(22) Filed: **Mar. 5, 2022**

(65) **Prior Publication Data**
US 2022/0306152 A1 Sep. 29, 2022

Related U.S. Application Data
(60) Provisional application No. 63/200,431, filed on Mar. 5, 2021.

(51) **Int. Cl.**
B60W 60/00 (2020.01)
B60W 30/14 (2006.01)
(Continued)

(52) **U.S. Cl.**
CPC **B60W 60/0011** (2020.02); **B60W 30/143** (2013.01); **B60W 40/04** (2013.01);
(Continued)

(58) **Field of Classification Search**
CPC B60W 60/0011; B60W 60/0015; B60W 60/00274; B60W 30/143; B60W 40/04;
(Continued)

(56) **References Cited**
U.S. PATENT DOCUMENTS

4,296,901 A 10/1981 Perrott
4,833,469 A 5/1989 David
(Continued)

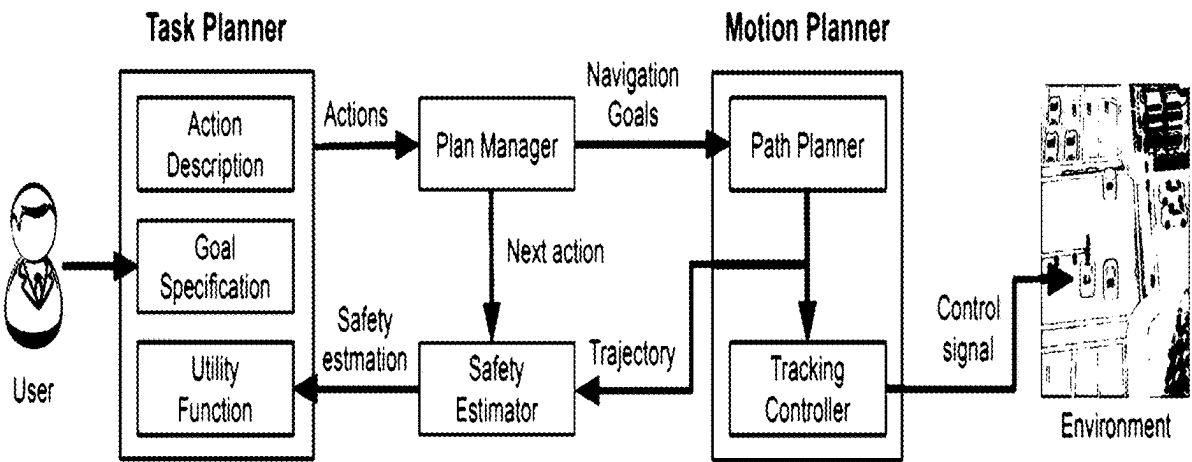
OTHER PUBLICATIONS
Quach Hai Tho, Huynh Cong Phap, Pham Anh Phuong, A Predictive Control Solution for Contingency Motion Planning for Autonomous Vehicle, 2019 IEEE-RIVF International Conference on Computing and Communication Technologies (RIVF) (pp. 1-6) (Year: 2019).*

Primary Examiner — Scott A Browne
Assistant Examiner — Terry C Buse
(74) *Attorney, Agent, or Firm* — Hoffberg & Associates;
Steven M. Hoffberg

(57) **ABSTRACT**

Autonomous vehicles plan at a task level to compute a sequence of symbolic actions to fulfill service requests, where efficiency is the main concern. The vehicle computes continuous trajectories to perform actions at the motion level, where safety is important. Task-motion planning in autonomous driving faces the problem of maximizing task-level efficiency while ensuring motion-level safety. Task-Motion Planning for Urban Driving (TMPUD) enables the task and motion planners to communicate about the safety level of driving behaviors. The motion planner incrementally advances the vehicle toward a goal with an associated incremental utility, based on at least a safety of motion trajectories. The task planner defines the goal and a sequence of the actions to advance the vehicle toward the goal, dependent an optimization of aggregate prospective utility of the task and the safety of the motion trajectories.

20 Claims, 6 Drawing Sheets



(51)	Int. Cl. B60W 40/04 B60W 40/06	(2006.01) (2012.01)	8,355,834 B2	1/2013	Duggan
			8,364,334 B2	1/2013	Au
			8,412,449 B2	4/2013	Trepagnier
			8,433,790 B2	4/2013	Polley
(52)	U.S. Cl. CPC	B60W 40/06 (2013.01); B60W 60/0015 (2020.02); B60W 60/00274 (2020.02); B60W 2540/18 (2013.01); B60W 2554/80 (2020.02)	8,437,875 B2	5/2013	Hernandez
			8,437,890 B2	5/2013	Anderson
			8,442,713 B2	5/2013	Kim
			8,474,043 B2	6/2013	Sturges
(58)	Field of Classification Search CPC	B60W 40/06 ; B60W 2554/80 ; B60W 2540/18	8,576,430 B2	11/2013	Balduccini
			8,577,538 B2	11/2013	Lenser
			8,578,002 B1	11/2013	Roesch
			8,583,313 B2	11/2013	Mian
		See application file for complete search history.	8,601,034 B2	12/2013	Roesch
			8,606,589 B2	12/2013	McGinn
			8,612,084 B2	12/2013	Hennessy
			8,671,182 B2	3/2014	Vogel, III
(56)	References Cited U.S. PATENT DOCUMENTS		8,677,486 B2	3/2014	Olney
			8,706,394 B2	4/2014	Trepagnier
			8,744,648 B2	6/2014	Anderson
			8,751,143 B2	6/2014	Kelly
			8,755,997 B2	6/2014	Au
			8,755,999 B2	6/2014	Kelly
			8,768,555 B2	7/2014	Duggan
			8,784,034 B2	7/2014	Lert, Jr.
			8,798,828 B2	8/2014	Erlston
			8,843,244 B2	9/2014	Phillips
			8,880,287 B2	11/2014	Lee
			8,935,071 B2	1/2015	Lee
			8,947,531 B2	2/2015	Fischer
			8,948,955 B2	2/2015	Zhu
			8,954,194 B2	2/2015	Allis
			8,988,524 B2	3/2015	Smyth
			8,990,387 B2	3/2015	Burchfield
			9,055,094 B2	6/2015	Wease
			9,059,960 B2	6/2015	Burchfield
			9,097,800 B1	8/2015	Zhu
			9,100,363 B2	8/2015	Burchfield
			9,110,905 B2	8/2015	Polley
			9,117,201 B2	8/2015	Kennell
			9,120,484 B1	9/2015	Ferguson
			9,120,485 B1	9/2015	Dolgov
			9,135,432 B2	9/2015	Roesch
			9,139,363 B2	9/2015	Lert
			9,140,814 B2	9/2015	Welker
			9,199,667 B2	12/2015	Di Cairano
			9,201,421 B1	12/2015	Fairfield
			9,201,424 B1	12/2015	Ogale
			9,202,382 B2	12/2015	Klinger
			9,208,456 B2	12/2015	McGinn
			9,223,025 B2	12/2015	Debrunner
			9,234,618 B1	1/2016	Zhu
			9,261,590 B1	2/2016	Brown
			9,265,187 B2	2/2016	Cavender-Bares
			9,288,938 B2	3/2016	Cavender-Bares
			9,298,186 B2	3/2016	Harvey
			9,327,734 B2	5/2016	Lombrozo
			9,349,055 B1	5/2016	Ogale
			9,373,149 B2	6/2016	Abhyanker
			9,373,262 B2	6/2016	Stigler
			9,383,752 B2	7/2016	Mian
			9,383,753 B1	7/2016	Templeton
			9,384,666 B1	7/2016	Harvey
			9,392,743 B2	7/2016	Camacho-Cook
			9,423,498 B1	8/2016	Brown
			9,432,929 B1	8/2016	Ross
			9,434,309 B1	9/2016	Smyth
			9,435,652 B2	9/2016	Ralston
			9,450,975 B2	9/2016	Wease
			9,451,020 B2	9/2016	Liu
			9,494,439 B1	11/2016	Ross
			9,494,940 B1	11/2016	Kentley
			9,494,943 B2	11/2016	Harvey
			9,507,346 B1	11/2016	Levinson
			9,508,260 B2	11/2016	Shaik
			9,510,316 B2	11/2016	Skaaksrud
			9,513,632 B1	12/2016	Gordon
			9,517,767 B1	12/2016	Kentley
			9,523,984 B1	12/2016	Herbach
			9,523,986 B1	12/2016	Abebe

(56)

References Cited

U.S. PATENT DOCUMENTS

9,535,423	B1	1/2017	Debreczeni	9,911,030	B1	3/2018	Zhu
9,536,427	B2	1/2017	Tonguz	9,913,240	B2	3/2018	Skaaksrud
9,545,995	B1	1/2017	Chau	9,915,950	B2	3/2018	Hartung
9,547,309	B2	1/2017	Ross	9,916,538	B2	3/2018	Zadeh
9,547,986	B1	1/2017	Curlander	9,916,703	B2	3/2018	Levinson
9,547,989	B2	1/2017	Fairfield	9,921,065	B2	3/2018	Brannstrom
9,557,736	B1	1/2017	Silver	9,925,462	B2	3/2018	Sakakibara
9,559,804	B2	1/2017	Ibrahim	9,933,779	B2	4/2018	Ross
9,561,941	B1	2/2017	Watts	9,939,817	B1	4/2018	Kentley-Klay
9,563,199	B1	2/2017	Ferguson	9,940,651	B2	4/2018	Ross
9,581,460	B1	2/2017	McNew	9,944,291	B2	4/2018	Gordon
9,584,535	B2	2/2017	Roesch	9,946,531	B1	4/2018	Fields
9,598,239	B2	3/2017	Lert, Jr.	9,946,890	B2	4/2018	Valasek
9,599,989	B1	3/2017	Brown	9,947,224	B2	4/2018	Fairfield
9,603,158	B1	3/2017	Ross	9,948,917	B2	4/2018	Inacio De Matos
9,606,539	B1	3/2017	Kentley	9,949,228	B2	4/2018	Skaaksrud
9,612,123	B1	4/2017	Levinson	9,950,568	B2	4/2018	Edgren
9,630,619	B1	4/2017	Kentley	9,955,436	B2	4/2018	Neves
9,632,502	B1	4/2017	Levinson	9,958,379	B1	5/2018	Zhu
9,645,578	B2	5/2017	Harvey	9,958,864	B2	5/2018	Kentley-Klay
9,662,068	B2	5/2017	Raymondos	9,958,875	B2	5/2018	Paduano
9,669,904	B2	6/2017	Hanson	9,959,754	B1	5/2018	King
9,672,446	B1	6/2017	Vallespi-Gonzalez	9,963,143	B2	5/2018	Lu
9,674,759	B2	6/2017	Czaja	9,964,952	B1	5/2018	Costa
9,679,191	B1	6/2017	Zhu	9,964,954	B1	5/2018	Silver
9,679,206	B1	6/2017	Ferguson	9,967,815	B2	5/2018	Condeixa
9,688,396	B2	6/2017	Avery, III	9,969,285	B2	5/2018	Henry
9,693,297	B2	6/2017	Condeixa	9,969,326	B2	5/2018	Ross
9,702,098	B1	7/2017	King	9,969,481	B2	5/2018	Stigler
9,702,443	B2	7/2017	Erlston	9,977,430	B2	5/2018	Shalev-Shwartz
9,707,966	B2	7/2017	Herbach	9,981,669	B2	5/2018	Gordon
9,710,710	B2	7/2017	Malecki	9,983,305	B2	5/2018	Pavek
9,718,471	B2	8/2017	Gordon	9,988,055	B1	6/2018	O'Flaherty et al.
9,720,412	B1	8/2017	Zhu	9,989,645	B2	6/2018	Donnelly
9,720,415	B2	8/2017	Levinson	10,000,124	B2	6/2018	Kentley-Klay
9,721,397	B2	8/2017	Gordon	10,000,338	B2	6/2018	Lert, Jr.
9,733,378	B2	8/2017	Carcatterra	10,007,264	B2	6/2018	Zhu
9,734,455	B2	8/2017	Levinson	10,007,271	B2	6/2018	Amla
9,739,881	B1	8/2017	Pavek	10,012,981	B2	7/2018	Garipey
9,740,205	B2	8/2017	Ross	10,012,990	B2	7/2018	Rander
9,746,444	B2	8/2017	Goroshevskiy	10,019,002	B2	7/2018	Harnett
9,754,490	B2	9/2017	Kentley	10,019,008	B2	7/2018	Kong
9,760,092	B2	9/2017	Ferguson	10,019,011	B1	7/2018	Green
9,761,136	B2	9/2017	Tonguz	10,030,418	B2	7/2018	McGinn
9,766,333	B1	9/2017	Brown	10,031,521	B1	7/2018	Newman
9,783,075	B2	10/2017	Henry	10,031,526	B1	7/2018	Li
9,783,262	B2	10/2017	Dubose	10,037,553	B2	7/2018	Ross
9,788,282	B2	10/2017	Neves	10,040,632	B2	8/2018	Lert, Jr.
9,798,329	B2	10/2017	Shattil	10,048,683	B2	8/2018	Levinson
9,802,661	B1	10/2017	Kentley-Klay	10,049,328	B2	8/2018	Jiang
9,802,759	B2	10/2017	Lert, Jr.	10,053,091	B2	8/2018	Jiang
9,804,594	B2	10/2017	Garipey	10,054,945	B2	8/2018	Zhu
9,804,599	B2	10/2017	Kentley-Klay	10,055,653	B2	8/2018	Cohen
9,804,601	B2	10/2017	Lombrozo	10,061,313	B2	8/2018	Letwin
9,805,605	B2	10/2017	Ramanujam	10,061,325	B2	8/2018	Watts
9,821,801	B2	11/2017	Di Cairano	10,065,638	B1	9/2018	Wood
9,821,807	B2	11/2017	Herbach	10,065,654	B2	9/2018	Nishi
9,833,901	B2	12/2017	Perrone	10,073,456	B2	9/2018	Mudalige
9,834,224	B2	12/2017	Gordon	10,073,462	B2	9/2018	Debreczeni
9,836,973	B2	12/2017	Gordon	10,074,223	B2	9/2018	Newman
9,857,795	B2	1/2018	Gupta	10,083,604	B2	9/2018	Ricci
9,857,798	B2	1/2018	Ogale	10,086,782	B1	10/2018	Konrardy
9,862,391	B2	1/2018	Morfin	10,089,116	B2	10/2018	Valasek
9,864,378	B1	1/2018	Ferguson	10,095,236	B1	10/2018	Ferguson
9,868,332	B2	1/2018	Anderson	10,096,067	B1	10/2018	Slusar
9,874,871	B1	1/2018	Zhu	10,109,195	B2	10/2018	Gordon
9,878,664	B2	1/2018	Kentley-Klay	10,118,577	B1	11/2018	Sweeney
9,884,630	B1	2/2018	Ross	10,118,639	B2	11/2018	Zhu
9,891,333	B2	2/2018	Valsvik	10,122,736	B2	11/2018	Baxley
9,896,100	B2	2/2018	Gordon	10,123,473	B2	11/2018	Cavender-Bares
9,898,005	B2	2/2018	Mei	10,126,136	B2	11/2018	Iagnemma
9,902,396	B2	2/2018	Itagaki	10,126,742	B2	11/2018	Ross
9,904,286	B2	2/2018	Kozak	10,126,749	B2	11/2018	Rander
9,910,434	B1	3/2018	Nelson	10,127,465	B2	11/2018	Cohen
9,910,441	B2	3/2018	Levinson	10,127,818	B2	11/2018	Mandeville-Clarke
				10,133,275	B1	11/2018	Kobilarov
				10,134,278	B1	11/2018	Konrardy
				10,137,896	B2	11/2018	Zhuang
				10,137,903	B2	11/2018	Tascione

(56)

References Cited

U.S. PATENT DOCUMENTS

10,139,237 B2	11/2018	Outwater	10,296,006 B2	5/2019	Lee
10,139,818 B2	11/2018	Tao	10,298,910 B1	5/2019	Kroeger
10,139,823 B2	11/2018	Prokhorov	10,303,171 B1	5/2019	Brady
10,139,828 B2	11/2018	Ho	10,303,174 B2	5/2019	Kentley-Klay
10,140,468 B2	11/2018	Valasek	10,303,182 B2	5/2019	Harvey
10,143,040 B2	11/2018	Condeixa	10,303,183 B2	5/2019	Harvey
10,152,891 B2	12/2018	Rusciolelli	10,303,959 B2	5/2019	Cohen
10,156,845 B1	12/2018	Greenberger	10,305,765 B2	5/2019	Church
10,156,848 B1	12/2018	Konrardy	10,308,430 B1	6/2019	Brady
10,156,849 B1	12/2018	Zych	10,309,777 B2	6/2019	Zhang
10,156,850 B1	12/2018	Ansari	10,309,778 B2	6/2019	Zhang
10,157,423 B1	12/2018	Fields	10,309,792 B2	6/2019	Iagnemma
10,160,378 B2	12/2018	Sweeney	10,310,499 B1	6/2019	Brady
10,160,457 B1	12/2018	O'Flaherty et al.	10,310,500 B1	6/2019	Brady
10,160,484 B2	12/2018	Lee	10,310,514 B2	6/2019	Harvey
10,162,354 B2	12/2018	Kong	10,310,515 B2	6/2019	Harvey
10,163,139 B2	12/2018	Ross	10,310,517 B2	6/2019	Paduano
10,166,994 B1	1/2019	Fields	10,311,731 B1	6/2019	Li
10,168,703 B1	1/2019	Konrardy	10,317,231 B2	6/2019	Ferencz
10,171,967 B2	1/2019	Ameixieira	10,317,899 B2	6/2019	Liu
10,173,679 B2	1/2019	Gordon	10,317,911 B2	6/2019	Harvey
10,179,700 B2	1/2019	Lert, Jr.	10,317,912 B2	6/2019	Harvey
10,187,751 B2	1/2019	Coutinho	10,317,913 B2	6/2019	Harvey
10,188,024 B2	1/2019	Rusciolelli	10,319,224 B2	6/2019	de Azevedo
10,191,493 B2	1/2019	Zhu	10,324,463 B1	6/2019	Konrardy
10,197,407 B2	2/2019	Mouthaan	10,327,160 B2	6/2019	Lopes
10,198,619 B1	2/2019	Zhu	10,331,127 B2	6/2019	Oba
10,202,117 B2	2/2019	Gordon	10,331,133 B2	6/2019	Lombrozo
10,203,697 B2	2/2019	Ogale	10,331,136 B2	6/2019	Perrone
10,205,457 B1	2/2019	Josefsberg	10,331,138 B2	6/2019	Zhu
10,209,715 B2	2/2019	Hardy	10,331,141 B2	6/2019	Grimm
10,214,240 B2	2/2019	Ghose	10,332,320 B2	6/2019	Lakshamanan
10,216,196 B2	2/2019	Harvey	10,334,050 B2	6/2019	Kentley-Klay
10,220,705 B2	3/2019	Ramanujam	10,336,321 B1	7/2019	Fields
10,220,857 B2	3/2019	Jones	10,338,594 B2	7/2019	Long
10,222,211 B2	3/2019	Chen	10,342,067 B2	7/2019	Coutinho
10,222,462 B2	3/2019	Brown	10,343,559 B2	7/2019	Xiao
10,222,798 B1	3/2019	Brady	10,343,685 B2	7/2019	Zhu
10,223,479 B1	3/2019	Konrardy	10,343,698 B2	7/2019	Poeppel
10,223,916 B2	3/2019	Song	10,345,808 B2	7/2019	Wilkinson
10,225,348 B2	3/2019	Wang	10,345,809 B2	7/2019	Ross
10,227,075 B2	3/2019	Zhu	10,345,810 B1	7/2019	Zhu
10,228,690 B2	3/2019	Bostick	10,349,011 B2	7/2019	Du
10,229,590 B2	3/2019	Du	10,351,261 B1	7/2019	Bryant
10,233,021 B1	3/2019	Brady	10,353,390 B2	7/2019	Linscott
10,234,863 B2	3/2019	Ross	10,353,393 B2	7/2019	Zhu
10,235,881 B2	3/2019	Nishi	10,353,694 B1	7/2019	Fields
10,241,509 B1	3/2019	Fields	10,353,931 B2	7/2019	Wheeler
10,241,516 B1	3/2019	Brady	10,354,157 B2	7/2019	Cohen
10,243,604 B2	3/2019	Ross	10,358,147 B2	7/2019	Zamorano Morfin
10,245,993 B1	4/2019	Brady	10,359,783 B2	7/2019	Williams
10,246,097 B1	4/2019	Fields	10,360,021 B2	7/2019	Pereira Cabral
10,248,119 B2	4/2019	Kentley-Klay	10,364,027 B2	7/2019	Loveland
10,248,120 B1	4/2019	Siegel	10,365,654 B2	7/2019	Wood
10,248,124 B2	4/2019	Bellaiche	10,365,657 B2	7/2019	Tokuyama
10,249,109 B1	4/2019	Konrardy	10,369,974 B2	8/2019	Carlson
10,253,468 B1	4/2019	Linville	10,372,129 B1	8/2019	Urmson
10,254,763 B2	4/2019	Tatourian	10,372,130 B1	8/2019	Kaushansky
10,256,890 B2	4/2019	Neves	10,372,141 B2	8/2019	Donnelly
10,259,514 B2	4/2019	Kentley-Klay	10,373,097 B2	8/2019	Kulkarni
10,260,898 B2	4/2019	McNew	10,373,268 B1	8/2019	Orphys
10,261,514 B2	4/2019	Zych	10,379,538 B1	8/2019	Sheckells
10,262,217 B2	4/2019	Cohen	10,380,890 B2	8/2019	Wang
10,266,180 B1	4/2019	Fields	10,386,192 B1	8/2019	Konrardy
10,267,634 B2	4/2019	Chen	10,386,856 B2	8/2019	Wood
10,267,635 B2	4/2019	Chen	10,388,155 B2	8/2019	Curlander
10,268,200 B2	4/2019	Fang	10,388,162 B2	8/2019	de Moura
10,272,778 B2	4/2019	Zhu	10,392,025 B2	8/2019	Ross
10,272,924 B2	4/2019	Luo	10,394,245 B2	8/2019	Li
10,284,777 B2	5/2019	Rogers	10,395,285 B2	8/2019	Ross
10,288,439 B2	5/2019	Pedersen	10,395,332 B1	8/2019	Konrardy
10,289,110 B2	5/2019	Zhu	10,397,019 B2	8/2019	Hartung
10,293,932 B2	5/2019	Alzahrani	10,399,458 B2	9/2019	Prunty
10,295,363 B1	5/2019	Konrardy	10,401,852 B2	9/2019	Levinson
10,296,004 B2	5/2019	Nishi	10,401,867 B2	9/2019	Strautmann
			10,405,215 B2	9/2019	Tavares Coutinho
			10,407,076 B2	9/2019	Luo
			10,409,279 B2	9/2019	Kwon
			10,410,250 B2	9/2019	Singhal

(56)

References Cited

U.S. PATENT DOCUMENTS

10,410,747 B2	9/2019	Matos	10,528,836 B1	1/2020	Krishnan
10,416,670 B1	9/2019	Fields	10,529,027 B1	1/2020	Konrardy
10,416,671 B2	9/2019	Herbach	10,531,004 B2	1/2020	Wheeler
10,416,677 B2	9/2019	Dean	10,532,885 B1	1/2020	Brady
10,421,460 B2	9/2019	Jiang	10,534,364 B2	1/2020	Zhu
10,421,463 B2	9/2019	Luo	10,536,497 B2	1/2020	Condeixa
10,423,162 B2	9/2019	Yalla	10,543,838 B2	1/2020	Kentley-Klay
10,425,954 B2	9/2019	Karjee	10,543,844 B2	1/2020	Gordon
10,429,194 B2	10/2019	Wheeler	10,545,024 B1	1/2020	Konrardy
10,429,849 B2	10/2019	Zhang	10,545,029 B2	1/2020	Yang
10,430,653 B2	10/2019	Malecki	10,545,507 B2	1/2020	Aitken
10,431,018 B1	10/2019	Fields	10,546,560 B2	1/2020	Bradley
10,433,243 B2	10/2019	Lopes	10,549,752 B2	2/2020	Zhu
10,435,015 B2	10/2019	Kong	10,554,527 B2	2/2020	Lopes
10,435,242 B2	10/2019	Lert, Jr.	10,554,901 B2	2/2020	Kiser
10,436,595 B2	10/2019	Wang	10,558,222 B2	2/2020	Fridman
10,436,885 B2	10/2019	Wheeler	10,558,864 B2	2/2020	Huang
10,437,247 B2	10/2019	Patel	10,562,538 B2	2/2020	Lan
10,437,256 B2	10/2019	Andert	10,563,993 B1	2/2020	Ho
10,438,493 B2	10/2019	Bavar	10,564,643 B2	2/2020	Lui
10,440,547 B2	10/2019	Ameixieira	10,567,650 B2	2/2020	Rogers
10,444,759 B2	10/2019	Douillard	10,569,651 B2	2/2020	Zhu
10,446,031 B2	10/2019	Agnew	10,569,663 B2	2/2020	Webb
10,446,037 B2	10/2019	Kentley-Klay	10,569,773 B2	2/2020	Zhao
10,449,957 B2	10/2019	Nagy	10,571,916 B2	2/2020	Tschanz
10,451,514 B2	10/2019	Xu	10,571,922 B2	2/2020	Greenfield
10,452,065 B2	10/2019	Xiao	10,572,514 B2	2/2020	Wheeler
10,452,070 B2	10/2019	Greenfield	10,572,717 B1	2/2020	Zhu
10,459,441 B2	10/2019	Zhuang	10,573,178 B2	2/2020	Nascimento
10,459,444 B1	10/2019	Kentley-Klay	10,576,966 B2	3/2020	Endo
10,466,712 B2	11/2019	Ferguson	10,576,991 B2	3/2020	Gao
10,467,581 B2	11/2019	Laury	10,579,054 B2	3/2020	Zhao
10,467,915 B2	11/2019	Kessler	10,579,065 B2	3/2020	Wang
10,469,282 B1	11/2019	Konrardy	10,579,070 B1	3/2020	Konrardy
10,469,753 B2	11/2019	Yang	10,584,971 B1	3/2020	Askeland
10,471,976 B2	11/2019	Mian	10,586,458 B2	3/2020	Bavar
10,473,780 B1	11/2019	Brown	10,588,033 B2	3/2020	Behera
10,474,149 B2	11/2019	Palanisamy	10,591,608 B2	3/2020	Ibrahim
10,474,157 B2	11/2019	Yu	10,591,910 B2	3/2020	Levinson
10,474,159 B2	11/2019	Ferguson	10,591,912 B2	3/2020	Pedersen
10,474,160 B2	11/2019	Huang	10,593,042 B1	3/2020	Douillard
10,474,161 B2	11/2019	Huang	10,595,175 B2	3/2020	Ramalho de Oliveira
10,474,164 B2	11/2019	Wheeler	10,596,339 B2	3/2020	Musuku
10,474,916 B2	11/2019	Krishnan	10,598,489 B2	3/2020	Zhang
10,477,449 B2	11/2019	Matos	10,599,141 B2	3/2020	Liu
10,489,529 B2	11/2019	Cahoon	10,599,546 B1	3/2020	Walther
10,489,686 B2	11/2019	Vallespi-Gonzalez	10,606,270 B2	3/2020	Englard
10,490,068 B2	11/2019	Nascimento	10,606,274 B2	3/2020	Yalla
10,493,622 B2	12/2019	Sweeney	10,606,278 B2	3/2020	Shalev-Shwartz
10,493,936 B1	12/2019	Konrardy	10,606,786 B2	3/2020	Fox
10,496,098 B2	12/2019	Zhu	10,607,293 B2	3/2020	Gordon
10,496,099 B2	12/2019	Wilkinson	10,611,384 B1	4/2020	VandenBerg, III
10,496,766 B2	12/2019	Levinson	10,611,389 B2	4/2020	Khosla
10,498,600 B2	12/2019	Ramos de Azevedo	10,613,489 B2	4/2020	Luo
10,501,014 B2	12/2019	Castro	10,613,547 B2	4/2020	Riess
10,503,165 B2	12/2019	Hummelshøj	10,613,550 B2	4/2020	Khosla
10,503,172 B2	12/2019	Englard	10,618,519 B2	4/2020	Marden
10,504,306 B1	12/2019	Konrardy	10,621,860 B2	4/2020	Coelho de Azevedo
10,506,509 B2	12/2019	Condeixa	10,627,810 B2	4/2020	Liu
10,507,787 B2	12/2019	Ferguson	10,627,830 B2	4/2020	Stein
10,508,986 B1	12/2019	Zhu	10,629,080 B2	4/2020	Kazemi
10,509,947 B1	12/2019	Douillard	10,635,108 B2	4/2020	Liu
10,513,161 B2	12/2019	Anderson	10,635,109 B2	4/2020	Guo
10,514,690 B1	12/2019	Siegel	10,636,297 B2	4/2020	Wang
10,514,692 B2	12/2019	Liu	10,642,275 B2	5/2020	Silva
10,514,700 B2	12/2019	Cantrell	10,645,848 B1	5/2020	Lu
10,514,709 B2	12/2019	Shattil	10,647,250 B1	5/2020	Diehl
10,518,770 B2	12/2019	Kroop	10,647,333 B1	5/2020	Donnelly
10,520,319 B2	12/2019	Zhu	10,649,453 B1	5/2020	Svegliato
10,527,417 B2	1/2020	Chen	10,649,458 B2	5/2020	Sun
10,527,450 B2	1/2020	McNew	10,649,462 B2	5/2020	Shalev-Shwartz
10,527,720 B2	1/2020	Apker	10,649,469 B2	5/2020	Salas-Moreno
10,527,734 B2	1/2020	Adachi	10,654,476 B2	5/2020	Wray
10,528,048 B2	1/2020	Cavender-Bares	10,656,657 B2	5/2020	Djuric
10,528,059 B2	1/2020	Donnelly	10,659,975 B2	5/2020	Carreira
			10,664,918 B1	5/2020	Slusar
			10,668,925 B2	6/2020	Zhu
			10,670,411 B2	6/2020	Starns
			10,670,416 B2	6/2020	Wheeler

(56)

References Cited

U.S. PATENT DOCUMENTS

10,671,075 B1	6/2020	Kobilarov	10,775,790 B2	9/2020	Luo
10,671,076 B1	6/2020	Kobilarov	10,775,792 B2	9/2020	Cooper
10,671,077 B2	6/2020	Ros Sanchez	10,775,801 B2	9/2020	Zhang
10,671,082 B2	6/2020	Huang	10,780,880 B2	9/2020	Wood
10,671,961 B2	6/2020	Cao	10,782,687 B2	9/2020	Kawamoto
10,674,332 B2	6/2020	Mineiro Ramos de Azevedo	10,782,693 B2	9/2020	Zhang
10,678,234 B2	6/2020	Sun	10,782,694 B2	9/2020	Zhang
10,678,253 B2	6/2020	Zeng	10,782,699 B2	9/2020	Tao
10,679,497 B1	6/2020	Konrardy	10,782,703 B2	9/2020	Shalev-Shwartz
10,683,012 B2	6/2020	Zhu	10,788,839 B2	9/2020	Zhang
10,685,244 B2	6/2020	Ge	10,788,841 B2	9/2020	Zhang
10,685,403 B1	6/2020	Konrardy	10,795,360 B2	10/2020	Nakhaei Sarvedani
10,691,126 B1	6/2020	Konrardy	10,795,367 B2	10/2020	Milstein
10,691,127 B2	6/2020	Kobilarov	10,795,375 B2	10/2020	Shalev-Shwartz
10,691,130 B2	6/2020	Phillips	10,796,174 B2	10/2020	Zhang
10,691,138 B2	6/2020	Antunes Marques Esteves	10,796,204 B2	10/2020	Rohani
10,692,371 B1	6/2020	Nix	10,796,402 B2	10/2020	Yan
10,698,407 B2	6/2020	Ostafew	10,796,562 B1	10/2020	Wild
10,698,409 B1	6/2020	Siegel	10,800,606 B2	10/2020	Lert, Jr.
10,698,414 B2	6/2020	Stein	10,801,845 B2	10/2020	Wheeler
10,699,579 B2	6/2020	Hashimoto	10,802,477 B1	10/2020	Konrardy
10,705,220 B2	7/2020	Kim	10,803,325 B2	10/2020	Bai
10,705,525 B2	7/2020	Smolyanskiy	10,807,599 B2	10/2020	Zhu
10,705,534 B2	7/2020	Kim	10,809,081 B1	10/2020	Kentley-Klay
10,705,536 B2	7/2020	Miao	10,809,722 B2	10/2020	Glebov
10,705,539 B2	7/2020	Pedersen	10,809,726 B2	10/2020	Kong
10,705,814 B2	7/2020	Schulte	10,809,736 B2	10/2020	Xu
10,706,480 B1	7/2020	Orphys	10,810,872 B2	10/2020	Tao
10,708,823 B2	7/2020	Condeixa	10,812,996 B2	10/2020	Tavares Coutinho
10,710,592 B2	7/2020	Lin	10,813,074 B2	10/2020	Costa
10,710,633 B2	7/2020	Carlson	10,814,882 B2	10/2020	Zhu
10,712,745 B2	7/2020	Zych	10,816,346 B2	10/2020	Wheeler
10,712,746 B2	7/2020	Li	10,816,984 B2	10/2020	Zhang
10,712,750 B2	7/2020	Kentley-Klay	10,816,995 B2	10/2020	Zhang
10,719,886 B1	7/2020	Konrardy	10,818,035 B1	10/2020	Guo
10,720,059 B2	7/2020	Bartel	10,818,105 B1	10/2020	Konrardy
10,725,469 B2	7/2020	Harnett	10,818,187 B2	10/2020	Perko
10,726,379 B1	7/2020	Donnelly	10,821,971 B1	11/2020	Fields
10,726,498 B1	7/2020	Konrardy	10,823,575 B2	11/2020	Zhang
10,726,499 B1	7/2020	Konrardy	10,824,144 B1	11/2020	Fields
10,730,365 B2	8/2020	Rice	10,824,145 B1	11/2020	Konrardy
10,730,531 B1	8/2020	Phillips	10,824,153 B2	11/2020	Zhang
10,732,639 B2	8/2020	Palanisamy	10,824,170 B2	11/2020	Paduano
10,732,645 B2	8/2020	Switkes	10,824,415 B1	11/2020	Fields
10,733,673 B1	8/2020	Slusar	10,828,999 B1	11/2020	Konrardy
10,733,761 B2	8/2020	Kroeger	10,829,063 B1	11/2020	Konrardy
10,735,518 B2	8/2020	Magalhães De Matos	10,829,149 B1	11/2020	Garimella
10,739,768 B2	8/2020	Liao-Mcpherson	10,831,188 B2	11/2020	Hammond
10,739,774 B2	8/2020	Parashar	10,831,191 B1	11/2020	Fields
10,739,775 B2	8/2020	Sun	10,831,196 B2	11/2020	Lombrozo
10,739,776 B2	8/2020	Mukadam	10,831,202 B1	11/2020	Askeland
10,739,780 B1	8/2020	Silver	10,831,204 B1	11/2020	Fields
10,740,850 B1	8/2020	Slusar	10,831,210 B1	11/2020	Kobilarov
10,740,988 B2	8/2020	Liu	10,831,212 B2	11/2020	Coq
10,743,159 B2	8/2020	Ameixieira	10,832,066 B2	11/2020	Cohen
10,745,003 B2	8/2020	Kentley-Klay	10,832,141 B2	11/2020	Boni
10,745,011 B2	8/2020	Zhao	10,832,502 B2	11/2020	Levinson
10,747,234 B1	8/2020	Konrardy	10,836,395 B2	11/2020	Liu
10,747,597 B2	8/2020	Shen	10,836,405 B2	11/2020	Wray
10,748,218 B2	8/2020	Konrardy	10,837,788 B1	11/2020	Kentley-Klay
10,753,754 B2	8/2020	DeLizio	10,838,426 B2	11/2020	Fridman
10,753,758 B2	8/2020	Ferencz	10,839,234 B2	11/2020	Wang
10,754,341 B2	8/2020	Li	10,839,340 B2	11/2020	Skaaksrud
10,754,348 B2	8/2020	McClendon	10,839,426 B2	11/2020	e Costa
10,755,581 B2	8/2020	de Moura	10,839,473 B2	11/2020	Pedersen
10,756,909 B2	8/2020	Condeixa	10,841,496 B2	11/2020	Wheeler
10,761,542 B1	9/2020	Fairfield	10,843,722 B2	11/2020	Letwin
10,762,396 B2	9/2020	Vallespi-Gonzalez	10,845,816 B2	11/2020	Shalev-Shwartz
10,768,620 B1	9/2020	Tran	10,845,820 B2	11/2020	Wheeler
10,768,621 B1	9/2020	Nix	10,852,721 B1	12/2020	Smith
10,768,626 B2	9/2020	Sun	10,855,922 B2	12/2020	Park
10,769,947 B2	9/2020	de Moura	10,857,896 B2	12/2020	Bridges
10,773,597 B2	9/2020	Zhao	10,857,994 B2	12/2020	Iagnemma
10,775,184 B2	9/2020	Ho	10,859,395 B2	12/2020	Wheeler
10,775,488 B2	9/2020	Bradley	10,860,022 B2	12/2020	Korchev
			10,860,036 B2	12/2020	Szubocsev
			10,864,920 B1	12/2020	Donnelly
			10,866,108 B2	12/2020	Pedersen
			10,867,188 B2	12/2020	Huang

(56)

References Cited

U.S. PATENT DOCUMENTS

10,870,368	B2	12/2020	Ing	2012/0316725	A1	12/2012	Trepagnier
10,870,437	B2	12/2020	Battles	2013/0274986	A1	10/2013	Trepagnier
10,872,476	B2	12/2020	Battles	2013/0321627	A1	12/2013	Turn, Jr.
10,882,535	B2	1/2021	Lan	2014/0032017	A1	1/2014	Anderson
10,883,843	B2	1/2021	Outwater	2014/0067188	A1	3/2014	Mian
10,884,422	B2	1/2021	Zhang	2014/0136414	A1	5/2014	Abhyanker
10,885,727	B2	1/2021	Manoria	2014/0195095	A1	7/2014	Flohr
10,886,023	B2	1/2021	Matos	2014/0201126	A1	7/2014	Zadeh
10,887,431	B2	1/2021	Khasis	2014/0214259	A1	7/2014	Trepagnier
10,890,912	B2	1/2021	Cavender-Bares	2014/0214474	A1	7/2014	Balduccini
10,891,138	B2	1/2021	Valasek	2014/0214487	A1	7/2014	Balduccini
10,891,694	B1	1/2021	Leise	2014/0214580	A1	7/2014	Balduccini
10,897,575	B2	1/2021	Wheeler	2014/0214581	A1	7/2014	Balduccini
10,906,558	B1	2/2021	Hwang	2014/0214582	A1	7/2014	Gobeyn
10,908,613	B2	2/2021	Zhang	2014/0253722	A1	9/2014	Smyth
10,909,377	B2	2/2021	Chen	2014/0278682	A1	9/2014	Kennell
10,915,106	B2	2/2021	Zych	2014/0278683	A1	9/2014	Kennell
10,915,116	B2	2/2021	Teng	2015/0081156	A1	3/2015	Trepagnier
10,915,965	B1	2/2021	Fields	2015/0092178	A1	4/2015	Debrunner
10,916,077	B2	2/2021	Zhang	2015/0153175	A1	6/2015	Skaaksrud
10,916,142	B2	2/2021	Fairfield	2015/0154557	A1	6/2015	Skaaksrud
10,921,135	B2	2/2021	Jiang	2015/0177736	A1	6/2015	Anderson
10,921,811	B2	2/2021	Levinson	2015/0229906	A1	8/2015	Inacio De Matos
10,921,812	B2	2/2021	Wilson	2015/0253768	A1	9/2015	Meng
10,921,825	B2	2/2021	Koch	2015/0298786	A1	10/2015	Stigler
10,922,556	B2	2/2021	Dreyfuss	2015/0339355	A1	11/2015	Haanpaa
10,928,207	B2	2/2021	Zhang	2015/0350914	A1	12/2015	Baxley
10,928,523	B2	2/2021	Adachi	2016/0011318	A1	1/2016	Cohen
10,928,820	B1	2/2021	Tao	2016/0021178	A1	1/2016	Liu
10,928,829	B2	2/2021	Tatourian	2016/0036558	A1	2/2016	Ibrahim
10,932,156	B2	2/2021	Amorim de Faria Cardote	2016/0231746	A1	8/2016	Hazelton
10,977,111	B2	4/2021	Rungta	2016/0236617	A1	8/2016	Smyth
10,997,467	B1	5/2021	Alsallakh	2016/0273922	A1	9/2016	Stefan
11,030,476	B2	6/2021	Xu	2016/0280238	A1	9/2016	Zamorano Morfin
11,036,774	B2	6/2021	Zhao	2016/0313739	A1	10/2016	Mian
11,055,200	B2	7/2021	Prabhu Kholkar	2016/0320773	A1	11/2016	Skaaksrud
11,074,103	B2	7/2021	Okuno	2016/0334229	A1	11/2016	Ross
11,150,655	B2	10/2021	Zhou	2016/0334230	A1	11/2016	Ross
11,150,658	B2	10/2021	Ouyang	2016/0334797	A1	11/2016	Ross
11,165,783	B1	11/2021	Eiers	2016/0339587	A1	11/2016	Rublee
11,170,300	B2	11/2021	Dalli	2016/0375976	A1	12/2016	Stigler
2001/0021888	A1	9/2001	Burns	2017/0003681	A1	1/2017	Ross
2002/0143461	A1	10/2002	Burns	2017/0015405	A1	1/2017	Chau
2004/0035315	A1	2/2004	Richards	2017/0017236	A1	1/2017	Song
2008/0027591	A1	1/2008	Lenner	2017/0060129	A1	3/2017	Ross
2008/0027599	A1	1/2008	Logan	2017/0083957	A1	3/2017	Ross
2008/0059015	A1	3/2008	Whittaker	2017/0090480	A1	3/2017	Ho
2008/0093498	A1	4/2008	Leal	2017/0120814	A1	5/2017	Kentley
2008/0161986	A1	7/2008	Breed	2017/0120902	A1	5/2017	Kentley
2008/0161987	A1	7/2008	Breed	2017/0123419	A1	5/2017	Levinson
2009/0182786	A1	7/2009	Haanpaa	2017/0123421	A1	5/2017	Kentley
2009/0306881	A1	12/2009	Dolgov	2017/0123422	A1	5/2017	Kentley
2010/0030473	A1	2/2010	Au	2017/0123428	A1	5/2017	Levinson
2010/0076631	A1	3/2010	Mian	2017/0123429	A1	5/2017	Levinson
2010/0106344	A1	4/2010	Edwards	2017/0124476	A1	5/2017	Levinson
2010/0106356	A1	4/2010	Trepagnier	2017/0124781	A1	5/2017	Douillard
2010/0114416	A1	5/2010	Au	2017/0126810	A1	5/2017	Kentley
2010/0225954	A1	9/2010	Balduccini	2017/0132334	A1	5/2017	Levinson
2011/0153136	A1	6/2011	Anderson	2017/0132934	A1	5/2017	Kentley
2011/0153338	A1	6/2011	Anderson	2017/0136842	A1	5/2017	Anderson
2011/0288714	A1	11/2011	Flohr	2017/0139411	A1	5/2017	Hartung
2011/0295423	A1	12/2011	Anderson	2017/0160742	A1	6/2017	Ross
2011/0295424	A1	12/2011	Johnson	2017/0164423	A1	6/2017	Ross
2012/0044043	A1	2/2012	Nettleton	2017/0166215	A1	6/2017	Rander
2012/0046818	A1	2/2012	Nettleton	2017/0227965	A1	8/2017	DeCenzo
2012/0046927	A1	2/2012	Nettleton	2017/0235316	A1	8/2017	Shattil
2012/0046983	A1	2/2012	Nettleton	2017/0248963	A1	8/2017	Levinson
2012/0050787	A1	3/2012	Balduccini	2017/0248964	A1	8/2017	Kentley
2012/0053703	A1	3/2012	Nettleton	2017/0277186	A1	9/2017	Ross
2012/0053775	A1	3/2012	Nettleton	2017/0284819	A1	10/2017	Donnelly
2012/0083947	A1	4/2012	Anderson	2017/0285642	A1	10/2017	Rander
2012/0095651	A1	4/2012	Anderson	2017/0294130	A1	10/2017	Donnelly
2012/0101680	A1	4/2012	Trepagnier	2017/0315229	A1	11/2017	Pavek
2012/0166019	A1	6/2012	Anderson	2017/0316333	A1	11/2017	Levinson
2012/0283906	A1	11/2012	Anderson	2017/0323179	A1	11/2017	Vallespi-Gonzalez
				2017/0329346	A1	11/2017	Latotzki
				2017/0341236	A1	11/2017	Patrick
				2017/0351261	A1	12/2017	Levinson
				2017/0353943	A1	12/2017	Skaaksrud

(56)	References Cited			2018/0196433	A1	7/2018	Rander
	U.S. PATENT DOCUMENTS			2018/0196439	A1	7/2018	Levinson
				2018/0196440	A1	7/2018	Zhu
				2018/0201182	A1	7/2018	Zhu
2017/0371355	A1	12/2017	Paduano	2018/0203443	A1	7/2018	Newman
2018/0005123	A1	1/2018	Lagos	2018/0203450	A1	7/2018	Zhu
2018/0009445	A1	1/2018	Nishi	2018/0204111	A1	7/2018	Zadeh
2018/0011494	A1	1/2018	Zhu	2018/0204122	A1	7/2018	Boni
2018/0017968	A1	1/2018	Zhu	2018/0204141	A1	7/2018	Nettleton
2018/0023960	A1	1/2018	Fridman	2018/0208215	A1	7/2018	Zamorano Morfin
2018/0024553	A1	1/2018	Kong	2018/0211534	A1	7/2018	de Moura
2018/0024562	A1	1/2018	Bellaiche	2018/0216942	A1	8/2018	Wang
2018/0024565	A1	1/2018	Fridman	2018/0217614	A1	8/2018	Salas-Moreno
2018/0024568	A1	1/2018	Fridman	2018/0224869	A1	8/2018	Paduano
2018/0032082	A1	2/2018	Shalev-Shwartz	2018/0225968	A1	8/2018	Wang
2018/0033310	A1	2/2018	Kentley-Klay	2018/0233047	A1	8/2018	Mandeville-Clarke
2018/0039287	A1	2/2018	Shattil	2018/0238698	A1	8/2018	Pedersen
2018/0045832	A1	2/2018	Ibrahim	2018/0247160	A1	8/2018	Rohani
2018/0047292	A1	2/2018	Hashimoto	2018/0253647	A1	9/2018	Yu
2018/0050704	A1	2/2018	Tascione	2018/0257660	A1	9/2018	Ibrahim
2018/0059672	A1	3/2018	Li	2018/0259956	A1	9/2018	Kawamoto
2018/0061242	A1	3/2018	Bavar	2018/0259958	A1	9/2018	Kalanick
2018/0086344	A1	3/2018	Zhu	2018/0267537	A1	9/2018	Kroop
2018/0086351	A1	3/2018	Zhu	2018/0275678	A1	9/2018	Andert
2018/0088576	A1	3/2018	Kong	2018/0282955	A1	10/2018	McClendon
2018/0088582	A1	3/2018	Kong	2018/0284774	A1	10/2018	Kawamoto
2018/0088590	A1	3/2018	Zhu	2018/0288774	A1	10/2018	Karjee
2018/0093671	A1	4/2018	Allan	2018/0292222	A1	10/2018	Lin
2018/0095467	A1	4/2018	Perrone	2018/0292825	A1	10/2018	Smolyanskiy
2018/0107942	A1	4/2018	Jiang	2018/0292831	A1	10/2018	Kong
2018/0111612	A1	4/2018	Jiang	2018/0297606	A1	10/2018	Luo
2018/0114258	A1	4/2018	Ross	2018/0300964	A1	10/2018	Lakshamanan
2018/0114259	A1	4/2018	Ross	2018/0304889	A1	10/2018	Shalev-Shwartz
2018/0127000	A1	5/2018	Jiang	2018/0304900	A1	10/2018	Luo
2018/0127001	A1	5/2018	Ricci	2018/0307229	A1	10/2018	Stein
2018/0129215	A1	5/2018	Hazelton	2018/0307239	A1	10/2018	Shalev-Shwartz
2018/0136643	A1	5/2018	Tao	2018/0307240	A1	10/2018	Shalev-Shwartz
2018/0136644	A1	5/2018	Levinson	2018/0307245	A1	10/2018	Khawaja
2018/0136651	A1	5/2018	Levinson	2018/0312238	A1	11/2018	Stigler
2018/0141564	A1	5/2018	Ross	2018/0314266	A1	11/2018	Shalev-Shwartz
2018/0143622	A1	5/2018	Zhu	2018/0321685	A1	11/2018	Yalla
2018/0143632	A1	5/2018	Zhu	2018/0322546	A1	11/2018	Ross
2018/0143639	A1	5/2018	Singhal	2018/0327091	A1	11/2018	Burks
2018/0143644	A1	5/2018	Li	2018/0329411	A1	11/2018	Levinson
2018/0143647	A1	5/2018	Wang	2018/0330173	A1	11/2018	Zhu
2018/0143649	A1	5/2018	Miao	2018/0334166	A1	11/2018	Zhu
2018/0150086	A1	5/2018	Nobukawa	2018/0335781	A1	11/2018	Chase
2018/0154829	A1	6/2018	Kentley-Klay	2018/0336421	A1	11/2018	Huang
2018/0162186	A1	6/2018	Anderson	2018/0341274	A1	11/2018	Donnelly
2018/0162412	A1	6/2018	Gao	2018/0342157	A1	11/2018	Donnelly
2018/0164822	A1	6/2018	Chu	2018/0348775	A1	12/2018	Yu
2018/0164827	A1	6/2018	Chu	2018/0349713	A1	12/2018	Jiang
2018/0170392	A1	6/2018	Yang	2018/0349802	A1	12/2018	Jiang
2018/0170395	A1	6/2018	Luo	2018/0356821	A1	12/2018	Kentley-Klay
2018/0172821	A1	6/2018	Apker	2018/0356823	A1	12/2018	Cooper
2018/0173240	A1	6/2018	Fang	2018/0364657	A1	12/2018	Luo
2018/0178791	A1	6/2018	Zhu	2018/0364700	A1	12/2018	Liu
2018/0183873	A1	6/2018	Wang	2018/0364701	A1	12/2018	Liu
2018/0186378	A1	7/2018	Zhuang	2018/0364702	A1	12/2018	Liu
2018/0186403	A1	7/2018	Zhu	2018/0364703	A1	12/2018	Liu
2018/0188026	A1	7/2018	Zhang	2018/0364704	A1	12/2018	Liu
2018/0188027	A1	7/2018	Zhang	2018/0365908	A1	12/2018	Liu
2018/0188037	A1	7/2018	Wheeler	2018/0370540	A1	12/2018	Yousuf
2018/0188039	A1	7/2018	Chen	2018/0373245	A1	12/2018	Nishi
2018/0188040	A1	7/2018	Chen	2018/0373268	A1	12/2018	Antunes Marques Esteves
2018/0188041	A1	7/2018	Chen	2018/0374359	A1	12/2018	Li
2018/0188042	A1	7/2018	Chen	2018/0375939	A1	12/2018	Magalhães De Matos
2018/0188043	A1	7/2018	Chen	2018/0376357	A1	12/2018	Tavares Coutinho
2018/0188044	A1	7/2018	Wheeler	2019/0004510	A1	1/2019	Xiao
2018/0188059	A1	7/2018	Wheeler	2019/0004516	A1	1/2019	Liu
2018/0188060	A1	7/2018	Wheeler	2019/0004518	A1	1/2019	Zhou
2018/0188727	A1	7/2018	Zhuang	2019/0004522	A1	1/2019	Zych
2018/0188734	A1	7/2018	Zhu	2019/0004524	A1	1/2019	Wang
2018/0188742	A1	7/2018	Wheeler	2019/0004533	A1	1/2019	Huang
2018/0188743	A1	7/2018	Wheeler	2019/0004534	A1	1/2019	Huang
2018/0189323	A1	7/2018	Wheeler	2019/0004535	A1	1/2019	Huang
2018/0189578	A1	7/2018	Yang	2019/0018411	A1	1/2019	Herbach
2018/0189717	A1	7/2018	Cao	2019/0018412	A1	1/2019	Tschanz
2018/0190046	A1	7/2018	Levinson	2019/0025843	A1	1/2019	Wilkinson

(56)

References Cited

U.S. PATENT DOCUMENTS

2019/0028370	A1	1/2019	Church	2019/0220016	A1	7/2019	Phillips
2019/0035275	A1	1/2019	Nishi	2019/0227550	A1	7/2019	Yershov
2019/0039609	A1	2/2019	Wood	2019/0227553	A1	7/2019	Kentley-Klay
2019/0049342	A1	2/2019	Anderson	2019/0235488	A1	8/2019	Beth
2019/0049946	A1	2/2019	Ross	2019/0235499	A1	8/2019	Kazemi
2019/0050729	A1	2/2019	Lakshmanan	2019/0235532	A1	8/2019	Paduano
2019/0053074	A1	2/2019	Behera	2019/0243370	A1	8/2019	Li
2019/0056737	A1	2/2019	Palanisamy	2019/0248487	A1	8/2019	Holtz
2019/0056742	A1	2/2019	Ho	2019/0250000	A1	8/2019	Zhang
2019/0061765	A1	2/2019	Marden	2019/0250609	A1	8/2019	Luo
2019/0066409	A1	2/2019	Moreira da Mota	2019/0250636	A1	8/2019	Szubocsev
2019/0066506	A1	2/2019	Kazemi	2019/0250640	A1	8/2019	O'Flaherty et al.
2019/0068434	A1	2/2019	Moreira da Mota	2019/0258246	A1	8/2019	Liu
2019/0071091	A1	3/2019	Zhu	2019/0258251	A1	8/2019	Ditty
2019/0071092	A1	3/2019	Ma	2019/0265703	A1	8/2019	Hicok
2019/0071093	A1	3/2019	Ma	2019/0266179	A1	8/2019	Wheeler
2019/0072965	A1	3/2019	Zhang	2019/0266420	A1	8/2019	Ge
2019/0072966	A1	3/2019	Zhang	2019/0270408	A1	9/2019	Castro
2019/0072973	A1	3/2019	Sun	2019/0271549	A1	9/2019	Zhang
2019/0072979	A1	3/2019	Sukhomlinov	2019/0277632	A1	9/2019	Zhang
2019/0073426	A1	3/2019	Balduccini	2019/0278277	A1	9/2019	Tao
2019/0078896	A1	3/2019	Zhu	2019/0278284	A1	9/2019	Zhang
2019/0079524	A1	3/2019	Zhu	2019/0278290	A1	9/2019	Zhang
2019/0080602	A1	3/2019	Rice	2019/0286143	A1	9/2019	Ross
2019/0084571	A1	3/2019	Zhu	2019/0286155	A1	9/2019	Stein
2019/0086924	A1	3/2019	Greenfield	2019/0291728	A1	9/2019	Shalev-Shwartz
2019/0094868	A1	3/2019	Zych	2019/0295421	A1	9/2019	Bavar
2019/0105968	A1	4/2019	Rice	2019/0302768	A1	10/2019	Zhang
2019/0107840	A1	4/2019	Green	2019/0310627	A1	10/2019	Halder
2019/0113351	A1	4/2019	Antony	2019/0310636	A1	10/2019	Halder
2019/0120640	A1	4/2019	Ho	2019/0310650	A1	10/2019	Halder
2019/0120946	A1	4/2019	Wheeler	2019/0310654	A1	10/2019	Halder
2019/0120947	A1	4/2019	Wheeler	2019/0315232	A1	10/2019	Ing
2019/0120948	A1	4/2019	Yang	2019/0315357	A1	10/2019	Zhang
2019/0122037	A1	4/2019	Russell	2019/0317455	A1	10/2019	Leon
2019/0122386	A1	4/2019	Wheeler	2019/0317507	A1	10/2019	Zhang
2019/0129831	A1	5/2019	Goldberg	2019/0317508	A1	10/2019	Zhang
2019/0130878	A1	5/2019	Bradley	2019/0317512	A1	10/2019	Zhang
2019/0134821	A1	5/2019	Patrick	2019/0317513	A1	10/2019	Zhang
2019/0137991	A1	5/2019	Agarwal	2019/0317515	A1	10/2019	Zhang
2019/0138008	A1	5/2019	Ross	2019/0317520	A1	10/2019	Zhang
2019/0146508	A1	5/2019	Dean	2019/0318411	A1	10/2019	Dhungana
2019/0146509	A1 *	5/2019	Dean G05D 1/0214	2019/0318550	A1	10/2019	Lakshamanan
			701/25	2019/0324456	A1	10/2019	Ryan
2019/0147253	A1	5/2019	Bai	2019/0324463	A1	10/2019	Zhu
2019/0147254	A1	5/2019	Bai	2019/0325223	A1	10/2019	Chen
2019/0147255	A1	5/2019	Homayounfar	2019/0325546	A1	10/2019	Hagestad
2019/0156134	A1	5/2019	Krishnan	2019/0329903	A1	10/2019	Thompson
2019/0156150	A1	5/2019	Krishnan	2019/0332123	A1	10/2019	Donnelly
2019/0156679	A1	5/2019	Bartel	2019/0332875	A1	10/2019	Vallespi-Gonzalez
2019/0161080	A1	5/2019	Gochev	2019/0333120	A1	10/2019	Ross
2019/0163191	A1	5/2019	Sorin	2019/0333164	A1	10/2019	Fox
2019/0168769	A1	6/2019	Zhu	2019/0346851	A1	11/2019	Liu
2019/0171912	A1	6/2019	Vallespi-Gonzalez	2019/0349794	A1	11/2019	Tavares Coutinho
2019/0174276	A1	6/2019	Mineiro Ramos de Azevedo	2019/0354911	A1	11/2019	Alaniz
2019/0176684	A1	6/2019	Zych	2019/0359202	A1	11/2019	Zhu
2019/0179311	A1	6/2019	Paden	2019/0361432	A1	11/2019	Levinson
2019/0179979	A1	6/2019	Melick	2019/0361444	A1	11/2019	Herbach
2019/0185018	A1	6/2019	Tao	2019/0367019	A1	12/2019	Yan
2019/0186939	A1	6/2019	Cox	2019/0367020	A1	12/2019	Yan
2019/0187715	A1	6/2019	Zhang	2019/0367021	A1	12/2019	Zhao
2019/0187723	A1	6/2019	Tao	2019/0367022	A1	12/2019	Zhao
2019/0195998	A1	6/2019	Campbell	2019/0368882	A1	12/2019	Wheeler
2019/0196471	A1	6/2019	Vaughn	2019/0369616	A1	12/2019	Ostafew
2019/0202561	A1	7/2019	Weekes	2019/0369626	A1	12/2019	Lui
2019/0204092	A1	7/2019	Wheeler	2019/0371174	A1	12/2019	de Moura
2019/0204425	A1	7/2019	Abari	2019/0377345	A1	12/2019	Bachrach
2019/0204427	A1	7/2019	Abari	2019/0377349	A1	12/2019	Van der Merwe
2019/0204842	A1	7/2019	Jafari Tafti	2019/0377351	A1	12/2019	Phillips
2019/0204843	A1	7/2019	Fang	2019/0378423	A1	12/2019	Bachrach
2019/0212161	A1	7/2019	Pedersen	2019/0382007	A1	12/2019	Casas
2019/0212744	A1	7/2019	Milstein	2019/0382031	A1	12/2019	Hu
2019/0212754	A1	7/2019	Smith	2019/0383945	A1	12/2019	Wang
2019/0220011	A1	7/2019	Della Penna	2019/0384301	A1	12/2019	Greenfield
2019/0220015	A1	7/2019	Phillips	2019/0384304	A1	12/2019	Towal
				2019/0385450	A1	12/2019	Kim
				2019/0387060	A1	12/2019	Kentley-Klay
				2019/0391585	A1	12/2019	Zhang
				2020/0001862	A1	1/2020	Luo

(56)

References Cited

U.S. PATENT DOCUMENTS

2020/0001863	A1	1/2020	Li	2020/0182640	A1	6/2020	Ho
2020/0003564	A1	1/2020	Zhang	2020/0183395	A1	6/2020	Levandowski
2020/0004241	A1	1/2020	Levinson	2020/0191601	A1	6/2020	Jiang
2020/0004261	A1	1/2020	Kim	2020/0192372	A1	6/2020	Levandowski
2020/0013225	A1	1/2020	Park	2020/0192373	A1	6/2020	Levandowski
2020/0014759	A1	1/2020	Wunderlich	2020/0192374	A1	6/2020	Riggs
2020/0019165	A1	1/2020	Levandowski	2020/0192375	A1	6/2020	Riggs
2020/0019175	A1	1/2020	Dean	2020/0192376	A1	6/2020	Levandowski
2020/0019801	A1	1/2020	Krishnan	2020/0192377	A1	6/2020	Levandowski
2020/0021728	A1	1/2020	Yang	2020/0192378	A1	6/2020	Levandowski
2020/0023838	A1	1/2020	Zhang	2020/0192379	A1	6/2020	Levandowski
2020/0026276	A1	1/2020	Zhang	2020/0192380	A1	6/2020	Bernstein
2020/0026283	A1	1/2020	Barnes	2020/0192381	A1	6/2020	Levandowski
2020/0026285	A1	1/2020	Perrone	2020/0192402	A1	6/2020	Wang
2020/0026294	A1	1/2020	Kim	2020/0193606	A1	6/2020	Douillard
2020/0027354	A1	1/2020	Goldman	2020/0201329	A1	6/2020	Levandowski
2020/0031340	A1	1/2020	Tao	2020/0201350	A1	6/2020	Newman
2020/0033147	A1	1/2020	Ahn	2020/0207360	A1	7/2020	Dougherty
2020/0033872	A1	1/2020	Burch, V	2020/0207369	A1	7/2020	Mehta
2020/0041296	A1	2/2020	Ho	2020/0207371	A1	7/2020	Dougherty
2020/0042007	A1	2/2020	Zhang	2020/0207375	A1	7/2020	Mehta
2020/0043326	A1	2/2020	Tao	2020/0209853	A1	7/2020	Leach
2020/0050195	A1	2/2020	Gross	2020/0209857	A1	7/2020	Djuric
2020/0050199	A1	2/2020	Park	2020/0209872	A1	7/2020	Xu
2020/0051346	A1	2/2020	Zhang	2020/0225032	A1	7/2020	Chen
2020/0055362	A1	2/2020	Anderson	2020/0225673	A1	7/2020	Ebrahimi Afrouzi
2020/0064483	A1	2/2020	Li	2020/0231106	A9	7/2020	Sweeney
2020/0064842	A1	2/2020	Kentley-Klay	2020/0231142	A1	7/2020	Liu
2020/0064851	A1	2/2020	Wilkinson	2020/0233415	A1	7/2020	Panzica
2020/0064859	A1	2/2020	Zhang	2020/0233418	A1	7/2020	Liu
2020/0064861	A1	2/2020	Zhang	2020/0233420	A1	7/2020	Liu
2020/0073385	A1	3/2020	Jobanputra	2020/0233429	A1	7/2020	Zhang
2020/0073739	A1	3/2020	Rungta	2020/0240799	A1	7/2020	Gao
2020/0074024	A1	3/2020	Levinson	2020/0240805	A1	7/2020	Kanajan
2020/0082180	A1	3/2020	Wang	2020/0241546	A1	7/2020	Sun
2020/0089243	A1	3/2020	Poeppel	2020/0249677	A1	8/2020	Maat
2020/0089245	A1	3/2020	Yadmellat	2020/0250067	A1	8/2020	Walther
2020/0101974	A1	4/2020	Ha	2020/0250981	A1	8/2020	Kazemi
2020/0108785	A1	4/2020	Sweeney	2020/0262263	A1	8/2020	Doerksen
2020/0110835	A1	4/2020	Zhao	2020/0265249	A1	8/2020	Ge
2020/0111169	A1	4/2020	Halder	2020/0272148	A1	8/2020	Karasev
2020/0116497	A1	4/2020	Jiang	2020/0282907	A1	9/2020	Diehl
2020/0116867	A1	4/2020	Zhu	2020/0282987	A1	9/2020	Zhu
2020/0117207	A1	4/2020	Zhang	2020/0284581	A1	9/2020	Zhang
2020/0117575	A1	4/2020	Prabhu Kholkar	2020/0285240	A1	9/2020	Diehl
2020/0120253	A1	4/2020	Wheeler	2020/0285658	A1	9/2020	Wheeler
2020/0122721	A1	4/2020	Zhang	2020/0290647	A1	9/2020	Anderson
2020/0122830	A1	4/2020	Anderson	2020/0293051	A1	9/2020	Hasegawa
2020/0124719	A1	4/2020	Noujeim	2020/0293052	A1	9/2020	Hasegawa
2020/0125094	A1	4/2020	Zhang	2020/0293053	A1	9/2020	Hasegawa
2020/0125102	A1	4/2020	Jiang	2020/0298863	A1	9/2020	Lin
2020/0130864	A1	4/2020	Brockers	2020/0301435	A1	9/2020	Phillips
2020/0133270	A1	4/2020	Han	2020/0310417	A1	10/2020	Pedersen
2020/0134525	A1	4/2020	Goldman	2020/0310442	A1	10/2020	Halder
2020/0137928	A1	4/2020	Lu	2020/0310444	A1	10/2020	Hasegawa
2020/0139973	A1	5/2020	Palanisamy	2020/0327234	A1	10/2020	Zhou
2020/0142405	A1	5/2020	Havens	2020/0331480	A1	10/2020	Zhang
2020/0142428	A1	5/2020	Donnelly	2020/0333470	A1	10/2020	Oh
2020/0142732	A1	5/2020	Okuno	2020/0333785	A1	10/2020	Cooper
2020/0145569	A1	5/2020	Wheeler	2020/0341469	A1	10/2020	Smolyanskiy
2020/0149231	A1	5/2020	Lo Vaglio	2020/0341487	A1	10/2020	Hazelton
2020/0149906	A1	5/2020	Tu	2020/0341490	A1	10/2020	Silva
2020/0150682	A1	5/2020	Donnelly	2020/0342693	A1	10/2020	Jiang
2020/0159216	A1	5/2020	Le	2020/0346637	A1	11/2020	Zhou
2020/0159225	A1	5/2020	Zeng	2020/0348668	A1	11/2020	Poulet
2020/0160067	A1	5/2020	Huang	2020/0348676	A1	11/2020	Zhou
2020/0172115	A1	6/2020	Zhu	2020/0348684	A1	11/2020	Zhang
2020/0172116	A1	6/2020	Zhu	2020/0349848	A1	11/2020	Bartel
2020/0174472	A1	6/2020	Zhang	2020/0356090	A1	11/2020	Thakur
2020/0174486	A1	6/2020	Luo	2020/0356100	A1	11/2020	Nagarajan
2020/0174765	A1	6/2020	Schulte	2020/0356849	A1	11/2020	Xu
2020/0175691	A1	6/2020	Zhang	2020/0363813	A1	11/2020	He
2020/0175695	A1	6/2020	Zhang	2020/0371533	A1	11/2020	Kentley-Klay
2020/0180740	A1	6/2020	Christ	2020/0379457	A1	12/2020	Ostafew
2020/0182639	A1	6/2020	Ho	2020/0379462	A1	12/2020	Kawamoto
				2020/0379474	A1	12/2020	Zhang
				2020/0383580	A1	12/2020	Shouldice
				2020/0387155	A1	12/2020	Liu
				2020/0388154	A1	12/2020	Kim

(56)

References Cited

U.S. PATENT DOCUMENTS

2020/0393261	A1	12/2020	Zhang	2021/0041882	A1	2/2021	Lacaze	
2020/0393837	A1	12/2020	Zhang	2021/0042575	A1	2/2021	Firner	
2020/0394474	A1	12/2020	Vallespi-Gonzalez	2021/0046861	A1	2/2021	Li	
2020/0401145	A1	12/2020	Milstein	2021/0046946	A1	2/2021	Nemec	
2020/0402323	A1	12/2020	Liu	2021/0048304	A1	2/2021	Pedersen	
2020/0406893	A1	12/2020	Choe	2021/0048991	A1	2/2021	Tanner	
2020/0408921	A1	12/2020	Oh	2021/0049243	A1	2/2021	Venkatadri	
2020/0409351	A1	12/2020	Zhu	2021/0049415	A1	2/2021	Whiteson	
2020/0409377	A1	12/2020	Ready-Campbell	2021/0049903	A1	2/2021	Zhang	
2020/0409386	A1	12/2020	Thakur	2021/0053407	A1	2/2021	Smith	
2020/0410252	A1	12/2020	Tsoi	2021/0065027	A1	3/2021	Yamamoto	
2020/0410255	A1	12/2020	Guo	2021/0086370	A1	3/2021	Zhang	
2020/0410703	A1	12/2020	Guo	2021/0088337	A1	3/2021	Koubaa	
2021/0004012	A1	1/2021	Marchetti-Bowick	2021/0117730	A1	4/2021	Alsallakh	
2021/0009163	A1	1/2021	Urtasun	2021/0133502	A1	5/2021	Dees	
2021/0009166	A1	1/2021	Li	2021/0173831	A1	6/2021	Crabtree	
2021/0018916	A1	1/2021	Thakur	2021/0188316	A1 *	6/2021	Marchetti-Bowick
2021/0018917	A1	1/2021	Levandowski					G06N 3/045
2021/0018918	A1	1/2021	Levandowski	2021/0232915	A1	7/2021	Dalli	
2021/0024100	A1	1/2021	Calleija	2021/0247781	A1	8/2021	Liu	
2021/0024144	A1	1/2021	Patnaik	2021/0271253	A1	9/2021	Liu	
2021/0026348	A1	1/2021	Gogna	2021/0278854	A1	9/2021	Serrano	
2021/0026355	A1	1/2021	Chen	2021/0287556	A1	9/2021	Hong	
2021/0031760	A1	2/2021	Ostafew	2021/0304066	A1	9/2021	Tomioka	
2021/0031801	A1	2/2021	Wood	2021/0311504	A1	10/2021	Chai	
2021/0033410	A1	2/2021	Niemiec	2021/0380105	A1 *	12/2021	Hudecek G05D 1/0088
2021/0034068	A1	2/2021	Shalev-Shwartz	2021/0394788	A1	12/2021	Guo	
2021/0034412	A1	2/2021	Televitckiy	2022/0027737	A1	1/2022	Dalli	
2021/0035442	A1	2/2021	Baig	2022/0055215	A1	2/2022	Hasegawa	
2021/0035450	A1	2/2021	Gao	2022/0057804	A1	2/2022	Hasegawa	
2021/0039669	A1	2/2021	Watson	2022/0058815	A1	2/2022	Xu	
2021/0039682	A1	2/2021	Wu	2022/0146997	A1 *	5/2022	Stepanova G06N 20/00
2021/0039779	A1	2/2021	Salas-Moreno	2023/0316924	A1 *	10/2023	Hruschka G08G 1/166
								701/301
				2024/0067209	A1 *	2/2024	Bárdos B60W 60/0011

* cited by examiner

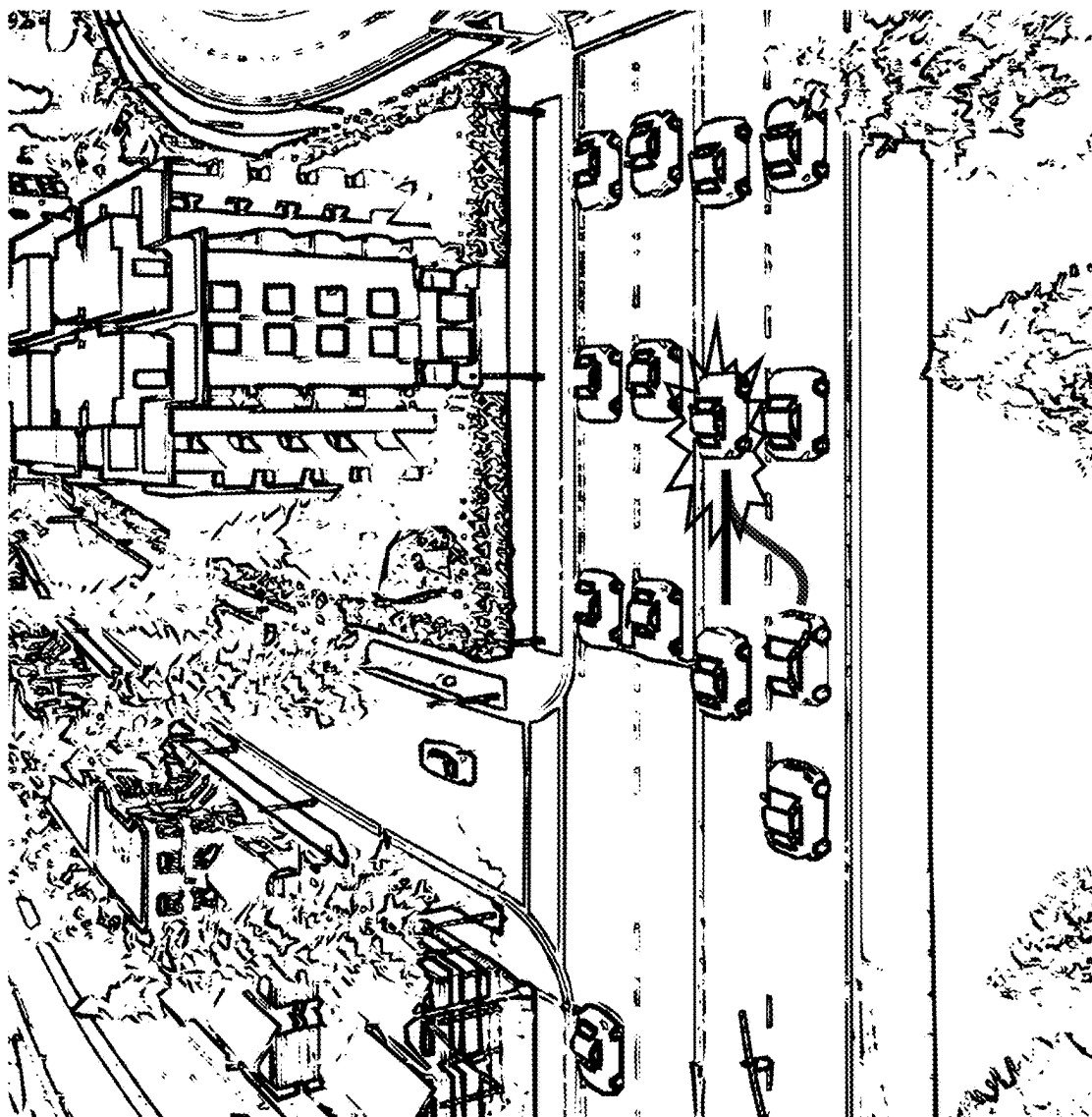
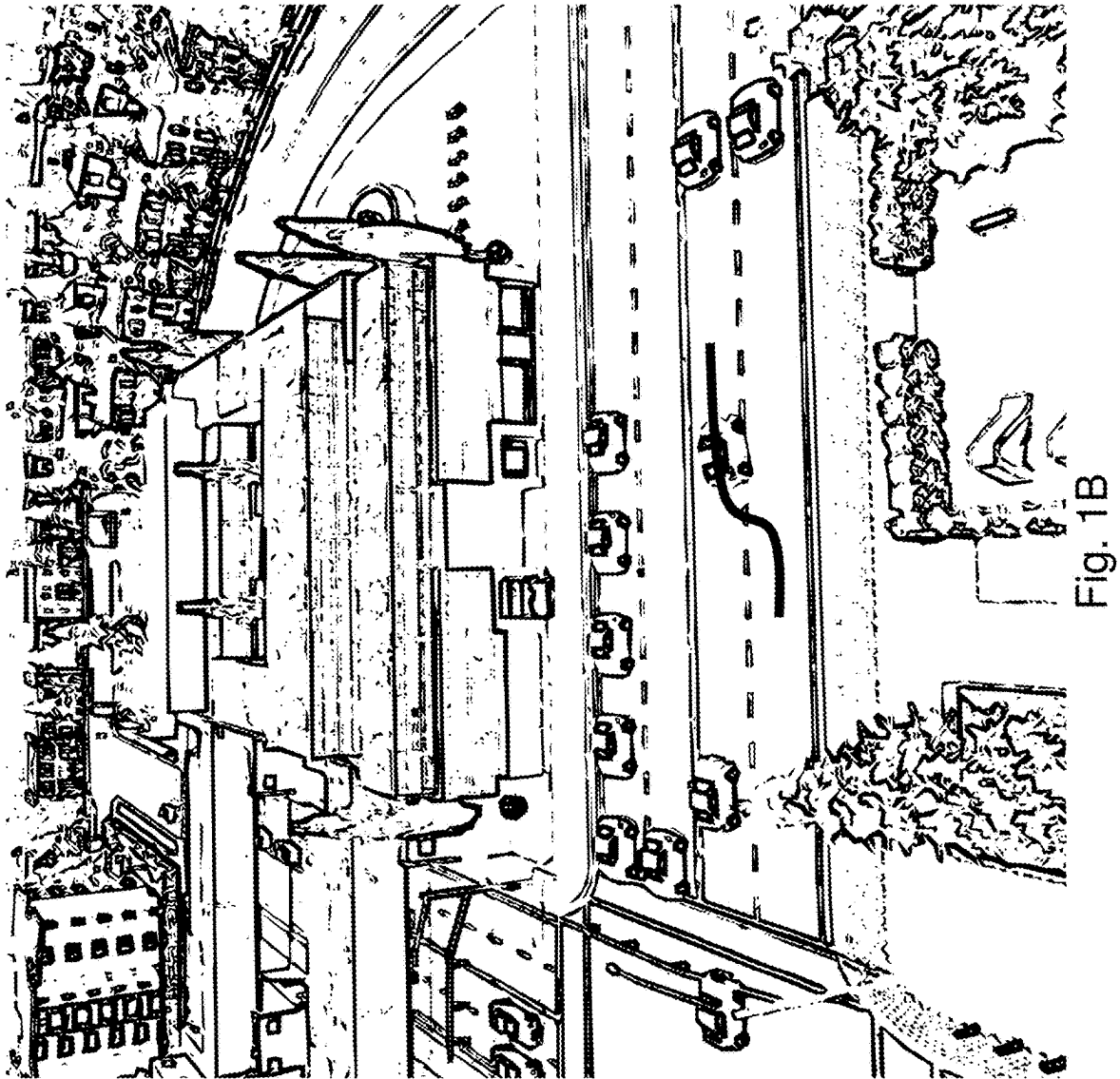


Fig. 1A



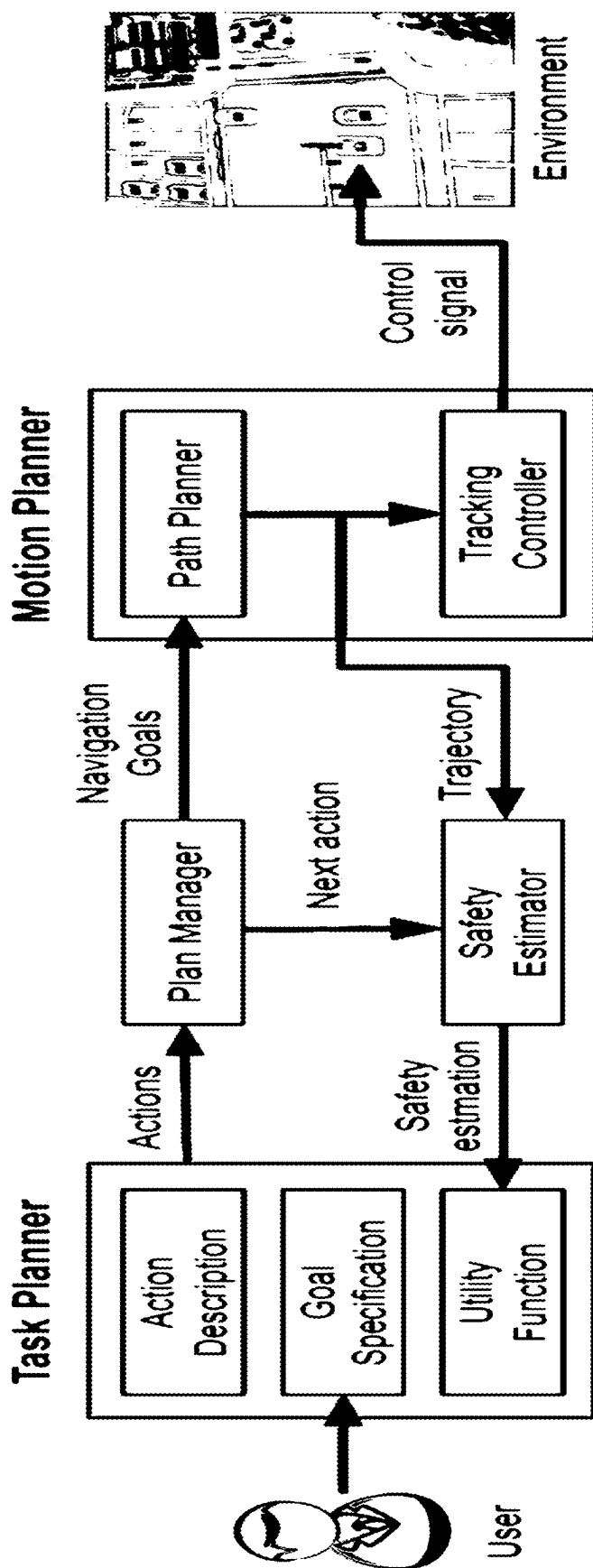


Fig. 2

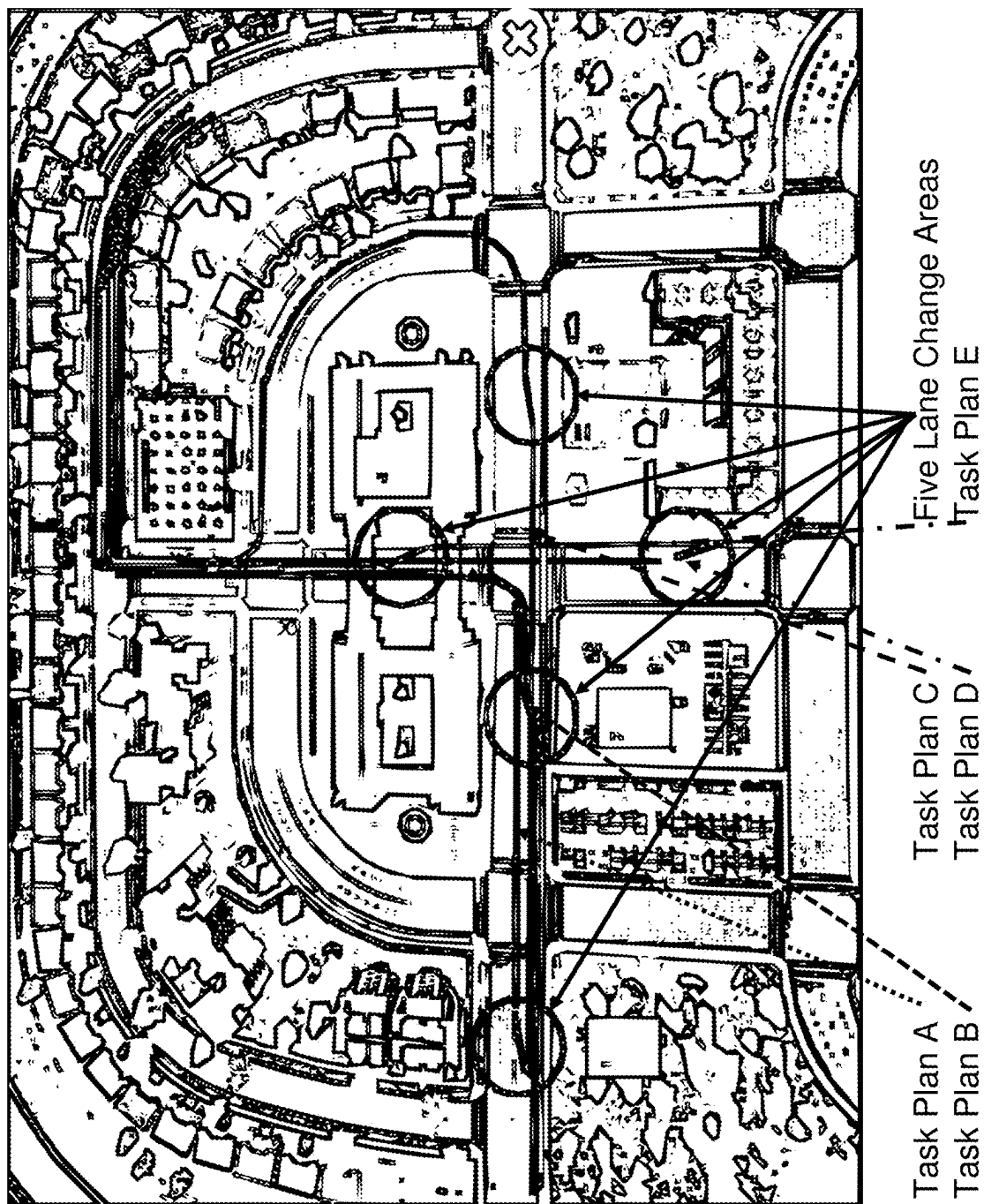


Fig. 3

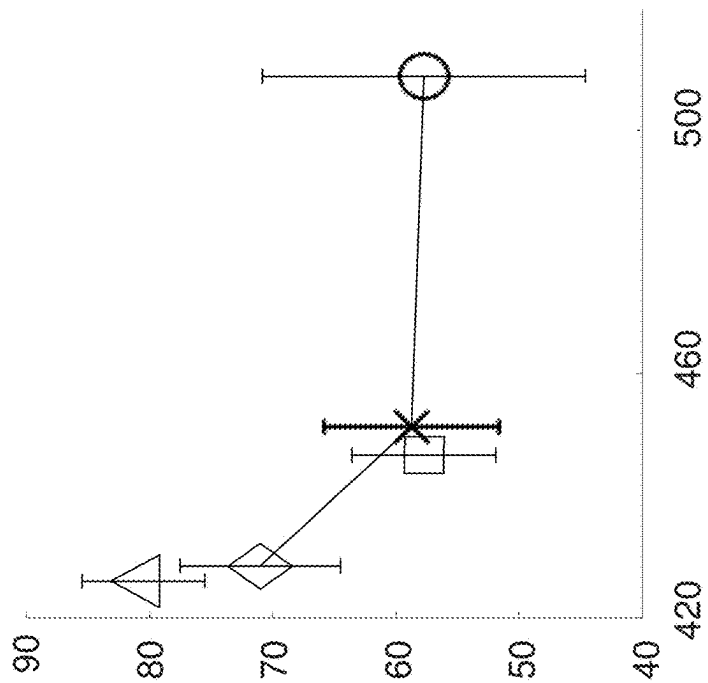


Fig. 4B

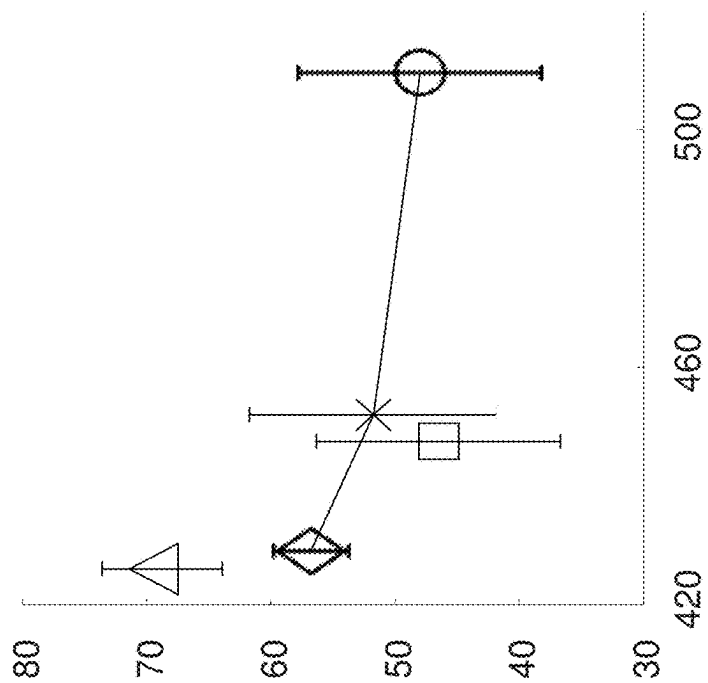
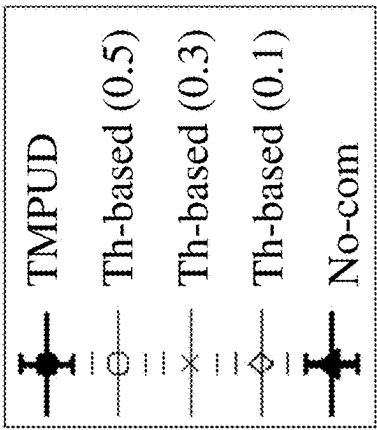


Fig. 4A



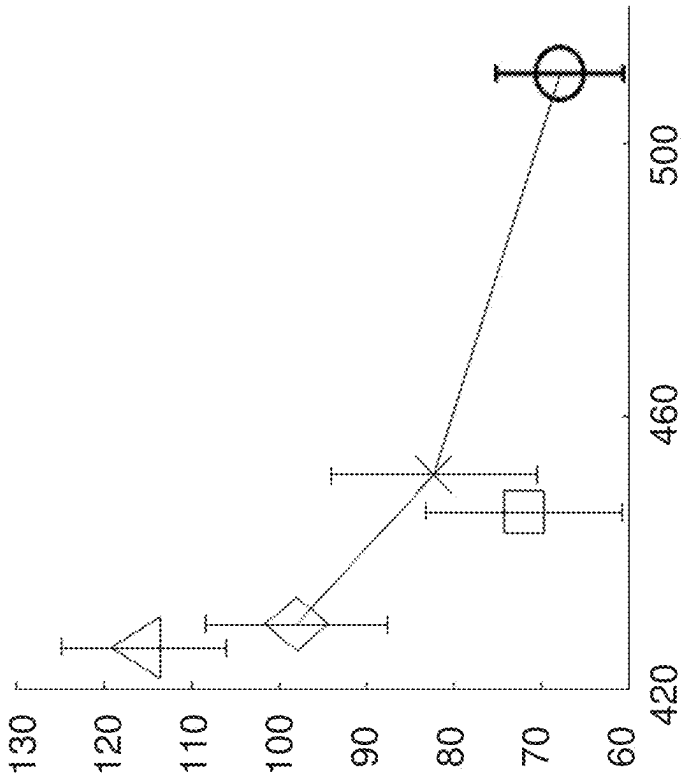


Fig. 4D

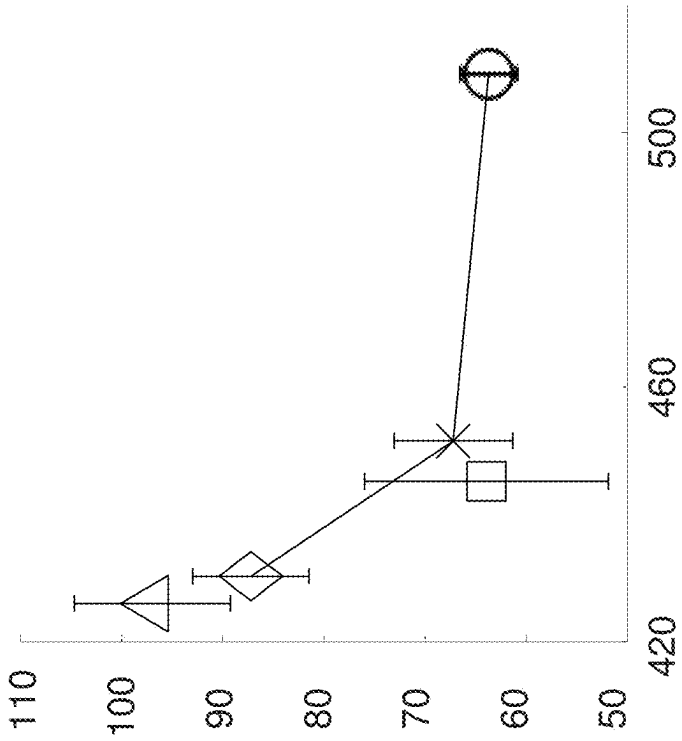


Fig. 4C

1

TASK-MOTION PLANNING FOR SAFE AND EFFICIENT URBAN DRIVING

CROSS REFERENCE TO RELATED APPLICATION

The present application is a non-provisional of, and claims benefit under 35 U.S.C. § 119(e) of, U.S. Provisional Patent Application No. 62/200,431, filed Mar. 5, 2021, the entirety of which is expressly incorporated herein by reference.

FIELD OF THE INVENTION

The present invention relates to the field of autonomous driving systems, and more particularly to a system which enables interaction between task and motion planners.

INCORPORATION BY REFERENCE

Citation or identification of any reference herein, or any section of this application shall not be construed as an admission that such reference is available as prior art. The disclosure of each publication and patent listed or referenced herein are hereby incorporated by reference in their entirety in this application, see 37 C.F.R. § 1.57(c), and shall be treated as if the entirety thereof forms a part of this application. Such references are provided for their disclosure of technologies as may be required to enable practice of the present invention, to provide written description for claim language, to make clear applicant's possession of the invention with respect to the various aggregates, combinations, permutations, and sub-combinations of the respective disclosures or portions thereof (within a particular reference or across multiple references) in conjunction with the combinations, permutations, and sub-combinations of various disclosure provided herein, to demonstrate the non-abstract nature of the technology, and for any other purpose. Except as expressly indicated, the scope of the invention is inclusive, and therefore the disclosure of a technology or teaching within these incorporated materials is intended to encompass that technology or teaching as being an option of, or an addition to, other disclosure of the present invention. Likewise, the combination of incorporated teachings consistent with this disclosure is also encompassed. The citation of references is intended to be part of the disclosure of the invention, and not merely supplementary background information. While cited references may be prior art, the combinations thereof and with the material disclosed herein is not admitted as being prior art.

The incorporation by reference does not extend to teachings which are inconsistent with the invention as expressly described herein as being essential. The incorporated references are rebuttable evidence of a proper interpretation of terms, phrases, and concepts employed herein by persons of ordinary skill in the art. No admission is made that any incorporated reference is analogous art to the issues presented to the inventor, and the selection, combination, and disclosure of these disparate teachings is itself a part of the invention herein disclosed.

BACKGROUND OF THE INVENTION

Autonomous driving technologies have the great potential of reshaping urban mobility in people's daily life [1], [2], [3]. To be deemed useful, autonomous vehicles (hereinafter "vehicles") must be time-efficient in accomplishing service

2

tasks, which frequently requires symbolic actions such as "Merge left, go straight, turn left, and park right", while at the same time ensuring safety in executing such actions on the road [4], [5], [6].

Generally, autonomous vehicles need to plan at the task level to compute a sequence of symbolic actions toward fulfilling service requests from people. In this process, how the actions are implemented in the real world is out of consideration at the task level. At the same time, vehicles must plan at the motion level to compute continuous trajectories, and desired control signals (e.g., for steering, accelerating, and braking) to implement the symbolic actions. While the task planner hopes that all the symbolic actions can be implemented by the vehicles, there is the safety concern that must be considered at the motion level. For instance, lane-changing behaviors can be dangerous in heavy traffic. FIGS. 1A and 1B show two situations for a vehicle that are dangerous and safe, respectively. FIG. 1A shows a risky situation for the vehicle (blue) to merge left due to the busy traffic. FIG. 1B shows a safe situation exists for the vehicle to merge left. The goal of TMPUD is to enable the motion level to take symbolic actions from, and communicate safety to the task level toward efficient and safe autonomous driving behaviors.

Although task planning (frequently referred to as behavior planning in autonomous driving [7]) and motion planning have been individually conducted in autonomous driving, there is little research from the literature focusing on the interaction between task and motion levels. There is the critical need of developing algorithms to bridge the gap between task planning and motion planning to help vehicles improve the task-completion efficiency while ensuring the safety of driving behaviors.

The robotics community has studied the integration of task and motion planning, mostly in manipulation domains [8], [9], [10], [11]. In comparison to those domains, autonomous driving algorithms must consider the uncertainty from the ego vehicle, and the surrounding objects (including other vehicles) on the road. The uncertainty must be quantitatively evaluated at the motion level, and taken into consideration for planning at the task level. For instance, when the left lane is busy and missing the next crossing does not introduce much extra distance, the task planner should avoid forcing the vehicle to merge left. Such behaviors are possible, only if the interactions between task and motion levels are enabled.

Motion-Level Planning for Autonomous Driving: Safety is of the most importance at the motion level, and highly relies on the motion-level controllers. Early research in robotics (mostly on manipulation problems) has developed a "safe set" algorithm to avoid unsafe situations in human-robot interactions [14], where it offers a theoretical guarantee of safety. That algorithm has been improved to further account for the uncertainty from the real world [15], where both efficiency and safety were modeled in human-robot interface scenarios. Those methods focused on robot manipulation domains, where it is frequently assumed the acting agent being the only one that makes changes in the world, and hence are not applicable to autonomous driving domains.

Within the autonomous driving context, researchers have developed a series of learning and decision-making methods to enable motion planners to learn safe behaviors [16], [17], [18], [19], [20], [21]. The above-mentioned methods (in robotics and autonomous driving) mainly focus on motion-

level behaviors, and do not look into how motion-level behaviors can be sequenced at the task level to accomplish complex driving tasks.

Task-Level Planning for Autonomous Driving: Task planning has been applied to autonomous driving. For instance, one of the earliest works on this topic demonstrated that task planning techniques enable vehicles to complete complex tasks, such as to avoid temporary roadblocks [13]. However, their work did not consider costs of driving behaviors, and hence performs poorly in task-completion efficiency. Similarly, task planners in [22], [23], [24] have no interaction with the motion planner, and safety was not modeled in generating the driving behaviors.

More recent research has enabled vehicles to periodically verify the task sequences and motion trajectories against the actual traffic situation [25]. In case of possible dangers detected at the motion level, re-planning is triggered at the task level. The main limitation of this is that the triggering is deterministic, and highly depends on a safety threshold. The threshold must be set beforehand to ensure safety, which frequently produces over-conservative behaviors, and significantly reduces the task-level efficiency.

Task and Motion Planning: Researchers have integrated task and motion planning in robotics, where the primary domain is robot manipulation [26], [27], [28], [29], [8]. Research on manipulation is mostly concerned with the motion-level feasibility, e.g., in grasping and ungrasping behaviors, and accomplishing high-level tasks, such as stacking objects. Those methods did not consider the uncertainty from other agents (e.g., vehicles on the road). As a result, their systems produce over-optimistic (and hence risky) behaviors, assuming no other agents making changes in the world, and are not applicable to autonomous driving domains.

Further work has surveyed frameworks for autonomous driving [7], including works that plan at both task and motion levels. However, their motion planners do not provide any feedback to the task level, except for infeasible actions.

SUMMARY OF THE INVENTION

The present invention provides a system and method for task and motion planning for urban driving, which is useful for both real-time guidance and autonomous vehicles.

Autonomous vehicles need planning capabilities at two separate levels. On the one hand, at the task level, the vehicle needs to compute a sequence of actions to accomplish human-specific goals (say to buy groceries and add gasoline before going home) using action knowledge provided by domain experts. This so-called task planning problem is traditionally a problem studied in the AI community. On the other hand, the vehicle needs to compute motion trajectories that connect current and goal locations. At the motion level, the vehicle needs to consider its surrounding vehicles to ensure safety. Motion planning is traditionally a robotics problem.

The present technology brings task planning and motion planning together, and applies the integrated system onto autonomous driving scenarios. As a result, an approach, called Task-Motion Planning for Urban Driving (TMPUD), enables efficient task-level behaviors, while ensuring motion-level safety guarantees. See:

Ding, Yan, Xiaohan Zhang, Xingyue Zhan, and Shiqi Zhang. "Task-motion planning for safe and efficient urban driv-

ing." In 2020 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), pp. 2119-2125. IEEE, 2020;

Zhang, Xiaohan, Yifeng Zhu, Yan Ding, Yuke Zhu, Peter Stone, and Shiqi Zhang. "Visually Grounded Task and Motion Planning for Mobile Manipulation." arXiv preprint arXiv:2202.10667 (2022).

Ding, Yan, Xiaohan Zhang, Xingyue Zhan, and Shiqi Zhang. "Learning to Ground Objects for Robot Task and Motion Planning." arXiv preprint arXiv:2202.06674 (2022).

Phiquepal, Camille, and Marc Toussaint. "Combined task and motion planning under partial observability: An optimization-based approach." In 2019 International Conference on Robotics and Automation (ICRA), pp. 9000-9006. IEEE, 2019.

Woods, Grayson Landis. "Evaluation of Local Kinematic Motion Planning Algorithms for a Truck and Trailer System." PhD diss., 2020.

He, Zichen, Jiawei Wang, and Chunwei Song. "A review of mobile robot motion planning methods: from classical motion planning workflows to reinforcement learning-based architectures." arXiv preprint arXiv:2108.13619 (2021).

An existing task planning (an Answer Set Programming, or ASP), approach, and motion planning algorithms (provided by the CARLA simulator), are used. See, Lifschitz, Vladimir. Answer set programming. Berlin: Springer, 2019.

Brewka, Gerhard, Thomas Eiter, and Miroslaw Truszczyński. "Answer set programming at a glance." Communications of the ACM 54, no. 12 (2011): 92-103.

Eiter, Thomas, Giovambattista Ianni, and Thomas Krennwallner. "Answer set programming: A primer." In Reasoning Web International Summer School, pp. 40-110. Springer, Berlin, Heidelberg, 2009.

Erdem, Esra, Michael Gelfond, and Nicola Leone. "Applications of answer set programming." AI Magazine 37, no. 3 (2016): 53-68.

Lifschitz, Vladimir. "Answer set planning." In International Conference on Logic Programming and Nonmonotonic Reasoning, pp. 373-374. Springer, Berlin, Heidelberg, 1999.

Gebser, Martin, Torsten Schaub, and Sven Thiele. "Gringo: A new grounder for answer set programming." In International Conference on Logic Programming and Nonmonotonic Reasoning, pp. 266-271. Springer, Berlin, Heidelberg, 2007.

Lifschitz, Vladimir. "Answer set programming and plan generation." Artificial Intelligence 138, no. 1-2 (2002): 39-54.

Bonatti, Piero, Francesco Calimeri, Nicola Leone, and Francesco Ricca. "Answer set programming." A 25-year perspective on logic programming (2010): 159-182.

Gebser, Martin, Roland Kaminski, and Torsten Schaub. "Complex optimization in answer set programming." Theory and Practice of Logic Programming 11, no. 4-5 (2011): 821-839.

Niemela, Ilkka, Patrik Simons, and Tommi Syrjänen. "Smodels: a system for answer set programming." arXiv preprint cs/0003033 (2000).

Liu, Guohua, Tomi Janhunen, and Ilkka Niemela. "Answer set programming via mixed integer programming." In Thirteenth International Conference on the Principles of Knowledge Representation and Reasoning. 2012.

Brewka, Gerhard, Thomas Eiter, and Miroslaw Truszczyński. "Answer set programming: An introduction to the special issue." AI Magazine 37, no. 3 (2016): 5-6.

5

Eiter, Thomas, Giovambattista Ianni, Roman Schindlauer, and Hans Tompits. "A uniform integration of higher-order reasoning and external evaluations in answer-set programming." In *IJCAI*, vol. 5, pp. 90-96. 2005.

Toni, Francesca, and Marek Sergot. "Argumentation and answer set programming." *Logic Programming, Knowledge Representation, and Nonmonotonic Reasoning* (2011): 164-180.

US Patent and Patent Application Nos. 20220027737; 20210304066; 20210232915; 20210173831; 20210086370; 20210065027; 20200174765; 20200142732; 20200117575; 20200110835; 20200073739; 20190354911; 20190333164; 20190318411; 20190073426; 20190028370; 20180204122; 20180005123; 20150339355; 20150253768; 20140278683; 20140278682; 20140214582; 20140214581; 20140214580; 20140214487; 20140214474; 20120050787; 20100225954; 20090182786; 11,170,300; 11,165,783; 11,074,103; 11,055,200 11,036,774; 10,977,111; 10,832,141; 10,706,480; 10,705,814; 10,373,268; 10,305,765; 9,925,462; 9,584,535; 9,450,975; 9,135,432; 9,117,201; 9,110,905; 9,100,363; 9,059,960; 9,055,094; 8,990,387; 8,677,486; 8,671,182; 8,601,034; 8,578,002; 8,576,430; 8,474,043; 8,433,790; 8,289,882; 8,272,055; 8,127,353; 7,440,942; 7,219,350; and 7,197,699.

The simulation platform is provided by the autonomous driving community—CARLA, see CARLA.org. It simulates the ego vehicle's behaviors, as long as how the surrounding vehicles respond to the ego vehicle's behaviors. github.com/carla-simulator/carla/blob/dev/LI-CENSE. See also, US 20220042258; 20210390725; 20210326606; and 20200226377.

Gómez-Hudlamo, Carlos, Javier Del Egidio, Luis M. Bergasa, Rafael Barea, Elena López-Guillén, Felipe Arango, Javier Araluce, and Joaquin López. "Train here, drive there: Simulating real-world use cases with fully-autonomous driving architecture in carla simulator." In *Workshop of Physical Agents*, pp. 44-59. Springer, Cham, 2020.

Niranjan, D. R., and B. C. VinayKarthik. "Deep Learning based Object Detection Model for Autonomous Driving Research using CARLA Simulator." In *2021 2nd International Conference on Smart Electronics and Communication (ICOSEC)*, pp. 1251-1258. IEEE, 2021.

Deschaut, Jean-Emmanuel. "KITTI-CARLA: a KITTI-like dataset generated by CARLA Simulator." *arXiv preprint arXiv:2109.00892* (2021).

Stević, Stevan, Momčilo Krunic, Marko Dragojevid, and Nives Kaprocki. "Development and validation of ADAS perception application in ROS environment integrated with CARLA simulator." In *2019 27th Telecommunications Forum (TELFOR)*, pp. 1-4. IEEE, 2019.

Zhang, Wei, Siyu Fu, Zixu Cao, Zhiyuan Jiang, Shunqing Zhang, and Shugong Xu. "An SDR-in-the-loop Carla simulator for C-V2X-based autonomous driving." In *IEEE INFOCOM 2020-IEEE Conference on Computer Communications Workshops (INFOCOM WKSHPS)*, pp. 1270-1271. IEEE, 2020.

TMPUD does not depend on any particular simulation platform, vehicle model, or the selections of task and motion planners. From the simulation perspective, as long as the simulation platform is able to provide how the ego vehicle and environment respond to the ego vehicle's behaviors, they can be used for prototyping and evaluation purposes. TMPUD provides a generic way of computing task-motion plans. CARLA was selected as the evaluation platform

6

because it well supports the simulation of sensors, traffic lights, weathers, and road conditions. However, one can easily implement TMPUD using other popular simulators, such as AirSim (github.com/microsoft/AirSim) and Gazebo (github.com/osrf/gazebo). There are a number of such open-source simulation platforms, and many more that are not open-source.

The technology operates at two different levels; a high level task planning which permits determines goals and intermediate waypoints, for example, as well as low level motion planning which makes short-time scale decisions regarding movement options to achieve the same overall objectives. In general, the high level (long term, prospective, goal oriented) and low level (short term, concurrent, operations-oriented) planning must be both efficient and safe, and these disparate themes are combined using a cost-function. When the motion planner causes a deviation from a nominal task plan, the task planner then re-executes in order to replan the task based on the deviation. One way to consider the task planner and the motion planner is that the former is operative proactively based on predicted states and initial conditions to achieve a plan for a future action, while the motion planner is responsive to initial conditions and real time (sensor) data to plan a current action than as achieved nearly simultaneously with the planning.

Task-Motion Planning for Urban Driving (TMPUD) is thus provided for efficient and safe autonomous urban driving. TMPUD enables the interaction between task and motion planners through enabling the motion-level safety estimation and task-level replanning capabilities.

TMPUD has been evaluated using CARLA, an autonomous driving platform for simulating urban driving scenarios. [12] suggest TMPUD improves both safety and efficiency, in comparison to two baseline methods from the literature [13], [8]. TMPUD supports the interaction between task and motion levels, and aims at improving both safety and efficiency of autonomous driving behaviors. The TMPUD algorithm supports motion-level safety evaluation, and enables the task planner to dynamically adjust high-level plans to account for current road conditions toward accomplishing long-term driving tasks.

Task Planning

A task planning domain is specified by D^t , including a set of states, S , and a set of actions, A . A factored state space is assumed such that each state $s \in S$ is defined by the values of a fixed set of variables; each action $a \in A$ is defined by its preconditions and effects. A utility function maps the state transition to a real number, which takes both cost function $Cost(s,a,s')$ and safety function $Safe(s,a,s')$ into account. Specifically, the cost and safety functions respectively reflect the cost and safety of conducting action a in state s .

Given domain D^t and a task planning problem, a plan $p \in P$ is computed, starting from an initial state $s^{init} \in S$ and finishing in a goal state $s^g \in S$. A plan p consists of a sequence of transitions that can be represented as: $p = \langle s_0, a_0, \dots, s_{N-1}, a_{N-1}, s_N \rangle$, where $s_0 = s^{init}$, $s_N = s^g$ and P denotes a set of satisfactory plans. Task planner P^t can produce an optimal plan p^* among all satisfactory plans, where γ is a constant coefficient and $\gamma > 0$

$$p^* = \operatorname{argmin}_{p \in P} \sum_{(s,a,s') \in p} \left[Cost(\langle s, a, s' \rangle) + \frac{\gamma}{1 + e^{Safe(\langle s,a,s' \rangle) - 1}} \right].$$

Motion Planning

A motion planning domain is specified by D^m , where a search is conducted directly in 2D space constrained by the urban road network. Some parts of the space are designated as free space, and the rest are designated as obstacles. The 2D space is represented as a region in Cartesian space such that the position and orientation of the vehicle can be uniquely represented as a pose, denoted by x .

It is noted that the technology is not limited to operation in a 2D space, and rather is also applicable to higher dimensional spaces, e.g., 3D spaces (such as for aerial autonomous vehicles), and ~1D spaces (such as railroad or other constrained path travel).

Given domain D^m , a motion planning problem can be specified by an initial pose x^i and a goal pose x^g . The motion planning problem is solved by a motion planner P^m consisting of path planner and tracking planner into two phases. In the first one, a path planner computes a collision-free trajectory ξ connecting pose x^i and pose x^g taking into account any motion constraints on the part of the vehicle with minimal trajectory length. In the second one, a tracking controller computes desired control signals to drive the vehicle to follow the computed trajectory. Due to the fundamental difference between representations at task and motion levels, in line with past research [26], [29], [8], [11], a state mapping function, $f: X \rightarrow f(s)$, is used to map the symbolic state s into a set of feasible poses X in continuous space, for motion planner to sample from. Availability of at least one pose $x \in X$ is assumed in each state s , such that the vehicle is in the free space of D^m . If it is not the case, the state s is declared infeasible.

Safety Estimation

Safety estimation aims at computing the safety level, $\text{Safe}(\langle s, a, s' \rangle)$, of the motion-level implementation of a symbolic action $\langle s, a, s' \rangle$. The goal of computing the safety value is to enable the task planner to incorporate the road condition into the process of sequencing high-level actions toward accomplishing complex driving tasks.

To perform symbolic action $\langle s, a, s' \rangle$, a motion planner is used to compute a sequence of continuous control signals, i.e., acceleration $\delta \in \Delta$ and steering angle $\theta \in \Theta$, to drive the vehicle following the planned trajectory, while ensuring no collision on the road. Sets Δ and Θ denote the operation specification of the controller, which generally depends on the adopted motion planner and the ego vehicle itself. Let $U_s(t)$ (mathematically $U_s(t) \subset \Delta \times \Theta$) specify a safe control set at time t , in which all elements, denoted by $u(t) = \langle \delta, \theta \rangle$, are safe for an ego vehicle to perform at time t . Intuitively, the size of safe control set U_s reflects the safety level. For instance, when $|U_s|$ is very small, meaning that very few control signals are safe, the vehicle can only be operated in very particular ways, indicating the safety level in general is low. Accordingly, the probability of elements sampled from set $\Delta \times \Theta$ being located in the safe set U_s is to represent the safety value of action $\langle s, a, s' \rangle$.

Safety Estimation Algorithm

Algorithm 1 summarizes the procedure of the safety estimation algorithm. The input includes symbolic action $\langle s, a, s' \rangle$, stating mapping function f , motion planner P^m consisting of path planner and tracking controller, and the controller's operation specification sets Δ and Θ . The output is the estimated safety value $\text{Safe}(\langle s, a, s' \rangle) \in [0.0, 1.0]$.

In algorithm 1, lines 1-3 aim to obtain the short-period trajectories of the ego and surrounding vehicles, where

$V_i, i \in [1, \dots, N]$ is the i th vehicle within the ego vehicle's sensing range. More specifically, a first sample of a pair of feasible initial and goal poses for the symbolic actions using the state mapping function (Line 1). Taking these two poses as input, the motion planner then computes a continuous trajectory for the ego vehicle for a short period of time $[t_1, t_2]$ (Line 2), where t_1 is the current time, and $t_2 = t_1 + T$ indicates the time horizon of the ego vehicle. Surrounding vehicles' trajectories are predicted, assuming their linear and angular speeds being stationary (Line 3), though there are more advanced methods [30], [31].

Lines 4-8 of algorithm 1 present a control loop that computes the safety estimation between the ego vehicle and the surrounding vehicles V_i , where $i \in [1, \dots, N]$, given that the ego vehicle is performing action $\langle s, a, s' \rangle$ at the motion level. A safe control set $U_i^s(t)$ is computed, similar to [19], that includes all safe control signals with regard to vehicle V_i at time t (Line 5). Parameter ω controls the sampling interval.

In Line 6 of algorithm 1, M elements are randomly sampled from the set $\Delta \times \Theta$, and compute probability $o_i(t)$ of the sampled elements falling in set $U_i^s(t)$. A list of values of safety estimation $\{o_i(t)\}$ is converted into a single value o_i^* using eqn. 1, where \max and mean are two functions to calculate the maximum and mean value of a list, respectively (Line 7). Although all surrounding vehicles can potentially introduce risks to the ego vehicle, the ego vehicle is assumed to only consider the most dangerous vehicle. Accordingly, Line 9 is used for selecting the minimum value, $o_i^*, i \in [1, \dots, N]$, as the overall safety value:

$$o_i^* = \frac{\max_{t \in T} \{o_i(t)\} + \text{mean}_{t \in T} \{o_i(t)\}}{2} \quad (1)$$

$$\text{Where } T = t_1 + \omega \times i, 0 \leq i \leq \frac{(t_2 - t_1)}{\omega}$$

Algorithm 1 Safety Estimation

Input: Symbolic action $\langle s, a, s' \rangle$, state mapping function f , motion planner P^m , control operation sets Δ and Θ

1: Sample initial and goal poses, $x \leftarrow f(s)$ and $x' \leftarrow f(s')$, given action $\langle s, a, s' \rangle$, and f .

2: Compute a collision-free trajectory, ξ^E , using P^m , where $\xi^E(t_1) = x, \xi^E(t_2) = x'$; and $[t_1, t_2]$ is the horizon

3: Predict trajectory ξ_i^s for the i th surrounding vehicle, where $i \in [1, \dots, N]$, and $[t_1, t_2]$ is the horizon

4: while for each vehicle V_i do

5: Compute safe control set $U_i^s(t)$ between the ego vehicle and vehicle V_i at time $t \in [t_1, t_2]$, where $U_i^s(t) \in \Delta \times \Theta$ and

$$t = t_1 + \omega \times i, i \leq \frac{(t_2 - t_1)}{\omega}$$

6: Sample M elements $\langle \delta, \theta \rangle$ randomly from set $\Delta \times \Theta$ and compute the probability $o_i(t)$ of the elements falling in set $U_i^s(t)$

7: Convert a list of estimated safety values, $\{o_i(t)\}$, into a scalar value o_i^* using Eqn. 1

8: end while

9: return $\min\{o_i^*, i = 1, \dots, N\}$

TMPUD

The motion planner P^m computes both costs (trajectory lengths) and safety values of the ego vehicle's navigation actions.

s^{init} is used to represent the initial state of the ego vehicle, and the goal (service request from people) is specified using s^g . The task planner P' computes a sequence of symbolic actions, and it requires two functions that are initialized and updated within the algorithm, including cost function Cost, and safety estimation function Safe. Motion planner P^m is used for computing motion trajectories, and generating control signals to move the ego vehicle. The state mapping function f is used for mapping symbolic states to 2D coordinates in continuous spaces.

The TMPUD Algorithm

Algorithm 2 summarizes the procedure of TMPUD. It starts by initializing the cost and safety estimation functions (Lines 1 and 2 of algorithm 2). Cost function Cost is initialized using the A* algorithm provided by CARLA, as shown in Line 1 of algorithm 2. In Line 2 of algorithm 2, TMPUD optimistically initializes the safety estimation function by setting 1.0 to all actions, indicating all task-level actions are completely safe. After that, an optimal task plan, $p^* = \langle s^{init}, a_0, s_1, \dots, s^g \rangle$ is computed in Line 3 of algorithm 2. The head and tail elements of the plan, s^{init} and s^g , correspond to the initial and goal poses respectively.

Lines 4-19 of algorithm 2 form TMPUD's main control loop that enables the interaction between task and motion planners. The loop's termination condition is the task-level plan being empty, i.e., the goal has been achieved (Line 4 of algorithm 2). Specifically, TMPUD estimates the safety level, μ , of action $\langle s, a, s' \rangle$ (Line 5 of algorithm 2). Functions Safe and Cost are updated using μ and A* search in Line 6 of algorithm 2. Then a new optimal plan p' is computed in Line 7 of algorithm 2. Lines 8-18 of algorithm 2 is for plan monitoring and action execution. If the task planner suggests the same plan (Line 8 of algorithm 2), the vehicle will continue to execute action a at the motion level. The goal state is sampled from state mapping function in Line 9 of algorithm 2. Lines 10-14 of algorithm 2 is a loop to execute the action. Specifically, the motion planner will compute and execute a desired control signal $\langle \delta, \theta \rangle$ repeatedly until the vehicle reaches the goal pose (Line 10 of algorithm 2). The vehicle's current pose x will be updated after each execution (Line 13 of algorithm 2). After completing the operation, the tuple $\langle s, a \rangle$ will be removed from the plan p (Line 15 of algorithm 2). On the contrary, if the task planner suggests a new plan p' different from the plan p , the currently optimal p' will replace the non-optimal plan p (Line 17 of algorithm 2).

Algorithm 2 TMPUD algorithm

Input: Initial state s^i , goal specification s^g , task planner P' , state mapping function f , motion planner P^m , and safety estimator (Algorithm 1)

- 1: Initialize cost function Cost with sampled poses $x \in f(s): \text{Cost}(\langle s, a, s' \rangle) \leftarrow A^*(x, x')$
- 2: Initialize safety estimation $\text{Safe}(s, a, s') \leftarrow 1.0$
- 3: Compute an optimal task plan p using Cost and Safe functions:

$$p \leftarrow P'(\langle s^{init}, s^g, \text{Cost}, \text{Safe} \rangle), \text{ where } p = \langle s^{init} \rightarrow a_0, s_1, a_1, \dots, s^g \rangle$$

- 4: while Plan p is not empty do
- 5: Extract the first action of $p(s, a, s')$ and compute safety value μ using Algorithm 1
- 6: Update Safe function: $\text{Safe}(\langle \exists a, s' \rangle) \leftarrow \mu$ and Cost function:

$$\text{Cost}(\langle s, a, s' \rangle) \leftarrow A^*(x, x')$$

- 7: Generate a new plan: $p' \leftarrow P'(\langle s, s^g, \text{Cost}, \text{Safe} \rangle)$
- 8: if $p' = p$ then
- 9: $x' \leftarrow f(s')$
- 10: while $x' \neq x$ do
- 11: Call motion planner $\langle \delta, \theta \rangle \leftarrow P^m(x, x')$
- 12: Execute the control signal $\langle \delta, \theta \rangle$
- 13: Update the vehicle's current pose x
- 14: end while
- 15: Remove the tuple $\langle s, a \rangle$ from plan p
- 16: else
- 17: Update current plan $p \leftarrow p'$
- 18: end if
- 19: end while

Task Planner

The task planner P' is implemented using Answer Set Programming (ASP), which is a popular declarative language for knowledge representation and reasoning, and ASP has been used for task planning [32], [33], [11], [34]. For example, predicate $\text{leftof}(\text{La1}, \text{La2})$ can be used to specify lane La1 being on the left of lane La2. Five driving actions are modelled, including mergeleft, mergeright, forward, turnleft, and turnright. For instance, action mergeright can be used to help the vehicle merge to the right lane, where constraints, such as "changeright" is allowed only if there exists a lane on the right, have been modeled as well.

Motion Planner

At the motion level, path planner firstly generates a desired continuous trajectory with the minimal traveling distance using A* search. The trajectory includes a set of waypoints (each in the form of a pair of x-y coordinate and orientation), and the trajectory is delivered to the tracking controller, along with the vehicle's current pose and speed. The controller uses a proportional-integral-derivative (PID) controller [35] to generate control signals, e.g., for steering, throttle, and brake. PID controller is very popular due to its simplicity, flexibility, and robustness.

CARLA, an open-source 3D urban driving simulator [12] was developed to support development, training, and validation of autonomous driving systems. Compared to other simulation platforms, e.g., [36], [37], see, U.S. Pat. Nos. 11,150,655; 11,030,476; 10,997,467; 10,596,339; 9,662,068; 11,150,658; 10,588,033; 10,425,954; 20210394788; 20210311504; 20210278854; 20210271253; 20210133502; 20210117730; 20190004518; 20220058815; 20220057804; 20220055215; 20210287556; 20210247781; 20210088337; 20200310444; 20200293053; 20200293052; 20200293051; 20190053074; and 20180288774, CARLA provides open digital assets (urban layouts, buildings, vehicles) that were created for this purpose and can be used freely.

See also:

- Bondi, Elizabeth, Debadeepta Dey, Ashish Kapoor, Jim Piavis, Shital Shah, Fei Fang, Bistra Dilkina et al. "Airsim-w: A simulation environment for wildlife conservation with uavs." In Proceedings of the 1st ACM SIGCAS Conference on Computing and Sustainable Societies, pp. 1-12. 2018.
- Shah, Shital, Debadeepta Dey, Chris Lovett, and Ashish Kapoor. "Airsim: High-fidelity visual and physical simulation for autonomous vehicles." In Field and service robotics, pp. 621-635. Springer, Cham, 2018.
- Nguyen, Justin, Peter K. Nguyen, and Mujahid Abdulrahim. "Development of an Unmanned Traffic Management Simulation with Robot Operating System and Gazebo." In AIAA SCITECH 2022 Forum, p. 1918. 2022.

Mehrooz, Golizheh, Emad Ebeid, and Peter Schneider-Kamp. "System design of an open-source cloud-based framework for internet of drones application." In 2019 22nd Euromicro Conference on Digital System Design (DSD), pp. 572-579. IEEE, 2019.

Zhu, Donglin, Guanghui Xu, Xiaoting Wang, Xiaogang Liu, and Dewei Tian. "PairCon-SLAM: Distributed, Online, and Real-Time RGBD-SLAM in Large Scenarios." IEEE Transactions on Instrumentation and Measurement 70 (2021): 1-14.

Nikolenko, Sergey I. "Synthetic Simulated Environments." In Synthetic Data for Deep Learning, pp. 195-215. Springer, Cham, 2021.

de Figueiredo, Rui Pimentel, Jonas le Fevre Sejerssen, Jakob Grimm Hansen, Martim Brandao, and Erdal Kayacan. "Real-Time Volumetric-Semantic Exploration and Mapping: An Uncertainty-Aware Approach." In 2021 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), pp. 9064-9070. IEEE, 2021.

Yoon, Sugjoon, Dongcho Shin, Younghoon Choi, and Kyungtae Park. "Development of a flexible and expandable UTM simulator based on open sources and platforms." Aerospace 8, no. 5 (2021): 133.

The CARLA software provides two functionalities: First, it enables an ego vehicle to evaluate the safety level based on its surrounding vehicles' locations and speeds. Second, it computes task-level plans (a sequence of symbolic actions), and motion-level plans (a trajectories in continuous space) at the same time.

An autonomous vehicle (AV) (e.g., a driverless car, a driverless auto, a self-driving car, a robotic car, etc.) is a vehicle that is capable of sensing an environment of the vehicle and traveling (e.g., navigating, moving, etc.) in the environment without human input. An AV uses a variety of techniques to detect the environment of the AV, such as radar, laser light, lidar, Global Positioning System (GPS), odometry, and/or computer vision. In some instances, an AV uses a control system to interpret information received from one or more sensors, to identify a route for traveling, to identify an obstacle in a route, and to identify relevant traffic signs associated with a route.

The AV includes a processor, which may be local to the AV, remote from the AV at a data center, for example, or distributed through a variety of predetermined or ad hoc computing resources. Often, it is useful to implement artificial intelligence and/or machine learning to help manage the extremely high dimensionality of the sensor dataset, rule base, and control options. The processor may include reduced instruction set computing (RISC) processors, complex instruction set processors (CISC), single instruction-multiple data (SIMD) processors or other parallel processing systems, artificial neural network (ANN) processors or implementations, field programmable gate arrays (FPGA), application-specific integrated circuits (ASIC) and the like, and typically will include multiple processors, with some dedicated to particular tasks.

An autonomous vehicle (AV) map of a geographic location may be used for determining nominal driving paths on lanes of roadways (e.g., roadway segments) in the map on which an AV may operate (e.g., route, travel, or perform one or more autonomous operations). For example, a nominal driving path including one or more lanes on one or more roadway segments is determined by generating a center line through lane boundaries of a lane. However, a nominal driving path may not describe a proper driving path through lanes on roadway segments over which an AV can travel. For example, nominal driving paths may include inconsistencies

associated with the lane boundaries of the roadway. As an example, a centerline of lane boundaries may provide inaccuracies for AV travel, based on different markings from a first lane to a second lane in a roadway where the width of the lane boundaries are determined. Additionally or alternatively, an AV of a first size may not operate on a nominal driving path, the same as an AV of a second size on the same nominal path. For example, a large sized AV may be limited (e.g., constrained) in movement as compared to a smaller sized AV when traversing a nominal driving path based on the lane boundaries in the roadway of the AV map. Additionally or alternatively, a nominal driving path may be inefficiently determined from aspects of a lane polygon that requires additional storage of points on the polygon and/or additional computations. In this way, a nominal driving path may be less complete and/or result in less efficient processing for operating and/or routing the AV. In addition, a map may be generated that provides an AV fewer operating options and/or driving options, may not account for the proper structure of lanes, and/or may implement additional processing functions to modify or augment the AV map for lanes with incomplete or incorrect physical markings. Therefore, while maps are useful, and permit geographic reference of structures and events, they typically cannot be relied upon for safe traverse during operation of the AV, and sensor data and real-time processing is required for safety and reliability. Further, the limitations on the data available before a task is begun, or before a portion of a task is implemented, impose limits on task planning.

Therefore, an AV should have processing capability for both safe motion planning and task planning available during operation.

A map generation system may contain or receive map data associated with a map of a geographic location, wherein the map data is associated with a roadway or traverse passage in the geographic location. The map generation system determines a general motion path including one or more trajectories for an AV, and the map data may be acquired by various means, and preferably based on one or more traversals of the path by one or more vehicles. The map generation system may generate driving path information based on one or more trajectory points in the one or more trajectories of the driving path. In this way, the map generation system provides and/or generates the driving path data associated with the driving path to an AV for controlling travel of the AV.

A vehicle computing system of an AV may receive driving path data associated with a desired path, including one or more trajectories (or ranges or limits on the available trajectories) that an AV can traverse. For example, the actual travel path and trajectory may be dependent on vehicle speed, traffic, obstacles or hazards, uncontrolled excursions from the desired path (e.g., skids), weather, and other factors.

The AV will therefore typically plan a route in advance of travel, and then make decisions during travel for particular path options dependent on real-time calculations. In this case, a real time calculation is meant to encompass calculations that occur between receipt of sensor data and when the AV must respond to the sensor data to avoid adverse effect. For example, an adaptive suspension may require millisecond scale response times, while a path planning system responsive to a posted traffic signal observed by a camera may have seconds of planning time.

The AV computing system can determine at least one feature of the environment or roadway in the intended (or avoided) path based on the map data, non-real time data

(such as historical or old traffic data) and real-time data. In some cases, the vehicle computing system can determine a lateral constraint associated with lateral movement of the AV based on the driving path data associated with the trajectory. Accordingly, the map enables the vehicle computing system to generate and/or traverse a route in a more efficient manner with less processing delays and/or routing for the AV to be performed by the vehicle processing system (e.g., completely by the vehicle processing system).

The map generation system and/or the AV may include one or more devices capable of receiving, storing, and/or providing map data associated with a map of a geographic location (e.g., a country, a state, a city, a portion of a city, a township, a portion of a township, etc.). For example, AV maps are used for routing an AV on a roadway specified in the AV maps. The map data may include data associated with a road (e.g., an identity and/or a location of a roadway of a road, an identity and/or location of a segment of a road, etc.), data associated with features of a road, such as an object in proximity to a road (e.g., a building, a lamppost, a crosswalk, a curb of the road, etc.), data associated with a lane of a roadway (e.g., the location and/or direction of a travel lane, a parking lane, a turning lane, a bicycle lane, etc.), data associated with traffic control of a road (e.g., the location of and/or instructions associated with lane markings, traffic signs, traffic lights, etc.), and/or the like. A map of a geographic location may include one or more routes that include one or more roadways. Map data associated with a map of the geographic location may associate each roadway of the one or more roadways with an indication of whether an AV can travel on that roadway. Features of a road may be based on data collected by and/or received from one or more sensors located on an AV as the AV travels on one or more roads in a geographic location.

The map may include dynamic information, such as traffic light timing, diurnal/weekly/monthly/annual traffic density patterns and changes, correlations between patterns at different locations, etc. Further, to the extent that the map is available for use by a human occupant of the AV, the map may also include points of interest, sponsored points of interest (location-based advertising), promotions, and the like. Further, the map may include locations of electric vehicle (EV) charging stations, to allow planning energy availability and replenishment, in addition to endpoint route.

A road refers to a paved or otherwise improved path between two places that allows for travel by a vehicle (e.g., an AV). Additionally or alternatively, a road includes a roadway and a sidewalk in proximity to (e.g., adjacent, near, next to, touching, etc.) the roadway. A roadway may include a portion of road on which a vehicle is intended to travel and is not restricted by a physical barrier or by separation so that the vehicle is able to travel laterally. Additionally or alternatively, a roadway includes one or more lanes, such as a travel lane (e.g., a lane upon which a vehicle travels, a traffic lane, etc.), a parking lane (e.g., a lane in which a vehicle parks), a bicycle lane (e.g., a lane in which a bicycle travels), a turning lane (e.g., a lane in which a vehicle turns from), and/or the like. A roadway may be connected to another roadway, for example a lane of a roadway may be connected to another lane of the roadway and/or a lane of the roadway may be connected to a lane of another roadway.

Note that the present technology is not limited to on-road automobiles, and rather may be used for off-road, unmanned autonomous vehicles (UAV), pedestrians, bicycles, mopeds, motorcycles, snowmobiles, and other types of vehicles or travel situations. The present technology in general seeks to optimize the task planning with the motion planning in a safe

and efficient manner. Note that safety is often a statistical consideration, and what is managed is the margin of safety or predicted margin of safety, since other than in extreme cases, operation in a designated unsafe manner is undesirable. On the other hand, in certain sports or emergencies, operation outside of safe ranges is desired, and this can also be accommodated within the paradigm. Likewise, efficiency is typically desired, but the metric may be designed based on various cost functions. Thus, where time is of the essence, a high weighting of time may lead to an optimal path which would otherwise be considered inefficient or unsafe, or both. More generally, by combining the various considerations of efficiency and safety into a combined determination, hard constraints are avoided, and therefore more options are available during motion to achieve an optimal result.

A map generation system may include one or more devices capable of receiving map data, determining a driving path for an AV including one or more trajectories in a lane of the roadway based on one or more traversals of the roadway by one or more vehicles, generating driving path information based on one or more trajectory points in the one or more trajectories of the driving path in the roadway, and/or providing driving path data associated with the driving path for controlling the AV. For example, the map generation system can include one or more computing systems including one or more processors (e.g., one or more servers, etc.).

AVs may include one or more devices capable of receiving driving path data and determining a route in a lane including a driving path based on the driving path data. The AV may include one or more devices capable of controlling travel, operation, and/or routing of the AV based on the driving path data. For example, the one or more devices may control travel and one or more functionalities associated with the fully autonomous mode of the AV in a lane on the driving path, based on the driving path information including feature information associated with the driving path, for example, by controlling the one or more devices (e.g., a device that controls acceleration, a device that controls steering, a device that controls braking, etc.) of AV based on sensor data, position data, and/or map data associated with determining the features in the lane. The AV may include one or more devices capable of receiving map data, determining a route in a lane that includes the driving path for an AV, including one or more trajectories in a roadway based on one or more traversals of the roadway by one or more vehicles, generating driving path information based on one or more trajectory points in the one or more trajectories of the driving path in the roadway, and/or providing driving path data associated with the driving path for controlling the AV. For example, AV can include one or more computing systems including one or more processors (e.g., one or more servers, etc.).

The map generation system and/or AV may include one or more devices capable of receiving, storing, and/or providing map data (e.g., map data, AV map data, coverage map data, hybrid map data, submap data, etc.) associated with a map (e.g., a map, a submap, an AV map, a coverage map, a hybrid map, etc.) of a geographic location (e.g., a country, a state, a city, a portion of a city, a township, a portion of a township, etc.). For example, maps are used for routing AV on a roadway specified in the map.

The network may include one or more wired and/or wireless networks. For example, the network may include a cellular network (e.g., a long-term evolution (LTE) network, a third generation (3G) network, a fourth generation (4G) network, a fifth generation (5G) network, a sixth generation

15

(6G) network, a WiFi network (e.g., within IEEE-802.11 series of standards, e.g., WiFi 5, WiFi 6, WiFi 6E, WiFi 7), a low earth orbiting satellite network, Starlink, WiMax, etc.), a local area network (LAN), a wide area network (WAN), a metropolitan area network (MAN), an ad hoc network, the Internet, a fiber optic-based network, a cloud computing network, and/or the like, and/or a combination of these or other types of networks.

The AV computing system may include vehicle command system, perception system, prediction system, task planning system, and motion planning system that cooperate to perceive a surrounding environment of AV, determine a motion plan and control the motion (e.g., the travel vector and parameters) of AV accordingly.

The AV computing system may be is connected to or include a positioning system. The positioning system may determine a position (e.g., a current position, a past position, etc.) of AV, and typically includes a geographic positioning system (GPS) and/or inertial guidance system. The positioning system may determine a position of AV based on an inertial sensor, a satellite positioning system, triangulation based on network components (e.g., network access points, cellular towers, Wi-Fi access points, etc.), and/or proximity to network components, and/or the like.

The AV computing system may receive sensor data from one or more sensors that are coupled to or otherwise included in AV. For example, one or more sensors may include a Light Detection and Ranging (LIDAR) system, a Radio Detection and Ranging (RADAR) system, one or more cameras (e.g., visible spectrum cameras, infrared cameras, etc.), and/or the like. The sensor data may include data that describes a location of objects within the surrounding environment of the AV. One or more sensors may collect sensor data that includes data that describes a location (e.g., in three-dimensional space relative to the AV) of points that correspond to objects within the surrounding environment of AV.

The sensor data may include a location (e.g., a location in three-dimensional space relative to the LIDAR system) of a number of points (e.g., a point cloud) that correspond to objects that have reflected a ranging laser. The LIDAR system may measure distances by measuring a Time of Flight (TOF) that a short laser pulse takes to travel from a sensor of the LIDAR system to an object and back, and the LIDAR system calculates the distance of the object to the LIDAR system based on the known speed of light. Map data may include LIDAR point cloud maps associated with a geographic location (e.g., a location in three-dimensional space relative to the LIDAR system of a mapping vehicle) of a number of points (e.g., a point cloud) that correspond to objects that have reflected a ranging laser of one or more mapping vehicles at the geographic location. As an example, a map can include a LIDAR point cloud layer that represents objects and distances between objects in the geographic location of the map.

The sensor data may include a location (e.g., a location in three-dimensional space relative to the RADAR system) of a number of points that correspond to objects that have reflected a ranging radio wave. Radio waves (e.g., pulsed radio waves or continuous radio waves) transmitted by the RADAR system can reflect off an object and return to a receiver of the RADAR system. The RADAR system can then determine information about the object's location and/or speed. The RADAR system may provide information about the location and/or the speed of an object relative to

16

the RADAR system based on the radio waves. Multipath exploitation RADAR may be used to detect non-line of sight features.

Image processing techniques (e.g., range imaging techniques, such as, for example, structure from motion, structured light, stereo triangulation, etc.) can be performed by the system to identify a location (e.g., in three-dimensional space relative to the one or more cameras) of a number of points that correspond to objects that are depicted in images captured by one or more cameras. Other sensors can identify the location of points that correspond to objects as well. Sensor fusion may be used to merge related data, such as from a time-of-flight (TOF) sensor to provide additional data and analysis.

The map database may provide detailed information associated with the map, features of the roadway in the geographic location, and information about the surrounding environment of the AV for the AV to use while driving (e.g., traversing a route, planning a route, determining a motion plan, controlling the AV, etc.).

The vehicle computing system may receive a vehicle pose from localization system based on one or more sensors that are coupled to or otherwise included in AV. The localization system may include a LIDAR localizer, a low-quality pose localizer, and/or a pose filter. For example, the localization system may employ a pose filter that receives and/or determines one or more valid pose estimates (e.g., not based on invalid position data, etc.) from the LIDAR localizer and/or a low-quality pose localizer, for determining a map-relative vehicle pose. For example, the low-quality pose localizer determines a low quality pose estimate in response to receiving position data from positioning system for operating (e.g., routing, navigating, controlling, etc.) the AV under manual control (e.g., in a coverage lane). The LIDAR localizer may determine a LIDAR pose estimate in response to receiving sensor data (e.g., LIDAR data, RADAR data, etc.) from sensors for operating (e.g., routing, navigating, controlling, etc.) the AV under autonomous control (e.g., in a coverage lane).

A vehicle command system may include a navigation system, and a lane association system that cooperate to route and/or navigate the AV in a geographic location. The vehicle command system may track a current objective of the AV, including a current service, a target pose, and/or a coverage plan (e.g., development testing, etc.). The navigation system may determine and/or provide a route plan (e.g., a task plan) for the AV based on the current state of the AV, map data (e.g., lane graph, etc.), and one or more vehicle commands (e.g., a target pose). For example, navigation system may determine a route plan (e.g., plan, re-plan, deviation, etc.) including one or more lanes (e.g., current lane, future lane, etc.) in one or more roadways the AV may traverse on a route to a destination (e.g., target, trip drop-off, etc.).

The navigation system may determine a route plan based on one or more lanes received from lane association system. The lane association system may determine one or more lanes of a route in response to receiving a vehicle pose from the localization system. For example, the lane association system determines, based on the vehicle pose, that the AV is on a coverage lane, and in response to determining that the AV is on the coverage lane, determines one or more candidate lanes (e.g., routable lanes) within a distance of the vehicle pose associated with the AV. For example, the lane association system determines, based on the vehicle pose, that the AV is on an AV lane, and in response to determining that the AV is on the AV lane, determines one or more candidate lanes (e.g., routable lanes) within a distance of the

vehicle pose associated with the AV. The navigation system generates a cost function for each of one or more candidate lanes the AV may traverse on a route to a destination. For example, navigation system generates the cost function that describes a cost (e.g., a cost over a time period) of following (e.g., adhering to) one or more lanes to reach a target pose.

The perception system may detect and/or track objects (e.g., vehicles, pedestrians, bicycles, and/or the like) that are proximate to (e.g., in proximity to the surrounding environment of) the AV over a time period. The perception system can retrieve (e.g., obtain) map data from map database that provides detailed information about the surrounding environment of the AV. For example, the perception system may determine differences between the map data and a current sensor stream, and thereby infer mobile or dynamically changing elements and static elements. This, in turn, permits a risk assessment with respect to change of position or orientation of objects and their potential interaction with the AV during travel.

The perception system may determine one or more objects that are proximate to AV based on sensor data received from one or more sensors and/or map data from the map database. For example, the perception system determines, for the one or more objects that are proximate, state data associated with a state of such object. The state data associated with an object includes data associated with a location of the object (e.g., a position, a current position, an estimated position, etc.), data associated with a speed of the object (e.g., a magnitude of velocity of the object), data associated with a direction of travel of the object (e.g., a heading, a current heading, etc.), data associated with an acceleration rate of the object (e.g., an estimated acceleration rate of the object, etc.), data associated with an orientation of the object (e.g., a current orientation, etc.), data associated with a size of the object (e.g., a size of the object as represented by a bounding shape such as a bounding polygon or polyhedron, a footprint of the object, etc.), data associated with a type of the object (e.g., a class of the object, an object with a type of vehicle, an object with a type of pedestrian, an object with a type of bicycle, etc.), and/or the like.

The perception system may determine state data for an object over a number of iterations of determining state data. For example, perception system may update the state data for each object of a plurality of objects during each iteration.

The prediction system may receive the state data associated with one or more objects from perception system. The prediction system may predict one or more future locations for the one or more objects based on the state data. For example, the prediction system may predict the future location of each object of a plurality of objects within a time period (e.g., 0.5 second, 1 second, 2, seconds, 3 seconds, 4 seconds, 5 seconds, 10 seconds, 20 seconds, etc.). The prediction system may predict that an object will adhere to the object's direction of travel according to the speed of the object. The prediction system may use machine learning techniques or modeling techniques to make a prediction based on state data associated with an object.

The motion planning system may determine a motion plan for AV based on a prediction of a location associated with an object provided by the prediction system and/or based on state data associated with the object provided by the perception system. For example, the motion planning system may determine a motion plan (e.g., an optimized motion plan) for the AV that causes AV to travel relative to the object based on the prediction of the location for the object

provided by the prediction system and/or the state data associated with the object provided by the perception system.

The motion planning system may receive a route plan as a command from the navigation system. The motion planning system may determine a cost function for each of one or more motion plans of a route for AV based on the locations and/or predicted locations of one or more objects. The cost function includes such parameters as time, objective, energy cost, safety risk, event cost, vehicle operation cost (e.g., tires, brakes, fuel/electricity), etc.

For example, the motion planning system determines the cost function that describes a cost (e.g., a cost over a time period) of following (e.g., adhering to) a motion plan (e.g., a selected motion plan, an optimized motion plan, etc.) as well as a predicted risk and associated costs of the predicted risks. The cost associated with the cost function increases and/or decreases based on elements of a motion plan (e.g., a selected motion plan, an optimized motion plan, a preferred motion plan, etc.).

For example, while a non-risk adjusted cost function increases and/or decreases based on the AV deviating from the motion plan to avoid a collision with an object, a risk adjusted cost function would generally decreased as a result of properly executed collision avoidance maneuvers. More generally, the risks are less discrete. Any time an AV changes lanes, there is a potential risk, though in some cases, the risk of changing lanes is lower than the risk or cost-compensated risk of remaining in the same lane. That is, the collision or adverse event is a low probability, but not zero, and the risk probability is generally included in the motion plan to mitigate unnecessary risks that do not substantially improve task efficiency. However, where task efficiency value of an action is substantial, and exceeds the risk-adjusted cost of the action, then the system should take the action.

The motion planning system may determine a cost of following a motion plan. For example, motion planning system determines a motion plan for AV based on one or more cost functions. The motion planning system determines a motion plan (e.g., a selected motion plan, an optimized motion plan, a preferred motion plan, etc.) that minimizes a risk-adjusted cost function. The motion planning system may provide a motion plan to vehicle controls (e.g., a device that controls acceleration, a device that controls steering, a device that controls braking, an actuator that controls gas flow, etc.) to implement the motion plan. Alternately, the motion planner may be integrated into the motion controller, and the plan need not be a separate and discrete communication.

Each main process within the system may be associated with its physical processor, instructions, memory, data communication interface, etc., or multiple functions may be combined in a single hardware platform. Typically, in order to guaranty deterministic performance, assist in achieving fault tolerance, provide opportunity for diagnostics, repair, and upgrades, separate hardware is provided for specific tasks, and the communications between the modules is discrete.

In a typical module, a bus permits communication among the components. The processor is implemented in hardware, firmware, or a combination of hardware and software. For example, processor includes one or more processing elements (e.g., a central processing unit (CPU), a graphics processing unit (GPU), an accelerated processing unit (APU), etc.), a microprocessor, a digital signal processor (DSP), and/or any processing component (e.g., a field-programmable gate array (FPGA), an application-specific

integrated circuit (ASIC), etc.) that can be programmed to perform a function. A memory may include random access memory (RAM), read only memory (ROM), and/or another type of dynamic or static storage device (e.g., flash memory, magnetic memory, optical memory, etc.) that stores information and/or instructions for use by the processor.

A storage component stores information and/or software related to the operation and use of device. For example, the storage component includes a solid state mass storage device such as a NVMe®, PCIe 3.0 or PCIe 4.0 storage device.

An input component may include a component that permits the device to receive information, such as via user input (e.g., a touch screen display, a keyboard, a keypad, a mouse, a button, a switch, a microphone, etc.). Additionally, or alternatively, the input component includes a sensor for sensing information (e.g., a global positioning system (GPS) component, an accelerometer, a gyroscope, an actuator, etc.).

An output component may include a component that provides output information from the device (e.g., a display, a speaker, one or more light-emitting diodes (LEDs), etc.).

A communication interface may include a transceiver-like component (e.g., a transceiver, a separate receiver and transmitter, etc.) that enables the device to communicate with other devices, such as via a wired connection, a wireless connection, or a combination of wired and wireless connections. The communication interface can permit the device to receive information from another device and/or provide information to another device. For example, the communication interface may include an Ethernet interface, an optical interface, a coaxial interface, an infrared interface, a radio frequency (RF) interface, a universal serial bus (USB) interface, a Wi-Fi interface, a cellular network interface, and/or the like.

The device can perform one or more processes described herein, e.g., by executing software instructions stored by a computer-readable medium, such as a memory and/or the storage component. A computer-readable medium (e.g., a non-transitory computer-readable medium) is defined herein as a non-transitory memory device. A memory device includes memory space located inside of a single physical storage device or memory space spread across multiple physical storage devices. Software instructions can be read into the memory and/or storage component from another computer-readable medium or from another device via communication interface. When executed, software instructions stored in the memory and/or storage component cause the processor to perform one or more processes described herein. Additionally, or alternatively, hardwired circuitry can be used in place of or in combination with software instructions to perform one or more processes described herein. Thus, embodiments described herein are not limited to any specific combination of hardware circuitry and software.

The roadway may be associated with map data (e.g., map data, AV map data, coverage map data, hybrid map data, submap data, route data, etc.) that defines one or more attributes of (e.g., metadata associated with) the roadway (e.g., attributes of a roadway in a geographic location, attributes of a segment of a roadway, attributes of a lane of a roadway, attributes of an edge of a roadway, etc.). An attribute of a roadway may include a road edge of a road (e.g., a location of a road edge of a road, a distance of location from a road edge of a road, an indication whether a location is within a road edge of a road, etc.), an intersection, connection, or link of a road with another road, a roadway of a road, a distance of a roadway from another roadway (e.g., a distance of an end of a lane and/or a

roadway segment or extent to an end of another lane and/or an end of another roadway segment or extent, etc.), a lane of a roadway of a road (e.g., a travel lane of a roadway, a parking lane of a roadway, a turning lane of a roadway, lane markings, a direction of travel in a lane of a roadway, etc.), one or more objects (e.g., a vehicle, vegetation, a pedestrian, a structure, a building, a sign, a lamppost, signage, a traffic sign, a bicycle, a railway track, a hazardous object, etc.) in proximity to and/or within a road (e.g., objects in proximity to the road edges of a road and/or within the road edges of a road), a sidewalk of a road, and/or the like.

The lane (and/or a roadway segment or extent) may have one or more ends. For example, an end of a lane (and/or a roadway segment or extent) is associated with or corresponds to a geographic location at which map data associated with the lane (and/or the roadway segment or extent) ends (e.g., is unavailable). As an example, an end of a lane can correspond to a geographic location at which map data for that lane ends.

The map data may include a link (e.g., a connection) that connects or links a lane (and/or a roadway segment or extent) to another lane (and/or to another roadway segment or extent). As an example, the map data includes a unique identifier for each lane (and/or roadway segment or extent), and the unique identifiers are associated with one another in the map data to indicate a connection or link of a lane to another lane (or a connection or link of a roadway segment or extent to another roadway segment or extent). For example, the unique identifiers can be associated with one another in the map data to indicate that a lane (and/or a roadway segment or extent) is a predecessor lane or a successor lane to another lane (and/or a predecessor or successor roadway segment or extent to another roadway segment or extent). As an example, a heading of travel (e.g., direction) of a predecessor lane to another lane is from the predecessor lane to another lane, and a heading of travel of a successor lane to another lane is from another lane to the successor lane.

The process includes determination of a driving path including one or more trajectories. The map generation system may determine a driving path including one or more trajectories for an AV in a roadway based on one or more traversals of the roadway by one or more vehicles. For example, the map generation system may determine a driving path in the roadway to represent an indication of a centerline path in at least one lane of the roadway for controlling the AV during operation (e.g., follow) on the driving path. As an example, map generation system may determine the centerline path based on the lane markings on the road and/or based on one or more traversals of the roadway by one or more vehicles and/or a determination of where a vehicle will drive in a lane of the roadway. The map generation system may determine a driving path that includes feature information based on features of the roadway (e.g., section of curb, marker, object, etc.) for controlling an AV to autonomously determine objects in the roadway. For example, the map generation system determines a driving path that includes the left and right edges of a lane in the roadway; in this way, the map generation system determines a driving path to control the AV in a roadway that includes a position of features (e.g., a portion of the feature, a section of the feature) in the roadway, while road edges and control measures may remain unchanged. As an example, the map generation system determines a driving path including feature information associated with lateral regions, for example, by determining the features of the roadway in the lateral regions. The map generation system may determine

21

an entry point and end point of the driving path that is associated with entry information and/or end (e.g., exit) information for traversing the driving path, the entry and/or end information comprising at least one of heading information, curvature information, and acceleration information of the driving path.

The map generation system may determine a driving path in a lane in the geographic location that includes a first trajectory (e.g., a spline, a polyline, etc.); as an example, the map generation system may determine a single trajectory for a driving path in the roadway and/or a plurality of trajectories (e.g., a spline, a polyline, etc.) for a driving path in the roadway. As an example, the map generation system determines at least one trajectory of a driving path based on features in the roadway and/or traversals of the roadway by one or more vehicles (e.g., straightaways where paint lines are present, straight through intersections, straightaways where paint lines are not present, placement informed by average vehicle paths data, etc.) and/or the like. The map generation system may determine a trajectory for a driving path based on information obtained from a vehicle (e.g., autonomous vehicles, non-autonomous vehicles, etc.) representing a path in the roadway. For example, the map generation system may obtain information for determining a driving path based on one or more trajectories of the roadway associated with one or more traversals of the roadway by one or more vehicles (e.g., autonomous vehicles, non-autonomous vehicles, etc.), a number of traversals of the roadway by one or more vehicles, a position of the vehicle associated with one or more traversals, interventions associated with one or more traversals of the roadway by one or more vehicles, a number of objects (e.g., a number of hazards, a number of bicycles, a railway track in proximity to the roadway, etc.) associated with one or more traversals of the roadway by one or more vehicles, a distance and/or position (e.g., a vehicle pose, an average distance to a vehicle pose, a mileage, etc.) associated with one or more traversals of the roadway by one or more vehicles (e.g., a distance until a detection of an event, a distance until detection of a potentially harmful or a harmful event to an AV, to a rider of the AV, to a pedestrian, a distance between a first detection of an event and a second detection of an event, miles per event, etc.), one or more traffic controls of the roadway associated with one or more traversals of the roadway by one or more AVs, one or more aspects of the roadway (e.g., a dimension of one or more lanes of the roadway, a width of one or more lanes of the roadway, a number of bicycle lanes of the roadway, etc.) associated with one or more traversals of the roadway by one or more AVs, a speed of one or more AVs associated with one or more traversals of the roadway by the one or more AVs, and/or the like.

The map generation system may determine a single trajectory for at least one lane in the roadway and/or a driving path based on information including LIDAR point cloud maps (e.g., map point data, etc.) associated with a geographic location (e.g., a location in three-dimensional space relative to the LIDAR system of a mapping vehicle) of a number of points (e.g., a point cloud) that correspond to objects that have reflected a ranging laser of one or more mapping vehicles at the geographic location. As an example, a map can include a LIDAR point cloud layer that represents objects and distances between objects in the geographic location of the map.

The map generation system may include a driving path that includes a primary path in the driving path, the primary path including a first trajectory of the driving path. For

22

example, map generation system may determine a primary path in the driving path by identifying that the primary path satisfies a threshold indicating a driving path for controlling the AV in an autonomous mode. For example, the primary path may be based on information indicating a path for an AV to autonomously follow. The map generation system may determine a secondary path in the driving path. For example, the map generation system may determine a secondary path identifying a trajectory in the driving path that may not satisfy a threshold indicating a driving path for controlling the AV to traverse the path autonomously (lanes where a driving path does not need to be clearly defined, turning lanes in intersections, defined turns in intersections, diverging/converging lanes, etc.).

For example, the map generation system may determine a secondary driving path that AV cannot operate on (e.g., drive) under the fully-autonomous mode. For example, map generation system may determine the secondary path in the driving path as an estimate of where an AV may drive. The proposal of a primary path or secondary path may be dependent on a safety factor, and therefore the safety determination is not limited to autonomous modes only, and rather may also predict manual or semi-automated safety parameters.

The map generation system may determine a driving path linking a first and a second driving path (e.g., a primary path to a primary path, a primary path to a secondary path, a secondary path to a primary path, etc.). For example, the first trajectory and second trajectory in the primary path each include an end point that is linked (e.g., logically connected) by the map generation system. The map generation system may determine a link for the first trajectory based on attributes of the point (e.g., an entry point of the trajectory, an end point of the trajectory), for example a position of a point, a heading of the trajectory at a point, an acceleration at a point (e.g., an entry point of the trajectory, an end point of the trajectory), and/or a curvature at a point (e.g., an entry point of the trajectory, an end point of the trajectory), and/or the like. For example, map generation system may determine a driving path that includes a first trajectory in a primary path linked to a second trajectory in a primary path, as a predecessor driving path (e.g., trajectory) to a successor driving path (e.g., trajectory), the link having continuity to generate the logical connection between the primary and secondary lane, in this way, providing continuity for one or more of a position of the endpoint, a heading of the trajectory at the end point, an acceleration at the end point, and a curvature at the end point. The map generation system may determine a link (e.g., logical connection) including continuity of a heading and/or a curvature associated with an entry point of the secondary path in the driving path for the heading and curvature associated with an end point of the primary path. In another example, the map generation system may determine a link (e.g., logical connection) that includes continuity of a heading and/or a curvature associated with an entry point of the primary path in the driving path to the heading and curvature associated with an end point of the secondary path. The map generation system may determine a primary driving path to include not more than one predecessor primary driving path linked to one successor primary driving path. The map generation system may determine continuity to provide a transition between a first driving path and a second driving path. The map generation system may determine a link between a first point and a second point, based on one or more attributes, for example, to provide logical connections to enhance the transition (e.g., smooth) across the link.

US 12,384,410 B2

23

See, US 20200401145. See also, U.S. Pat. Nos. 4,296, 901; 4,833,469; 4,940,925; 5,281,901; 5,341,130; 5,375, 059; 5,390,125; 5,402,355; 5,438,517; 5,548,516; 5,610, 815; 5,612,883; 5,629,855; 5,640,323; 5,646,843; 5,650, 703; 5,657,226; 5,680,306; 5,684,696; 5,747,683; 5,838, 562; 5,938,710; 5,995,882; 6,069,420; 6,122,572; 6,151, 539; 6,269,763; 6,351,697; 6,393,362; 6,442,456; 6,799, 100; 6,804,607; 7,047,888; 7,302,316; 7,335,067; 7,343, 232; 7,494,090; 7,496,226; 7,542,828; 7,591,630; 7,693, 624; 7,737,878; 7,844,396; 7,911,400; 7,949,541; 7,979, 172; 7,979,173; 7,991,505; 8,060,271; 8,068,949; 8,103, 398; 8,109,223; 8,126,642; 8,255,092; 8,280,623; 8,301, 326; 8,355,834; 8,364,334; 8,412,449; 8,437,875; 8,437, 890; 8,442,713; 8,577,538; 8,583,313; 8,606,589; 8,612, 084; 8,706,394; 8,744,648; 8,751,143; 8,755,997; 8,755, 999; 8,768,555; 8,784,034; 8,798,828; 8,843,244; 8,880, 287; 8,935,071; 8,947,531; 8,948,955; 8,954,194; 8,988, 524; 9,097,800; 9,120,484; 9,120,485; 9,139,363; 9,140, 814; 9,199,667; 9,201,421; 9,201,424; 9,202,382; 9,208, 456; 9,223,025; 9,234,618; 9,261,590; 9,265,187; 9,288, 938; 9,298,186; 9,327,734; 9,349,055; 9,373,149; 9,373, 262; 9,383,752; 9,383,753; 9,384,666; 9,392,743; 9,423, 498; 9,432,929; 9,434,309; 9,435,652; 9,451,020; 9,494, 439; 9,494,940; 9,494,943; 9,507,346; 9,508,260; 9,510, 316; 9,513,632; 9,517,767; 9,523,984; 9,523,986; 9,535, 423; 9,536,427; 9,545,995; 9,547,309; 9,547,986; 9,547, 989; 9,557,736; 9,559,804; 9,561,941; 9,563,199; 9,581, 460; 9,598,239; 9,599,989; 9,603,158; 9,606,539; 9,612, 123; 9,630,619; 9,632,502; 9,645,578; 9,669,904; 9,672, 446; 9,674,759; 9,679,191; 9,679,206; 9,688,396; 9,693, 297; 9,702,098; 9,702,443; 9,707,966; 9,710,710; 9,718, 471; 9,720,412; 9,720,415; 9,721,397; 9,733,378; 9,734, 455; 9,739,881; 9,740,205; 9,746,444; 9,754,490; 9,760, 092; 9,761,136; 9,766,333; 9,783,075; 9,783,262; 9,788, 282; 9,798,329; 9,802,661; 9,802,759; 9,804,594; 9,804, 599; 9,804,601; 9,805,605; 9,821,801; 9,821,807; 9,833, 901; 9,834,224; 9,836,973; 9,857,795; 9,857,798; 9,862, 391; 9,864,378; 9,868,332; 9,874,871; 9,878,664; 9,884, 630; 9,891,333; 9,896,100; 9,898,005; 9,902,396; 9,904, 286; 9,910,434; 9,910,441; 9,911,030; 9,913,240; 9,915, 950; 9,916,538; 9,916,703; 9,921,065; 9,933,779; 9,939, 817; 9,940,651; 9,944,291; 9,946,531; 9,946,890; 9,947, 224; 9,948,917; 9,949,228; 9,950,568; 9,955,436; 9,958, 379; 9,958,864; 9,958,875; 9,959,754; 9,963,143; 9,964, 952; 9,964,954; 9,967,815; 9,969,285; 9,969,326; 9,969, 481; 9,977,430; 9,981,669; 9,983,305; 9,988,055; 9,989, 645; 10000124; 10000338; 10007264; 10007271; 10012981; 10012990; 10019002; 10019008; 10019011; 10030418; 10031521; 10031526; 10037553; 10040632; 10048683; 10049328; 10053091; 10054945; 10055653; 10061313; 10061325; 10065638; 10065654; 10073456; 10073462; 10074223; 10083604; 10086782; 10089116; 10095236; 10096067; 10109195; 10118577; 10118639; 10122736; 10123473; 10126136; 10126742; 10126749; 10127465; 10127818; 10133275; 10134278; 10137896; 10137903; 10139237; 10139818; 10139823; 10139828; 10140468; 10143040; 10152891; 10156845; 10156848; 10156849; 10156850; 10157423; 10160378; 10160457; 10160484; 10162354; 10163139; 10166994; 10168703; 10171967; 10173679; 10179700; 10187751; 10188024; 10191493; 10197407; 10198619; 10202117; 10203697; 10205457; 10209715; 10214240; 10216196; 10220705; 10220857; 10222211; 10222462; 10222798; 10223479; 10223916; 10225348; 10227075; 10228690; 10229590; 10233021; 10234863; 10235881; 10241509; 10241516; 10243604; 10245993; 10246097; 10248119; 10248120; 10248124; 10249109; 10253468; 10254763; 10256890;

24

10259514; 10260898; 10261514; 10262217; 10266180; 10267634; 10267635; 10268200; 10272778; 10272924; 10284777; 10288439; 10289110; 10293932; 10295363; 10296003; 10296004; 10298910; 10303171; 10303174; 10303182; 10303183; 10303959; 10308430; 10309777; 10309778; 10309792; 10310499; 10310500; 10310514; 10310515; 10310517; 10311731; 10317231; 10317899; 10317911; 10317912; 10317913; 10319224; 10324463; 10327160; 10331127; 10331133; 10331136; 10331138; 10331141; 10332320; 10334050; 10336321; 10338594; 10342067; 10343559; 10343685; 10343698; 10345808; 10345809; 10345810; 10349011; 10351261; 10353390; 10353393; 10353694; 10353931; 10354157; 10358147; 10359783; 10360021; 10364027; 10365654; 10365657; 10369974; 10372129; 10372130; 10372141; 10373097; 10379538; 10380890; 10386192; 10386856; 10388155; 10388162; 10392025; 10394245; 10395285; 10395332; 10397019; 10399458; 10401852; 10401867; 10405215; 10407076; 10409279; 10410250; 10410747; 10416670; 10416671; 10416677; 10421460; 10421463; 10423162; 10429194; 10429849; 10430653; 10431018; 10433243; 10435015; 10435242; 10436595; 10436885; 10437247; 10437256; 10438493; 10440547; 10444759; 10446031; 10446037; 10449957; 10451514; 10452065; 10452070; 10459441; 10459444; 10466712; 10467581; 10467915; 10469282; 10469753; 10471976; 10473780; 10474149; 10474157; 10474159; 10474160; 10474161; 10474164; 10474916; 10477449; 10489529; 10489686; 10490068; 10493622; 10493936; 10496098; 10496099; 10496766; 10498600; 10501014; 10503165; 10503172; 10504306; 10506509; 10507787; 10508986; 10509947; 10513161; 10514690; 10514692; 10514700; 10514709; 10518770; 10520319; 10527417; 10527450; 10527720; 10527734; 10528048; 10528059; 10528836; 10529027; 10531004; 10532885; 10534364; 10536497; 10543838; 10543844; 10545024; 10545029; 10545507; 10546560; 10549752; 10554527; 10554901; 10558222; 10558864; 10562538; 10563993; 10564643; 10567650; 10569651; 10569663; 10569773; 10571916; 10571922; 10572514; 10572717; 10573178; 10576966; 10576991; 10579054; 10579065; 10579070; 10584971; 10586458; 10591608; 10591910; 10591912; 10593042; 10595175; 10598489; 10599141; 10599546; 10606270; 10606274; 10606278; 10606786; 10607293; 10611384; 10611389; 10613489; 10613547; 10613550; 10618519; 10621860; 10627810; 10627830; 10629080; 10635108; 10635109; 10636297; 10642275; 10645848; 10647250; 10647333; 10649453; 10649458; 10649462; 10649469; 10654476; 10656657; 10659975; 10664918; 10668925; 10670411; 10670416; 10671075; 10671076; 10671077; 10671082; 10671961; 10674332; 10678234; 10678253; 10679497; 10683012; 10685244; 10685403; 10691126; 10691127; 10691130; 10691138; 10692371; 10698407; 10698409; 10698414; 10699579; 10705220; 10705525; 10705534; 10705536; 10705539; 10708823; 10710592; 10710633; 10712745; 10712746; 10712750; 10719886; 10720059; 10725469; 10726379; 10726498; 10726499; 10730365; 10730531; 10732639; 10732645; 10733673; 10733761; 10735518; 10739768; 10739774; 10739775; 10739776; 10739780; 10740850; 10740988; 10743159; 10745003; 10745011; 10747234; 10747597; 10748218; 10753754; 10753758; 10754341; 10754348; 10755581; 10756909; 10761542; 10762396; 10768620; 10768621; 10768626; 10769947; 10773597; 10775184; 10775488; 10775790; 10775792; 10775801; 10780880; 10782687; 10782693; 10782694; 10782699; 10782703; 10788839; 10788841; 10795360; 10795367; 10795375; 10796174; 10796204; 10796402; 10796562;

US 12,384,410 B2

25

10800606; 10801845; 10802477; 10803325; 10807599;
10809081; 10809722; 10809726; 10809736; 10810872;
10812996; 10813074; 10814882; 10816346; 10816984;
10816995; 10818035; 10818105; 10818187; 10821971;
10823575; 10824144; 10824145; 10824153; 10824170;
10824415; 10828999; 10829063; 10829149; 10831188;
10831191; 10831196; 10831202; 10831204; 10831210;
10831212; 10832066; 10832502; 10836395; 10836405;
10837788; 10838426; 10839234; 10839340; 10839426;
10839473; 10841496; 10843722; 10845816; 10845820;
10852721; 10855922; 10857896; 10857994; 10859395;
10860022; 10860036; 10864920; 10866108; 10867188;
10870368; 10870437; 10872476; 10882535; 10883843;
10884422; 10885727; 10886023; 10887431; 10890912;
10891138; 10891694; 10897575; 10906558; 10908613;
10909377; 10915106; 10915116; 10915965; 10916077;
10916142; 10921135; 10921811; 10921812; 10921825;
10922556; 10928207; 10928523; 10928820; 10928829;
10932156; 20010021888; 20020143461; 20040035315;
20080027591; 20080027599; 20080059015; 20080093498;
20080161986; 20080161987; 20090306881; 20100030473;
20100076631; 20100106344; 20100106356; 20100114416;
20110153136; 20110153338; 20110288714; 20110295423;
20110295424; 20120044043; 20120046818; 20120046927;
20120046983; 20120053703; 20120053775; 20120083947;
20120095651; 20120101680; 20120166019; 20120283906;
20120316725; 20130274986; 20130321627; 20140032017;
20140067188; 20140136414; 20140195095; 20140201126;
20140214259; 20140253722; 20150081156; 20150092178;
20150153175; 20150154557; 20150177736; 20150229906;
20150298786; 20150350914; 20160011318; 20160021178;
20160036558; 20160231746; 20160236617; 20160273922;
20160280238; 20160313739; 20160320773; 20160334229;
20160334230; 20160334797; 20160339587; 20160375976;
20170003681; 20170015405; 20170017236; 20170060129;
20170083957; 20170090480; 20170120814; 20170120902;
20170123419; 20170123421; 20170123422; 20170123428;
20170123429; 20170124476; 20170124781; 20170126810;
20170132334; 20170132934; 20170136842; 20170139411;
20170160742; 20170164423; 20170166215; 20170227965;
20170235316; 20170248963; 20170248964; 20170277186;
20170284819; 20170285642; 20170294130; 20170315229;
20170316333; 20170323179; 20170329346; 20170341236;
20170351261; 20170353943; 20170371355; 20180009445;
20180011494; 20180017968; 20180023960; 20180024553;
20180024562; 20180024565; 20180024568; 20180032082;
20180033310; 20180039287; 20180045832; 20180047292;
20180050704; 20180059672; 20180061242; 20180086344;
20180086351; 20180088576; 20180088582; 20180088590;
20180093671; 20180095467; 20180107942; 20180111612;
20180114258; 20180114259; 20180127000; 20180127001;
20180129215; 20180136643; 20180136644; 20180136651;
20180141564; 20180143622; 20180143632; 20180143639;
20180143644; 20180143647; 20180143649; 20180150086;
20180154829; 20180162186; 20180162412; 20180164822;
20180164827; 20180170392; 20180170395; 20180172821;
20180173240; 20180178791; 20180183873; 20180186378;
20180186403; 20180188026; 20180188027; 20180188037;
20180188039; 20180188040; 20180188041; 20180188042;
20180188043; 20180188044; 20180188059; 20180188060;
20180188727; 20180188734; 20180188742; 20180188743;
20180189323; 20180189578; 20180189717; 20180190046;
20180196433; 20180196439; 20180196440; 20180201182;
20180203443; 20180203450; 20180204111; 20180204141;
20180208215; 20180211534; 20180216942; 20180217614;
20180224869; 20180225968; 20180233047; 20180238698;
20180247160; 20180253647; 20180257660; 20180259956;

26

20180259958; 20180267537; 20180275678; 20180282955;
20180284774; 20180292222; 20180292825; 20180292831;
20180297606; 20180300964; 20180304889; 20180304900;
20180307229; 20180307239; 20180307240; 20180307245;
20180312238; 20180314266; 20180321685; 20180322546;
20180327091; 20180329411; 20180330173; 20180334166;
20180335781; 20180336421; 20180341274; 20180342157;
20180348775; 20180349713; 20180349802; 20180356821;
20180356823; 20180364657; 20180364700; 20180364701;
20180364702; 20180364703; 20180364704; 20180365908;
20180370540; 20180373245; 20180373268; 20180374359;
20180375939; 20180376357; 20190004510; 20190004516;
20190004522; 20190004524; 20190004533; 20190004534;
20190004535; 20190018411; 20190018412; 20190025843;
20190035275; 20190039609; 20190049342; 20190049946;
20190050729; 20190056737; 20190056742; 20190061765;
20190066409; 20190066506; 20190068434; 20190071091;
20190071092; 20190071093; 20190072965; 20190072966;
20190072973; 20190072979; 20190078896; 20190079524;
20190080602; 20190084571; 20190086924; 20190094868;
20190105968; 20190107840; 20190113351; 20190120640;
20190120946; 20190120947; 20190120948; 20190122037;
20190122386; 20190129831; 20190130878; 20190134821;
20190137991; 20190138008; 20190146508; 20190146509;
20190147253; 20190147254; 20190147255; 20190156134;
20190156150; 20190156679; 20190161080; 20190163191;
20190168769; 20190171912; 20190174276; 20190176684;
20190179311; 20190179979; 20190185018; 20190186939;
20190187715; 20190187723; 20190195998; 20190196471;
20190202561; 20190204092; 20190204425; 20190204427;
20190204842; 20190204843; 20190212161; 20190212744;
20190212754; 20190220011; 20190220015; 20190220016;
20190227550; 20190227553; 20190235488; 20190235499;
20190235532; 20190243370; 20190248487; 20190250000;
20190250609; 20190250636; 20190250640; 20190258246;
20190258251; 20190265703; 20190266179; 20190266420;
20190270408; 20190271549; 20190277632; 20190278277;
20190278284; 20190278290; 20190286143; 20190286155;
20190291728; 20190295421; 20190302768; 20190310627;
20190310636; 20190310650; 20190310654; 20190315232;
20190315357; 20190317455; 20190317507; 20190317508;
20190317512; 20190317513; 20190317515; 20190317520;
20190318550; 20190324456; 20190324463; 20190325223;
20190325546; 20190329903; 20190332123; 20190332875;
20190333120; 20190346851; 20190349794; 20190359202;
20190361432; 20190361444; 20190367019; 20190367020;
20190367021; 20190367022; 20190368882; 20190369616;
20190369626; 20190371174; 20190377345; 20190377349;
20190377351; 20190378423; 20190382007; 20190382031;
20190383945; 20190384301; 20190384304; 20190385450;
20190387060; 20190391585; 20200001862; 20200001863;
20200003564; 20200004241; 20200004261; 20200013225;
20200014759; 20200019165; 20200019175; 20200019801;
20200021728; 20200023838; 20200026276; 20200026283;
20200026285; 20200026294; 20200027354; 20200031340;
20200033147; 20200033872; 20200041296; 20200042007;
20200043326; 20200050195; 20200050199; 20200051346;
20200055362; 20200064483; 20200064842; 20200064851;
20200064859; 20200064861; 20200073385; 20200074024;
20200082180; 20200089243; 20200089245; 20200101974;
20200108785; 20200111169; 20200116497; 20200116867;
20200117207; 20200120253; 20200122721; 20200122830;
20200124719; 20200125094; 20200125102; 20200130864;
20200133270; 20200134525; 20200137928; 20200139973;
20200142405; 20200142428; 20200145569; 20200149231;
20200149906; 20200150682; 20200159216; 20200159225;
20200160067; 20200172115; 20200172116; 20200174472;

20200174486; 20200175691; 20200175695; 20200180740;
 20200182639; 20200182640; 20200183395; 20200191601;
 20200192372; 20200192373; 20200192374; 20200192375;
 20200192376; 20200192377; 20200192378; 20200192379;
 20200192380; 20200192381; 20200192402; 20200193606;
 20200201329; 20200201350; 20200207360; 20200207369;
 20200207371; 20200207375; 20200209853; 20200209857;
 20200209872; 20200225032; 20200225673; 20200231106;
 20200231142; 20200233415; 20200233418; 20200233420;
 20200233429; 20200240799; 20200240805; 20200241546;
 20200249677; 20200250067; 20200250981; 20200262263;
 20200265249; 20200272148; 20200282907; 20200282987;
 20200284581; 20200285240; 20200285658; 20200290647;
 20200298863; 20200301435; 20200310417; 20200310442;
 20200327234; 20200331480; 20200333470; 20200333785;
 20200341469; 20200341487; 20200341490; 20200342693;
 20200346637; 20200348668; 20200348676; 20200348684;
 20200349848; 20200356090; 20200356100; 20200356849;
 20200363813; 20200371533; 20200379457; 20200379462;
 20200379474; 20200383580; 20200387155; 20200388154;
 20200393261; 20200393837; 20200394474; 20200402323;
 20200406893; 20200408921; 20200409351; 20200409377;
 20200409386; 20200410252; 20200410255; 20200410703;
 20210004012; 20210009163; 20210009166; 20210018916;
 20210018917; 20210018918; 20210024100; 20210024144;
 20210026348; 20210026355; 20210031760; 20210031801;
 20210033410; 20210034068; 20210034412; 20210035442;
 20210035450; 20210039669; 20210039682; 20210039779;
 20210041882; 20210042575; 20210046861; 20210046946;
 20210048304; 20210048991; 20210049243; 20210049415;
 20210049903; and 20210053407.

It is an object to provide a method of operating a vehicle, comprising: planning motion of the vehicle, comprising computing motion trajectories of an action to incrementally advance the vehicle toward a goal with an associated incremental utility, based on at least a safety with respect to an environment of operation of the computed motion trajectories; and planning the task for the vehicle, comprising defining the goal and a sequence of the actions to advance the vehicle toward the goal, selectively dependent an optimization of an aggregate prospective utility of the task and the safety of the motion trajectories to advance the vehicle toward the goal.

It is also an object to provide a non-transitory computer readable medium containing a program for operating a vehicle, comprising: instructions for planning motion of the vehicle, comprising computing motion trajectories of an action to incrementally advance the vehicle toward a goal with an associated incremental utility, based on at least a safety with respect to an environment of operation of the computed motion trajectories; and instructions for planning the task for the vehicle, comprising defining the goal and a sequence of the actions to advance the vehicle toward the goal, selectively dependent an optimization of an aggregate prospective utility of the task and the safety of the motion trajectories to advance the vehicle toward the goal.

It is another object to provide a system for operating a vehicle, comprising: a sensor configured to receive information about an environment of operation of the vehicle; at least one automated processor; a motion planner configured to plan a motion of the vehicle, configured to compute motion trajectories with the at least one automated processor, an action to incrementally advance the vehicle toward a goal with an associated incremental utility, based on at least a safety of the motion trajectories with respect to an environment of operation of the vehicle; and a task planner configured to plan the task for the vehicle with the at least

one automated processor, comprising defining the goal and a sequence of the actions to advance the vehicle toward the goal, selectively dependent an optimization of an aggregate prospective utility of the task and the safety of the motion trajectories to advance the vehicle toward the goal.

It is a further object to provide a method of operating an autonomous vehicle, comprising: determining a safety of motion of the autonomous vehicle in an environment dependent on real-time conditions of operation; planning a route for the autonomous vehicle selectively dependent on the determined safety of motion of the autonomous vehicle in the environment and optimization of a utility of the planned route; planning the motion of the autonomous vehicle according to the planned route, comprising selecting motion options consistent with the planned route that are safe with respect to the environment dependent on real-time conditions of operation, wherein the planned route is responsive to the planned motion; and controlling the autonomous vehicle according to the planned route and planned motion.

A further object provides a method of controlling an autonomous vehicle, comprising: receiving data relating to a relationship of the autonomous vehicle with respect to the environment; determining a motion and environment-dependent safety of the autonomous vehicle within an environment of operation; continuously planning a utility-optimized route for an autonomous vehicle along a path having execution options within the route, updated dependent on the determined motion and environment-dependent safety of the autonomous vehicle; continuously planning the motion of the autonomous vehicle according to the planned utility-optimized route, comprising selection of the execution options which alter a relation of the autonomous vehicle with the environment, that meet at least one safety criterion with respect to the determined a motion and environment-dependent safety; and controlling the autonomous vehicle according to the planned utility-optimized route and planned motion, to thereby achieve safe and efficient travel of the autonomous vehicle.

Another object provides a method of operating a vehicle, comprising: planning a task for the vehicle, comprising a safe sequence of actions to accomplish goals which optimize the task; and planning motion of the vehicle, comprising computing motion trajectories that connect a current location with a goal location, based on at least safety with respect to surrounding vehicles.

It is an object of the invention to provide a method of operating a vehicle, comprising: planning motion of the vehicle, comprising computing motion trajectories that connect a current location with a goal location determined according to a planned task, based on a utility optimization of vehicle motion based on at least safety with respect to an environment of operation; and planning the task for the vehicle, comprising a sequence of actions to accomplish goals, selectively dependent on at least the safety.

It is an object to provide a non-transitory computer readable medium containing a program for operating a vehicle, comprising: instructions for planning motion of the vehicle, comprising computing motion trajectories that connect a current location with a goal location according to a planned task, based on a utility optimization of vehicle motion based on at least safety with respect to an environment of operation; and instructions for planning the task for the vehicle, comprising a sequence of actions to accomplish goals, selectively dependent in at least the safety.

It is a further object to provide a system for operating a vehicle, comprising: a motion planner configured to plan a motion of the vehicle, according to computed motion tra-

jectories that connect a current location with a goal location, based on a utility optimization of vehicle motion based on at least safety with respect to an environment of operation; and a task planner configured to plan the task for the vehicle, to define a sequence of actions to accomplish goals selectively dependent on at least the safety.

It is a still further object to provide a method of operating an autonomous vehicle, comprising: determining a safety of operation of the autonomous vehicle in an environment dependent on real-time conditions of operation; planning a route for the autonomous vehicle selectively dependent on the determined safety of operation in the environment; planning motion of the autonomous vehicle according to the planned route, comprising selection of options consistent with the route that optimize a utility function and a safety with respect to the environment selectively dependent on the determined safety of operation in the environment, wherein the planned route is responsive to the planned motion; and controlling the autonomous vehicle according to the planned route and planned motion.

The selected options may be responsive to a cost of a maneuver, a benefit of the maneuver, and a determined safety of the maneuver.

The method may further comprise updating the planning of the route based on the planned motion in real time.

The safety of operation may be determined statistically based on a predicted risk.

The safety of operation may be determined based on a risk of collision.

It is another object to provide a method of controlling an autonomous vehicle, comprising: receiving data relating to a relationship of the autonomous vehicle with respect to the environment; determining a motion and environment-dependent safety of the autonomous vehicle within an environment of operation; continuously planning a route for an autonomous vehicle along a path having execution options within the route, updated dependent on the determined motion and environment-dependent safety of the autonomous vehicle; continuously planning motion of the autonomous vehicle according to the planned route, comprising selection of the execution options which alter a relation of the autonomous vehicle with the environment, that meet at least one utility criterion and at least one safety criterion; and controlling the autonomous vehicle according to the planned route and planned motion, to thereby achieve safe and efficient travel of the autonomous vehicle.

The safety may be determined based on various sensors, such as radar, lidar, video cameras, sonar, inertial sensors, OBD-II data stream (see, en.wikipedia.org/wiki/On-board_diagnostics, CANbus, ISO 15765-4), weather sensors, on-line social network database, real time traffic information database, and/or based on intervehicle communications, for example.

Where explicit intervehicle communications are supported, the task plan, the motion plan, or both may be coordinated between vehicles, either in a centralized or decentralized manner, using vehicle-to-vehicle communications. Further, sensor data may be relayed between vehicles to provide advance warning, especially to the task planner, though in some cases, short latency warnings and environmental conditions may have direct impact on the motion planning.

The environmental conditions may be local vehicular motion of another vehicle, weather conditions (rain, puddles, sun glare, black ice, snow, freezing conditions, tornado warning, hail, etc.), traffic, history of incidents (e.g., accidents, emergency maneuvers, law enforcement) at a

location, obstacles and hazards at a location (e.g., detours, potholes, obstructed vision, pedestrians and cyclists, animals, children playing), etc.

In a typical case, the autonomous vehicle in a lane catches up to another vehicle travelling slower in the same lane. The motion planner considers the option of switching lanes, which may reduce overall travel time (i.e., increase efficiency), but may also lead to other obstructions in the lane, and incurs a collision risk dependent on other vehicles surrounding the autonomous vehicle. Therefore, both the incremental maneuver by the motion planner of changing lanes, and the larger plan of increasing efficiency according to a cost function or utility function, are each dependent on the safety of the autonomous vehicle. The motion planner is principally concerned with the safety of the autonomous vehicle during the maneuver, while the task planner is concerned with the change in safety before and after the maneuver, as well as the predicted safety during the maneuver and predicted safety after the maneuver. The task planner may, for example, consider distance and time, two likely important (but non-exclusive) determinates of utility, which in some cases could lead to a selection of a completely different route. Other utility issues are fuel consumption, fuel availability, tolls, availability of services such as food and lodging for extended trips with human passengers, and the like.

The planning of the task may comprise specifying a task planning domain by D' , including a set of states, S , and a set of actions, A ; providing a factored state space such that each state $s \in S$ is defined by values of a fixed set of variables, and each action $a \in A$ is defined by its preconditions and effects; and defining a utility function which maps a state transition to a real number, which takes both a cost function $\text{Cost}(s, a, s')$ and a safety function $\text{Safe}(s, a, s')$ of conducting action a in state s into account.

The method may further comprise computing a plan $p \in P$, given domain D' and a task planning problem, is computed, starting from an initial state $s^{\text{init}} \in S$ and finishing in a goal state $s^g \in S$; representing a plan p , consisting of a sequence of transitions represented as $p = \langle s_0, a_0, \dots, s_{N-1}, a_{N-1}, s_N \rangle$, where $s_0 = s^{\text{init}}$, $s_N = s^g$ and P denotes a set of satisfactory plans; and producing an optimal plan p^* with a task planner P' among all the satisfactory plans, where γ is a constant coefficient and $\gamma > 0$,

$$p^* = \underset{p \in P}{\operatorname{argmin}} \sum_{(s, a, s') \in p} \left[\text{Cost}(\langle s, a, s' \rangle) + \frac{\gamma}{1 + e^{\text{Safe}(\langle s, a, s' \rangle) - 1}} \right].$$

The method may further comprise conducting a search directly in a two-dimensional Cartesian space such that a position and an orientation of the vehicle is uniquely represented as a pose, denoted by x and constrained by the urban road network, wherein some parts of the space are designated as free space, and remaining parts are designated as obstacles, and a motion planning domain is specified by D'' , wherein given domain D'' , a motion planning problem is specified by an initial pose x^i and a goal pose x^g .

The method may further comprise planning the motion by a motion planner P'' consisting of a path planner and a tracking planner into two phases, wherein: in a first phase, the path planner computes a collision-free trajectory ξ connecting pose x^i and pose x^g taking into account any motion constraints on the part of the vehicle with a minimal trajectory length; and in a second phase, computing control

31

signals with a tracking controller to drive the vehicle to follow the computed trajectory.

The method may further comprise mapping a systolic state s with a state mapping function, $f: X=f(s)$, into a set of feasible poses X in a continuous space as available options for the motion planner, wherein availability of at least one pose $x \in X$ is assumed in each state s , such that the vehicle is in a free space of D^m , and if it is not in a free space of D^m , the state s is declared infeasible.

The method may further comprise computing a safety level, $\text{Safe}(\langle s, a, s' \rangle)$, of a motion-level implementation of a symbolic action $\langle s, a, s' \rangle$, wherein the safety level enables the task planner to incorporate a road condition into a process of sequencing high-level actions toward accomplishing complex driving tasks.

The method may further comprise computing a sequence of continuous control signals to perform symbolic action $\langle s, a, s' \rangle$, comprising an acceleration $\delta \in \Delta$ and steering angle $\theta \in \Theta$, to drive the vehicle following a trajectory, while ensuring no collision on the road, wherein sets Δ and Θ denote an operation specification of the tracking controller.

$U_s(t) \subset \Delta \times \Theta$ may specify a safe control set at time t , in which all elements, denoted by $u(t) = \langle \delta, \theta \rangle$, are safe for the vehicle to perform at time t , such that a probability of elements sampled from set $\Delta \times \Theta$ being located in the safe set U_s represents the safety value of action $\langle s, a, s' \rangle$.

The method may further comprise:

receiving an input which includes a symbolic action $\langle s, a, s' \rangle$, stating mapping function f , motion planner P^m consisting of path planner and tracking controller, and a tracking controller's operation specification sets Δ and Θ ;

obtaining short-period trajectories of the vehicle and surrounding vehicles, where $V_i, i \in [1, \dots, N]$, is the i th vehicle within a sensing range of the vehicle;

iteratively:

computing a safety estimation between the vehicle and the surrounding vehicles V_i , where $i \in [1, \dots, N]$, given that the vehicle is performing action $\langle s, a, s' \rangle$, at a motion level;

computing a safe control set $U_i^s(t)$ that includes all safe control signals with regard to the vehicle V_i at time t ;

randomly sampling M elements from the set $\Delta \times \Theta$, and computing a probability $o_i(t)$ of the sampled elements falling in set $U_i^s(t)$;

converting a list of values of safety estimation $\{o_i(t)\}$ into a single value o^*_i according to

$$o^*_i = \frac{\max_{t \in T} \{o_i(t)\} + \text{mean}_{t \in T} \{o_i(t)\}}{2};$$

and

selecting a minimum value $o^*, i \in [1, \dots, N]$, as an overall safety value, where $T = t_1 + \omega \times i$,

$$0 \leq i \leq \frac{(t_2 - t_1)}{\omega};$$

and

producing an output of an estimated safety value $\text{Safe}(\langle s, a, s' \rangle) \in [0.0, 1.0]$.

32

The method may further comprise:

receiving inputs: Symbolic action $\langle s, a, s' \rangle$, state mapping function f , motion planner P^m , control operation sets Δ and Θ ;

sampling initial and goal poses, $x \leftarrow f(s)$ and $x' \leftarrow f(s')$, given action $\langle s, a, s' \rangle$, and f ;

computing a collision-free trajectory, ξ^E , using P^m , where $\xi^E(t_1) = x, \xi(t_2) = x'$; and $[t_1, t_2]$ is the horizon;

predicting a trajectory ξ_i^s for an i th surrounding vehicle V_i , where $i \in [1, \dots, N]$, and $[t_1, t_2]$ is the horizon;

for each surrounding vehicle V_i :

computing a safe control set $U_i^s(t)$ between the vehicle and vehicle V_i at time $t \in [t_1, t_2]$, where $U_i^s(t) \subset \Delta \times \Theta$ and

$$t = t_1 + \omega \times i, i \leq \frac{(t_2 - t_1)}{\omega};$$

sampling M elements $\langle \delta, \theta \rangle$ randomly from set $\Delta \times \Theta$ and computing a probability $o_i(t)$ of the elements falling in set $U_i^s(t)$;

converting a list of estimated safety values, $\{o_i(t)\}$, into a scalar value o^*_i using

$$o^*_i = \frac{\max_{t \in T} \{o_i(t)\} + \text{mean}_{t \in T} \{o_i(t)\}}{2};$$

and

selecting a minimum value, $o^*, i \in [1, \dots, N]$, as a safety value.

A motion planner P^m may compute both costs and safety values of the vehicle's navigation actions; s^{init} may represent an initial state of the vehicle, and the goal of the task is specified using s^g ; a task planner P^t may compute a sequence of symbolic actions, employing a cost function Cost , and a safety estimation function Safe ; a motion planner P^m may be used for computing motion trajectories, and generating control signals to move the vehicle; and a state mapping function f used for mapping symbolic states to 2D coordinates in continuous spaces.

The method may further comprise: initializing a cost function and a safety estimation function; computing an optimal task plan, $p^* = \langle s^{init}, a_0, s_1, \dots, s^g \rangle$ wherein s^{init} and s^g correspond to initial and goal poses respectively; estimating a safety level, μ , of action $\langle s, a, s' \rangle$; updating the safety estimation function using u and the cost function using p^* ; and computing a new optimal plan p' .

A motion planner may compute and execute a desired control signal $\langle \delta, \theta \rangle$ repeatedly until the vehicle reaches the goal pose.

The method may further comprise:

receiving inputs comprising: an initial state s^i , goal specification s^g , task planner P^t , state mapping function f , motion planner P^m , and safety estimator;

initialize a cost function Cost with sampled poses $x \in f(s): \text{Cost}(\langle s, a, s' \rangle) \leftarrow A^*(x, x')$;

initialize a safety estimation function Safe with $\text{Safe}(s, a, s') \leftarrow 1.0$.

computing an optimal task plan p using Cost and Safe functions:

$p \leftarrow P^t(s^{init}, s^g, \text{Cost}, \text{Safe})$, where $p = (s^{init} \rightarrow a_0, s_1, a_1, \dots, s^g)$

until plan p is not empty;

33

extracting a first action of $p, \langle s, a, s' \rangle$, and computing a safety value μ ;

updating the Safe function: $\text{Safe}(\langle \exists a, s' \rangle) \leftarrow \mu$ and the Cost function:

$$\text{Cost}(\langle s, a, s' \rangle) \leftarrow A^*(x, x')$$

generating a new plan: $p' \leftarrow P'(s, s^g, \text{Cost}, \text{Safe})$;

if $p' = p$ then $x' \leftarrow f(s')$, and while $x' \neq x$, call a motion planner $\langle \delta, \theta \rangle \leftarrow P''(x, x')$, execute a control signal $\langle \delta, \theta \rangle$, and update the vehicle's current pose x ;

removing a tuple $\langle s, a \rangle$ from plan p ;

else updating current plan $p \leftarrow p'$.

The task planner P' may be implemented using Answer Set Programming (ASP).

The environment of operation may comprise surrounding vehicles, e.g., vehicles in motion.

The utility optimization may comprise minimizing a travel distance while maintaining a margin of safety.

It is also an object to provide a method of operating a vehicle, comprising: planning a task for the vehicle, comprising an efficient sequence of actions to accomplish goals, e.g., according to action knowledge; and planning motion of the vehicle, comprising computing motion trajectories that efficiently connect a current location with a goal location, based on at least surrounding vehicles to ensure safety.

It is a further object to provide a non-transitory computer readable medium containing a program for operating a vehicle, comprising: instructions for planning a task for the vehicle, comprising an efficient sequence of actions to accomplish goals, e.g., according to action knowledge; and instructions for planning motion of the vehicle, comprising computing motion trajectories that efficiently connect a current location with a goal location, based on at least surrounding vehicles to ensure safety.

It is a still further object to provide a system for operating a vehicle, comprising: a task planner configured to plan a task for the vehicle, to define an efficient sequence of actions to accomplish goals, e.g., according to action knowledge; and a motion planner configured to plan motion of the vehicle, according to computed motion trajectories that efficiently connect a current location with a goal location, based on at least surrounding vehicles to ensure safety.

Another object provides a method of operating a vehicle, comprising: planning a task for the vehicle, comprising a sequence of actions to accomplish goals, e.g., according to action knowledge; and planning motion of the vehicle, comprising computing motion trajectories that connect a current location with a goal location, based on a cost optimization of vehicle motion based on at least safety with respect to surrounding vehicles.

A further object comprises a non-transitory computer readable medium containing a program for operating a vehicle, comprising: instructions for planning a task for the vehicle, comprising a sequence of actions to accomplish goals, e.g., according to action knowledge; and instructions for planning motion of the vehicle, comprising computing motion trajectories that connect a current location with a goal location, based on a cost optimization of vehicle motion based on at least safety with respect to surrounding vehicles.

A still further object provides a system for operating a vehicle, comprising: a task planner configured to plan a task for the vehicle, to define a sequence of actions to accomplish goals, e.g., according to action knowledge; and a motion planner configured to plan motion of the vehicle, according to computed motion trajectories that connect a current

34

location with a goal location, based on a cost optimization of vehicle motion based on at least safety with respect to surrounding vehicles.

An object further provides a method of operating an autonomous vehicle, comprising: planning a route for the autonomous vehicle; planning motion of the autonomous vehicle according to the planned route, comprising selection of options consistent with the route that are cost efficient and safe with respect to surrounding vehicles; and controlling the autonomous vehicle according to the planned route and planned motion.

A further object provides a method of controlling an autonomous vehicle, comprising: planning a route for the autonomous vehicle along a path having execution options within the route; receiving data relating to a relationship of the autonomous vehicle with respect to other vehicles along the route; planning motion of the autonomous vehicle according to the planned route, comprising selection of options consistent with the route and which alter a relation of the autonomous vehicle with the other vehicles, that are cost efficient and safe with respect to the other vehicles; and controlling the autonomous vehicle according to the planned route and planned motion comprising a selected option.

BRIEF DESCRIPTION OF THE DRAWINGS

FIGS. 1A and 1B show a risky situation for the vehicle to merge left due to the busy traffic (FIG. 1A), and a safe situation for the vehicle to merge left (FIG. 1B).

FIG. 2 shows an overview of the TMPUD algorithm that consists of four components, the task planner, plan manager, motion planner and safety estimator.

FIG. 3 shows an illustrative example of operation of the system, where the vehicle is tasked with driving from the very left to the top-right area.

FIGS. 4A-4D show results of an abstraction simulation which compare the overall performances of TMPUD and two baseline methods.

DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENTS

Example 1

FIG. 2 shows an overview of algorithm TMPUD that consists of four components, i.e., task planner, plan manager, motion planner and safety estimator. The task planner includes components of goal specification, action description, and utility function, where users' service requests are received by the goal specification component. The task planner computes a sequence of symbolic actions that are passed to the plan manager. The plan manager generates navigation goals (i.e., a pair of two poses) to path planner, which is then used for computing a continuous trajectory for connecting 2D poses. The trajectory will be used in the two components of safety estimator and tracking controller. Safety estimator uses this trajectory to estimate actions' safety levels, and then the utility function in task planner can be updated accordingly. Tracking controller computes the desired control signals to drive the vehicle to follow the trajectory from the path planner.

FIG. 3. An illustrative example, where the vehicle is tasked with driving from the very left to the top-right area. The vehicle needs to compute plans at both task and motion levels. The vehicle starts with executing Plan A (blue color). While it is getting close to Area 1 (a red circle), the motion-level safety estimator reports a low safety value

35

based on the local road condition. This computed safety value is incorporated into task planner's cost function. Using the updated cost function, the task planner re-computes an optimal plan (Plan B), and suggests the vehicle to go straight and merge left in Area 2. The interaction between task and motion levels, supported by TMPUD, enables the vehicle to dynamically adjust its high-level task plans to avoid unsafe behaviors.

TMPUD starts with using an optimal task planner to compute Plan A. The vehicle takes the first symbolic action from Plan A (trajectory in blue color), and executes the action using the motion planner. Getting close to Area 1, the vehicle plans to merge left. However, the safety estimator at the motion level reports a low safety value in Area 1. This computed safety value is incorporated into task planner, where the task planner integrates the safety value into its cost function, and re-computes an optimal plan, Plan B. Different from Plan A, Plan B suggests the vehicle to go straight, and merge left in Area 2. In this trial, the vehicle was able to follow Plan B all the way to the goal. TMPUD enabled the vehicle to avoid the risky behavior of merging left in Area 1 without introducing extra motion cost. See, youtu.be/8NHQYUqMyoI.

Experiments conducted in CARLA are referred as being in full simulation. All vehicles move at a constant speed (20 km/h) on average. In full simulation, ego vehicle performs the whole plan at the task level in the presence of other vehicles. Different numbers of vehicles (200 and 120) are spawned, and traffic of the two environments referred to as being heavy and normal respectively.

Running full simulation using CARLA is time-consuming, preventing conducting of large-scale experiments. For instance, results are based on tens of thousands of experimental trials, and full simulation in this scale would have required months of computation time. To conduct large numbers of experimental trials, an abstract simulation platform was developed, where action outcomes are sampled from pre-computed probabilistic world models. Parameters of the world models (for abstract simulation) are learned by repeatedly spawning the ego and surrounding vehicles in a small area, and statistically analyzing the results of the vehicles' interaction.

In particular, a large effort was made in analyzing the outcomes of "merging lane" actions due to its significant potential risks. The probabilities of the three different outcomes of "merging lane" actions were empirically computed, including "merge", "collide", and "stop". Two domain factors were introduced into the abstract simulation platform, including density and acceleration. In high-density environments, the ego vehicle is surrounded by three vehicles, while this number is reduced to one in low-density environments. In high-acceleration environments, surrounding vehicles' acceleration (in m/s²) is randomly sampled in [-1.0, 1.0], while this range is [-0.5, 0.5] in low-acceleration environments.

The goal of TMPUD is to improve task-completion efficiency (to reduce traveling distance), while guaranteeing safety. So, the two most important evaluation metrics are traveling distance and the number of unsafe behaviors, where unsafe behaviors cause either collisions or force at least one surrounding vehicle to stop (to avoid collisions).

The two baseline methods are selected from the literature, and referred to as No-communication (No-com), and Threshold-based (Th-based). The No-com baseline [13] forces the vehicle to execute all task-level actions at the motion level, while driving behaviors' safety values are not considered. The Th-based baseline [8] enables the motion

36

planner to "reject" a task-level action when its safety value is lower than a threshold β , where a higher (lower) β threshold makes a vehicle more conservative (aggressive). In case of an action being rejected, the task planner will compute a new plan to avoid the risky action. Three versions of the Th-based baseline were developed with different β values (0.1, 0.3, and 0.5).

TABLE I

FULL SIMULATION: TRAVELING DISTANCE AND NUMBER OF COLLISIONS AND STOPS FOR THREE ALGORITHMS UNDER DIFFERENT TRAFFIC CONDITIONS (NORMAL AND HEAVY TRAFFIC).

Algorithm	Travelling Distance (m)	Num. of collisions and stops
Normal Traffic		
TMPUD	514	0
Th-based $\beta = 0.5$	537	0
$\beta = 0.3$	513	5
$\beta = 0.1$	478	24
No-com	426	48
Heavy Traffic		
TMPUD	530	2
Th-based $\beta = 0.5$	545	2
$\beta = 0.3$	528	7
$\beta = 0.1$	497	35
No-com	426	54

Results from Full Simulation

Table I presents the results in comparing TMPUD to the two baseline methods. As shown in the table, in both road conditions, TMPUD achieved the lowest traveling distance, in comparison to those methods that produced compared safety levels (in terms of the number of collisions and stops). For instance, under normal traffic, only the Th-based baseline with $\beta=0.5$ was able to completely avoid collisions and stops, but it produced an average traveling distance of 537 m. In comparison, TMPUD required only 514 m, while completely avoided collisions and stops. Under heavy traffic, TMPUD (again) produced the best performance in safety (based on the number of collisions and stops), while requiring less traveling distance in comparison to the only baseline (Th-based with $\beta=0.5$) that produced comparable performance in safety. The experimental trials (200 for each approach) from full simulation took eight full workdays.

FIGS. 4A-4D show abstraction simulation of the overall performances of TMPUD and two baseline methods. The x-axis represents the average traveling distance, and the y-axis represents the total number of collisions and stops. FIGS. 4A-4D correspond to four different road conditions. The road conditions, low-density and low-acceleration (FIG. 4A), low-density and high-acceleration (FIG. 4B), high-density and low-acceleration (FIG. 4C), high-density and high-acceleration (FIG. 4D). Under each road condition, each algorithm was evaluated using 4000 trials. Batch-based evaluations were employed with four batches for significance analysis, where each batch includes 1000 trials.

Results from Abstract Simulation

FIGS. 4A-4D present the performances of TMPUD and the baseline methods in both traveling distance and the number of unsafe behaviors. The x-axis corresponds to the average traveling distance, and y-axis corresponds to the total number of collisions and stops (both are considered failure cases of driving behaviors). From FIGS. 4A-4D, TMPUD is shown to be the most efficient (x-axis) among

those methods that produced comparable performances in safety (y-axis), except that Th-based ($\beta=0.5$) produced slightly less unsafe behaviors (but it performed poorly in efficiency).

There are a few side observations. Not surprisingly, No-com produced the worst performance of in safety (y-axis), though its traveling distance remains the lowest. This is because, using No-com, the vehicle blindly executes task-level actions while unrealistically believing driving behaviors are always safe. The Th-based baseline's performance depends on its safety threshold (β), where a greater value produces safer but less efficient behaviors. The results show that TMPUD improves vehicles' task-completion efficiency, while ensuring safety in different road conditions.

Focusing on urban driving scenarios, both a safety evaluation algorithm, and a task-motion planning algorithm, called TMPUD, are provided for autonomous driving. TMPUD bridges the gap between task planning and motion planning in autonomous driving. TMPUD was extensively evaluated using a 3D urban driving simulator (CARLA) and an abstract simulator. Results suggest that TMPUD improves the task-completion efficiency in different road conditions, while ensuring the safety of driving behaviors.

TMPUD may also be implemented using different task and motion planners, and these in turn may be evaluated in different testing platforms (e.g., using simulators with a physics engine) under different conditions. The technology may be applied to various autonomous mobile platforms, such as robots, drones.

A phrase such as an "aspect" does not imply that such aspect is essential to the subject technology or that such aspect applies to all configurations of the subject technology. A disclosure relating to an aspect may apply to all configurations, or one or more configurations. An aspect may provide one or more examples. A phrase such as an aspect may refer to one or more aspects and vice versa. A phrase such as an "embodiment" does not imply that such embodiment is essential to the subject technology or that such embodiment applies to all configurations of the subject technology. A disclosure relating to an embodiment may apply to all embodiments, or one or more embodiments. An embodiment may provide one or more examples. A phrase such as an embodiment may refer to one or more embodiments and vice versa. A phrase such as a "configuration" does not imply that such configuration is essential to the subject technology or that such configuration applies to all configurations of the subject technology. A disclosure relating to a configuration may apply to all configurations, or one or more configurations. A configuration may provide one or more examples. A phrase such as a configuration may refer to one or more configurations and vice versa.

Certain units described in this specification have been labeled as modules in order to more particularly emphasize their implementation independence. A module is "[a] self-contained hardware or software component that interacts with a larger system." Alan Freedman, "The Computer Glossary" 268 (8th ed. 1998). A module may include a machine- or machines-executable instructions. For example, a module may be implemented as a hardware circuit including custom VLSI circuits or gate arrays, off-the-shelf semiconductors such as analog circuits, quantum computers, microprocessors, logic chips, transistors, or other discrete components. A module may also be implemented in programmable hardware devices such as field programmable gate arrays, programmable array logic, programmable logic devices or the like.

Modules may also include software-defined units or instructions, that when executed by a processing machine or device, transform data stored on a data storage device from a first state to a second state. An identified module of executable code may, for instance, include one or more physical or logical blocks of computer instructions that may be organized as an object, procedure, or function. Nevertheless, the executables of an identified module need not be physically located together, but may include disparate instructions stored in different locations that, when joined logically together, include the module, and when executed by the processor, achieve the stated data transformation. A module of executable code may be a single instruction, or many instructions, and may even be distributed over several different code segments, among different programs, and/or across several memory devices. Similarly, operational data may be identified and illustrated herein within modules, and may be embodied in any suitable form and organized within any suitable type of data structure. The operational data may be collected as a single data set, or may be distributed over different locations including over different storage devices. The absence of a module reflects the inability of system including the module to execute in given circumstances to perform the function of the respective module, and not that its physical or logical constituents are excluded, that is, the module is unavailable. In the foregoing description, numerous specific details are provided, such as examples of programming, software modules, user selections, network transactions, distributed ledgers, blockchains, smart contracts, database queries, database structures, hardware modules, hardware circuits, hardware chips, etc., to provide a thorough understanding of the present embodiments. One skilled in the relevant art will recognize, however, that the invention requires a specific implementation that requires special purpose technology for implementation, that generic hardware alone will not achieve the objectives set forth herein.

As used herein, various terminology is for the purpose of describing particular implementations only and is not intended to be limiting of implementations. For example, as used herein, an ordinal term (e.g., "first," "second," "third," etc.) used to modify an element, such as a structure, a component, an operation, etc., does not by itself indicate any priority or order of the element with respect to another element, but rather merely distinguishes the element from another element having a same name (but for use of the ordinal term). The term "coupled" is defined as connected, although not necessarily directly, and not necessarily mechanically; two items that are "coupled" may be unitary with each other, but in that case the unitary element must meet established criteria for each item. The terms "a" and "an" are defined as one or more unless this disclosure explicitly requires otherwise. The term "substantially" is defined as largely but not necessarily wholly what is specified (and includes what is specified; e.g., substantially 90 degrees includes 90 degrees and substantially parallel includes parallel), as understood by a person of ordinary skill in the art.

The phrase "and/or" means "and" or "or". To illustrate, A, B, and/or C includes: A alone, B alone, C alone, a combination of A and B, a combination of A and C, a combination of B and C, or a combination of A, B, and C. In other words, "and/or" operates as an "inclusive or". Similarly, the phrase "A, B, C, or a combination thereof" or "A, B, C, or any combination thereof" includes A alone, B alone, C alone, a combination of A and B, a combination of A and C, a combination of B and C, or a combination of A, B, and C.

As used herein, whether in the above description or the following claims, the terms “comprising,” “including,” “carrying,” “having,” “containing,” “involving,” and the like are to be understood to be open-ended, that is, to mean including but not limited to. The terms “comprise” (and any form of comprise, such as “comprises” and “comprising”), “have” (and any form of have, such as “has” and “having”), and “include” (and any form of include, such as “includes” and “including”). As a result, an apparatus that “comprises,” “has,” or “includes” one or more elements possesses those one or more elements, but is not limited to possessing only those one or more elements. Likewise, a method that “comprises,” “has,” or “includes” one or more steps possesses those one or more steps, but is not limited to possessing only those one or more steps.

Some implementations are described herein in connection with thresholds. As used herein, satisfying a threshold may refer to a value being greater than the threshold, more than the threshold, higher than the threshold, greater than or equal to the threshold, less than the threshold, fewer than the threshold, lower than the threshold, less than or equal to the threshold, equal to the threshold, etc.

The terms “about” or “approximately” are intended to denote a range for a quantitative parameter that achieves substantially the same result in the same manner, with either a predictable relation between input parameter and behavior, a statistically insignificant change in response with respect to the change between a nominal input parameter and another input parameter within the stated range of “about” or “approximately”. Thus, a feature would be outside a range of “about” or “approximately” if the result is achieved in a substantially different manner, a substantially different result is achieved, within the range statistically significant and meaningful differences in output response are achieved based on differences between the nominal parameter and the putative one which is “about” or “approximately” the same, or the result is unpredictable to an extent that the output response unpredictable deviates from the benchmark established. “Substantially” and “significant” are interpreted according to the understanding of persons of ordinary skill in the art, dependent on the context, and are intended to represent a reasonable range of quantitative difference which may be ignored or compensated without change in cause or effect.

It will be apparent that systems and/or methods, described herein, can be implemented in different forms of hardware, software, or a combination of hardware and software. The actual specialized control hardware or software code used to implement these systems and/or methods is not limiting of the implementations. Thus, the operation and behavior of the systems and/or methods are described herein without reference to specific software code, it being understood that software and hardware can be designed to implement the systems and/or methods based on the description herein. It is also understood that the algorithms are not limited by particular expressions, and rather are intended to encompass functional equivalents regardless of expression. Further, as is known and well understood, semantic expressions relating inputs or available data and output or action are themselves algorithms.

Even though particular combinations of features are recited in the claims and/or disclosed in the specification, these combinations are not intended to limit the disclosure of possible implementations. In fact, many of these features can be combined in ways not specifically recited in the claims and/or disclosed in the specification. Although each dependent claim listed below may directly depend on only

one claim, the disclosure of possible implementations includes each dependent claim in combination with every other claim in the claim set.

No element, act, or instruction used herein should be construed as critical or essential unless explicitly described as such. Also, as used herein, the articles “a” and “an” are intended to include one or more items, and may be used interchangeably with “one or more.” Furthermore, as used herein, the term “set” is intended to include one or more items (e.g., related items, unrelated items, a combination of related and unrelated items, etc.), and may be used interchangeably with “one or more.” Where only one item is intended, the term “one” or similar language is used. Also, as used herein, the terms “has,” “have,” “having,” and/or the like are intended to be open-ended terms. Further, the phrase “based on” is intended to mean “based, at least in part, on” unless explicitly stated otherwise.

Any embodiment of any of the systems, methods, and article of manufacture can “consist of” or “consist essentially of”, rather than “comprise”, “have”, or “include”, any of the described steps, elements, and/or features. Thus, in any of the claims, the term “consisting of” or “consisting essentially of” can be substituted for any of the open-ended linking verbs recited above, in order to change the scope of a given claim from what it would otherwise be using the open-ended linking verb. Thus, the transitional phrases “consisting of” and “consisting essentially of,” respectively, shall be considered exclusionary transitional phrases, as set forth, with respect to claims, in the United States Patent Office Manual of Patent Examining Procedures. Additionally, the terms “wherein” or “whereby” may be used interchangeably with “where”.

Further, a device or system that is configured in a certain way is configured in at least that way, but it can also be configured in other ways than those specifically described. The feature or features of one embodiment may be applied to other embodiments, even though not described or illustrated, unless expressly prohibited by this disclosure or the nature of the embodiments.

The phrase “configured to” means a specification or clarification of the structure or composition of an element defining what the element is, by way of a specific description of its configuration and interface with other elements or an external constraint. The phrase “adapted to” means a specification or clarification of a function or relationship of an element defining what the element does, by way of a specific description of its adaptation and interface with other elements or an external constraint. Functional language within such a specification of an element within a claim is taken to be an affirmative limitation, and not a mere intended use. Functional language or context within a claim preamble is to be considered non-limiting and outside of the claim scope, unless integrated by specific reference and inclusion by the express claim scope.

The claims hereinbelow are to be construed as excluding abstract subject matter as judicially excluded from patent protection, and the scope of all terms and phrases is to be constrained to only include that which is properly encompassed. By way of example, if a claim phrase is amenable of construction to encompass either patent eligible subject matter and patent ineligible subject matter, then the claim shall be interpreted to cover only the patent eligible subject matter. The scope of the claims shall be considered definite in accordance with the ability of a judicial or administrative court or tribunal to make this determination, regardless of any retroactive or ex post facto changes in interpretation by such court or tribunal. The various disclosure expressly

provided herein, in conjunction with the incorporated references, are to be considered to encompass any combinations, permutations, and sub-combinations of the respective disclosures or portions thereof, and shall not be limited by the various exemplary combinations specifically described herein.

REFERENCES

- [1] J.-F. Bonnefon, A. Shariff, and I. Rahwan, "The social dilemma of autonomous vehicles," *Science*, vol. 352, no. 6293, pp. 1573-1576, 2016.
- [2] A. Geiger, P. Lenz, and R. Urtasun, "Are we ready for autonomous driving? the kitti vision benchmark suite," in 2012 IEEE Conference on Computer Vision and Pattern Recognition. IEEE, 2012, pp. 3354-3361.
- [3] M. Maurer, J. C. Gerdes, B. Lenz, H. Winner et al., "Autonomous driving," Berlin, Germany: Springer Berlin Heidelberg, vol. 10, pp. 978-3, 2016.
- [4] C. J. Haboucha, R. Ishaq, and Y. Shiftan, "User preferences regarding autonomous vehicles," *Transportation Research Part C: Emerging Technologies*, vol. 78, pp. 37-49, 2017.
- [5] P. Koopman and M. Wagner, "Autonomous vehicle safety: An interdisciplinary challenge," *IEEE Intelligent Transportation Systems Magazine*, vol. 9, no. 1, pp. 90-96, 2017.
- [6] P. Cao, Z. Xu, Q. Fan, and X. Liu, "Analysing driving efficiency of mandatory lane change decision for autonomous vehicles," *IET Intelligent Transport Systems*, vol. 13, no. 3, pp. 506-514, 2018.
- [7] B. Paden, M. Cáp, S. Z. Yong, D. Yershov, and E. Frazzoli, "A survey of motion planning and control techniques for self-driving urban vehicles," *IEEE Transactions on intelligent vehicles*, vol. 1, no. 1, pp. 33-55, 2016.
- [8] S. Srivastava, E. Fang, L. Riano, R. Chitnis, S. Russell, and P. Abbeel, "Combined task and motion planning through an extensible planner-independent interface layer," in 2014 IEEE international conference on robotics and automation (ICRA). IEEE, 2014, pp. 639-646.
- [9] B. Kim, L. P. Kaelbling, and T. Lozano-Pérez, "Learning to guide task and motion planning using score-space representation," in 2017 IEEE International Conference on Robotics and Automation (ICRA). IEEE, 2017, pp. 2810-2817.
- [10] C. R. Garrett, T. Lozano-Perez, and L. P. Kaelbling, "Ffrob: Leveraging symbolic planning for efficient task and motion planning," *The International Journal of Robotics Research*, vol. 37, no. 1, pp. 104-136, 2018.
- [11] S.-Y. Lo, S. Zhang, and P. Stone, "Petlon: planning efficiently for task-level-optimal navigation," in *Proceedings of the 17th International Conference on Autonomous Agents and MultiAgent Systems (AAMAS)*, 2018, pp. 220-228.
- [12] A. Dosovitskiy, G. Ros, F. Codevilla, A. Lopez, and V. Koltun, "Carla: An open urban driving simulator," in *Conference on Robot Learning*, 2017, pp. 1-16.
- [13] C. Chen, A. Gaschler, M. Rickert, and A. Knoll, "Task planning for highly automated driving," in 2015 IEEE Intelligent Vehicles Symposium (IV). IEEE, 2015, pp. 940-945.
- [14] C. Liu and M. Tomizuka, "Control in a safe set: Addressing safety in human-robot interactions," in *ASME 2014 Dynamic Systems and Control Conference*. American Society of Mechanical Engineers Digital Collection, 2014.
- [15] C. Liu, and M. Tomizuka, "Safe exploration: Addressing various uncertainty levels in human robot interactions," in 2015 American Control Conference (ACC). IEEE, 2015, pp. 465-470.
- [16] J. Chen, B. Yuan, and M. Tomizuka, "Model-free deep reinforcement learning for urban autonomous driving," in 2019 IEEE Intelligent Transportation Systems Conference (ITSC), 2019, pp. 2765-2771.
- [17] J. Chen, S. E. Li, and M. Tomizuka, "Interpretable end-to-end urban autonomous driving with latent deep reinforcement learning," *arXiv preprint arXiv:2001.08726*, 2020.
- [18] J. Chen, W. Zhan, and M. Tomizuka, "Autonomous driving motion planning with constrained iterative lqr," *IEEE Transactions on Intelligent Vehicles*, vol. 4, no. 2, pp. 244-254, 2019.
- [19] C. Liu and M. Tomizuka, "Enabling safe freeway driving for automated vehicles," in 2016 American Control Conference (ACC). IEEE, 2016, pp. 3461-3467.
- [20] J. Bi, V. Dhiman, T. Xiao, and C. Xu, "Learning from interventions using hierarchical policies for safe learning," in *Proceedings of the Thirty-Fourth AAAI Conference on Artificial Intelligence*, 2020.
- [21] C. Paxton, V. Raman, G. D. Hager, and M. Kobilarov, "Combining neural networks and tree search for task and motion planning in challenging environments," in 2017 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS). IEEE, 2017, pp. 6059-6066.
- [22] K. B. Lim, S. Park, S. Kim, J. M. Jeong, and Y.-S. Yoon, "Behavior planning of an unmanned ground vehicle with actively articulated suspension to negotiate geometric obstacles," in 2009 IEEE/RSJ International Conference on Intelligent Robots and Systems. IEEE, 2009, pp. 821-826.
- [23] C. Xiu and H. Chen, "A behavior-based path planning for autonomous vehicle," in *International Conference on Intelligent Robotics and Applications*. Springer, 2010, pp. 1-9.
- [24] J. Wei, J. M. Snider, T. Gu, J. M. Dolan, and B. Litkouhi, "A behavioral planning framework for autonomous driving," in 2014 IEEE Intelligent Vehicles Symposium Proceedings. IEEE, 2014, pp. 458-464.
- [25] C. Chen, M. Rickert, and A. Knoll, "Combining task and motion planning for intersection assistance systems," in 2016 IEEE Intelligent Vehicles Symposium (IV). IEEE, 2016, pp. 1242-1247.
- [26] S. Cambon, R. Alami, and F. Gravot, "A hybrid approach to intricate motion, manipulation and task planning," *The International Journal of Robotics Research*, vol. 28, no. 1, pp. 104-126, 2009.
- [27] J. Wolfe, B. Marthi, and S. Russell, "Combined task and motion planning for mobile manipulation," in *Twentieth International Conference on Automated Planning and Scheduling*, 2010.
- [28] D. S. Nau, T.-C. Au, O. Ilghami, U. Kuter, J. W. Murdock, D. Wu, and F. Yaman, "Shop2: An htn planning system," *Journal of artificial intelligence research*, vol. 20, pp. 379-404, 2003.
- [29] E. Erdem, K. Haspalamutgil, C. Palaz, V. Patoglu, and T. Uras, "Combining high-level causal reasoning with low-level geometric reasoning and motion planning for robotic manipulation," in 2011 IEEE International Conference on Robotics and Automation. IEEE, 2011, pp. 4575-4581.
- [30] A. Houenou, P. Bonnifait, V. Cherfaoui, and W. Yao, "Vehicle trajectory prediction based on motion model and

maneuver recognition,” in 2013 IEEE/RSJ international conference on intelligent robots and systems. IEEE, 2013, pp. 4363-4369.

[31] S. Ammoun and F. Nashashibi, “Real time trajectory prediction for collision risk estimation between vehicles,” in 2009 IEEE 5th International Conference on Intelligent Computer Communication and Processing. IEEE, 2009, pp. 417-422.

[32] V. Lifschitz, “Answer set programming and plan generation,” *Artificial Intelligence*, vol. 138, no. 1-2, pp. 39-54, 2002.

S. Amiri, S. Bajracharya, C. Goktolgal, J. Thomason, and S. Zhang, “Augmenting knowledge through statistical, goal-oriented human-robot dialog,” in 2019 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS). IEEE, 2019, pp. 744-750.

[34] Y.-q. Jiang, S.-q. Zhang, P. Khandelwal, and P. Stone, “Task planning in robotics: an empirical comparison of pddl- and asp-based systems,” *Frontiers of Information Technology & Electronic Engineering*, vol. 20, no. 3, pp. 363-373, 2019.

[35] M. T. Emirler, I. M. C. Uygur, B. Aksun Güvenc, and L. Güvenc, “Robust pid steering control in parameter space for highly automated driving,” *International Journal of Vehicular Technology*, 2014.

[36] S. Shah, D. Dey, C. Lovett, and A. Kapoor, “Airsim: High-fidelity visual and physical simulation for autonomous vehicles,” in *Field and service robotics*. Springer, 2018, pp. 621-635.

[37] N. Koenig and A. Howard, “Design and use paradigms for gazebo, an open-source multi-robot simulator,” in 2004 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)(IEEE Cat. No. 04CH37566), vol. 3. IEEE, 2004, pp. 2149-2154.

[38] Rajasekaran, Sanguthevar, and Suneeta Ramaswami. “Optimal mesh algorithms for the Voronoi diagram of line segments and motion planning in the plane.” *Journal of Parallel and Distributed Computing* 26, no. 1 (1995): 99-115.

[39] Ahmed, Nizam. “Robot Motion Planning.” (1997).

[40] Hopcroft, John E., and Gordon T. Wilfong. “Reducing multiple object motion planning to graph searching.” *SIAM Journal on Computing* 15, no. 3 (1986): 768-785.

[41] Tang, Kai. “On computing contact configurations of a curved chain.” *Graphical Models and Image Processing* 61, no. 6 (1999): 341-361.

[42] Garrett, Caelan Reed, Tomis Lozano-Pdrez, and Leslie Pack Kaelbling. “FFRob: An efficient heuristic for task and motion planning.” In *Algorithmic Foundations of Robotics XI*, pp. 179-195. Springer, Cham, 2015.

[43] Kaelbling, Leslie Pack, and Tomás Lozano-Pérez. “Integrated task and motion planning in belief space.” *The International Journal of Robotics Research* 32, no. 9-10 (2013): 1194-1227.

[44] Garrett, Caelan Reed, Rohan Chitnis, Rachel Holladay, Beomjoon Kim, Tom Silver, Leslie Pack Kaelbling, and Tomis Lozano-Pdrez. “Integrated task and motion planning.” *arXiv preprint arXiv:2010.01083* (2020).

[45] Dantam, Neil T., Zachary K. Kingston, Swarat Chaudhuri, and Lydia E. Kavraki. “An incremental constraint-based framework for task and motion planning.” *The International Journal of Robotics Research* 37, no. 10 (2018): 1134-1151.

[46] Rao, Nageswara S. V. “An Algorithmic Framework for Robot Navigation in Unknown Terrains.” (1988).

[47] Ramaswami, Suneeta. “Algorithmic Motion Planning and Related Geometric Problems on Parallel Machines (Dissertation Proposal).” (1993).

[48] Guibas, Leonidas J., Micha Sharir, and Shmuel Sifrony. “On the general motion-planning problem with two degrees of freedom.” *Discrete & Computational Geometry* 4, no. 5 (1989): 491-521.

[49] Halperin, Dan. “On the complexity of a single cell in certain arrangements of surfaces related to motion planning.” *Discrete & Computational Geometry* 11, no. 1 (1994): 1-33.

[50] Srivastava, Siddharth, Eugene Fang, Lorenzo Riano, Rohan Chitnis, Stuart Russell, and Pieter Abbeel. “Combined task and motion planning through an extensible planner-independent interface layer.” In 2014 IEEE international conference on robotics and automation (ICRA), pp. 639-646. IEEE, 2014.

[51] Kedem, Klara, and Micha Sharir. “An efficient motion-planning algorithm for a convex polygonal object in two-dimensional polygonal space.” *Discrete & Computational Geometry* 5, no. 1 (1990): 43-75.

[52] Lagriffoul, Fabien, Neil T. Dantam, Caelan Garrett, Aliakbar Akbari, Siddharth Srivastava, and Lydia E. Kavraki. “Platform-independent benchmarks for task and motion planning.” *IEEE Robotics and Automation Letters* 3, no. 4 (2018): 3765-3772.

[53] Garrett, Caelan Reed, Tomis Lozano-Pdrez, and Leslie Pack Kaelbling. “FFRob: An efficient heuristic for task and motion planning.” In *Algorithmic Foundations of Robotics XI*, pp. 179-195. Springer, Cham, 2015.

[54] Halperin, Dan, Mark H. Overmars, and Micha Sharir. “Efficient motion planning for an L-shaped object.” *SIAM Journal on Computing* 21, no. 1 (1992): 1-23.

[55] Kaelbling, Leslie Pack, and Tomis Lozano-Pdrez. “Hierarchical task and motion planning in the now.” In 2011 IEEE International Conference on Robotics and Automation, pp. 1470-1477. IEEE, 2011.

[56] Dantam, Neil T., Zachary K. Kingston, Swarat Chaudhuri, and Lydia E. Kavraki. “Incremental Task and Motion Planning: A Constraint-Based Approach.” In *Robotics: Science and systems*, vol. 12, p. 00052. 2016.

[57] Koltun, Vladlen. “Pianos are not flat: Rigid motion planning in three dimensions.” In *Symposium on Discrete Algorithms: Proceedings of the sixteenth annual ACM-SIAM symposium on Discrete algorithms*, vol. 23, no. 25, pp. 505-514. 2005.

[58] Lagriffoul, Fabien, Dimitar Dimitrov, Julien Bidot, Alessandro Saffiotti, and Lars Karlsson. “Efficiently combining task and motion planning using geometric constraints.” *The International Journal of Robotics Research* 33, no. 14 (2014): 1726-1747.

[59] van der Stappen, A. Frank, Mark H. Overmars, Mark de Berg, and Jules Vleugels. “Motion planning in environments with low obstacle density.” *Discrete & Computational Geometry* 20, no. 4 (1998): 561-587.

[60] Kornev, Ivan I., Vladislav I. Kibalov, and Oleg Shipitko. “Local path planning algorithm for autonomous vehicle based on multi-objective trajectory optimization in state lattice.” In *Thirteenth International Conference on Machine Vision*, vol. 11605, p. 1160511. International Society for Optics and Photonics, 2021.

[61] Seccamonte, Francesco, Juraj Kabzan, and Emilio Frazzoli. “On Maximizing Lateral Clearance of an Autonomous Vehicle in Urban Environments.” In 2019 IEEE Intelligent Transportation Systems Conference (ITSC), pp. 1819-1825. IEEE, 2019.

- [62] Broadhurst, Adrian, Simon Baker, and Takeo Kanade. A prediction and planning framework for road safety analysis, obstacle avoidance and driver information. Carnegie Mellon University, the Robotics Institute, 2004.
- [63] Sisbot, Emrah Akin, Aurdlie Clodic, Rachid Alami, and Maxime Ransan. "Supervision and motion planning for a mobile manipulator interacting with humans." In Proceedings of the 3rd ACM/IEEE international conference on Human robot interaction, pp. 327-334. 2008.
- [64] Best, Andrew, Sahil Narang, Daniel Barber, and Dinesh Manocha. "Autonovi: Autonomous vehicle planning with dynamic maneuvers and traffic constraints." In 2017 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), pp. 2629-2636. IEEE, 2017.

What is claimed is:

1. A method of operating a vehicle, comprising:

automatically planning a motion of the vehicle with an automated motion planner P^m , which conducts a search in a motion planning domain D^m to determine and optimum motion plan comprising an action a which solves a motion planning problem specified by an initial pose x^i representing a first position and a first orientation of the vehicle, a goal pose x^g representing a second position and a second orientation of the vehicle, and a road network providing constraints on the vehicle, and produces a control signal $\langle \delta, \theta \rangle$, wherein $\delta \in \Delta$ is an acceleration and $\theta \in \Theta$ is a steering angle of control operation sets Δ and Θ , such that $\langle \delta, \theta \rangle \leftarrow P^m(x, x')$ to achieve a collision-free motion trajectory ξ connecting the initial pose x^i and the goal pose x^g taking into account the constraints on the vehicle, to incrementally advance the vehicle toward a goal, the optimum motion plan comprising action a being selected dependent on an associated utility of the incremental advance that represents a change in value, based on at least a safety of the motion trajectory with respect to an environment of operation of the vehicle, a benefit resulting from the incremental advance, and a cost of the incremental advance; and

automatically planning a task for the vehicle with an automated task planner P^t , the task comprising a sequence of the actions to advance the vehicle toward the goal, selectively dependent on an optimization of an aggregate prospective utility of the task comprising the benefit resulting from achieving the goal, the costs associated with the sequence of actions, and the safety of the sequence of actions to advance the vehicle toward the goal, wherein the planning a task comprises:

calculating a plan $p \in P$ of a set of plans P based on a task planning problem within a task planning domain by D^t , including a set of states S within a factored state space, such that each state $s \in S$ is defined by values of a fixed set of variables, the task planning problem comprising an initial state $s^{init} \in S$, a goal state $s^g \in S$, and a set of actions A , each action $a \in A$ being defined by its starting state s and resulting state s' , the plan p consisting of a sequence of transitions represented as $p = \langle s_0, a_0, \dots, s_{N-1}, a_{N-1}, s_N \rangle$, where $s_0 = s^{init}$, $s_N = s^g$;

defining a utility function dependent on at least a cost function $\text{Cost}(s, a, s')$ and a safety function $\text{Safe}(s, a, s')$ of conducting action $\langle s, a, s' \rangle$ in state s ; and producing an optimal plan

$$p^* = \underset{p \in P}{\operatorname{argmin}} f(\text{Cost}(\langle s, a, s' \rangle), \text{Safe}(\langle s, a, s' \rangle))$$

based on the utility function.

2. The method according to claim 1, wherein the optimum plan p^* is produced based on the utility function

$$p^* = \underset{p \in P}{\operatorname{argmin}} \sum_{\langle s, a, s' \rangle \in p} \left[\text{Cost}(\langle s, a, s' \rangle) + \frac{\gamma}{1 + e^{\text{Safe}(\langle s, a, s' \rangle) - 1}} \right].$$

where γ is a constant coefficient and $\gamma > 0$.

3. The method according to claim 1, wherein the optimum action a comprises stopping the vehicle to avoid a collision.

4. The method according to claim 1, wherein the search is conducted directly in a two-dimensional Cartesian space such that the position and the orientation of the vehicle is uniquely represented as the pose, denoted by x and constrained by an urban road network, wherein some parts of the space are designated as free space, and remaining parts are designated as obstacles.

5. The method according to claim 4, further comprising: planning the motion a with the motion planner P^m comprising a path planner and a tracking planner; calculating with the path planner in a first phase, the collision-free trajectory ξ connecting the initial pose x^i and the goal pose x^g taking into account any motion constraints on the vehicle with a minimal trajectory length;

defining with the tracking planner in a second phase, control signal $\langle \delta, \theta \rangle$ to drive the vehicle to follow the calculated collision-free trajectory ξ ; and

mapping the states s with a state mapping function, $f: X = f(s)$, into a set of feasible poses X in a continuous space as available options for the motion planner P^m , wherein availability of at least one pose $x \in X$ is assumed in each state s , such that if state s is feasible, the vehicle is in a free space of D^m , and if state S is infeasible, the vehicle is not in a free space of D^m .

6. The method according to claim 1, further comprising: calculating the safety level, $\text{Safe}(\langle s, a, s' \rangle)$, of a motion-level implementation of the action $\langle s, a, s' \rangle$, wherein the safety level enables the task planner to incorporate a road condition into a process of sequencing actions toward accomplishing complex driving tasks; and calculating a sequence of continuous sequence of the control signal $\langle \delta, \theta \rangle$ to perform the action $\langle s, a, s' \rangle$, comprising the acceleration $\delta \in \Delta$ and the steering angle $\theta \in \Theta$, to drive the vehicle following the collision-free trajectory, while ensuring no collision on the road, wherein sets Δ and Θ denote an operation specification of a tracking controller to drive the vehicle to follow a collision-free trajectory,

wherein $U_s(t) \cup \Delta \times \Theta$ specifies a safe control set at time t , in which all elements, denoted by $u(t) = \langle \delta, \theta \rangle$, are safe for the vehicle to perform at time t , such that a

47

probability of elements sampled from set $\Delta \times \Theta$ being located in the safe control set U_s represents the safety level of action $\langle s, a, s' \rangle$.

7. The method according to claim 1, further comprising: receiving an input which includes the action $\langle s, a, s' \rangle$, a state mapping function f , the motion planner P^m consisting of path planner and tracking controller, and a tracking controller's operation specification sets Δ and Θ ;

obtaining short-period trajectories of the vehicle and surrounding vehicles, where $V_i, i \in [1, \dots, N]$ is an i th vehicle within a sensing range of the vehicle;

iteratively:

estimating a safety between the vehicle and the surrounding vehicles V_i , where $i \in [1, \dots, N]$, given that the vehicle is performing action $\langle s, a, s' \rangle$ at a motion level;

calculating a safe control set $U_i^s(t)$ that includes all safe control signals with regard to the surrounding vehicles V_i at time t ;

randomly sampling M elements from a set $\Delta \times \Theta$, and calculating a probability $o_i(t)$ of the sampled elements falling in set $U_i^s(t)$;

converting a list of values of the estimation of safety $\{o_i(t)\}$ into a single value o_i^* according to

$$o_i^* = \frac{\max_{t \in T} \{o_i(t)\} + \text{mean}_{t \in T} \{o_i(t)\}}{2};$$

and

selecting a minimum value, $o_i^*, i \in [1, \dots, N]$, as an overall safety value, where

$$0 \leq i \leq \frac{(t_2 - t_1)}{\omega};$$

and

producing an output of an estimated safety value $\text{Safe}(\langle s, a, s' \rangle) \in [0.0, 1.0]$.

8. The method according to claim 1, further comprising: receiving inputs:

action $\langle s, a, s' \rangle$,

state mapping function f ,

motion planner P^m , and

control operation sets Δ and Θ ;

sampling initial and goal poses $x \leftarrow f(s)$ and $x' \leftarrow f(s')$,

given action $\langle s, a, s' \rangle$, and f ;

calculating a collision-free trajectory ξ^E , using $P^m(x, x')$, where $\xi^E = x$, $\xi(t_2) = x'$, and $[t_1, t_2]$ is a horizon;

predicting a trajectory ξ_i^s for an i th surrounding vehicle V_i , where $i \in [1, \dots, N]$, and $[t_1, t_2]$ is the horizon;

for each surrounding vehicle V_i ;

calculating a safe control set $U_i^s(t)$ between the vehicle and surrounding vehicle V_i at time $t \in [t_1, t_2]$, where $U_i^s(t) \cup \Delta \times \Theta$ and

$$t = t_1 + \omega \times i, i \leq \frac{(t_2 - t_1)}{\omega}$$

48

sampling M elements randomly from set $\Delta \times \Theta$ and calculating a probability $o_i(t)$ of the elements falling in set $U_i^s(t)$; and

converting a list of estimated safety values, $\{o_i(t)\}$, into a scalar value o_i^* using

$$o_i^* = \frac{\max_{t \in T} \{o_i(t)\} + \text{mean}_{t \in T} \{o_i(t)\}}{2};$$

and

selecting a minimum value, $o_i^*, i \in [1, \dots, N]$, as a safety value.

9. The method according to claim 1, further comprising: calculating both costs and safety values of the vehicle's navigation actions with the motion planner P^m to produce motion trajectories;

generating the control signal $\langle \delta, \theta \rangle$ to move the vehicle; mapping states s to 2D coordinates in continuous spaces using a state mapping function f .

10. The method according to claim 1, further comprising: initializing the cost function $\text{Cost}(s, a, s')$ and the safety function $\text{Safe}(s, a, s')$;

estimating a safety level, μ , of action $\langle s, a, s' \rangle$;

updating the safety function $\text{Safe}(s, a, s')$ using μ and the cost function $\text{Cost}(s, a, s')$ using p^* ; and

calculating a new optimal plan p' .

11. The method according to claim 10, further comprising:

calculating and executing the control signal $\langle \delta, \theta \rangle$ repeatedly until the vehicle reaches the goal pose s^g with the motion planner P^m having as an output $\langle \delta, \theta \rangle$;

initializing the cost function $\text{Cost}(s, a, s')$ with sampled poses $x \in f(s)$: $\text{Cost}(\langle s, a, s' \rangle) \leftarrow A^*(x, x')$;

initializing the safety function $\text{Safe}(s, a, s')$ with $\text{Safe}(s, a, s') \leftarrow 1.0$;

calculating the optimal task plan p using the cost function $\text{Cost}(s, a, s')$ and the safety function $\text{Safe}(s, a, s')$:

$p \leftarrow P(s^{init}, s^g, \text{Cost}, \text{Safe})$, where $p = \langle s^{init} \rightarrow a_0, s_1, a_1, \dots, s^g \rangle$

until plan p is not empty:

extracting a first action of $p, \langle s, a, s' \rangle$, and calculating a safety value μ ;

updating the safety function $\text{Safe}(s, a, s')$: $\text{Safe}(\langle s, a, s' \rangle) \leftarrow \mu$ and the cost function $\text{Cost}(s, a, s')$: $\text{Cost}(\langle s, a, s' \rangle) \leftarrow A^*(x, x')$;

$(\langle s, a, s' \rangle) \leftarrow A^*(x, x')$;

generating a new plan: $p' \leftarrow P(s, s^g, \text{Cost}, \text{Safe})$; and if $p' = p$

then $x' \leftarrow f(s')$, and while $x' \neq x$,

calling the motion planner $\langle \delta, \theta \rangle \leftarrow P^m(x, x')$, executing the control signal $\langle \delta, \theta \rangle$, and updating the vehicle's current pose x ;

removing a tuple $\langle s, a \rangle$ from plan p ;

else updating current plan $p \leftarrow p'$.

12. The method according to claim 1, wherein the task is planned with a task planner P' , implemented using Answer Set Programming (ASP).

13. The method according to claim 1, wherein the environment of operation comprises surrounding vehicles, wherein the surrounding vehicles are in motion.

14. The method according to claim 1, wherein the optimization of the aggregate prospective utility comprises

49

minimizing with a travel distance of the vehicle while maintaining a margin of safety.

15. The method according to claim 1,

wherein the vehicle is an autonomous vehicle, and the task comprises navigating a route, further comprising determining a safety with respect to the environment of the vehicle dependent on real-time conditions of operation,

said automatically planning the task comprising selecting motion trajectory options consistent with the task that are safe with respect to a safety threshold, wherein the action comprises a maneuver, and the selected options are responsive to a cost of the maneuver, a utility of the maneuver, and a determined safety of the maneuver; further comprising controlling the autonomous vehicle according to the planned motion.

16. The method according to claim 1, further comprising automatically updating the planning of motion and planning of the task in real time dependent on real-time conditions of operation of the vehicle.

17. The method according to claim 1, wherein the safety is automatically statistically determined by the automated processor based on a predicted risk, comprising a risk of collision.

18. The method according to claim 1,

wherein the vehicle is an autonomous vehicle, the method further comprising:

receiving data relating to a relationship of the vehicle with respect to the environment of operation;

determining the safety of the motion trajectories comprising a motion and environment-dependent safety of the vehicle within the environment of operation dependent on the received data;

said automatically planning the task comprising continuously planning a utility-optimized route for the vehicle along a path toward the goal having execution options within the route, updated dependent on the determined motion and environment-dependent safety of the autonomous vehicle;

the utility-optimized route comprising a selection of the execution options which alter a relation of the vehicle with the environment of operation, that meet at least one safety criterion with respect to the determined motion and environment-dependent safety; and

controlling the vehicle according to the utility-optimized route and automatically planned motion, to thereby achieve safe and efficient advancement of the vehicle toward the goal.

19. A computer readable medium containing non-transitory instructions for controlling a programmable processor of an autonomous vehicle, comprising:

instructions for automatically planning a motion of the vehicle with an automated motion planner P^m , which conducts a search in a motion planning domain D^m to determine and optimum motion plan comprising an action a which solves a motion planning problem specified instructions for producing an optimal plan

$$p^* = \underset{p \in P}{\operatorname{argmin}} f(\operatorname{Cost}((s, a, s')), \operatorname{Safe}((s, a, s')))$$

based on the utility function.

20. A system for operating a vehicle, comprising:

a sensor configured to receive information about an environment of operation of the vehicle;

50

an automated motion planner P^m configured to plan a motion of the vehicle, which conducts a search in a motion planning domain D^m to determine and optimum motion plan comprising an action a which solves a motion planning problem specified by an initial pose x^i representing a first position and a first orientation of the vehicle, a goal pose x^g representing a second position and a second orientation of the vehicle, and a road network providing constraints on the vehicle, and produces a control signal $\langle \delta, \theta \rangle$, wherein $\delta \in \Delta$ is an acceleration and $\theta \in \Theta$ is a steering angle of control operation sets Δ and Θ , such that $\langle \delta, \theta \rangle \leftarrow P^m(x, x')$, to achieve a collision-free motion trajectory ξ connecting the initial pose x^i and the goal pose x^g and taking into account the constraints on the vehicle, to incrementally advance the vehicle toward a goal, the optimum motion plan comprising action a being selected dependent on an associated utility of the incremental advance that represents a change in value, based on at least a safety of the motion trajectory with respect to an environment of operation of the vehicle, a benefit resulting from the incremental advance, and a cost of the incremental advance; and

an automated task planner P^t configured to automatically plan a task for the vehicle, the task comprising a sequence of the actions to advance the vehicle toward the goal, selectively dependent on an optimization of an aggregate prospective utility of the task comprising the benefit resulting from achieving the goal, the costs associated with the sequence of actions, and the safety of the sequence of actions to advance the vehicle toward the goal, wherein the task is planned by:

calculation of a plan $p \in P$ of a set of plans P based on a task planning problem within a task planning domain by D^t , including a set of states S within a factored state space, such that each state $s \in S$ is defined by values of a fixed set of variables, the task by an initial pose x^i representing a first position and a first orientation of the vehicle, a goal pose x^g representing a second position and a second orientation of the vehicle, and a road network providing constraints on the vehicle, and produces a control signal, $\langle \delta, \theta \rangle$, wherein $\delta \in \Delta$ is an acceleration and $\theta \in \Theta$ is a steering angle of control operation sets Δ and Θ , such that $\langle \delta, \theta \rangle \leftarrow P^m(x, x')$, to achieve a collision-free motion trajectory ξ connecting the initial pose x^i and the goal pose x^g taking into account the constraints on the vehicle, to incrementally advance the vehicle toward a goal, the optimum motion plan comprising action a being selected dependent on an associated utility of the incremental advance that represents a change in value, based on at least a safety of the motion trajectory with respect to an environment of operation of the vehicle, a benefit resulting from the incremental advance, and a cost of the incremental advance; and

instructions for automatically planning a task for the vehicle with an automated task planner P^t , the task comprising a sequence of the actions to advance the vehicle toward the goal, selectively dependent on an optimization of an aggregate prospective utility of the task comprising the benefit resulting from achieving the goal, the costs associated with the sequence of actions, and the safety of the sequence of actions to advance the vehicle toward the goal, comprising:

51

instructions for calculating a plan $p \in P$ of a set of plans P based on a task planning problem within a task planning domain by D' , including a set of states S within a factored state space, such that each state $s \in S$ is defined by values of a fixed set of variables, the task planning problem comprising an initial state $s^{init} \in S$, a goal state $s^g \in S$, and a set of actions A , each action $a \in A$ being defined by its starting state s and resulting state s' , the plan p consisting of a sequence of transitions represented as $p = \langle s_0, a_0, \dots, s_{N-1}, a_{N-1}, s_N \rangle$, where $s_0 = s^{init}$, $s^N = s^g$;

instructions defining a utility function dependent on at least a cost function $Cost(s, a, s')$ and a safety function $Safe(s, a, s')$ of conducting action $\langle s, a, s' \rangle$ in state s ; and

planning problem comprising an initial state $s^{init} \in S$, a goal state $s^g \in S$, and a set of actions A , each action $a \in A$

52

being defined by its starting state s and resulting state s' , the plan p consisting of a sequence of transitions represented as $p = \langle s_0, a_0, \dots, s_{N-1}, a_{N-1}, s_N \rangle$, where $s_0 = s^{init}$, $s^N = s^g$;

determining an optimal plan p^* according to a utility function

$$p = \langle s_0, a_0, \dots, s_{N-1}, a_{N-1}, s_N \rangle,$$

dependent on at least a cost function $Cost(s, a, s')$ and a safety function $Safe(s, a, s')$ of conducting action $\langle s, a, s' \rangle$ in state s ; and

an output configured to control the vehicle according to the control signal $\langle \delta, \theta \rangle$ of the planned motion.

* * * * *