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## **CHAPTER 2**

Class Width = 
$$\frac{\text{Range of data}}{\text{Number of classes}}$$

(round up to next convenient number)

$$Midpoint = \frac{(Lower class limit) + (Upper class limit)}{2}$$

Relative Frequency = 
$$\frac{\text{Class frequency}}{\text{Sample size}} = \frac{f}{n}$$

Population Mean: 
$$\mu = \frac{\sum x}{N}$$

Sample Mean: 
$$\overline{x} = \frac{\sum x}{n}$$

Weighted Mean: 
$$\overline{x} = \frac{\sum (x \cdot w)}{\sum w}$$

Mean of a Frequency Distribution: 
$$\bar{x} = \frac{\sum (x \cdot f)}{n}$$

Range = 
$$(Maximum entry) - (Minimum entry)$$

Population Variance: 
$$\sigma^2 = \frac{\sum (x - \mu)^2}{N}$$

Population Standard Deviation:

$$\sigma = \sqrt{\sigma^2} = \sqrt{\frac{\sum (x - \mu)^2}{N}}$$

Sample Variance: 
$$s^2 = \frac{\sum (x - \overline{x})^2}{n - 1}$$

Sample Standard Deviation: 
$$s = \sqrt{s^2} = \sqrt{\frac{\sum (x - \overline{x})^2}{n - 1}}$$

*Empirical Rule* (or 68-95-99.7 Rule) For data with a (symmetric) bell-shaped distribution:

- 1. About 68% of the data lies between  $\mu \sigma$  and  $\mu + \sigma$ .
- 2. About 95% of the data lies between  $\mu 2\sigma$  and  $\mu + 2\sigma$ .
- 3. About 99.7% of the data lies between  $\mu 3\sigma$  and  $\mu + 3\sigma$ .

**Chebychev's Theorem** The portion of any data set lying within k standard deviations (k > 1) of the mean is at

least 
$$1 - \frac{1}{k^2}$$
.

Sample Standard Deviation of a Frequency Distribution:

$$s = \sqrt{\frac{\sum (x - \overline{x})^2 f}{n - 1}}$$

Standard Score: 
$$z = \frac{\text{Value - Mean}}{\text{Standard deviation}} = \frac{x - \mu}{\sigma}$$

#### **CHAPTER 3**

Classical (or Theoretical) Probability:

$$P(E) = \frac{\text{Number of outcomes in event } E}{\text{Total number of outcomes}}$$
in sample space

Empirical (or Statistical) Probability:

$$P(E) = \frac{\text{Frequency of event } E}{\text{Total frequency}} = \frac{f}{n}$$

Probability of a Complement: P(E') = 1 - P(E)

Probability of occurrence of both events A and B:

$$P(A \text{ and } B) = P(A) \cdot P(B|A)$$

$$P(A \text{ and } B) = P(A) \cdot P(B) \text{ if } A \text{ and } B \text{ are independent}$$

Probability of occurrence of either A or B or both:

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$P(A \text{ or } B) = P(A) + P(B) \text{ if } A \text{ and } B \text{ are }$$
mutually exclusive

Permutations of n objects taken r at a time:

$$_{n}P_{r} = \frac{n!}{(n-r)!}$$
, where  $r \le n$ 

Distinguishable Permutations:  $n_1$  alike,  $n_2$  alike, ...,  $n_k$  alike:

$$\frac{n!}{n_1! \cdot n_2! \cdot n_2! \cdots n_k!},$$

where 
$$n_1 + n_2 + n_3 + \cdots + n_k = n$$

Combination of n objects taken r at a time:

$$_{n}C_{r} = \frac{n!}{(n-r)!r!}$$

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### **CHAPTER 4**

Mean of a Discrete Random Variable:  $\mu = \sum xP(x)$ 

Variance of a Discrete Random Variable:

$$\sigma^2 = \sum (x - \mu)^2 P(x)$$

Standard Deviation of a Discrete Random Variable:

$$\sigma = \sqrt{\sigma^2} = \sqrt{\sum (x - \mu)^2 P(x)}$$

Expected Value:  $E(x) = \mu = \sum xP(x)$ 

Binomial Probability of x successes in n trials:

$$P(x) = {}_{n}C_{x}p^{x}q^{n-x} = \frac{n!}{(n-x)!x!}p^{x}q^{n-x}$$

Population Parameters of a Binomial Distribution:

Mean: 
$$\mu = np$$
 Variance:  $\sigma^2 = npa$ 

Standard Deviation: 
$$\sigma = \sqrt{npq}$$

Geometric Distribution: The probability that the first success will occur on trial number x is  $P(x) = p(q)^{x-1}$ , where q = 1 - p.

Poisson Distribution: The probability of exactly x occurrences in an interval is  $P(x) = \frac{\mu^x e^{-\mu}}{x!}$ , where  $e \approx 2.71828$  and  $\mu$  is the mean number of occurences per interval unit.

#### **CHAPTER 5**

Standard Score, or z-Score:

$$z = \frac{\text{Value - Mean}}{\text{Standard deviation}} = \frac{x - \mu}{\sigma}$$

Transforming a z-Score to an x-Value:  $x = \mu + z\sigma$ 

**Central Limit Theorem** ( $n \ge 30$  or population is normally distributed):

Mean of the Sampling Distribution:  $\mu_{\overline{x}} = \mu$ 

Variance of the Sampling Distribution:  $\sigma_{\bar{x}}^2 = \frac{\sigma}{n}$ 

Standard Deviation of the Sampling Distribution (Standard Error):

$$\sigma_{\overline{x}} = \frac{\sigma}{\sqrt{n}}$$

z-Score = 
$$\frac{\text{Value - Mean}}{\text{Standard Error}} = \frac{\overline{x} - \mu_{\overline{x}}}{\sigma_{\overline{x}}} = \frac{\overline{x} - \mu}{\sigma/\sqrt{n}}$$

#### **CHAPTER 6**

*c*-Confidence Interval for  $\mu$ :  $\overline{x} - E < \mu < \overline{x} + E$ ,

where  $E = z_c \frac{\sigma}{\sqrt{n}}$  if  $\sigma$  is known and the population is

normally distributed or  $n \ge 30$ , or  $E = t_c \frac{s}{\sqrt{n}}$  if the population is normally or approximately normally distributed,  $\sigma$  is unknown, and n < 30

Minimum Sample Size to Estimate  $\mu$ :  $n = \left(\frac{z_c \sigma}{E}\right)^2$ 

Point Estimate for p, the population proportion of

successes: 
$$\hat{p} = \frac{x}{n}$$

*c*-Confidence Interval for Population Proportion p (when  $np \ge 5$  and  $nq \ge 5$ ):  $\hat{p} - E , where$ 

$$E = z_c \sqrt{\frac{\hat{p}\hat{q}}{n}}$$

Minimum Sample Size to Estimate p:  $n = \hat{p}\hat{q}\left(\frac{z_c}{E}\right)^2$ 

c-Confidence Interval for Population Variance  $\sigma^2$ :

$$\frac{(n-1)s^2}{\chi_R^2} < \sigma^2 < \frac{(n-1)s^2}{\chi_L^2}$$

*c*-Confidence Interval for Population Standard Deviation  $\sigma$ :

$$\sqrt{\frac{(n-1)s^2}{\chi_R^2}} < \sigma < \sqrt{\frac{(n-1)s^2}{\chi_L^2}}$$

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## CHAPTER 7

z-Test for a Mean  $\mu$ :  $z = \frac{\overline{x} - \mu}{\sigma / \sqrt{n}}$ , for  $\sigma$  known with a normal population, or for  $n \ge 30$ 

t-Test for a Mean  $\mu$ :  $t = \frac{\overline{x} - \mu}{s/\sqrt{n}}$ , for  $\sigma$  unknown,

population is normal or nearly normal, and n < 30. (d.f. = n - 1)

z-Test for a Proportion p (when  $np \ge 5$  and  $nq \ge 5$ ):

$$z = \frac{\hat{p} - \mu_{\hat{p}}}{\sigma_{\hat{p}}} = \frac{\hat{p} - p}{\sqrt{pq/n}}$$

Chi-Square Test for a Variance  $\sigma^2$  or Standard Deviation  $\sigma$ :

$$\chi^2 = \frac{(n-1)s^2}{\sigma^2}$$
 (d.f. =  $n-1$ )

### CHAPTER 8

Two-Sample z-Test for the Difference Between Means (Independent samples;  $n_1$  and  $n_2 \ge 30$  or normally distributed populations):

$$z=\frac{(\overline{x}_1-\overline{x}_2)-(\mu_1-\mu_2)}{\sigma_{\overline{x}_1-\overline{x}_2}},$$

where 
$$\sigma_{\overline{x}_1-\overline{x}_2} = \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$$

Two-Sample t-Test for the Difference Between Means (Independent samples from normally distributed populations,  $n_1$  or  $n_2 < 30$ ):

$$t = \frac{(\overline{x}_1 - \overline{x}_2) - (\mu_1 - \mu_2)}{\sigma_{\overline{x}_1 - \overline{x}_2}}$$

If population variances are equal, d.f. =  $n_1 + n_2 - 2$ 

$$\sigma_{\overline{x}_1 - \overline{x}_2} = \sqrt{\frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}} \cdot \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}.$$

If population variances are not equal, d.f. is the smaller of  $n_1 - 1$  or  $n_2 - 1$  and  $\sigma_{\overline{x}_1 - \overline{x}_2} = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$ .  $E = t_c s_e \sqrt{1 + \frac{1}{n} + \frac{n(x_0 - \overline{x})^2}{n \sum x^2 - (\sum x)^2}}$  (d.f. = n - 2)

t-Test for the Difference Between Means (Dependent

$$t = \frac{\overline{d} - \mu_d}{s_d / \sqrt{n}}$$
, where  $\overline{d} = \frac{\sum d}{n}$ ,  $s_d = \sqrt{\frac{\sum (d - \overline{d})^2}{n - 1}}$ 

and d.f. = 
$$n - 1$$

Two-Sample z-Test for the Difference Between Proportions  $(n_1\overline{p}, n_1\overline{q}, n_2\overline{p}, \text{ and } n_2\overline{q} \text{ must be at least 5})$ :

$$z = \frac{(\hat{p}_1 - \hat{p}_2) - (p_1 - p_2)}{\sqrt{\overline{p}\,\overline{q}\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}}, \text{ where } \overline{p} = \frac{x_1 + x_2}{n_1 + n_2}$$

## CHAPTER 9

Correlation Coefficient:

and  $\overline{q} = 1 - \overline{p}$ .

$$r = \frac{n\sum xy - (\sum x)(\sum y)}{\sqrt{n\sum x^2 - (\sum x)^2}\sqrt{n\sum y^2 - (\sum y)^2}}$$

t-Test for the Correlation Coefficient:

$$t = \frac{r}{\sqrt{\frac{1 - r^2}{n - 2}}} \quad \text{(d.f.} = n - 2)$$

Equation of a Regression Line:  $\hat{y} = mx + b$ ,

where 
$$m = \frac{n\sum xy - (\sum x)(\sum y)}{n\sum x^2 - (\sum x)^2}$$
 and

$$b = \overline{y} - m\overline{x} = \frac{\sum y}{n} - m\frac{\sum x}{n}$$

Coefficient of Determination:

$$r^{2} = \frac{\text{Explained variation}}{\text{Total variation}} = \frac{\sum (\hat{y}_{i} - \overline{y})^{2}}{\sum (y_{i} - \overline{y})^{2}}$$

Standard Error of Estimate: 
$$s_e = \sqrt{\frac{\sum (y_i - \hat{y}_i)^2}{n-2}}$$

c-Prediction Interval for y:  $\hat{y} - E < y < \hat{y} + E$ ,

$$E = t_c s_e \sqrt{1 + \frac{1}{n} + \frac{n(x_0 - \overline{x})^2}{n \sum x^2 - (\sum x)^2}} \quad (d.f. = n - 2)$$

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### **CHAPTER 10**

Chi-Square: 
$$\chi^2 = \sum \frac{(O-E)^2}{E}$$

Goodness-of-Fit Test: d.f. = k - 1

Test of Independence:

$$d.f. = (no. of rows - 1)(no. of columns - 1)$$

Two-Sample *F*-Test for Variances:  $F = \frac{s_1^2}{s_2^2}$ , where

$$s_1^2 \ge s_2^2$$
, d.f.<sub>N</sub> =  $n_1 - 1$ , and d.f.<sub>D</sub> =  $n_2 - 1$ 

One-Way Analysis of Variance Test:

$$F = \frac{MS_B}{MS_W}$$
, where  $MS_B = \frac{SS_B}{k-1} = \frac{\sum n_i (\overline{x}_i - \overline{\overline{x}})^2}{k-1}$ 

and 
$$MS_W = \frac{SS_W}{N-k} = \frac{\sum (n_i - 1)s_i^2}{N-k}$$

$$(d.f._N = k - 1, d.f._D = N - k)$$

## **CHAPTER 11**

Test Statistic for Sign Test:

When  $n \le 25$ , the test statistic is the smaller number of + or - signs.

When 
$$n > 25$$
,  $z = \frac{(x + 0.5) - 0.5n}{\frac{\sqrt{n}}{2}}$ , where x is the

smaller number of + or - signs and n is the total number of + and - signs.

Test Statistic for Wilcoxon Rank Sum Test:

$$z = \frac{R - \mu_R}{\sigma_R}$$
, where  $R = \text{sum of the ranks for the}$ 

smaller sample, 
$$\mu_R = \frac{n_1(n_1 + n_2 + 1)}{2}$$
,

$$\sigma_R = \sqrt{\frac{n_1 n_2 (n_1 + n_2 + 1)}{12}}$$
, and  $n_1 \le n_2$ 

Test Statistic for the Kruskal-Wallis Test:

Given three or more independent samples, the test statistic for the Kruskal-Wallis test is

$$H = \frac{12}{N(N+1)} \left( \frac{R_1^2}{n_1} + \frac{R_2^2}{n_2} + \dots + \frac{R_k^2}{n_k} \right)$$
$$-3(N+1). \quad (d.f. = k-1)$$

Spearman Rank Correlation Coefficient:

$$r_s = 1 - \frac{6\sum d^2}{n(n^2 - 1)}$$

Test Statistic for the Runs Test:

When  $n_1 \le 20$  and  $n_2 \le 20$ , the test statistic is G, the number of runs.

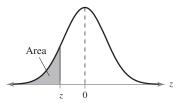
When  $n_1 > 20$  or  $n_2 > 20$ , the test statistic is

$$z = \frac{G - \mu_G}{\sigma_G}$$
, where  $G =$  number of runs,

$$\mu_G = \frac{2n_1n_2}{n_1 + n_2} + 1$$
, and

$$\sigma_G = \sqrt{\frac{2n_1n_2(2n_1n_2 - n_1 - n_2)}{(n_1 + n_2)^2(n_1 + n_2 - 1)}}$$

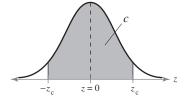
Table 4 — Standard Normal Distribution



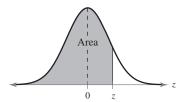
z	.09	.08	.07	.06	.05	.04	.03	.02	.01	.00
-3.4	.0002	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003
-3.3	.0003	.0004	.0004	.0004	.0004	.0004	.0004	.0005	.0005	.0005
-3.2	.0005	.0005	.0005	.0006	.0006	.0006	.0006	.0006	.0007	.0007
-3.1	.0007	.0007	.0008	.0008	.0008	.0008	.0009	.0009	.0009	.0010
-3.0	.0010	.0010	.0011	.0011	.0011	.0012	.0012	.0013	.0013	.0013
- 2.9	.0014	.0014	.0015	.0015	.0016	.0016	.0017	.0018	.0018	.0019
- 2.8	.0019	.0020	.0021	.0021	.0022	.0023	.0023	.0024	.0025	.0026
- 2.7	.0026	.0027	.0028	.0029	.0030	.0031	.0032	.0033	.0034	.0035
-2.6	.0036	.0037	.0038	.0039	.0040	.0041	.0043	.0044	.0045	.0047
- 2.5	.0048	.0049	.0051	.0052	.0054	.0055	.0057	.0059	.0060	.0062
- 2.4	.0064	.0066	.0068	.0069	.0071	.0073	.0075	.0078	.0080	.0082
- 2.3	.0084	.0087	.0089	.0091	.0094	.0096	.0099	.0102	.0104	.0107
- 2.2	.0110	.0113	.0116	.0119	.0122	.0125	.0129	.0132	.0136	.0139
- 2.1	.0143	.0146	.0150	.0154	.0158	.0162	.0166	.0170	.0174	.0179
-2.0	.0183	.0188	.0192	.0197	.0202	.0207	.0212	.0217	.0222	.0228
<b>– 1.9</b>	.0233	.0239	.0244	.0250	.0256	.0262	.0268	.0274	.0281	.0287
<b>-1.8</b>	.0294	.0301	.0307	.0314	.0322	.0329	.0336	.0344	.0351	.0359
<b>- 1.7</b>	.0367	.0375	.0384	.0392	.0401	.0409	.0418	.0427	.0436	.0446
- 1.6	.0455	.0465	.0475	.0485	.0495	.0505	.0516	.0526	.0537	.0548
<b>- 1.5</b>	.0559	.0571	.0582	.0594	.0606	.0618	.0630	.0643	.0655	.0668
- 1.4	.0681	.0694	.0708	.0721	.0735	.0749	.0764	.0778	.0793	.0808
- 1.3	.0823	.0838	.0853	.0869	.0885	.0901	.0918	.0934	.0951	.0968
- 1.2	.0985	.1003	.1020	.1038	.1056	.1075	.1093	.1112	.1131	.1151
- 1.1	.1170	.1190	.1210	.1230	.1251	.1271	.1292	.1314	.1335	.1357
<b>-1.0</b>	.1379	.1401	.1423	.1446	.1469	.1492	.1515	.1539	.1562	.1587
- 0.9	.1611	.1635	.1660	.1685	.1711	.1736	.1762	.1788	.1814	.1841
- 0.8	.1867	.1894	.1922	.1949	.1977	.2005	.2033	.2061	.2090	.2119
- 0.7	.2148	.2177	.2206	.2236	.2266	.2296	.2327	.2358	.2389	.2420
- 0.6	.2451	.2483	.2514	.2546	.2578	.2611	.2643	.2676	.2709	.2743
-0.5	.2776	.2810	.2843	.2877	.2912	.2946	.2981	.3015	.3050	.3085
-0.4	.3121	.3156	.3192	.3228	.3264	.3300	.3336	.3372	.3409	.3446
-0.3	.3483	.3520	.3557	.3594	.3632	.3669	.3707	.3745	.3783	.3821
-0.2	.3859	.3897	.3936	.3974	.4013	.4052	.4090	.4129	.4168	.4207
-0.1	.4247	.4286	.4325	.4364	.4404	.4443	.4483	.4522	.4562	.4602
-0.0	.4641	.4681	.4721	.4761	.4801	.4840	.4880	.4920	.4960	.5000

## **Critical Values**

Level of Confidence c	z <sub>c</sub>
0.80	1.28
0.90	1.645
0.95	1.96
0.99	2.575

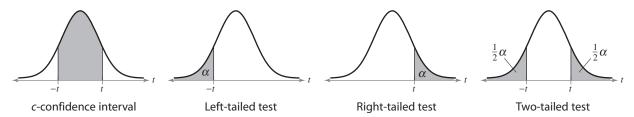


**Table 4** — **Standard Normal Distribution** *(continued)* 



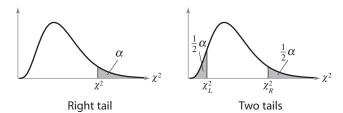
z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359
0.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753
0.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141
0.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517
0.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879
0.5	.6915	.6950	.6985	.7019	.7054	.7088	.7123	.7157	.7190	.7224
0.6	.7257	.7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549
0.7	.7580	.7611	.7642	.7673	.7704	.7734	.7764	.7794	.7823	.7852
0.8	.7881	.7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133
0.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.8790	.8810	.8830
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9279	.9292	.9306	.9319
1.5	.9332	.9345	.9357	.9370	.9382	.9394	.9406	.9418	.9429	.9441
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9686	.9693	.9699	.9706
1.9	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	.9761	.9767
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9916
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936
2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	.9951	.9952
2.6	.9953	.9955	.9956	.9957	.9959	.9960	.9961	.9962	.9963	.9964
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	.9973	.9974
2.8	.9974	.9975	.9976	.9977	.9977	.9978	.9979	.9979	.9980	.9981
2.9	.9981	.9982	.9982	.9983	.9984	.9984	.9985	.9985	.9986	.9986
3.0	.9987	.9987	.9987	.9988	.9988	.9989	.9989	.9989	.9990	.9990
3.1	.9990	.9991	.9991	.9991	.9992	.9992	.9992	.9992	.9993	.9993
3.2	.9993	.9993	.9994	.9994	.9994	.9994	.9994	.9995	.9995	.9995
3.3	.9995	.9995	.9995	.9996	.9996	.9996	.9996	.9996	.9996	.9997
3.4	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9998

Table 5— *t*-Distribution



	Level of						
	confidence, c	0.50	0.80	0.90	0.95	0.98	0.99
	One tail, $\alpha$	0.25	0.10	0.05	0.025	0.01	0.005
d.f.	Two tails, $lpha$	0.50	0.20	0.10	0.05	0.02	0.01
1		1.000	3.078	6.314	12.706	31.821	63.657
2		.816	1.886	2.920	4.303	6.965	9.925
3		.765	1.638	2.353	3.182	4.541	5.841
4		.741	1.533	2.132	2.776	3.747	4.604
5		.727	1.476	2.015	2.571	3.365	4.032
6		.718	1.440	1.943	2.447	3.143	3.707
7		.711	1.415	1.895	2.365	2.998	3.499
8		.706	1.397	1.860	2.306	2.896	3.355
9		.703	1.383	1.833	2.262	2.821	3.250
10		.700	1.372	1.812	2.228	2.764	3.169
11		.697	1.363	1.796	2.201	2.718	3.106
12		.695	1.356	1.782	2.179	2.681	3.055
13		.694	1.350	1.771	2.160	2.650	3.012
14		.692	1.345	1.761	2.145	2.624	2.977
15		.691	1.341	1.753	2.131	2.602	2.947
16		.690	1.337	1.746	2.120	2.583	2.921
17		.689	1.333	1.740	2.110	2.567	2.898
18		.688	1.330	1.734	2.101	2.552	2.878
19		.688	1.328	1.729	2.093	2.539	2.861
20		.687	1.325	1.725	2.086	2.528	2.845
21		.686	1.323	1.721	2.080	2.518	2.831
22		.686	1.321	1.717	2.074	2.508	2.819
23		.685	1.319	1.714	2.069	2.500	2.807
24		.685	1.318	1.711	2.064	2.492	2.797
25		.684	1.316	1.708	2.060	2.485	2.787
26		.684	1.315	1.706	2.056	2.479	2.779
27		.684	1.314	1.703	2.052	2.473	2.771
28		.683	1.313	1.701	2.048	2.467	2.763
29		.683	1.311	1.699	2.045	2.462	2.756
$\infty$		.674	1.282	1.645	1.960	2.326	2.576

Table 6— Chi-Square Distribution



Degrees of						α				
freedom	0.995	0.99	0.975	0.95	0.90	0.10	0.05	0.025	0.01	0.005
1	_		0.001	0.004	0.016	2.706	3.841	5.024	6.635	7.879
2	0.010	0.020	0.051	0.103	0.211	4.605	5.991	7.378	9.210	10.597
3	0.072	0.115	0.216	0.352	0.584	6.251	7.815	9.348	11.345	12.838
4	0.207	0.297	0.484	0.711	1.064	7.779	9.488	11.143	13.277	14.860
5	0.412	0.554	0.831	1.145	1.610	9.236	11.071	12.833	15.086	16.750
6	0.676	0.872	1.237	1.635	2.204	10.645	12.592	14.449	16.812	18.548
7	0.989	1.239	1.690	2.167	2.833	12.017	14.067	16.013	18.475	20.278
8	1.344	1.646	2.180	2.733	3.490	13.362	15.507	17.535	20.090	21.955
9	1.735	2.088	2.700	3.325	4.168	14.684	16.919	19.023	21.666	23.589
10	2.156	2.558	3.247	3.940	4.865	15.987	18.307	20.483	23.209	25.188
11	2.603	3.053	3.816	4.575	5.578	17.275	19.675	21.920	24.725	26.757
12	3.074	3.571	4.404	5.226	6.304	18.549	21.026	23.337	26.217	28.299
13	3.565	4.107	5.009	5.892	7.042	19.812	22.362	24.736	27.688	29.819
14	4.075	4.660	5.629	6.571	7.790	21.064	23.685	26.119	29.141	31.319
15	4.601	5.229	6.262	7.261	8.547	22.307	24.996	27.488	30.578	32.801
16	5.142	5.812	6.908	7.962	9.312	23.542	26.296	28.845	32.000	34.267
17	5.697	6.408	7.564	8.672	10.085	24.769	27.587	30.191	33.409	35.718
18	6.265	7.015	8.231	9.390	10.865	25.989	28.869	31.526	34.805	37.156
19	6.844	7.633	8.907	10.117	11.651	27.204	30.144	32.852	36.191	38.582
20	7.434	8.260	9.591	10.851	12.443	28.412	31.410	34.170	37.566	39.997
21	8.034	8.897	10.283	11.591	13.240	29.615	32.671	35.479	38.932	41.401
22	8.643	9.542	10.982	12.338	14.042	30.813	33.924	36.781	40.289	42.796
23	9.260	10.196	11.689	13.091	14.848	32.007	35.172	38.076	41.638	44.181
24	9.886	10.856	12.401	13.848	15.659	33.196	36.415	39.364	42.980	45.559
25	10.520	11.524	13.120	14.611	16.473	34.382	37.652	40.646	44.314	46.928
26	11.160	12.198	13.844	15.379	17.292	35.563	38.885	41.923	45.642	48.290
27	11.808	12.879	14.573	16.151	18.114	36.741	40.113	43.194	46.963	49.645
28	12.461	13.565	15.308	16.928	18.939	37.916	41.337	44.461	48.278	50.993
29	13.121	14.257	16.047	17.708	19.768	39.087	42.557	45.722	49.588	52.336
30	13.787	14.954	16.791	18.493	20.599	40.256	43.773	46.979	50.892	53.672
40	20.707	22.164	24.433	26.509	29.051	51.805	55.758	59.342	63.691	66.766
50	27.991	29.707	32.357	34.764	37.689	63.167	67.505	71.420	76.154	79.490
60	35.534	37.485	40.482	43.188	46.459	74.397	79.082	83.298	88.379	91.952
70	43.275	45.442	48.758	51.739	55.329	85.527	90.531	95.023	100.425	104.215
80	51.172	53.540	57.153	60.391	64.278	96.578	101.879	106.629	112.329	116.321
90	59.196	61.754	65.647	69.126	73.291	107.565	113.145	118.136	124.116	128.299
100	67.328	70.065	74.222	77.929	82.358	118.498	124.342	129.561	135.807	140.169