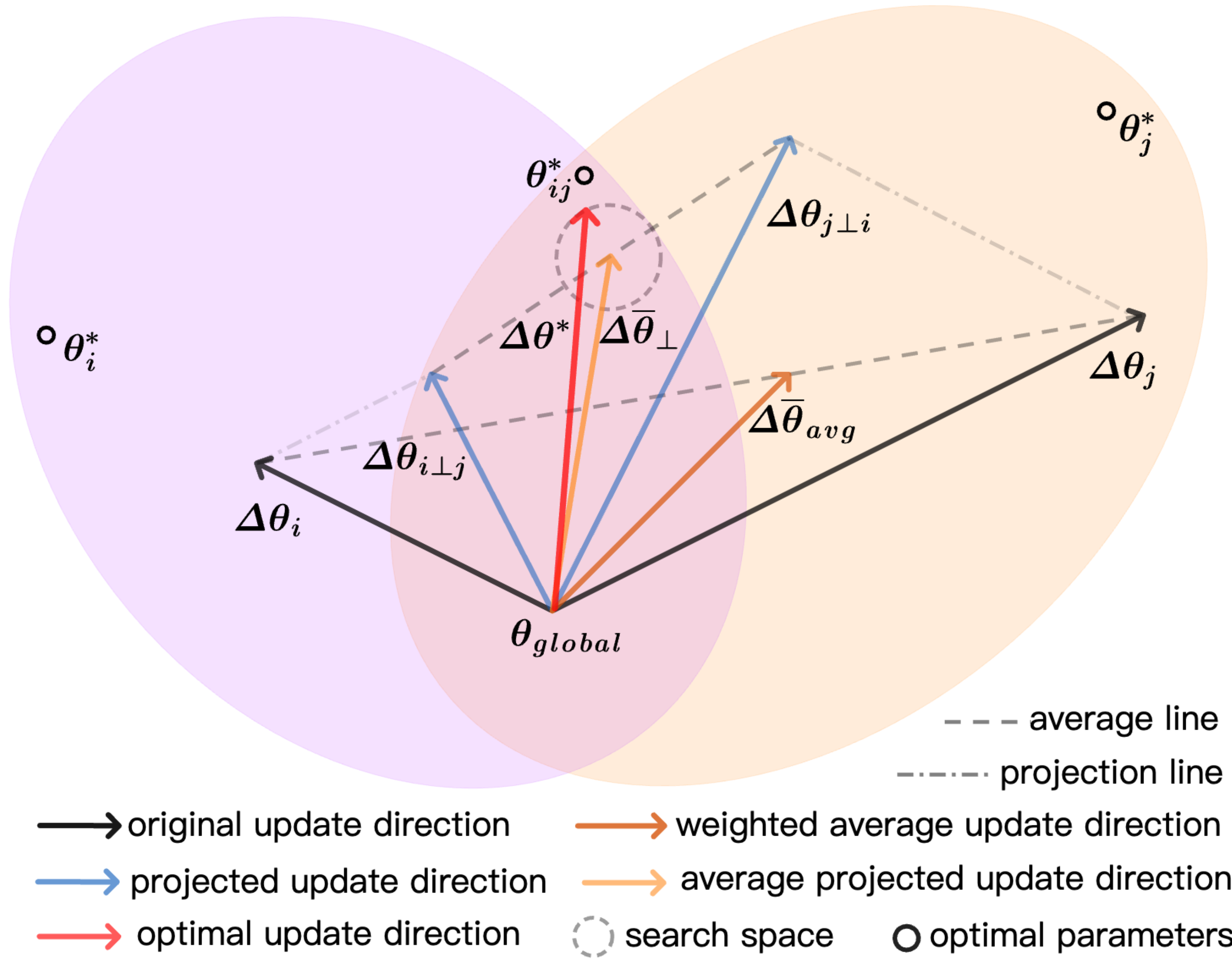


Introduction and Motivation

- **Personalized Federated Learning:** aims to learn a tailored model for each client while still benefiting from the global model to enhance their models and address data scarcity.
- **Key Challenge:** Negative transfer (NF) is a critical challenge in PFL, and existing methods primarily focus on adapting the local data distribution on the client side, **they only resist NF rather than fundamentally avoiding it.**



- **Motivation:** when $\Delta\theta_i \cdot \Delta\theta_j < 0$, the update from client i negatively impacts client j because it leads to an increase in the loss of client j , which is referred to as **client update conflict**.

$$\Delta\mathcal{L}_j = \mathcal{L}_j(h_j, \theta_g + \Delta\theta_i) - \mathcal{L}_j(h_j, \theta_g) = -\frac{1}{\alpha} \Delta\theta_i \cdot \Delta\theta_j \quad (1)$$

$$\Delta\mathcal{L}_{\text{total}} = -\frac{1}{\alpha} \sum_{i=1}^N \sum_{j=1}^N p_i p_j \Delta\theta_i \cdot \Delta\theta_j \quad (2)$$

The classical FedAvg $\Delta\bar{\theta}_{\text{avg}}$ tends to be dominated by the $\Delta\theta_j$ from clients with more data, leading to insufficient optimization for client i .

Contributions

- CONFREE is the first method to address client update conflicts in pFL. By optimizing global model aggregation, it provides each client with more effective and comprehensive global information.
- CONFREE is model-agnostic, which requires a single modification to the server aggregation program that can be easily applied to enhance various client-side personalization techniques.

Methodology

- **Guidance Vector:** minimizes negative conflicts with parameter updates from other clients.

$$\Delta\bar{\theta}_{\perp} = \frac{1}{N} \sum_{i=1}^N \left(\Delta\theta_i - \sum_{j \neq i, \cos \theta_{ij} < 0} \frac{\Delta\theta_i \cdot \Delta\theta_j}{\|\Delta\theta_j\|^2} \Delta\theta_j \right) \quad (3)$$

- **Optimization Objective:** maximize the worst local improvement among all clients.

$$\min \Delta\mathcal{L}_{\text{total}} \approx \max_{\mathbf{d} \in \Theta} \frac{1}{N} \sum_{j=1}^N \min_{j \in [N]} \mathbf{d} \cdot \Delta\theta_j \quad \text{s.t.} \quad \|\mathbf{d} - \Delta\bar{\theta}_{\perp}\| \leq c \|\Delta\bar{\theta}_{\perp}\|$$

- **Dual Problem:**

$$\min_{w \in \mathcal{W}, \lambda \geq 0} \max_{\mathbf{d} \in \Theta} \mathbf{d} \cdot \Delta\theta_w - \frac{\lambda}{2} (\|\mathbf{d} - \Delta\bar{\theta}_{\perp}\|^2 - c^2 \|\Delta\bar{\theta}_{\perp}\|^2) \quad (4)$$

where $\mathbf{d}^* = \Delta\bar{\theta}_{\perp} + \frac{c \|\Delta\bar{\theta}_{\perp}\|}{\|\Delta\theta_{w^*}\|} \Delta\theta_{w^*}$ and $\lambda = \frac{\|\Delta\theta_{w^*}\|}{c \|\Delta\bar{\theta}_{\perp}\|}$.

- **Final Objective Function:**

$$w^* = \arg \min_{w \in \mathcal{W}} \mathbf{d} \cdot \Delta\theta_w + c \|\Delta\bar{\theta}_{\perp}\| \|\Delta\theta_w\| \quad (5)$$

CONFREE

Input: N clients, local datasets $\{\mathcal{D}_1, \dots, \mathcal{D}_N\}$, learning rates $\{\eta, \alpha\}$, total communication rounds T .

Output: Conflict-free global aggregation parameter θ_g^{t+1} .

- 1: Initialize global parameter θ_g .
- 2: **for** each global iteration $t = 1, 2, \dots, T$ **do**
- 3: **for** client $i = 1, 2, \dots, N$ **in parallel do**
- 4: Update local head h_i^{t+1} via $h_i^{t+1} \leftarrow h_i^t - \eta \nabla_{h_i^t} \mathcal{L}_i(h_i^t, \theta_g^t; D_i)$
- 5: Update shared parameter θ_i^t via $\theta_i^t \leftarrow \theta_g^t - \alpha \nabla_{\theta_g^t} \mathcal{L}_i(h_i^{t+1}, \theta_g^t; D_i)$
- 6: Compute shared parameter update $\Delta\theta_i^t = \theta_i^t - \theta_g^t$.
- 7: **end for**
- 8: **for** each client update $\Delta\theta_i^t$ **do**
- 9: Adjust $\Delta\theta_i^t$ using projection for all $\Delta\theta_j^t$ (where $j \neq i$) with negative cosine similarity.
- 10: **end for**
- 11: Compute the conflict-free guidance vector by averaging the adjusted updates using $\Delta\bar{\theta}_{\perp} = \frac{1}{N} \sum_{i=1}^N \left(\Delta\theta_i - \sum_{j \neq i, \cos \theta_{ij} < 0} \frac{\Delta\theta_i \cdot \Delta\theta_j}{\|\Delta\theta_j\|^2} \Delta\theta_j \right)$.
- 12: Solve optimization problem to find w^* using $w^* = \arg \min_{w \in \mathcal{W}} \mathbf{d} \cdot \Delta\theta_w + c \|\Delta\bar{\theta}_{\perp}\| \|\Delta\theta_w\|$.
- 13: Compute λ and \mathbf{d}^* based on the solution.
- 14: **Server Aggregation:** $\theta_g^{t+1} \leftarrow \theta_g^t + \mathbf{d}^*$.
- 15: **end for**
- 16: **return** θ_g^{t+1} .

Empirical Results

Methods	Pathological heterogeneous		Practical heterogeneous ($\beta = 0.1$)					#S.	#T.
	Flowers102	CIFAR100	CIFAR10	CIFAR100	TINY	Flowers102			
Per-FedAvg	67.04	61.77	87.76	41.49	25.62	55.33	151.72	66.86	
+ CONFREE	67.64 ($\uparrow 0.60$)	62.45 ($\uparrow 0.68$)	88.23 ($\uparrow 0.47$)	41.76 ($\uparrow 0.27$)	27.42 ($\uparrow 1.80$)	55.96 ($\uparrow 0.63$)	148.19	67.38	
LG-FedAvg	63.89	63.32	89.23	47.63	33.75	51.48	148.39	46.71	
+ CONFREE	64.09 ($\uparrow 0.20$)	63.48 ($\uparrow 0.16$)	89.52 ($\uparrow 0.29$)	47.88 ($\uparrow 0.25$)	33.96 ($\uparrow 0.21$)	52.72 ($\uparrow 1.24$)	144.86	46.94	
APFL	68.87	63.53	89.45	54.18	41.16	63.65	292.85	56.27	
+ CONFREE	70.79 ($\uparrow 1.92$)	63.71 ($\uparrow 0.18$)	89.64 ($\uparrow 0.19$)	55.44 ($\uparrow 1.26$)	41.97 ($\uparrow 0.81$)	65.11 ($\uparrow 1.46$)	289.32	56.66	
FedROD	69.21	63.79	89.93	51.02	39.74	61.02	159.55	54.30	
+ CONFREE	69.56 ($\uparrow 0.35$)	64.02 ($\uparrow 0.23$)	90.80 ($\uparrow 0.87$)	52.57 ($\uparrow 1.55$)	40.98 ($\uparrow 1.24$)	61.52 ($\uparrow 0.50$)	156.02	54.81	
FedRep	68.62	67.41	90.40	51.33	41.72	57.52	151.52	56.90	
+ CONFREE	68.92 ($\uparrow 0.30$)	67.92 ($\uparrow 0.51$)	90.61 ($\uparrow 0.21$)	51.41 ($\uparrow 0.08$)	42.31 ($\uparrow 0.59$)	57.81 ($\uparrow 0.29$)	147.99	56.97	
FedCP	71.38	70.47	91.30	55.33	44.87	60.73	539.17	99.49	
+ CONFREE	71.73 ($\uparrow 0.35$)	70.98 ($\uparrow 0.51$)	91.72 ($\uparrow 0.42$)	55.68 ($\uparrow 0.35$)	45.62 ($\uparrow 0.75$)	61.51 ($\uparrow 0.78$)	535.64	99.59	
FedALA	68.82	67.33	90.67	57.24	44.56	62.92	683.23	55.91	
+ CONFREE	70.64 ($\uparrow 1.82$)	67.52 ($\uparrow 0.19$)	91.32 ($\uparrow 0.65$)	57.70 ($\uparrow 0.46$)	45.01 ($\uparrow 0.45$)	63.94 ($\uparrow 1.02$)	679.72	56.39	
FedPAC	74.48	72.60	90.86	61.94	46.63	68.56	160.01	110.67	
+ CONFREE	74.68 ($\uparrow 0.20$)	73.01 ($\uparrow 0.41$)	91.42 ($\uparrow 0.56$)	62.85 ($\uparrow 0.91$)	46.83 ($\uparrow 0.20$)	69.10 ($\uparrow 0.54$)	156.48	147.20	

Table 1: Comparison of eight SOTA methods combined with CONFREE. #S: communication overhead (MB), #T: computation overhead (s).

Methods	CIFAR100				Flowers102			
	C = 20		C = 60		C = 20		C = 60	
	P = 30%	P = 60%	P = 30%	P = 60%	P = 30%	P = 60%	P = 30%	P = 60%
APFL	52.85	53.64	43.56	44.02	62.92	63.94	45.88	50.31
+ CONFREE	53.49 ($\uparrow 0.64$)	54.11 ($\uparrow 0.47$)	44.90 ($\uparrow 1.34$)	44.46 ($\uparrow 0.44$)	64.14 ($\uparrow 1.22$)	64.48 ($\uparrow 0.54$)	49.30 ($\uparrow 3.42$)	52.53 ($\uparrow 2.22$)
FedROD	53.91	53.06	52.49	50.59	61.41	61.46	56.87	55.28
+ CONFREE	54.18 ($\uparrow 0.27$)	53.29 ($\uparrow 0.23$)	53.23 ($\uparrow 0.74$)	52.29 ($\uparrow 1.70$)	62.41 ($\uparrow 1.00$)	62.69 ($\uparrow 1.23$)	57.74 ($\uparrow 0.87$)	56.34 ($\uparrow 1.06$)
FedRep	50.95	51.03	44.36	44.04	58.44	57.42	49.40	48.72
+ CONFREE	51.11 ($\uparrow 0.16$)	51.39 ($\uparrow 0.36$)	44.60 ($\uparrow 0.24$)	44.37 ($\uparrow 0.33$)	58.93 ($\uparrow 0.49$)	58.10 ($\uparrow 0.68$)	49.93 ($\uparrow 0.53$)	49.16 ($\uparrow 0.44$)
FedCP	56.25	56.10	50.20	48.95	62.19	61.31	53.30	51.81
+ CONFREE	56.38 ($\uparrow 0.13$)	56.20 ($\uparrow 0.10$)	50.29 ($\uparrow 0.09$)	49.02 ($\uparrow 0.07$)	63.03 ($\uparrow 0.84$)	61.80 ($\uparrow 0.49$)	53.69 ($\uparrow 0.39$)	52.29 ($\uparrow 0.48$)
FedALA	56.62	56.97	58.01	58.15	62.19	62.48	56.54	58.71
+ CONFREE	56.98 ($\uparrow 0.36$)	57.45 ($\uparrow 0.48$)	58.40 ($\uparrow 0.39$)	58.60 ($\uparrow 0.45$)	63.50 ($\uparrow 1.31$)	63.70 ($\uparrow 1.22$)	59.33 ($\uparrow 2.79$)	60.88 ($\uparrow 2.17$)
FedPAC	61.45	61.61	61.93	62.84	67.49	68.08	58.95	59.04
+ CONFREE	62.09 ($\uparrow 0.64$)	62.23 ($\uparrow 0.62$)	62.63 ($\uparrow 0.70$)	63.34 ($\uparrow 0.50$)	67.83 ($\uparrow 0.34$)	68.86 ($\uparrow 0.78$)	60.20 ($\uparrow 1.25$)	60.78 ($\uparrow 1.74$)

Table 2: Comparison on different numbers of clients C and participation rates P on the CIFAR100 and Flowers102.

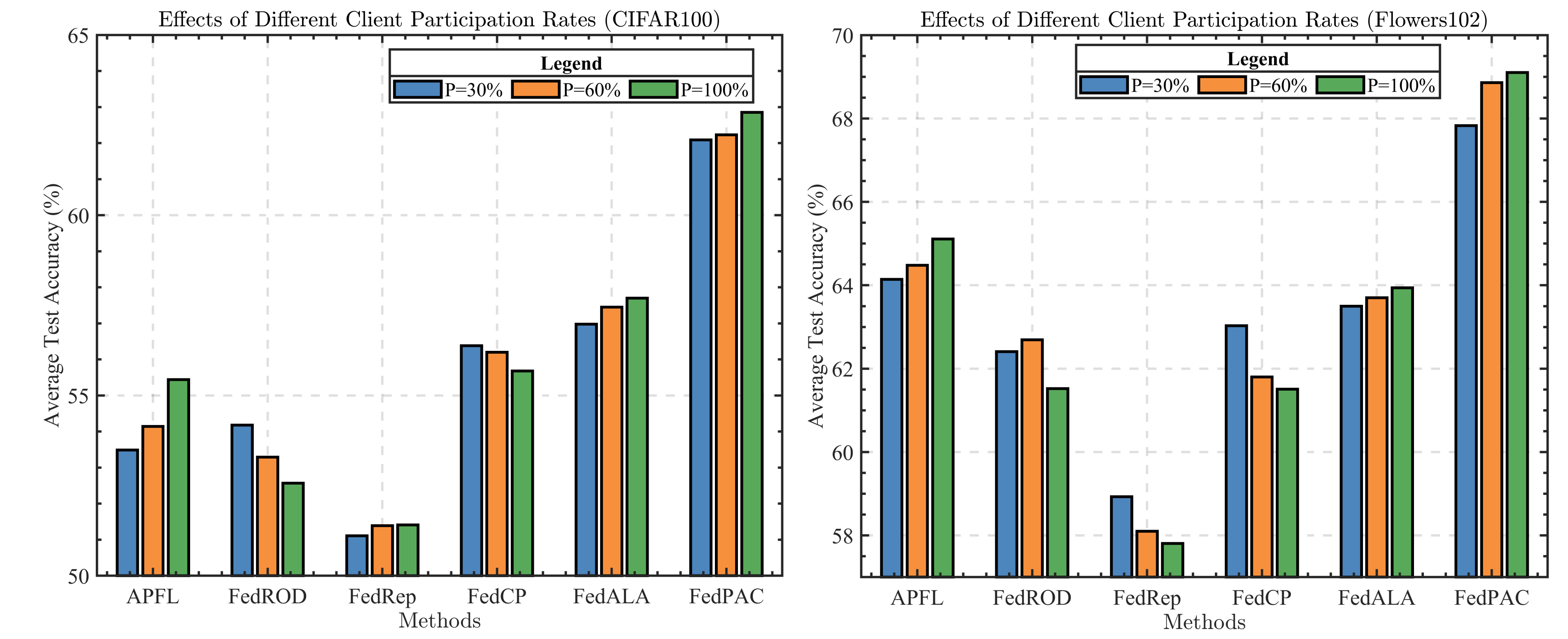


Figure 1: The average test accuracy of different client participation rates for six SOTA models combined with CONFREE on CIFAR100 and Flowers102.

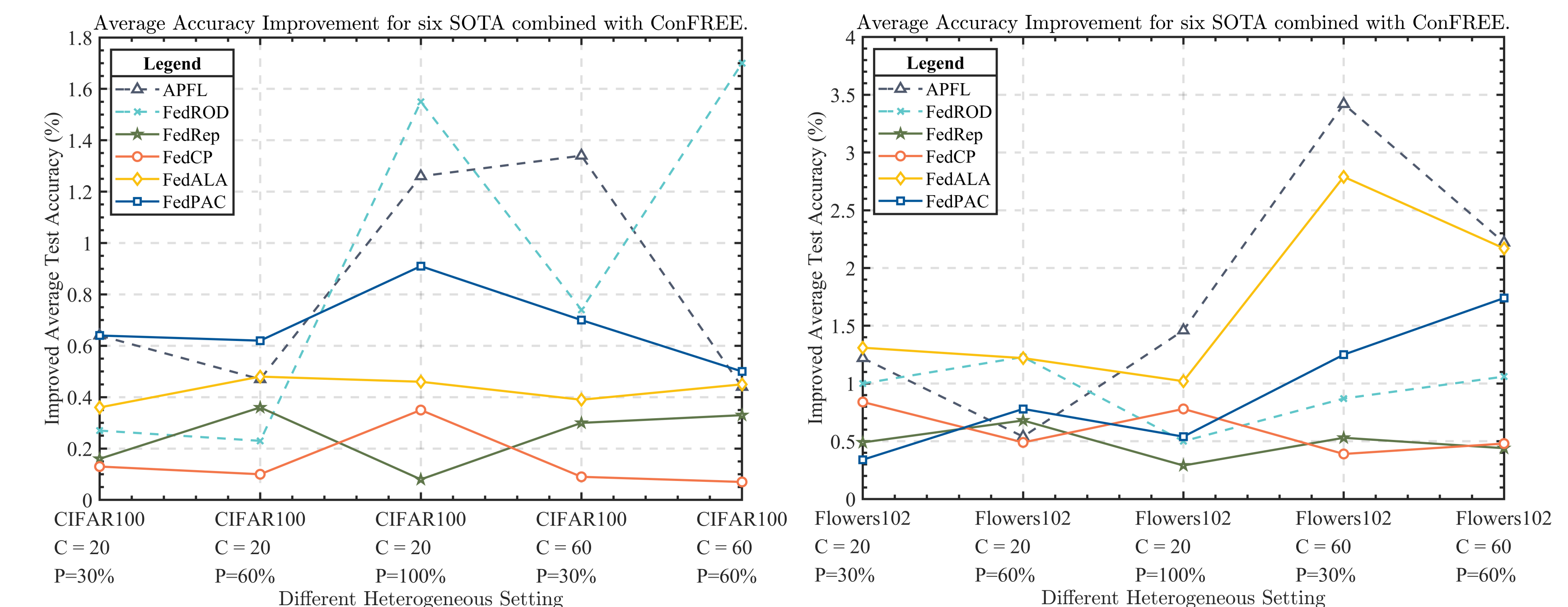


Figure 2: Comparison of six SOTA methods combined with CONFREE under different heterogeneous setting on CIFAR100 and Flowers102.