# Energy Usage Analysis

An Analysis of Solar Generation Effectiveness

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28 November 2024

## Introduction

## Scope & Objectives

About six years ago, I decided to remove my reliance on oil and to reduce my use of electricity imported from the National Grid. My aim was to try to reduce my energy costs and also to make a small contribution towards reducing the use of fossil fuels. So I obtained installation costs and received estimates of how much energy I could generate by using solar panels. The existing setup of oil powered central heating was replaced by the installation of a solar panel array, battery storage and ground source heat pump. I hoped to be able to only import from the grid when solar generation and storage failed to meet the demands of the house.

The main objective of this analysis is to see if the installation has met the predictions made during the sales process and to what extent I no longer have to rely on imported electricity, or, in other words, how effective the overall installation is. I used a sample of data for the month of September 2024 as a hopefully representative month (ie not the height of summer with peak solar generation and not winter with low solar generation and peak consumption).

In the final report, R code and outputs have been shown to demonstrate working, however to reduce the size of the document this is suppressed if repeating previous workings. All coding details are included in the submitted .rmd file. The main references sources used were: (Crawley, 2014), (Spiegel and Schiller, 2012) and (Hankin, 2024).

#### Summary of The Data

The data used in this analysis was collated from three sources and combined into a single .txt file, then imported into an R dataframe.

```
# Import all data from the tab-separated data file which is held in the data sub-folder
file_path <- './Data/Energy_September_2024.txt'
energy_df <- read.delim((file_path))
# Convert the string date to a valid date format
energy_df$Date <- as.Date(energy_df$Date, '%d/%m/%Y')</pre>
```

The data analysed comprises four parts, all daily data, with 30 observations, for each day in September 2024:

- Weather: Temperature and solar irradiance readings
- Energy Use: Electricity consumption
- Energy Source: The source of electricity: solar, battery or import from the grid

• Occupied: The approximate number of hours the house is occupied each day

All data and supporting files can be found online at Github<sup>1</sup>.

#### Weather

Weather data is sourced from the Balquhidder Weather Station<sup>2</sup> and consists of:

- Temp the mean daily temperature in °C. Derived from 6 readings taken at 4 hourly intervals over a 24 hour period
- Irrdnce irradiance, a measure of the solar energy experienced over a specified area, units are  $kW/m^2$  or  $W/m^2$  and this is used to calculate the theoretical power generated from an array of solar panels<sup>3</sup>

## Energy Use & Source

The distribution of power for the house is managed by a Tesla Powerwall and Controller and an iPhone app is used to monitor this, see Figure 1. All electricity data was downloaded via this app. The imported electricity data was in Wh but is usually reported in kWh.

Electricity used and where it is sourced from:

- *Home\_Total* total energy used by the house
- From Solar solar power generated by an array of 36 solar panels
- From\_PWall battery storage
- From\_Grid the national power grid

Electricity generated by the solar panels and where it is used (the controller intelligently makes the routing decisions):

- Solar\_Total total energy generated by the solar panels
- *To\_Home* consumption by the house
- $\bullet$   $To\_PWall$  for battery storage
- To Grid export to the national power grid

#### R Dataset

The sources of data were collated and loaded into an R dataset consisting of 30 observations and 12 columns, the first 4 rows of which are shown below:

```
# Display the first 4 rows of the data
head(energy_df,4)
```

##		Date	${\tt Home\_Total}$	From_Pwall	From_Solar	${\tt From\_Grid}$	Solar_Total	To_Home
##	1	2024-09-01	19048	11652	2180	5217	2360	2180
##	2	2024-09-02	11304	5224	1171	4909	1232	1171
##	3	2024-09-03	13867	7062	3690	3115	6372	3690
##	4	2024-09-04	16241	9315	4380	2546	6768	4380
##		To_Pwall To	o_Grid Temp	Irrdnce Occ	cupied			

<sup>&</sup>lt;sup>1</sup>https://github.com/StuartG24/Home-Solar-Usage-Analysis

<sup>&</sup>lt;sup>2</sup>https://www.blscc.org/weather

<sup>&</sup>lt;sup>3</sup>Wikipedia: https://en.wikipedia.org/wiki/Solar\_irradiance

##	1	172	9	12.9	73.18	24
##	2	50 1	l1	13.4	67.08	6
##	3	2664	18	9.9	269.36	0
##	4	2378	LO	9.5	344.50	0

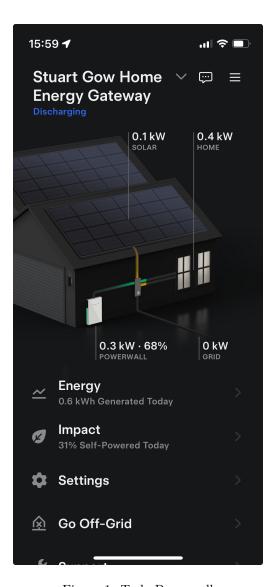


Figure 1: Tesla Powerwall

# Methods and Results

The data was analysed in three themes and each of these are described in the following sections. In summary:

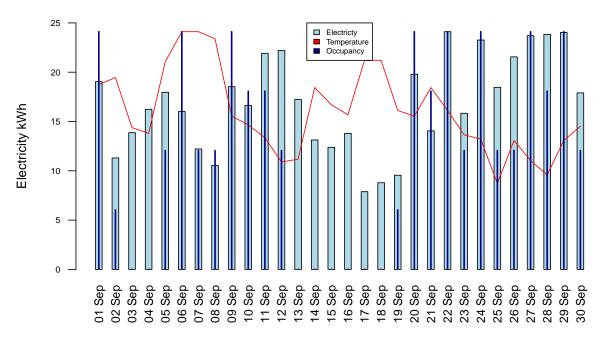
- Energy Consumption What drives energy consumption?
- Solar Generation Effectiveness How well does the installation meet sales promises?
- Solar Energy Sufficiency How well does solar generation meet the energy demand?

## **Energy Consumption**

Sanity Check & Visualisation

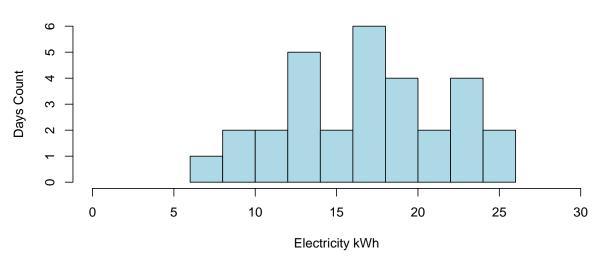
The energy consumption (electricity in kWh) of the house was compared to the weather and to occupancy and the figure below summarises this (nb: temperature and occupancy have been scaled to only show the relative size and so no values are displayed).

# **Daily Energy Consumption vs Weather & Occupancy**

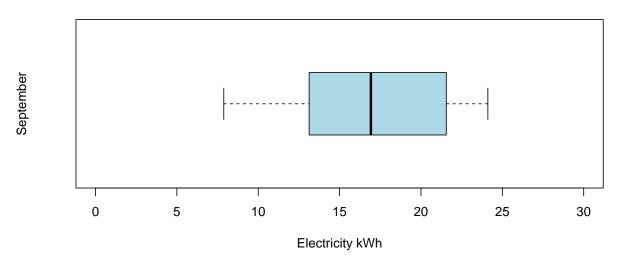


A quick examination of the energy demand was completed to visualise the distribution and identify any outliers.





# **Energy Consumption**

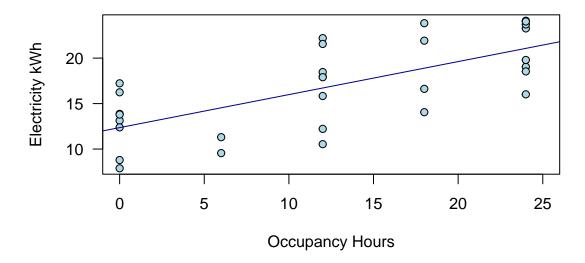


## Energy Demand Drivers

It was expected that the energy demand from the house would be related to the occupancy and the temperature, however visually there does not appear to be a strong link with temperature but potentially there is a link with occupancy. So three linear regressions were carried out to better identify any possible correlations.

First looking at the relationship between energy consumption and occupancy.

# **Daily Energy Demand vs Occupancy**



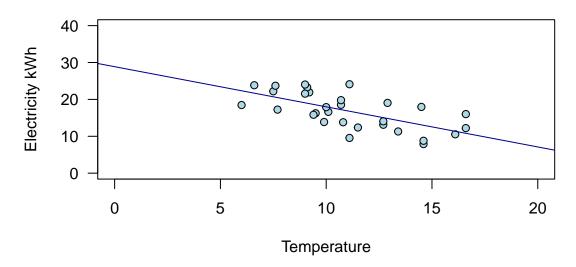
The scatter plot above is overlaid with the calculated linear regression line of: energy = 12.36 ( $\alpha$ ) + 0.36 ( $\beta$ ) \* occupancy. This linear regression calculation is used to see how strong the relationship is between a predictor variable (occupancy) and a response variable (energy consumption). The null hypothesis is that there is no relationship (no correlation) between energy consumption and occupancy and that the slope ( $\beta$ ) of the line is zero, or:

$$H_0: \beta = 0$$

The p-value calculated for the regression model is the probability, if  $H_0$  is true, of the observation or a an observation more extreme. Here more extreme is  $\beta$  greater than 0. The calculated p-value for the regression fit above was 2.24e-05 with an adjusted R-squared of 0.46. The p-value is less than the 5% critical value and so we can reject  $H_0$  and infer that energy and occupancy are correlated, however the relative low value of adjusted R-squared suggests that the correlation is not very strong.

Then looking at the relationship between energy demand and temperature (NB: same R Code so not printed to save space).





The scatter plot above is overlaid with the calculated linear regression line of:  $28.87 (\alpha) + -1.09 (\beta)$  \* temperature. In the same way as previously, the p-value was calculated to test a similar null hypothesis and determine if their is a correlation between energy consumption and temperature. This calculated p-value was 0.00011 with an adjusted R-squared of 0.4. Here the p-value is less than the 5% critical value and so we can reject  $H_0$  and infer that energy and temperature are inversely correlated, however the relative low value of adjusted R-squared suggests that the correlation is not very strong.

Then a multi-linear regression was performed looking at the relationship between energy demand and temperature plus occupancy (NB: A three dimensional scatter plot was not attempted).

```
# Multiple linear regression for energy and occupancy + temperature
regression_model <- lm(energy_df$Home_Total/1000 ~ energy_df$Temp + energy_df$Occupied)
regression_summary <- summary((regression_model))
alpha <- regression_summary$coefficients["(Intercept)", "Estimate"]
beta0 <- regression_summary$coefficients["energy_df$Occupied", "Estimate"]
p_value0 <- regression_summary$coefficients["energy_df$Temp", "Estimate"]
beta1 <- regression_summary$coefficients["energy_df$Temp", "Estimate"]
p_value1 <- regression_summary$coefficients["energy_df$Temp", "Pr(>|t|)"]
adj_r_squared <- regression_summary$adj.r.squared
#print(sprintf("Alpha: %.3f, Beta Occupancy: %.3f, Beta Temp: %.3f", alpha, beta0, beta1))
#print(sprintf("p-value Occp: %.4f, p-value Temp: %.4f, Adj R-Squared: %.3f", p_value0, p_value1, adj_r</pre>
```

The regression line determined was energy = 23.45 ( $\alpha$ ) + 0.33 ( $\beta$ ) \* occupancy + -0.97 ( $\beta$ ) \* temperature This fit had a p-value of 7.59e-08 for occupancy and 3.5e-07 for temperature and adjusted R-squared of 0.79. Here both p-values are less than the 5% critical value and so we can reject  $H_0$  and infer that energy and occupancy plus temperature (inversely) are correlated, the high value of adjusted R-squared suggests that the correlation is quite strong.

## Solar Generation Effectiveness

Background

The amount of energy generated by solar panels is a function of their size and the level of sunshine received, measured by irradiance. There is also a loss factor that reflects several things, such as the efficiency of the solar panels and the invertor. Additionally, irradiance observations (and forecasts) use data from local weather stations which may not experience the same shading from the sun as that experienced at the site of the solar panels.

```
Power(kWh) = Area(m^2) * Irradiance(kWh/m^2) * LossFactor
```

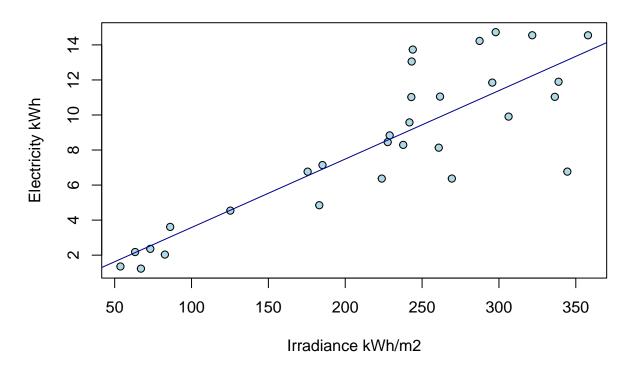
```
# The installation assumptions
solar_panels_count <- 36
solar_panels_area <- solar_panels_count * 2
solar_panels_max <- solar_panels_count * 275
solar_estimated_pa <- 7920
loss_factor <- solar_estimated_pa / solar_panels_max
irradiance_assumed <- solar_panels_max / solar_panels_area</pre>
```

As part of the sales process, estimates were provided of the forecast annual generation power for the proposed solar array. The forecast figures were 7,920 kWh pa using an area of 72  $m^2$ , irradiance 137.5 kWh/ $m^2$  pa and a loss factor of 0.8. Using the September observations of irradiance and actual generated solar energy, the effectiveness of the installation can be compared to these estimates (sales promises). It is very likely that the sales estimates were optimistic.

Sanity Check - Link Between Energy Generation & Irradiance

It is expected that solar generation is strongly related to irradiance and this was checked using a scatter plot and linear regression.

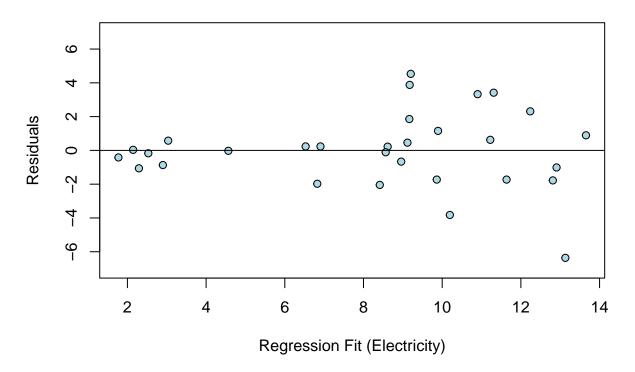
# Link Between Daily Solar Energy and Irradiance



```
alpha <- regression_summary$coefficients["(Intercept)", "Estimate"]
beta0 <- regression_summary$coefficients["energy_df$Irrdnce", "Estimate"]
p_value1 <- regression_summary$coefficients["energy_df$Irrdnce", "Pr(>|t|)"]
adj_r_squared <- regression_summary$adj.r.squared
#print(sprintf("Alpha: %.3f, Beta Irradiation: %.3f", alpha, beta0))
#print(sprintf("p-value Irradiation: %.4f, Adj R-Squared: %.3f", p_value0, adj_r_squared))</pre>
```

The scatter plot and linear regression confirmed the relationship, with a p-value < 0.005 and with a high adjusted R-squared of 0.71. Although the scatter plot does show that with higher levels of irradiance there is an increase in size and spread of the residuals and this is confirmed in the additional plot below. (NB: the regression calculation was repeated using log values and the regression fit was slightly improved, but to aid interpretation non-log values are reported here). This may have an impact on further analysis.

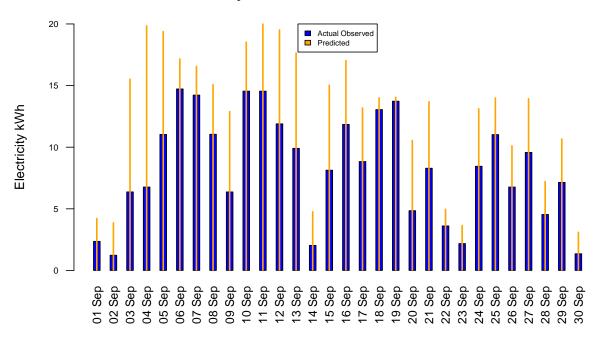
# **Residuals for The Calculated Regression Fit**



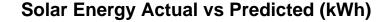
## $Evaluate\ Effectiveness$

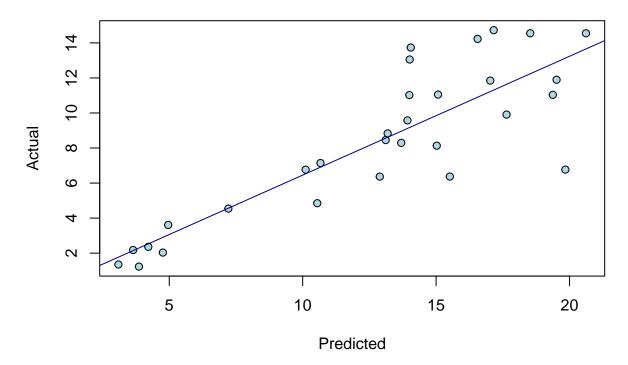
Using the formulae above and with the irradiance observations during September, the sales prediction for daily solar energy were calculated and compared with the actual energy generated. The means for the month are 12.8 kWh and 8.35 respectively. The daily totals are shown in the plot below and this clearly shows that the predicted generation is higher than the actual, although the differences do vary.





Further analysis was completed to better understand this. A scatter plot below shows the relationship between actual and predicted energy generation.





As expected the actual generated solar energy and predicted do appear to have a strong relationship, with a p-value < 0.005 and a high adjusted r-squared 0.71. (NB: with a similar spread of residuals as generation increases with higher irradiance).

Evaluate Effectiveness - T-Test

To try to better understand the relationship between the actual and predicted energy, a t-test was completed. The null hypothesis is that the installation performs as well as the sales promises; specifically that the average daily energy production in September  $\mu_{act}$  is the same as that promised (expected)  $\mu_{exp}$ .

$$H_0: \mu_{act} = \mu_{exp}$$

the alternative hypothesis is that the installation does not perform as promised

$$H_1: \mu_{act} < \mu_{exp}$$

A t-test was performed to evaluate  $H_0$  and to calculate the p-value which is the probability, if  $H_0$  is true, of obtaining the observation, or an observation more extreme. In this case more extreme is that the actual mean observed is less than the expected mean because we suspect that the installation does not perform as well as the sales promises; so a one-tailed paired test was used. Log values were used to make both samples closer to a normal distribution.

```
# Evaluate the T-Test
#t_test_result <- t.test(energy_df$Solar_Total/1000, solar_predicted, alternative = "less", paired = TR
t_test_result <- t.test(log10(energy_df$Solar_Total/1000), log10(solar_predicted), alternative = "less"</pre>
```

The p-value is < 0.005 which is statistically significant and the null hypothesis can be rejected at the 5% critical level. From this we can infer that the installation is not generating solar energy as effectively as originally promised.

Evaluate Effectiveness - Binomial Probability

```
# How often is the generated energy close to the predicted value?
# Number of days generated is within 75% of the predicted value for the observed days
nearPredicted <- energy_df$Solar_Total/1000 >= (0.75 * solar_predicted)
observedSuccess <- sum(nearPredicted)
p_value <- sum(dbinom(0:observedSuccess,30,0.5))

lower <- qbinom(0.025,30,0.5)
higher <- qbinom(0.975,30,0.5)</pre>
```

The above analysis strongly supports the view that the sales promises have not been met, however it is not clear why this is. Inefficiencies in the solar panels and invertor have already been reflected in the prediction calculation loss factor, so possibly the sales optimism is in the use of ambitious irradiance estimates compared to what was actually experienced during September 2024. To explore this, a view was taken that it would be an acceptable target to achieve 75% of what was predicted (a definition of 'success'). In September, this occurred on 6 days out of 30.

The null hypothesis to test the observations is that 'success' is achieved on on as many days as not;  $H_0$ : p(success) = 0.5. Success or failure can be considered as a binomial distribution, Bin(30, 0.5) and the probability of achieving the observed successes then calculated. The p-value is the probability, if the null hypothesis is true, of the observation or a more extreme observation. Here the more extreme observation is less than 6 days of 'success'. The calculated p-value is 0.001 which is below the critical value of 5% and therefore we can reject the null hypothesis and infer that the predicted energy is not met even at 75% of the predicted energy amount. Looking at this in another way, for  $H_0$  not to be rejected would require that 'success' is achieved on between 10 to 20 days per month; so the actual 6 days is well outside this range.

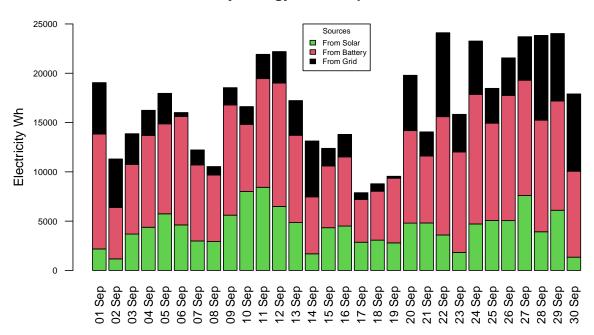
## Solar Energy Sufficiency

## Visual Examination

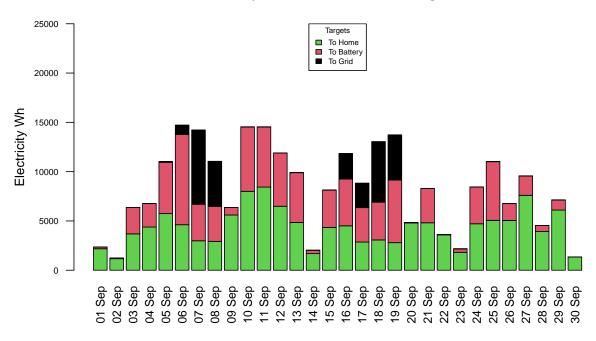
The energy demands of the house were examined to see how well these were met by solar generated electricity and how much any shortfalls needed to covered by imported electricity. The first stacked bar plot below shows the daily total energy consumed and how much is provided by: solar generation; the battery; or imported electricity. The second plot shows the daily total solar energy generated and where this is distributed to.

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# **Daily Energy Consumption & Sources**



# **Daily Solar Generation & Target**



# Calculate how the energy is consumed and distributed
average\_solar\_percent <- mean(c(energy\_df\$From\_Solar / energy\_df\$Home\_Total)) \* 100
solar\_home\_percent <- mean(c(energy\_df\$To\_Home / energy\_df\$Solar\_Total)) \* 100</pre>

```
solar_powerwall_percent <- mean(c(energy_df$To_Pwall / energy_df$Solar_Total)) * 100
solar_grid_percent <- mean(c(energy_df$To_Grid / energy_df$Solar_Total)) * 100</pre>
```

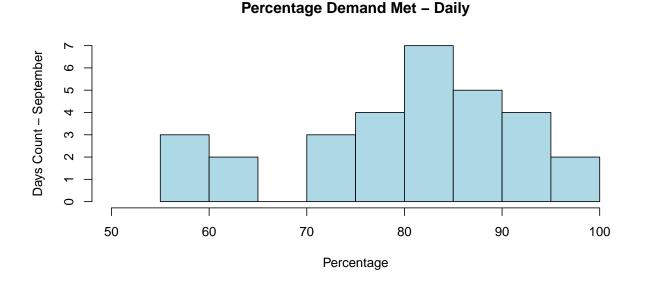
The first bar plot appears to clearly show that the generated solar energy is not sufficient to meet the total consumption needs, on average it only meets 26% of the daily demand. However, this is misleading as generated solar energy is often first stored in the battery for later use (it is sometime also exported to the gird if the battery becomes full). The second bar plot shows this more clearly, with solar energy distributed to the home, the battery or exported to the grid on average: 62%, 30%, and 8% respectively.

Successfully Meeting Demand - Binomial Probability

```
# Calculate an alternative approximation for solar generation
approximation_solar <- energy_df$Home_Total - energy_df$From_Grid
demand_met_percent <- (approximation_solar / energy_df$Home_Total) * 100
meanD <- mean(demand_met_percent)
sdD <- sd(demand_met_percent)</pre>
```

To take into account battery storage, an alternative approximation of how well the solar generation meets the needs of the house's energy consumption is to look at how much usage is catered for without any import from the grid. Using this approximation, the plot below shows the distribution of the percentage of demand that is met daily by solar generation in September. Across the month, on average, 80% of the demand is met and the range is from 56% up to 98%.

??? Also, there are 8 days when under 75% of the demand is met.



# A reasonable target for solar generation is to regularly meet 90% of the demand. A null hypothesis to test the observations is that average demand ( $\mu_{demand}$ ) met is 90%, ie $H_0$ : $\mu_{demand} = 90\%$ . The p-value is the probability, if $H_0$ is true, of an observation or an observation more extreme; here more extreme is $\mu_{demand}$ more than 90%. The distribution here approximates to a normal distribution N(80, 11.5) and using this the calculated p-value is 0.192 which is above the critical value of 5% and therefore we cannot reject the null hypothesis.

Successfully Meeting Demand - Fisher's Exact Test

In a previous section, looking at energy consumption, it appeared that occupancy was the bigger predictor of daily energy use. So it is interesting to see the relationship between successfully meeting demand (again, at > 90%) and significant occupancy (say, occupied > 50% of the day). For September, the true/false occurrence of meeting demand and of being occupied were determined and a contingency table prepared.

```
# Prepare a contingency table looking at meeting demand vs occupation

# Determine true / false for each combination
demand_met <- ((energy_df$Home_Total - energy_df$From_Grid) / energy_df$Home_Total) >= 0.90
occupied <- (energy_df$Occupied / 24) > 0.5
demandT_occpT <- sum(demand_met & occupied)
demandT_occpF <- sum(demand_met & !occupied)
demandF_occpT <- sum(!demand_met & occupied)
demandF_occpF <- sum(!demand_met & !occupied)

# Create matrix and display
contingency_table <- matrix(c(demandT_occpT,demandT_occpF,demandF_occpT,demandF_occpF), 2, 2, byrow=TRU
dimnames(contingency_table) <- list(Demand_Met=c(TRUE,FALSE), Occupied=c(TRUE,FALSE))
print(contingency_table)</pre>
## Occupied
## Demand_Met TRUE FALSE
```

The null hypothesis to consider is

2

10

4

14

TRUE

FALSE

##

##

```
H_0: p(demandmet|occupied) = p(demandmet|\overline{occupied})
```

The contingency table is used to perform a Fisher's exact test to determine the p-value which is the probability, if the null hypothesis is true, of obtaining the observation, or an observation more extreme. In this case more extreme is that demand is met less frequently, so a one-sided test is used.

```
# Perform Fisher's Exact Test - a one-sided test
result = fisher.test(contingency_table, alternative = "less")
p_value_f = result$p.value
```

The results of the one-sided Fisher's exact test gave a p-value of 0.545, this is above the critical 5% value and so we cannot reject the null hypothesis; there is no evidence to suggest that the demand is not met when occupied. This does seem surprising given the visualisation.

# Conclusions

- eg what conclusions were unexpected or surprising
- what have you learned from the data
- eg how has statistics helped you understand the data
- (conclusions are supported in the main body of the text)

xxxxx - Energy Consumption - What drives energy consumption? - Solar Generation Effectiveness - How well does the installation meet sales promises? - Solar Energy Sufficiency - How well does solar generation meet the energy demand?

# **Energy Consumption**

- Analysis showed that energy consumption is strongly linked to a combination of temperature and occupancy
- However the link with temperature only was surprisingly weak
  - The temperature in September was only in the range 6 to 17 with a mean of 11 and this is not very extreme.
  - Good insulation with the above may have reduced the impact, colder weather will have a bigger impact, the calcuated regression line suggesst this with an aenergy demand of nearl 30 kWh at freezing point
  - Occupancy also not strong but similarly not big temperature demands, also good insulation and heating left at a constant level so just utilities such as washing and cooking and lighting, tv etc which is probably lower than the heating?

## Solar Generation Effectiveness

- Analysis showed that the solar power generated is consistently less than that predicted during the month of September . . . but not why? . . . is it ineficciency or is it overforecast of irradiance?
- ?? probably throughout the year but only have monthly
- ?? but is this caused by inefficiency in the generation equipment or is it caused because the irradiance experienced is less than that predicted? don't have annual irradiance and generation figures to determine this

#### Solar Energy Sufficiency

- ?? looks like majority of demands are met
- ?? but a surprising statistical result

#### ??????? further work

?? Increased battery will smooth out across days? forecast storage/impact .. but can't see the intra-day detail to better analyse ?? Predict full year / annual generation using non September ?? monthly irradiance data: https://re.jrc.ec.europa.eu/pvg\_tools/en/#MR ?? box plots

##?? Discussion

TO DO: Structure into two sections

##?? Conclusion

# References

Crawley, M.J. (2014) Statistics: An introduction using R. 2nd Edition. John Wiley & Sons.

Hankin, R. (2024) 'Applied Statistics'. University of Stirling.

Spiegel, M.R. and Schiller, J. (2012) Schaum's Outline Probability and Statistics. 4th edn. McGraw Hill.