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State	Finished
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Time taken	4 mins 22 secs
Grade	10.00 out of 10.00 (100%)

Question 1

Correct

1.00 points out of 1.00

Which of the following are not true of a max-heap held in an array A?

- ☐ a. Each node is the root of its own heap.
- ☐ b. The largest element can be found in $O(1)$ time.
- ☐ c. The smallest element is contained in the last half of the array.
- ☐ d. The smallest element can be found in $O(n)$ time.
- ☒ e. All of the above are true. ✓
- ☐ f. None of the above are true.

Your answer is correct.

The correct answer is:

All of the above are true.

Question 2

Correct

1.00 points out of 1.00

What is the height of a heap with exactly 2^n nodes?

- ☐ a. $2n$
- ☒ b. n ✓
- ☐ c. None of the above
- ☐ d. $n-1$
- ☐ e. $\lg n$

Your answer is correct.

The correct answer is:

n

Question 3

Correct

1.00 points out of 1.00

If the array [12, 6, 8, 3, 7, 5] is meant to represent a max heap, which node violates the heap property?

- ☐ a. The node containing 12
- ☒ b. The node containing 6 ✓
- ☐ c. The node containing 8
- ☐ d. The node containing 3
- ☐ e. The node containing 7
- ☐ f. The node containing 5

Your answer is correct.

The correct answer is:

The node containing 6

Question 4

Correct

1.00 points out of 1.00

If the array [12, 6, 8, 3, 7, 5] is meant to represent a max heap, and If Max-Heapify is called on the node that violates the heap property, what is the resulting correct max heap?

- ☐ a. [12, 8, 6, 3, 7, 5]
- ☐ b. [12, 6, 8, 3, 7, 5]
- ☐ c. [12, 8, 7, 6, 5, 3]
- ☒ d. [12, 7, 8, 3, 6, 5] ✓
- ☐ e. None of the above.

Your answer is correct.

The correct answer is:

[12, 7, 8, 3, 6, 5]

Question 5

Correct

1.00 points out of 1.00

Is an array sorted in descending order a max heap, and is an array storing a correct max heap sorted in descending order?

- ☒ a. The sorted array is a max heap, but the max heap does not necessarily contain the numbers sorted in descending order. ✓
- ☐ b. The max heap contains the numbers sorted in descending order, but the sorted array is not necessarily a max heap.
- ☐ c. Both of the above are true.
- ☐ d. Neither of the above are true.

Your answer is correct.

The correct answer is:

The sorted array is a max heap, but the max heap does not necessarily contain the numbers sorted in descending order.

Question 6

Correct

1.00 points out of 1.00

Why is the time complexity of Max-Heapify $O(h)$ and not $O(h^2)$?

- ☐ a. The worst case is that the height of the heap is $O(\lg n)$
- ☒ b. $O(h)$ implies an upper and lower bound of h swaps. In many cases there will be 0 swaps, so h is only an upper bound, not a lower bound. ✓
- ☐ c. Max-Heapify will always swap at least 2 nodes.
- ☐ d. All of the above.
- ☐ e. None of the above.

Your answer is correct.

The correct answer is:

$O(h)$ implies an upper and lower bound of h swaps. In many cases there will be 0 swaps, so h is only an upper bound, not a lower bound.

Question 7

Correct

1.00 points out of 1.00

What is the time complexity to compute a median if Heapsort is used to sort the array and the middle item is returned?

- ☐ a. $O(n)$
- ☒ b. $O(n \lg n)$ ✓
- ☐ c. $O(n^2)$
- ☐ d. $O(n^3)$
- ☐ e. None of the above

Your answer is correct.

The correct answer is:

$O(n \lg n)$

Question 8

Correct

1.00 points out of 1.00

If one unit of space is the amount of memory required to hold 1 item being sorted, and n items are being sorted, how much space does Heapsort use?

- ☒ a. $n+1$ ✓
- ☐ b. $2n$
- ☐ c. $n \lg n$
- ☐ d. n^2
- ☐ e. None of the above

Your answer is correct.

The correct answer is:

$n+1$

Question 9

Correct

1.00 points out of 1.00

What is the time complexity of the maximum operation (the operation that returns the largest element in the queue) of a priority queue?

- ☒ a. $O(1)$ ✓
- ☐ b. $O(n)$
- ☐ c. $O(2n)$
- ☐ d. $O(n \lg n)$
- ☐ e. $O(n^2)$

Your answer is correct.

The correct answer is:

$O(1)$

Question 10

Correct

1.00 points out of 1.00

What is the time complexity of Heapsort on an already-sorted array?

- ☐ a. $O(1)$
- ☐ b. $O(n)$
- ☐ c. $O(2n)$
- ☒ d. $O(n \lg n)$ ✓
- ☐ e. $O(n^2)$

Your answer is correct.

The correct answer is:

$O(n \lg n)$