

QUICKSORT

CS340

Quicksort

- Like mergesort is a recursive algorithm
- **Divide:** Partition (rearrange) the array $A[p..r]$ into two (possibly empty) subarrays $A[p..q]$ and $A[q+1..r]$ such that each element of $A[p..q-1]$ is less than or equal to $A[q]$, which is, in turn, less than or equal to each element of $A[q+1..r]$. Compute the index q as part of this partitioning procedure.
- **Conquer:** Sort the two subarrays $A[p..q-1]$ and $A[q+1..r]$ by recursive calls to quicksort.
- **Combine:** The subarrays are already sorted, no work is needed to combine them.

Quicksort

QUICKSORT(A, p, r)

1 **if** $p < r$

2 $q = \text{PARTITION}(A, p, r)$

3 QUICKSORT($A, p, q - 1$)

4 QUICKSORT($A, q + 1, r$)

To sort an entire array A , the initial call is QUICKSORT($A, 1, A.length$).

Partitioning the Array

PARTITION(A, p, r)

1 $x = A[r]$

2 $i = p - 1$

3 **for** $j = p$ **to** $r - 1$

4 **if** $A[j] \leq x$

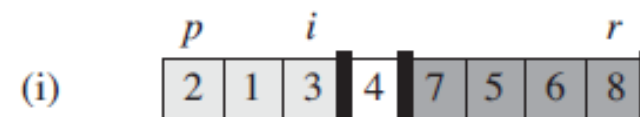
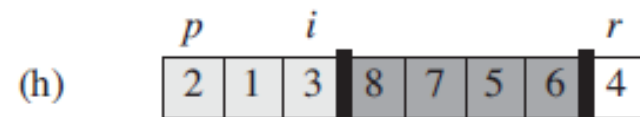
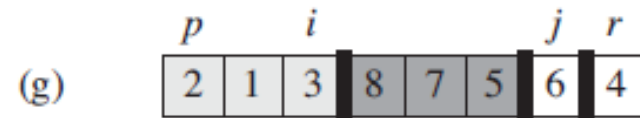
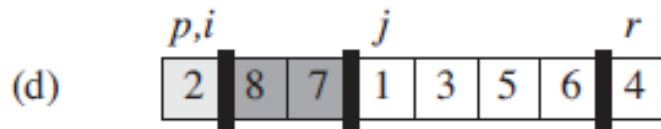
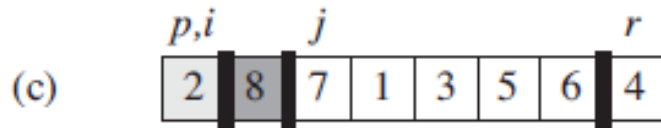
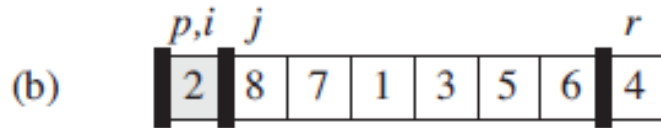
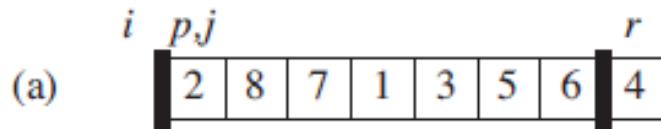
5 $i = i + 1$

6 exchange $A[i]$ with $A[j]$

7 exchange $A[i + 1]$ with $A[r]$

8 **return** $i + 1$

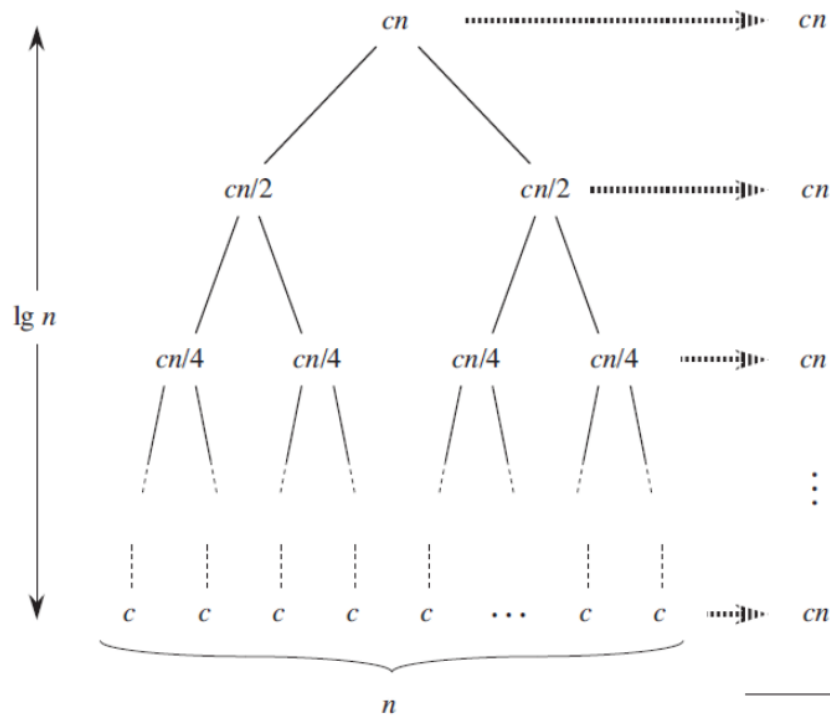
Partitioning the Array



What is the time complexity of partitioning?

Quicksort time complexity

- What is the worst case?
- What is the best case?



(d)

Total: $cn \lg n + cn$