

# SEARCH TREE METHODS

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CS340

# Search Tree Methods

- How to solve hard combinatorial problems?
- Exhaustive search (enumerating all candidate solutions and identifying the one with a desired property) takes too long.
- The set of all possible choices is called the “state space”.

# Searching the state space

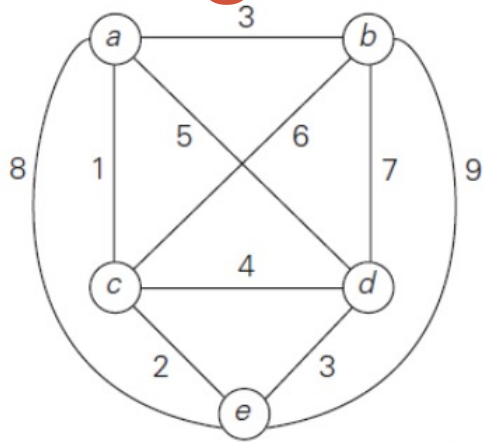
- Widely used in Artificial Intelligence
- Essentially a DFS
- Don't get your hopes up
  - The state space probably needs to be narrowed considerably
- Eg. Clique
  - The state space is all subsets of size  $k$ .
  - Search the state space to see if it contains a clique.
  - Is it possible to increase speed by thinking about the problem?

# Narrowing the state space

- For finding the max clique in a graph:
  - It is easy to find an upper bound on the size of a clique.
  - Vertices of low degree cannot be part of a large clique.
  - Removing low degree vertices might break up the graph.
  - Start by finding a small clique of size  $k'$  (which is much easier than finding a large clique), and stop considering vertices with degree lower than  $k'$ .
  - Keep track of the largest clique found, and stop considering cases where addition of all possible remaining vertices will not make a larger clique.
- The case where we stop considering is called “pruning”

# Narrow the State Space for Traveling Salesman?

# Traveling Salesman



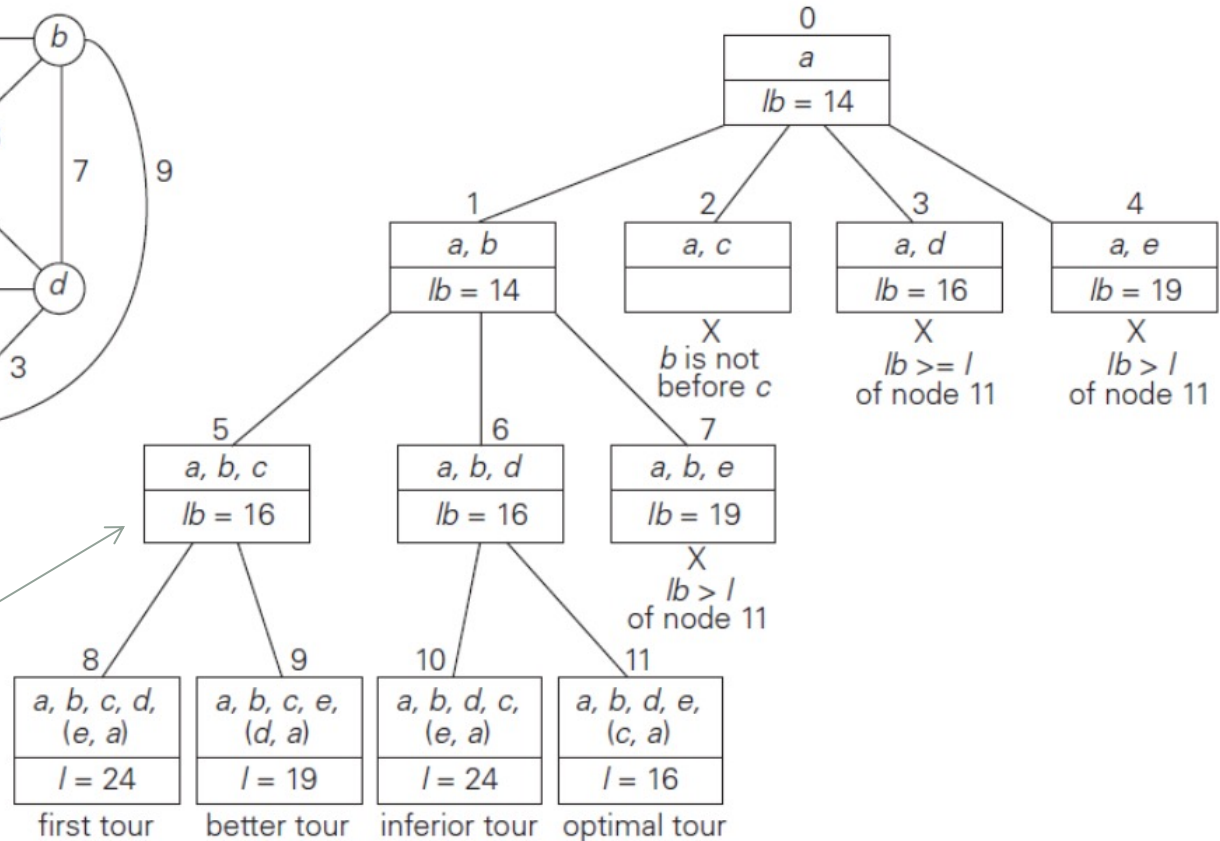
(a)

$$\text{Init LB} = [(1+3) + (3+6) + (1+2) + (3+4) + (2+3)]/2 = 14$$

$$\text{ABC LB} = [(1+3) + (3+6) + (6+1) + (3+4) + (2+3)]/2 = 16$$

$$\text{ABD LB} = [(1+3) + (3+7) + (1+2) + (3+7) + (2+3)]/2 = 16$$

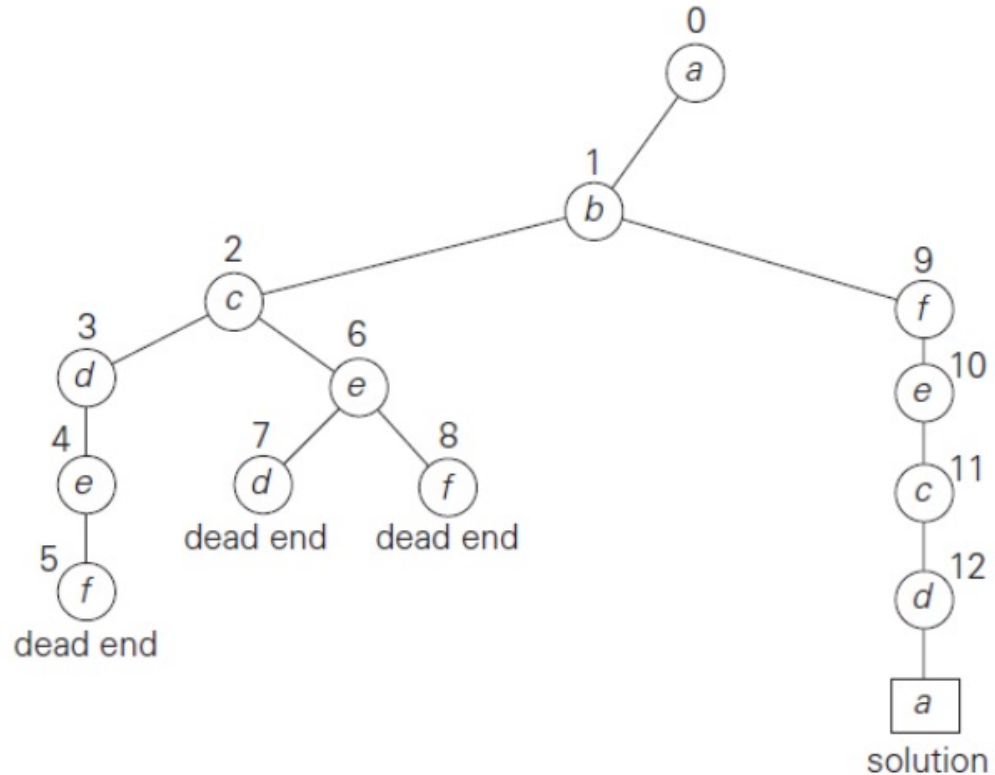
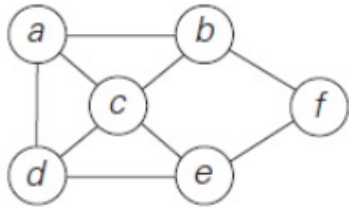
$$\text{ABE LB} = [(1+3) + (3+9) + (1+2) + (3+4) + (2+9)]/2 = 19$$



# Backtracking

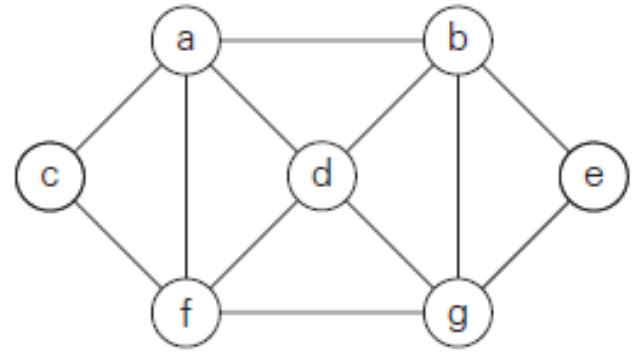
- When we have no way of ranking paths down the tree
  - One partial solution not known to be better than another partial solution

# Hamiltonian Circuit

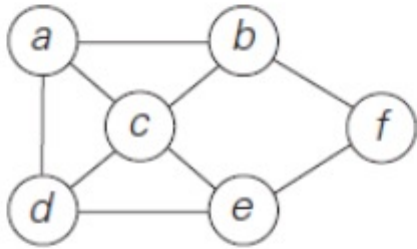




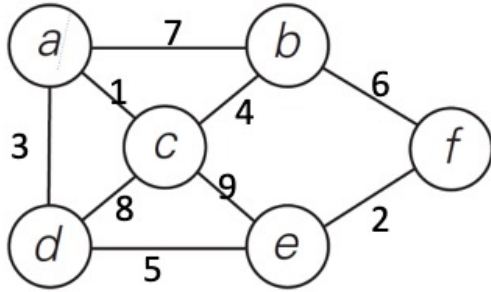
# Hamiltonian Circuit



# BFS/DFS



# Prim/Dijkstra



# Subset Sum

3 items, weights 5,1,3. Total weight for basket: 5

item 3 (w=3)	0					
item 2 (w=1)	0					
item 1 (w=5)	0					
	0	0	0	0	0	0
weight	0	1	2	3	4	5