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Distributed systems I

Winter Term 2019/20

G2T1 – Assignment 4 (theoretical part)

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1 - Global State

a)

¹ $C_1: e_{11} \ e_{21} \ e_{31} \ e_{12} \ e_{22}$
 $C_2: e_{11} \ e_{21} \ e_{31} \ e_{12} \ e_{22} \ e_{41}$ are they consistent ? justification missing

b)

² (i) The inequation gives true for all states that can follow the first one given, independent of how many states lie between them. To make sure that the other state lies on level $L + 1$ you can either check if any other state lies between them or check the timestamps. The timestamp of the process with that last event has to be 1 higher than in the other state.

² (ii) $S_{30} \rightarrow S_{31} = \text{true}$
 $S_{30} \rightarrow S_{32} = \text{true}$
 $S_{30} \rightarrow S_{42} = \text{true} ?$ justification?
 $S_{31} \rightarrow S_{32} = \text{true}$
 $S_{32} \rightarrow S_{42} = \text{true}$ not asked

So S_{32} and S_{42} are not on level $L + 1$, because S_{31} lies between them and S_{30} .

You either have to check the timestamps (not given) or check all other states if they lie between S_{30} and S_{31} . None of them do, so S_{31} is on level $L + 1$ of S_{30} .

it would be way better if you argument with the difference for each event instead of what lies where assuming you meant the same thing as mentioned in part i

² c)

See Figure 1

d)

- $\phi_1 = (x_2 - x_1) = 5$
 $\Rightarrow (\neg\phi_1)$ marked in blue
white?

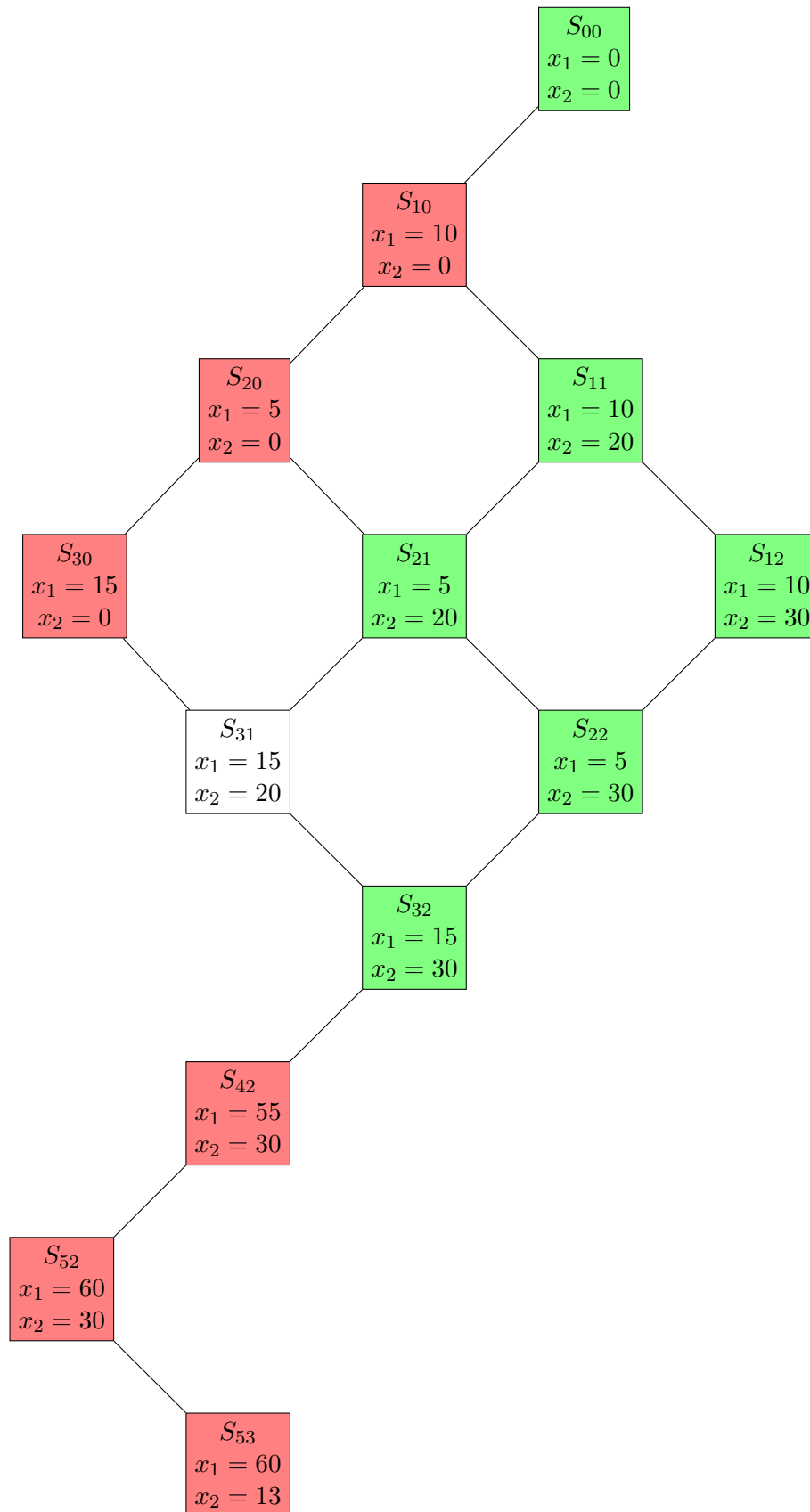


Figure 1: solution for 1.c)

- $\phi_2 = (x_2 - x_1) \leq 5$ and $(x_2 - x_1) > 0$
 $\Rightarrow (\phi_2)$ marked in green so in S00 $x_2 - x_1 > 0$!
- if they fulfill $(\neg\phi_1)$ and (ϕ_2) marked in red

1. safety condition $\neg\phi_1$ is not fulfilled in the state S_{31} and thereby not fulfilled.
2. liveness condition ϕ_2 is fulfilled in the end and thereby fulfilled.
 (therefore in any linearization)

2 - Transaction Processing

a)

The conflicting operation pairs are:

$$\{(w_1[u], w_3[u]), (r_1[y], w_2[y]), (r_3[y], w_2[y]), (r_2[x], w_3[x])\}$$

b)

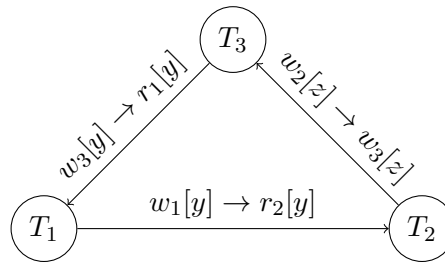


Figure 2: Serialization Graph for History H_1

It's clear that the serialization graph shown in Figure 2 contains a cycle, as such H_1 is not serializable.

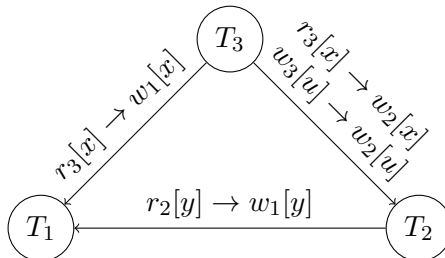


Figure 3: Serialization Graph for History H_2

The serialization graph shown in Figure 3 does not contain a cycle, which would imply that H_2 is serializable.

Unfortunately H_2 is not a correct history as it does not specify the order or the conflicting operations $w_1[x], w_2[x]$.

3 - Two-Phase Locking

H_1 : could be generated by 2-phase-locking. The shrinking phase for each transaction begins right after the last operation before the commit.

Execution split for each resource:

y : $rL_1 \rightarrow r_1 \rightarrow wL_1 \rightarrow w_1 \rightarrow wU_1 \rightarrow rL_2 \rightarrow r_2 \rightarrow c_1 \rightarrow rU_2 \rightarrow c_2 \rightarrow c_3$

x : only read operations \Rightarrow no conflicting locks possible

z : only read operations \Rightarrow no conflicting locks possible

w : $c_1 \rightarrow wL_2 \rightarrow w_2 \rightarrow wU_2 \rightarrow c_2 \rightarrow wL_3 \rightarrow w_3 \rightarrow wU_3 \rightarrow c_3$

H_2 : is not possible with 2-phase-locking!

Conflicting excerpt: $r_1[x] \rightarrow w_2[x] \rightarrow r_1[y]$

Either T_2 cannot acquire the write lock for $w_2[x]$ as T_1 still holds the read lock or T_1 is already in the lock shrinking phase when it wants to execute $r_1[y]$ (this is the first operation of T_1 on y) but both transactions commit.

H_3 : is not possible with 2-phase-locking! **is it even serializable?**

Conflicting excerpt: $r_1[y] \rightarrow w_3[y] \rightarrow w_1[z]$

Analogous situation to H_2 . Shrinking for T_1 can only happen after $w_1[z]$ but $r_1[y]$ and $w_3[y]$ are conflicting locks.