

# Security and Privacy, Blatt 3

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## Problem 1: Sum of negligible functions

Definition:  $v$  is negligible  $\implies \exists N \in \mathbb{N}$  such that  $\forall n > N$  and for all positive polynomials  $p$ :  $v(n) < \frac{1}{p(n)}$

$v$  and  $v'$  negligible:  $\exists N_1, N_2 \in \mathbb{N}$ , such that:

$$\begin{aligned} \forall n > N_1 : v(n) &< \frac{1}{p(n)} \\ \forall n > N_2 : v'(n) &< \frac{1}{p(n)} \end{aligned}$$

(by Definition)

Let  $w(n) = v(n) + v'(n)$ : For  $w$  to be negligible, we need an  $N_3 \in \mathbb{N}$ , such that  $\forall n > N_3 : w(n) < \frac{1}{p(n)}$ . We conclude from the above, that  $\forall n > (N_1 + N_2) : v(n) + v'(n) < \frac{1}{p(n)} + \frac{1}{p(n)}$ , Thus  $N_3 = N_1 + N_2 \implies \forall n > N_3 : w(n) < \frac{2}{p(n)}$ .

Since we're looking at the inverses of *all* positive polynomials, we can easily generate  $\frac{1}{p(n)}$  from  $\frac{2}{p(n)}$  by multiplying  $p(n)$  by 2, which makes just another polynomial  $2p(n)$ , at which we are looking anyways. This means, that also  $\forall n > N_3 : w(n) < \frac{1}{p(n)}$  holds for all positive polynomials  $p$ .

## Problem 2: Deterministic verifier in IPS

$V$  deterministic  $\implies V$  does not use any randomness. Thus the output of  $V$  for a given input (i.e. under same conditions) is always the same. That means, that one can think of a prover  $P'$  that just replays the messages from  $P$  to  $V$ . By definition there are only polynomially many messages. Thus a deterministic  $P'$  can be constructed to convince  $V$ .

Witnesses:

$x \in L$ : The witness  $w$  consists just of the messages, which  $P'$  has to send to  $V$  such that  $V$  accepts on  $(x, w)$ . This witness must exist for  $x \in L$ , because otherwise the probability for  $V$  to accept would be 0 (in contradiction to the definition of IPS).

$x \notin L$ : On the other hand there can not be a witness that leads to  $V$  accepting if  $x \notin L$ . Otherwise  $V$  would always accept when  $w$  is used, making the probability for  $V$  to accept 1, which again contradicts the definition of IPS.

This shows us for  $L \in \mathcal{IP}$  if  $V$  is a deterministic verifier for  $L$ , that  $L \in \mathcal{NP}$  holds.

**Problem 3: Anonymous credentials and IPS**

**Problem 4: Equivalent definition of computational ZK**

**Problem 5: Reducing the error probability 1**

