

# Security and Privacy, Blatt 1

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## Problem 1: Matching Algorithm

The desired algorithm is listed below (pseudo code):

```

struct result {
    bool match
    string matcher
}

bool match(m, t)
    result res = {true, ""}

    if (m is encrypted && t is encrypted) // both encrypted
        if (m is encrypted-symmetrically && t is encrypted-symmetrically)
            k_m = encryption_key of m
            k_t = encryption_key of t
            keys_match = match(k_m, k_t)
            res.match = keys_match.match
            res.matcher += keys_match.matcher
            t = apply_matcher(t, res.matcher) // apply the matcher to whole term
        if (keys_match) // both encrypted under same method and key
            inner_m = decrypt(m) // retrieve the plaintext of m
            inner_t = decrypt(t) // retrieve the plaintext of t
            inner_match = match(inner_m, inner_t) // match the plaintexts
            res.match = inner_match.match
            res.matcher += inner_match.matcher
    else
        res.match = false // different encryption methods
    else
        if (m is encrypted || t is encrypted)
            res.match = false // one encrypted one not
        else // both unencrypted
            if (m is tuple && t is tuple)
                // both are tuples, so check for match component-wise (assuming two components)
                first_match = match(first_component(m), first_component(t))
                t = apply_matcher(t, first_match.matcher) // apply matcher to whole term
                second_match = match(second_component(m), second_component(t))
                t = apply_matcher(t, second_match.matcher) // apply matcher to whole term
                res.match = first_match && second_match
                res.matcher += first_match.matcher + second_match.matcher
            else
                if (m is tuple || t is tuple)
                    res.match = false // one is tuple one not
                else
                    // both neither tuples nor encrypted, so m is constant and t is constant or variable
                    if (t is variable)
                        res.matcher += "ground_substitution:␣" + t + "␣->␣" + m + "␣"␣\n"
                        // t must be substituted by m
                    else
                        if (!equals(m, t))
                            res.match = false // constants mismatch

    if (res.match)
        print "matcher:␣\n" + res.matcher
    return res

term apply_matcher(t, matcher)
    foreach(substitution in matcher)
        foreach(symbol in t)
            if (symbol = substitution.symbol)
                replace(symbol, substitution.substitute)
    return t

```

Time complexity (Master Theorem):

$$f(n) = a \cdot f\left(\frac{n}{b}\right) + c(n)$$

$$a = 2$$

$$b = 2$$

$$c(n) \in \mathcal{O}(n^d); d = 2$$

$$b^d = 2^2 = 4 > a \implies f(n) \in \mathcal{O}(n^2)$$

Space complexity:

## Problem 2: Basics - Probability Theory

## Problem 3: Basics - Algorithms

a)

Product space:  $\Omega_A^{prod} = \{0, 1\} \times M \times \{0, 1\}^t \times \{0, 1\}^2$

Probability space:  $(\Omega_A^{prod}, 2^{\Omega_A^{prod}}, P)$

b)

$$Pr[A(z) = 1] = Pr[c = 1] \cdot (Pr[a = 1] + Pr[b \cdot a = 1]) = \frac{1}{2} \cdot \frac{1}{15} = \frac{1}{30}$$

c)

$$Pr[d \neq \perp] = Pr[c = 1] \cdot Pr[a < 12] = \frac{1}{2} \cdot \frac{12}{15} = \frac{2}{5}$$

(In words: the probability that d is assigned in a run of A.)

d)

$$Pr[A(z) \leq 24 | b = 2] = Pr[a = 12] = \frac{1}{15}$$

## Problem 4: Basics - Group Theory