

# Security and Privacy, Blatt 5

Franziska Hutter (3295896)  
Felix Truger (3331705)  
Felix Bühler (2973410)

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## Problem 1: Schnorr's protocol - special honest verifier zero-knowledge

It is easy to see, that  $(P, V)$  as given for Schnorr's protocol has the form of a  $\Sigma$ -protocol with commitment  $a$ , challenge  $e$  and response  $z$ . The "special honest verifier ZK" property requires:  $\exists$  ppt simulator  $M$  such that  $\forall x \in L_R$  and  $e \in \{0, 1\}^t : M(x, e) = \text{Trans}_{V^e}^P(x)$  where  $\text{Trans}_{V^e}^P(x)$  is the Transcript of an interaction between  $P$  and  $V$  using challenge  $e$  on input  $x$ .

## Problem 2: Homomorphic properties of algorithms

$p = (\mathcal{G}, q, g, h)$  fixed,  $r_0, r_1, v_0, v_1 \in \mathbb{Z}_q$ , we show:

$$\text{com}^{r_0+r_1}(p, v_0 + v_1) \stackrel{!}{=} \text{com}^{r_0}(p, v_0) \cdot \text{com}^{r_1}(p, v_1)$$

By just applying the definition of  $\text{com}$  in the Pedersen commitment scheme, we know:

$$\begin{aligned}\text{com}^{r_0+r_1}(p, v_0 + v_1) &= g^{v_0+v_1} \cdot h^{r_0+r_1} \\ \text{com}^{r_0}(p, v_0) &= g^{v_0} \cdot h^{r_0} \\ \text{com}^{r_1}(p, v_1) &= g^{v_1} \cdot h^{r_1}\end{aligned}$$

Thus:

$$\begin{aligned}\text{com}^{r_0}(p, v_0) \cdot \text{com}^{r_1}(p, v_1) &= g^{v_0} \cdot h^{r_0} \cdot g^{v_1} \cdot h^{r_1} \\ &= g^{v_0} \cdot g^{v_1} \cdot h^{r_0} \cdot h^{r_1} \\ &= g^{v_0+v_1} \cdot h^{r_0+r_1} \\ &= \text{com}^{r_0+r_1}(p, v_0 + v_1)\end{aligned}$$

## Problem 3: Building circuits for functions

## Problem 4: Garbled circuits

## Problem 5: 51%-Attack on Bitcoin