

# Nuance Matters: Probing Epistemic Consistency in Causal Reasoning

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## Abstract

Previous research on causal reasoning often overlooks the subtleties crucial to understanding causal reasoning. To address this gap, our study introduces the concept of *causal epistemic consistency*, which focuses on the self-consistency of Large Language Models (LLMs) in differentiating intermediates with nuanced differences in causal reasoning. We propose a suite of novel metrics – intensity ranking concordance, cross-group position agreement, and intra-group clustering – to evaluate LLMs on this front. Through extensive empirical studies on 21 high-profile LLMs, including GPT-4, Claude3, and LLaMA3-70B, we have favoring evidence that current models struggle to maintain epistemic consistency in identifying the polarity and intensity of intermediates in causal reasoning. Additionally, we explore the potential of using internal token probabilities as an auxiliary tool to maintain causal epistemic consistency. In summary, our study bridges a critical gap in AI research by investigating the self-consistency over fine-grained intermediates involved in causal reasoning.

## 1 Introduction

Previous studies in causal reasoning have primarily focused on discovering or determining the existence of a causal relationship between two variables (Roemmelé, Bejan, and Gordon 2011; Cui et al. 2024c). However, these causal relationships are not always absolute. They can be heavily influenced by additional intermediate factors, which may vary in both polarity and intensity (Fitzgerald and Howcroft 1998; Bauman et al. 2002). The polarity of these intermediates indicates whether they support or defeat (oppose) the original causal relationship, while their intensity determines the strength of this supporting or defeating influence.

Forming fine-grained differentiation is essential for precise causal modeling (Iwasaki and Simon 1994); however, it is insufficient for LLMs to merely generate these intermediates. It is as equally important to ensure that these intermediates are reliable and credible (Shi et al. 2023). One method to verify this is through assessing the consistency of LLMs’ perception of the intermediates. We posit that if LLMs can correctly differentiate their generated intermediates based on varying polarities and intensities, these intermediates are self-consistent and thus, more reliable for mak-

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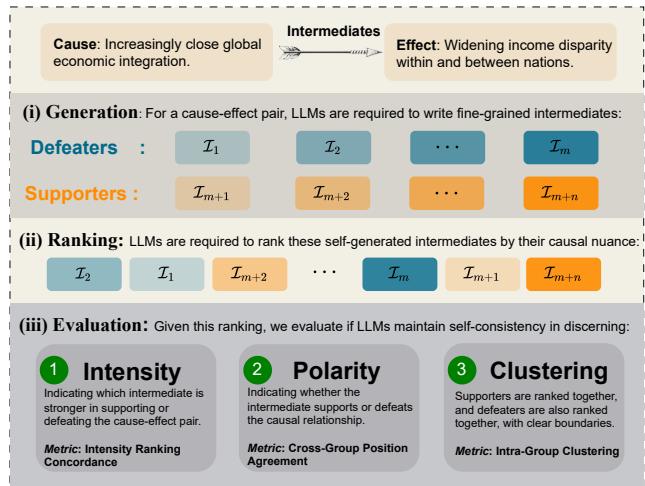


Figure 1: Overview of the evaluation framework for causal epistemic consistency. The first step involves instructing LLMs to generate fine-grained intermediates that influence a given causal relationship differently. The second step requires LLMs to rank their own generations based on their causal nuance. Finally, the proposed metrics are used to assess the self-consistency between ranking and generation, i.e., the LLMs’ causal epistemic consistency.

ing predictions and decisions. Drawing from this insight, our study proposes the concept of “**causal epistemic consistency**”:

**Definition 1 (Causal epistemic consistency)** *Causal epistemic consistency refers to an LLM’s ability to maintain self-consistency in differentiating its generated intermediates in three aspects: (i) discerning **intensity**: accurately assessing the intensity nuance in their causal impact. (ii) differentiating **polarity**: effectively distinguishing between supporting and defeating intermediates, and (iii) forming cohesive **clusters**: creating well-separated clusters of intermediates based on their polarity and intensity.*

To quantify LLMs’ ability to maintain causal epistemic consistency in the aforementioned aspects, we introduce a suite of novel metrics. These metrics include (i) Intensity ranking concordance, which measures the models’ self-

consistency in ranking self-generated intermediates with varying intensity; (ii) Cross-group position (CGP) agreement, which indicates the models' consistency in determining the polarity of intermediates, specifically whether they support or defeat the original causal relationship; and (iii) Intra-group clustering (IGC), which assesses models' consistency to rank its generated intermediates of the same type closely together. We illustrate the evaluation framework of causal epistemic consistency in Figure 1.

To unravel the causal epistemic consistency of current LLMs, our empirical study evaluates 21 high-profile LLMs, including the renowned closed-source GPT, Claude, and Gemini series, alongside various scales of cutting-edge open-source alternatives such as Gemma (2B and 7B) (Mesnard et al. 2024), LLaMA2 (7B, 13B, and 70B) (Touvron et al. 2023), Phi-3 (3.8B, 7B, and 14B) (Abdin et al. 2024), and LLaMA3 (8B and 70B) (Meta 2024). Contrary to initial expectations that LLMs would exhibit satisfactory performance, our findings reveal their striking incompetence in keeping causal epistemic consistency. Remarkably, even the advanced GPT-4 model performs unsatisfactorily. This underscores the complexities and challenges these models face in maintaining causal consistency and capturing causal nuances.

Furthermore, we explore whether internal token probability can serve as a useful signal for LLMs to maintain causal epistemic consistency. Our comprehensive empirical study highlights the application scope of internal token probability for LLMs to maintain causal epistemic consistency.

To summarize, our contributions are fourfold:

1. **Introduction of Causal Epistemic Consistency:** We propose the novel concept of causal epistemic consistency over fine-grained intermediates in causal reasoning, emphasizing self-consistency in differentiating the nuances hidden in fine-grained intermediates.
2. **Development of Evaluation Metrics:** We introduce a comprehensive suite of metrics designed to assess LLMs' causal epistemic consistency, covering aspects of intensity ranking concordance, cross-group position agreement, and intra-group clustering.
3. **Extensive Empirical Evaluation:** We assess the performance of 21 LLMs on their causal epistemic consistency, highlighting their deficiencies in maintaining causal epistemic consistency.
4. **Internal Token Probability Exploration:** We investigate the potential of using internal token probabilities as an auxiliary tool to help LLMs maintain causal epistemic consistency and highlight its application scope.

## 2 Task Definition

### 2.1 Problem Formulations

Causal epistemic consistency measures an LLM's self-consistency between generating fine-grained intermediates and subsequently ranking those fine-grained intermediates.

Specifically, in the generation phase, for a defeasible cause-effect pair  $(C, E)$ , an LLM is tasked

with generating an ordered sequence  $\mathcal{I}$  of fine-grained intermediates, consisting of a subsequence  $\mathcal{D} = (\mathcal{I}_1, \mathcal{I}_2, \dots, \mathcal{I}_m)$  as the defeater group and a subsequence  $\mathcal{A} = (\mathcal{I}_{m+1}, \mathcal{I}_{m+2}, \dots, \mathcal{I}_{m+n})$  as the supporter group. Each individual intermediate changes the causal strength of  $(C, E)$  differently. Specifically, the causal influence of these intermediates is expected in the following order:

$$\begin{aligned} \mathcal{CS}(E|C \oplus \mathcal{I}_1) &\leq \dots \leq \mathcal{CS}(E|C \oplus \mathcal{I}_m) \\ &\leq \mathcal{CS}(E|C) \end{aligned} \quad (1)$$

$$\mathcal{CS}(E|C \oplus \mathcal{I}_{m+1}) \leq \dots \leq \mathcal{CS}(E|C \oplus \mathcal{I}_{m+n})$$

where  $\mathcal{CS}(E|C)$  measures the causal strength (Luo et al. 2016; Zhang et al. 2022), quantifying the likelihood that the cause event  $C$  would lead to the occurrence of the effect event  $E$ .<sup>1</sup> The  $\oplus$  means the combination of two events. The gradient bar illustrates the varying degrees of intensity of the defeating intermediates, while the gradient bar represents the supporting intermediates. The color gradient darkens as the intensity increases, with a darker shade indicating a stronger influence, whether supporting or defeating.

Subsequently, in the ranking phase, the same LLM is asked again to rank its own generated intermediates  $\mathcal{I}$ , obtaining  $\mathcal{I}'$ , a permutation of  $\mathcal{I}$ . Ideally, an LLM with perfect causal epistemic consistency should have  $\mathcal{I} = \mathcal{I}'$ , satisfying the requirements of intensity, polarity, and clustering perfectly.

### 2.2 Key Research Questions

The study addresses three primary research questions:

- **RQ I:** How can we comprehensively measure the ability of LLMs to maintain the epistemic consistency over fine-grained intermediates in causal reasoning?
- **RQ II:** How well do current LLMs, with varying architectures and scales, maintain their causal epistemic consistency?
- **RQ III:** Are there any alternatives to prompting for LLMs to maintain causal epistemic consistency?

To answer **RQ I**, we propose novel metrics introduced in Section 3, which not only serve our specific study but also have broader applications across various tasks. In Section 4, we dive into the performance of twenty-one leading LLMs, exploring their ability to maintain epistemic consistency, thereby addressing **RQ II**. Lastly, in Section 5, we assess whether internal token probability offers a more effective—or perhaps less effective—alternative to prompting for preserving causal epistemic consistency in LLMs, answering **RQ III**.

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<sup>1</sup>In this context, we assume that only one fine-grained intermediate is active for a cause-effect pair at a time. This design choice reflects the reality that a single argument is more often responsible for influencing the causal relationship than multiple arguments acting simultaneously.

### 3 Metrics for Measuring Causal Epistemic Consistency

To evaluate the causal epistemic consistency of LLMs from the aspects of intensity, polarity, and clustering, we propose three types of automatic metrics: intensity ranking concordance, cross-group position agreement, and intra-group clustering. A graphical illustration of these metrics is shown in Figure 2. The mathematical notations below are consistent with Section 2.1.

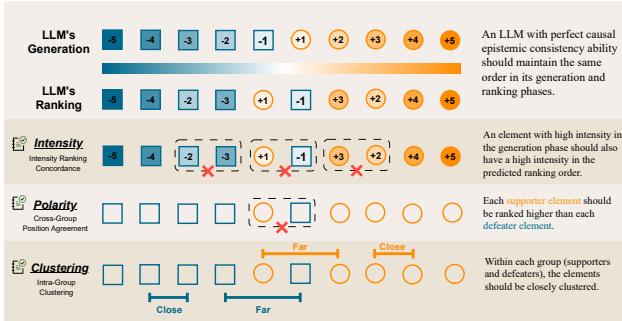


Figure 2: Illustration of the proposed metrics from three aspects: intensity (Section 3.1), polarity (Section 3.2), and clustering (Section 3.3). These metrics measure the self-consistency of LLMs in generating and ranking supporting (○) and defeating (□) intermediates with varying intensities. Numbers  $\textcolor{blue}{-5}$ ,  $\textcolor{blue}{-4}$ , ...,  $\textcolor{orange}{+4}$ ,  $\textcolor{orange}{+5}$  indicate the intensity of the generated intermediates, with the lowest value ( $\textcolor{blue}{-5}$ ) being the strongest generated defeater and the highest value ( $\textcolor{orange}{+5}$ ) the strongest generated supporter.

#### 3.1 Intensity: Intensity Ranking Concordance

To assess the concordance between the order from the generation phase and the order from the ranking phase of these fine-grained intermediates, we leverage the Kendall Tau distance (Kendall 1938). This metric quantifies the similarity between two orders by counting the number of pairwise agreements and disagreements. For a sequence  $\mathcal{I}$  of LLM-generated intermediates and its permutation  $\mathcal{I}'$  ranked by the same LLM, a pair of elements from  $\mathcal{I}$  is called *concordant* if they appear in the same order in both  $\mathcal{I}$  and  $\mathcal{I}'$ . Conversely, the pair is called *discordant* if their order is reversed in  $\mathcal{I}'$  compared to  $\mathcal{I}$ . The Kendall Tau  $\tau$  is calculated as:

$$\tau = \frac{(\# \text{ concordant pairs}) - (\# \text{ discordant pairs})}{k(k-1)/2} \quad (2)$$

where  $k$  is the number of elements in the list, and  $k(k-1)/2$  is the total number of pairs. The metric ranges from -1 to 1, where 1 indicates that these two lists are identical; -1 indicates completely reversed rankings; and values close to 0 indicate no association between the two lists. For our task, we have three intensity ranking concordance metrics:  $\tau\text{-}\mathcal{A}$ ,  $\tau\text{-}\mathcal{D}$ , and  $\tau\text{-all}$ , which evaluate the intensity ranking concordance within the supporter group, the defeater group, and the entire sequence of intermediates, respectively.

#### 3.2 Polarity: Cross-Group Position (CGP)

To assess the relative positioning of elements between these two polarities—the defeater group  $\mathcal{D}$  and the supporter group  $\mathcal{A}$ —we propose the Cross-Group Position (CGP) metric. This metric penalizes instances where elements from  $\mathcal{A}$  are ranked lower than those from  $\mathcal{D}$ <sup>2</sup>. Specifically, CGP is defined as:

$$\text{CGP}(\mathcal{I}', \mathcal{A}, \mathcal{D}) = 1 - \frac{\sum_{a \in \mathcal{A}} \sum_{d \in \mathcal{D}} \mathbb{1}[\text{index}(a) < \text{index}(d)]}{|\mathcal{A}| \times |\mathcal{D}|} \quad (3)$$

where  $\text{index}(x)$  denotes the index of element  $x$  in the ranked sequence  $\mathcal{I}'$ .  $\mathbb{1}[\cdot]$  denotes the indicator function that is set to 1 if the condition is true and 0 otherwise. CGP measures how often elements from  $\mathcal{A}$  precede the elements of  $\mathcal{D}$  in the ranked sequence  $\mathcal{I}'$ . It is normalized to the range [0, 1] by dividing with the maximum possible violations, i.e.,  $|\mathcal{A}| \times |\mathcal{D}|$ . Higher values indicate better differentiation between groups  $\mathcal{A}$  and  $\mathcal{D}$ .

#### 3.3 Clustering: Intra-Group Clustering (IGC)

In this subsection, we introduce Intra-Group Clustering (IGC), a metric for LLMs’ causal epistemic consistency by assessing the clustering degree of supporting and defeating intermediates. The intuition behind IGC is that all defeaters and all supporters should form cohesive clusters, with a minimal number of polarity changes (from supporting to defeating, or vice versa) when iterating the sequence.

**Clustering Distance Based on Polarity Change.** Given the LLM-ranked intermediates  $\mathcal{I}'$ , we define  $L_i$  to indicate which polarity (supporter  $\mathcal{A}$  or defeater  $\mathcal{D}$ ) each intermediate  $\mathcal{I}'_i$  belongs to.  $L_i$  is represented as a binary polarity that either  $L_i = \mathcal{A}$  or  $L_i = \mathcal{D}$ .  $d(i, j)$  is the sequence clustering distance between  $\mathcal{I}'_i$  and  $\mathcal{I}'_j$ , calculated as follows:

$$d(i, j) = \sum_{k=i}^{j-1} \mathbb{1}[L_k \neq L_{k+1} \wedge L_{k+1} \neq L_i] \quad (4)$$

where  $i < j$ . The distance is based on the number of polarity changes, excluding reversions to the initial polarity.

**IGC: A Measure of Clustering Quality in Sequence.** With the distance based on polarity change, we use the silhouette score (Rousseeuw 1987; Shahapure and Nicholas 2020) to measure how similar an element is to its own cluster compared to other clusters in sequence:

$$s(i) = \frac{d_{nc}(i) - d_{ic}(i)}{\max(d_{ic}(i), d_{nc}(i))} \quad (5)$$

where  $d_{ic}(i)$  and  $d_{nc}(i)$  are the intra-cluster distance and nearest cluster distance for each intermediate  $\mathcal{I}'_i$ .

1. The intra-cluster distance  $d_{ic}(i)$  captures the mean distance between  $\mathcal{I}'_i$  and all other intermediates belonging to the same group, reflecting *internal cohesion*. It is calculated as:

$$d_{ic}(i) = \frac{1}{|L_i| - 1} \sum_{L_j=L_i, \mathcal{I}'_j \neq \mathcal{I}'_i} d(i, j). \quad (6)$$

<sup>2</sup>We define the index of the strongest defeater to be the lowest and the strongest supporter to be the highest, consistent with Section 2.1.

Aspect	Intensity Ranking Concordance			Cross-Group Position	Intra-Group Clustering
	$\tau\text{-}\mathcal{A} \uparrow$	$\tau\text{-}\mathcal{D} \uparrow$	$\tau\text{-all} \uparrow$	CGP $\uparrow$	IGC $\uparrow$
<i>Closed-source LLMs</i>					
GPT-3.5 Turbo	0.074 $\pm$ 0.429	0.045 $\pm$ 0.407	0.304 $\pm$ 0.409	0.750 $\pm$ 0.329	0.762 $\pm$ 0.244
GPT-4	0.384 $\pm$ 0.413	0.203 $\pm$ 0.440	0.587 $\pm$ 0.347	0.911 $\pm$ 0.235	0.916 $\pm$ 0.176
GPT-4 Turbo	0.397 $\pm$ 0.541	0.226 $\pm$ 0.459	0.526 $\pm$ 0.510	0.849 $\pm$ 0.330	0.942 $\pm$ 0.151
GPT-4o mini	0.142 $\pm$ 0.444	0.154 $\pm$ 0.418	0.472 $\pm$ 0.375	0.865 $\pm$ 0.281	0.889 $\pm$ 0.196
GPT-4o	0.317 $\pm$ 0.466	0.229 $\pm$ 0.426	0.637 $\pm$ 0.266	<b>0.964 <math>\pm</math> 0.164</b>	<b>0.978 <math>\pm</math> 0.099</b>
Claude 3 Haiku	0.120 $\pm$ 0.429	0.069 $\pm$ 0.388	0.406 $\pm$ 0.344	0.828 $\pm$ 0.270	0.809 $\pm$ 0.234
Claude 3 Sonnet	0.272 $\pm$ 0.429	0.046 $\pm$ 0.423	0.533 $\pm$ 0.290	0.916 $\pm$ 0.204	0.893 $\pm$ 0.195
Claude 3 Opus	0.509 $\pm$ 0.457	0.381 $\pm$ 0.451	<b>0.688 <math>\pm</math> 0.342</b>	0.941 $\pm$ 0.204	0.957 $\pm$ 0.131
Claude 3.5 Sonnet	<b>0.610 <math>\pm</math> 0.507</b>	<b>0.440 <math>\pm</math> 0.501</b>	0.662 $\pm$ 0.492	0.885 $\pm$ 0.286	0.932 $\pm$ 0.159
Gemini 1.5 Flash	0.108 $\pm$ 0.451	0.115 $\pm$ 0.412	0.429 $\pm$ 0.362	0.842 $\pm$ 0.274	0.838 $\pm$ 0.225
Gemini 1.5 Pro	0.475 $\pm$ 0.435	0.165 $\pm$ 0.463	0.587 $\pm$ 0.326	0.900 $\pm$ 0.212	0.875 $\pm$ 0.205
<i>Open-source LLMs</i>					
Gemma-2B	-0.021 $\pm$ 0.412	0.001 $\pm$ 0.410	-0.002 $\pm$ 0.245	0.502 $\pm$ 0.190	0.468 $\pm$ 0.083
Gemma-7B	-0.006 $\pm$ 0.392	0.016 $\pm$ 0.389	0.085 $\pm$ 0.256	0.575 $\pm$ 0.203	0.484 $\pm$ 0.122
LLaMA2-7B	-0.018 $\pm$ 0.406	0.001 $\pm$ 0.412	-0.029 $\pm$ 0.261	0.477 $\pm$ 0.200	0.475 $\pm$ 0.092
LLaMA2-13B	-0.000 $\pm$ 0.411	0.026 $\pm$ 0.417	0.072 $\pm$ 0.256	0.560 $\pm$ 0.197	0.480 $\pm$ 0.109
LLaMA2-70B	0.012 $\pm$ 0.409	0.010 $\pm$ 0.434	0.234 $\pm$ 0.349	0.707 $\pm$ 0.271	0.629 $\pm$ 0.215
Phi-3 Mini (3.8B)	0.135 $\pm$ 0.431	0.012 $\pm$ 0.393	0.300 $\pm$ 0.336	0.740 $\pm$ 0.275	0.659 $\pm$ 0.222
Phi-3-Small (7.4B)	0.092 $\pm$ 0.443	0.204 $\pm$ 0.422	0.347 $\pm$ 0.348	0.753 $\pm$ 0.254	0.672 $\pm$ 0.220
Phi-3 Medium (14B)	-0.056 $\pm$ 0.441	0.154 $\pm$ 0.406	0.356 $\pm$ 0.367	0.801 $\pm$ 0.286	0.801 $\pm$ 0.230
LLaMA3-8B	0.030 $\pm$ 0.444	0.139 $\pm$ 0.436	0.273 $\pm$ 0.387	0.712 $\pm$ 0.285	0.639 $\pm$ 0.217
LLaMA3-70B	<b>0.357 <math>\pm</math> 0.469</b>	<b>0.343 <math>\pm</math> 0.419</b>	<b>0.586 <math>\pm</math> 0.415</b>	<b>0.887 <math>\pm</math> 0.274</b>	<b>0.923 <math>\pm</math> 0.177</b>
<i>Random</i>					
Random	-0.003 $\pm$ 0.409	0.005 $\pm$ 0.406	-0.008 $\pm$ 0.249	0.496 $\pm$ 0.192	0.467 $\pm$ 0.077

Table 1: Empirical study of LLMs on the proposed metrics for causal epistemic consistency.

2. The nearest cluster distance  $d_{nc}(i)$  captures the mean distance between  $\mathcal{I}'_i$  and all other points belonging to a different group, demonstrating the level of *separation* from other clusters. It is calculated as:

$$d_{nc}(i) = \frac{1}{|\mathcal{I}'| - |\mathcal{L}_i|} \sum_{L_j \neq L_i} d(i, j). \quad (7)$$

The final Intra-Group Clustering (IGC) metric is computed as the average clustering of all elements:

$$\text{IGC} = \frac{1}{|\mathcal{I}'|} \sum_{i=1}^{|\mathcal{I}'|} s(i). \quad (8)$$

**Range and Implications of IGC.** The range of  $s(i)$  is  $[-1, 1]$ : (i) Close to 1: The element is near its own group and far from the neighboring groups; (ii) Close to 0: The element is on the border between its cluster and a neighboring cluster. (iii) Close to -1: The element is in the wrong cluster. IGC quantifies the quality of cluster assignments, with a high score indicating well-clustered sequences. It is a general metric applicable to various contexts related to sequence clustering. Further details are in Appendix C.1.

## 4 Causal Epistemic Consistency of LLMs

### 4.1 Experimental Setup

**Foundational Dataset.** To ensure the defeasibility of causal pairs, allowing models to generate intermediates with varying polarity and intensity, we utilize the test dataset of  $\delta$ -CAUSAL (Cui et al. 2024c) as our foundational dataset, which comprises 1,970 defeasible cause-effect pairs.

**Three-Phase Assessment for LLMs’ Causal Epistemic Consistency.** There are three main phases in our experiments: (i) Intermediate generation: We provide LLMs with a single cause-effect pair and two preliminary intermediates: one supporting and one defeating. For each supporter and defeater, we instruct the LLMs to generate two weaker and two stronger intermediates. As a result, we compile a total of 10 intermediates as sequence  $\mathcal{I}$ , divided into two subsequences: subsequence  $\mathcal{D}$  comprised of  $m = 5$  intermediates that challenge the cause-effect relationship with differing intensities; and subsequence  $\mathcal{A}$  consisting of  $n = 5$  supporting intermediates that reinforce the cause-effect pair, also with varying intensities. The prompt for generating these fine-grained intermediates is presented in Figure 7; (ii) Intermediate ranking: From these generated intermediates, we use the same LLM to rank the intermediates to identify their polarities (supporting or defeating) and intensity. The

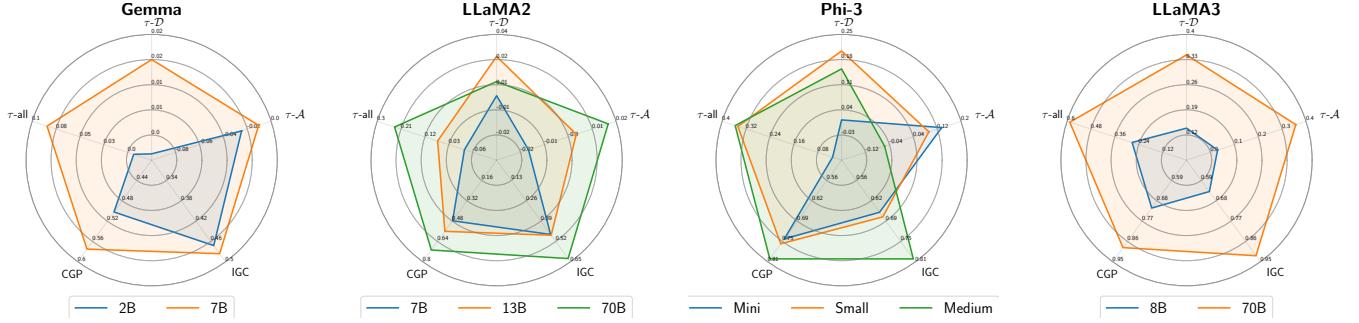


Figure 3: Radar charts comparing the performance of various LLM architectures and sizes (Gemma, LLaMA2, Phi-3, and LLaMA3) in maintaining causal epistemic consistency. Each color of the radar plot lines represents a different model size.

prompt for ranking these fine-grained intermediates is presented in Figure 8; and (iii) Evaluation: Based on the actual order of generated intermediates in the first phase and the predicted ranking order in the second phase, we evaluate the causal epistemic consistency from the perspectives of Intensity Ranking Concordance ( $\tau\text{-}\mathcal{A}$ ,  $\tau\text{-}\mathcal{D}$ ,  $\tau\text{-all}$ ), Cross-Group Position (CGP) agreement, and Intra-Group Clustering (IGC).

**Backbone Models.** We assess a comprehensive suite of LLMs for causal epistemic consistency. Our evaluation includes: (i) 11 Closed-source models: GPT-3.5 Turbo, GPT-4, GPT-4 Turbo, GPT-4o, GPT-4o mini, Claude 3 (Haiku, Sonnet, and Opus), Claude 3.5 (Sonnet) (Anthropic 2024), Gemini 1.5 (Flash and Pro) (Gemini-Team 2024); (ii) 10 Open-source models: Gemma (2B and 7B) (Mesnard et al. 2024), LLaMA2 (7B, 13B, and 70B) (Touvron et al. 2023), Phi-3 (mini, small, and medium) (Abdin et al. 2024), and LLaMA3 (8B and 70B) (Meta 2024).

## 4.2 Experimental Results

Table 1 presents a quantitative comparison of different models on causal epistemic consistency.

- **Closed-source models generally outperform open-source models:** For instance, GPT-4o achieves a  $\tau\text{-all}$  score of 0.632, a CGP score of 0.962, and an IGC score of 0.973, whereas LLaMA3-70B, the best-performing open-source model, only achieves a  $\tau\text{-all}$  score of 0.586, a CGP score of 0.887, and an IGC score of 0.923.
- **Maintaining consistency in intensity is more challenging than achieving consistency in polarity and clustering:** The patterns across different metrics are consistent among different models, suggesting that while LLMs can effectively maintain consistency over differentiating between supporting and defeating intermediates and clustering intermediates of the same polarity together, they find it more challenging to maintain consistent intensity rankings. Namely, achieving consistency over the nuances of causal intensity remains difficult.

## 4.3 Does a Larger Model Scale Mean Better Causal Epistemic Consistency?

Previous works (Kaplan et al. 2020; Hoffmann et al. 2024) have shown that with the increase in model scale, the im-

provement in performance follows a power-law relationship. However, the effectiveness of ‘just scaling’ for general causal understanding, especially in the context of causality, has become a subject of intense debate (Zečević et al. 2023).

Inspired by this question, we investigate whether increasing the model scale improves the causal epistemic consistency of LLMs. Since this model scale study is only possible for models available in multiple sizes, we conduct experiments with: (i) Gemma at sizes of 2B and 7B; (ii) LLaMA2 at sizes of 7B, 13B, and 70B; (iii) Phi-3 at sizes of 3.8B, 7B, and 14B; and (iv) LLaMA3 at sizes of 8B and 70B. The experimental results are presented in Figure 3. From these results, we clearly observe that **an increase in model size generally enhances causal epistemic consistency**. For instance, LLaMA2 and LLaMA3 demonstrate significant improvements at larger scales, particularly at 70B, where the causal epistemic consistency scores are notably higher compared to their smaller-scale counterparts.

## 4.4 Visualization of Causal Epistemic Consistency

We plot the causal epistemic consistency matrices of LLaMA3-70B and GPT-4o in Figure 4. In these matrices, the x-axis from left to right and the y-axis from top to bottom correspond to  $\text{[-5]} \text{ [-4]} \text{ [-3]} \text{ [-2]} \text{ [-1]} \text{ [1]} \text{ [2]} \text{ [3]} \text{ [4]} \text{ [5]}$ , where the square symbol  $\boxed{\cdot}$  represents defeators while the circle symbol  $\textcircled{\cdot}$  represents supporters. The numbers inside the symbols indicate the supporting or defeating intensity, with larger absolute values signifying stronger intensity (i.e.,  $\boxed{-5}$  is the strongest defeater and  $\textcircled{+5}$  is the strongest supporter). These matrices visualize how well the models maintain causal epistemic consistency by comparing the labels of intermediates of the generation phase with the predicted labels in the ranking phase.

The confusion matrices of other models are presented in Appendix D. From the results of the best closed-source and open-source models, we have the following observations:

- **Diagonal Dominance:** Higher values along the diagonal indicate better causal epistemic consistency. This dominance shows that the model often maintains consistency in both polarity and intensity by correctly matching the labels of intermediates from the generation phase to the ranking phase.
- **Off-Diagonal Elements:** These off-diagonal elements

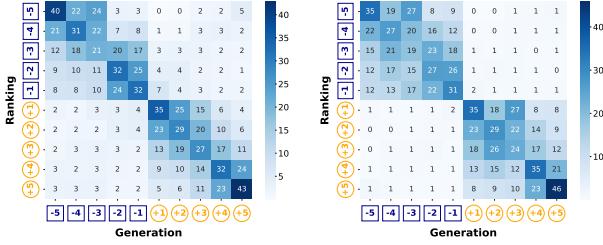


Figure 4: Visualization of LLaMA3-70B’s (left) and GPT-4o’s (right) alignment of intermediates’ predicted ranking versus their generation phase ranking, indicating the models’ self-consistency in intensity, polarity, and clustering. Each matrix element  $(i, j)$  indicates the percentage of instances where an intermediate ranked at position  $i$  during the generation phase was ranked at position  $j$  during the ranking phase. For example,  $(\text{---}, \text{++})$  indicates the percentage of instances with a label of defeater with an intensity of 3 in the generation phase that was ranked as the supporter with an intensity of 4 during the ranking phase.

represent the number of instances where the predicted labels during the ranking phase diverge from the labels during the generation phase. Higher values in these cells suggest cases where the model struggles to maintain consistency. For instance, a higher value far from the diagonal indicates a more significant discrepancy between the ranking and generation phases, reflecting lower causal epistemic consistency due to overestimation or underestimation of the intensity of the generated intermediates.

- **Cluster Separation:** These matrices also indicate that these two models cluster supporting and defeating intermediates well, as shown by lower values in the lower left and upper right corners.

## 5 Beyond Prompting: Leveraging Internal Token Probability

This section explores using internal token probability as an alternative to the prompting method in Section 4 for maintaining causal epistemic consistency.

### 5.1 Internal Token Probability

Internal token probability has proven to be a reliable indicator for sequence correlation estimation (Malinin and Gales 2021; Farquhar et al. 2024; Cui et al. 2024c). For each cause-effect pair  $(C, E)$  and any supporting or defeating intermediate  $\mathcal{I}_j$ , we utilize the token probabilities  $p$  to estimate the causal strength  $\mathcal{CS}(E|C \oplus \mathcal{I}_j)$  in Section 2.1:

$$\mathcal{CS}(E|C \oplus \mathcal{I}_j) = \prod_i p(E_i|C \oplus \mathcal{I}_j, w, E_{<i}) \quad (9)$$

where  $E_i$  is the  $i$ th token of  $E$  and  $E_{<i}$  is the first  $i - 1$  tokens of  $E$ .  $p(E_i|C \oplus \mathcal{I}_j, w, E_{<i})$  is the internal (conditional) token probability. The conjunction word  $w$  connects the combination of the cause and the intermediate to the effect, and explicitly indicates the causation such as “because” and “therefore”.

## 5.2 Experimental Setup

**Models and Datasets.** As closed-source models often do not provide a `logprob` API usage<sup>3</sup>, our investigation resorts to open-source LLMs including Gemma (2B and 7B) (Mesnard et al. 2024), LLaMA2 (7B, 13B, and 70B) (Touvron et al. 2023), Phi-3 (3.8B, 7B, and 14B), and LLaMA3 (8B and 70B). We use the same foundation dataset described in Section 4.1.

**Three-Phase Assessment.** The experiment in this section involves three phases: (i) Intermediate generation: This phase involves generating a sequence of intermediates,  $\mathcal{I}$ , following the same procedure described in Section 4.1; (ii) Intermediate ranking based on conditional token probability: In this phase, we calculate the causal strength based on the conditional token probability using  $\{\mathcal{CS}(E|C \oplus \mathcal{I}_j) | \mathcal{I}_j \in \mathcal{I}\}$ . (iii) Evaluation: We assess the models’ causal epistemic consistency using rankings from the generation phase and conditional probability values, based on the proposed metrics in Section 3.

**Conjunction Word Choices.** We study multiple conjunction words, including (i) coordinating conjunctions (Grammarly 2024): “so”; (ii) subordinate conjunctions (Traffis 2020): “because”, “since”, and “as”; and (iii) conjunctive adverbs (Ellis 2023): “therefore”, “thus”, and “hence”.

## 5.3 Results and Discussion

We analyze the results from two aspects: (i) the impact of conjunction words on models’ causal epistemic consistency; and (ii) the efficacy of internal token probability against the prompting strategy.

**Comparison of Different Conjunction Words.** We present the impact of different conjunction words on models’ causal epistemic consistency, with distinctions highlighted by varying colors on the x-axis labels in Figure 5. A consistent trend is observed across different models and causal epistemic consistency metrics. Specifically, coordinating conjunctions (“so”) and conjunctive adverbs (“therefore”, “thus”, “hence”) yield better results, while subordinate conjunctions (“because”, “since”, “as”) underperform. We posit that placing subordinate conjunctions at the beginning of sentences aligns poorly with the natural language patterns seen by LLMs, potentially degrading performance.

**Comparison with Prompting.** In Figure 6, we compare the efficacy of internal conditional token probability for evaluating causal epistemic consistency with that of prompting-based strategies. We present the relative difference in the three most representative metrics ( $\tau$ -all, CGP, and IGC) for various models (Gemma, LLaMA2, Phi-3, and LLaMA3) when compared against the prompting aspect. Each subplot corresponds to one of the metrics, showing the differences for each model. Each model is represented by a box plot, calculated from differences given various conjunctions (“so”, “because”, “since”, “as”, “therefore”, “thus”, and “hence”). Notably, the Gemma model and medium-sized LLaMA2 models (7B, 13B) exhibit enhanced

<sup>3</sup>Even though `logprob` is provided, users cannot compute the probability of an arbitrary token given an input. The potential reason might be to avoid model distillation.

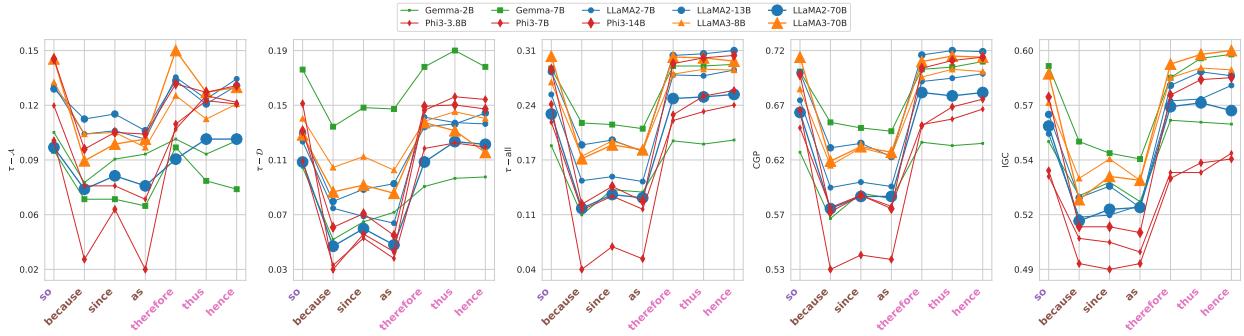


Figure 5: Impact of various conjunction words on the causal epistemic consistency across different LLMs. The x-axes categorize conjunction words into **coordinating conjunctions**, **subordinate conjunctions**, and **conjunctive adverbs**. The y-axes display values for causal epistemic consistency metrics. The analysis encompasses diverse model types (distinguished by marker color and shape) at different scales (represented by line thickness and marker size).

performance under the internal token probability method compared with prompting methods, indicating the effectiveness of internal token probability strategy on some models.

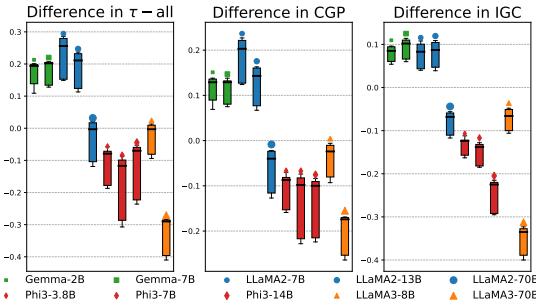


Figure 6: Relative differences in three metrics ( $\tau$ -all, CGP, and IGC) for various models using internal token probabilities versus prompting methods. Each box plot represents the distribution of differences for a model across different conjunction words. Markers above the box plots indicate models, aligned with the legend at the bottom. The marker shape and color indicate the model type, and the marker size represents the model size.

## 6 Related Work

**LLMs and Causality.** The investigation of LLMs in understanding and generating causal relations has garnered increasing attention. Previous studies often criticize LLMs for their propensity to inaccurately identify and comprehend the complex causal patterns among these facts (Jin et al. 2024; Li et al. 2024; Zečević et al. 2023; Cui et al. 2024b). Our study further contributes to this discourse by evaluating LLMs’ self-consistency in reasoning about fine-grained intermediates in causality and by providing metrics and empirical evidence for LLMs’ causal epistemic consistency.

**Defeasibility in Causal Reasoning.** Our study of fine-grained intermediates in causality extends the research initiated by  $\delta$ -CAUSAL (Cui et al. 2024c), which introduced the concepts of defeaters and supporters in causal analysis.

While  $\delta$ -CAUSAL provided a foundational framework for understanding causal defeasibility, it did not delve into the granularity necessary for nuanced causal reasoning. Our research advances this field by moving beyond the binary classification of intermediates as simply supporting or opposing. We refine the categorization of intermediates by considering both their polarity stance (supporting or opposing) and the intensity of their influence. This nuanced approach enhances the precision of causal analysis, enabling more reliable predictions in complex AI systems.

**Hallucination of LLMs.** LLMs suffer from generating nonsensical, fallacious, and undesirable content, known as hallucinations (Huang et al. 2023; Mouchel et al. 2024; Cui et al. 2024a). The most pertinent hallucination to causal epistemic consistency is the self-contradictory hallucination (Mündler et al. 2024), which means that LLMs generate two contradictory sentences given the same context. Specifically, our study on causal epistemic consistency investigates whether the causal intermediates generated by an LLM at various intensities contradict the ones ranked by the same LLM, similar to self-contradictory hallucinations. However, our study is distinctive in that we focus on the discrepancies between the causal intermediate generation and differentiating behaviors of LLMs, rather than the inconsistencies within the generated text. Additionally, our task focuses on self-consistency from a causal perspective, including the polarity (either supporting or defeating) and the intensity of these nuanced intermediates.

## 7 Conclusion

In conclusion, this study introduces causal epistemic consistency as a crucial framework for assessing the self-consistency of LLMs in distinguishing fine-grained causal intermediates. Supported by a novel suite of evaluation metrics, our comprehensive empirical analysis of 21 LLMs reveals significant limitations in their ability to maintain this consistency. This research addresses a critical gap in the understanding of complex causal reasoning and lays the foundation for the development of more self-consistent models capable of handling intricate causal relationships.

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## A Causal Conjunctions

In the context of causal epistemic consistency, the choice of conjunction words can significantly influence the interpretation of cause-effect relationships. Conjunctions serve as linguistic bridges that connect causes and effects, helping to clarify the nature and strength of these relationships. This section details the types of conjunctions used in our experiments and their implications for causal reasoning. Conjunctions that indicate causation can be broadly categorized into three types:

1. Coordinating conjunctions: These conjunctions are words that connect two or more clauses of the same grammatical types (Grammarly 2024). “For” and “so” are noteworthy because they usually indicate a causal relationship between two clauses.
2. Subordinating conjunctions: This type of conjunction links a dependent clause to an independent clause (Traffis 2020). “Because”, “since”, and “as” signify a causal relationship that the dependent clause is the cause of the independent clause.
3. Conjunctive adverbs: These adverbs or adverb phrases connect two independent clauses by indicating their relationship (Ellis 2023). “Therefore”, “thus”, and “hence” are common adverbs that indicate a causal relationship.

The typical usages of these conjunctions are presented in Table 2.

Conjunction	Usage	Applicable to autoregressive LLMs
<i>Coordinating conjunctions</i>		
For	{effect}, for {cause}	✗
So	{cause}, so {effect}	✓
<i>Subordinating conjunctions</i>		
Because	Because {cause}, {effect}	✓
Since	Since {cause}, {effect}	✓
As	As {cause}, {effect}	✓
<i>Conjunctive Adverbs</i>		
Therefore	{cause}; therefore, {effect}	✓
Thus	{cause}; thus, {effect}	✓
Hence	{cause}; hence, {effect}	✓

Table 2: Categorization of causal conjunctions used in the study, detailing their application in conditional probability calculations.

Though multiple conjunctions signify causality, the autoregressive nature of LLMs restricts our options to the conjunctions where the “cause” precedes the “effect” in the sentence.

## B Experimental Setup

### B.1 Configurations for Computing Infrastructure

The computing infrastructure of our experiments is as follows: the CPU model is an AMD EPYC 7543 32-Core processor. The GPU model is NVIDIA A100-SXM4-80GB. The total memory size is 503GB. The operating system is Ubuntu 20.04.6 LTS (Focal Fossa). The relevant libraries can be found in the `requirements.txt` file of our attached code supplementary file. We list the most essential packages in Table 3.

### B.2 Prompt Design of LLMs

**Generation.** Directly prompting models to generate 10 arguments—five defeaters followed by five supporters—has proven challenging and frequently results in unsatisfactory outputs, requiring multiple attempts for the same cause-effect pairs. To address this, we generate supporters and defeaters in a pairwise manner. This involves using the original defeater and supporter from the data and prompting the model four times for each cause-effect pair. The prompts are structured as follows:

Artifacts	Citation	Link	License
PyTorch	(Paszke et al. 2019)	<a href="https://pytorch.org/">https://pytorch.org/</a>	BSD-3 License
transformers	(Wolf et al. 2020)	<a href="https://huggingface.co/docs/transformers/index">https://huggingface.co/docs/transformers/index</a>	Apache License 2.0
Accelerate	(Gugger et al. 2022)	<a href="https://huggingface.co/docs/accelerate/index">https://huggingface.co/docs/accelerate/index</a>	Apache License 2.0
nltk	(Bird and Loper 2004)	<a href="https://www.nltk.org/">https://www.nltk.org/</a>	Apache License 2.0
numpy	(Harris et al. 2020)	<a href="https://numpy.org/">https://numpy.org/</a>	BSD License
matplotlib	(Hunter 2007)	<a href="https://matplotlib.org/">https://matplotlib.org/</a>	BSD compatible License
OpenAI API	N/A	<a href="https://platform.openai.com/docs/api-reference">https://platform.openai.com/docs/api-reference</a>	MIT License

Table 3: Details of the artifacts we use.

- Generate two weaker defeaters.
- Generate two stronger defeaters.
- Generate two weaker supporters.
- Generate two stronger supporters.

By prompting the model to generate only two intermediates at a time, the text becomes easier to parse. Furthermore, each model exhibits unique output characteristics. For instance, LLaMA often begins with "Sure, here is [...]" before listing arguments. Due to these unique output formats across different models, we provide tailored scripts for each model to ensure consistent and accurate text generation. The prompt we design to generate these fine-grained intermediates is illustrated in Figure 7. For the hyperparameter, we use the default hyperparameter. After the prompting, we have a set of intermediates consisting of a subset of supporters, denoted as  $\mathcal{A}$ , and a subset of defeaters, denoted as  $\mathcal{D}$ .

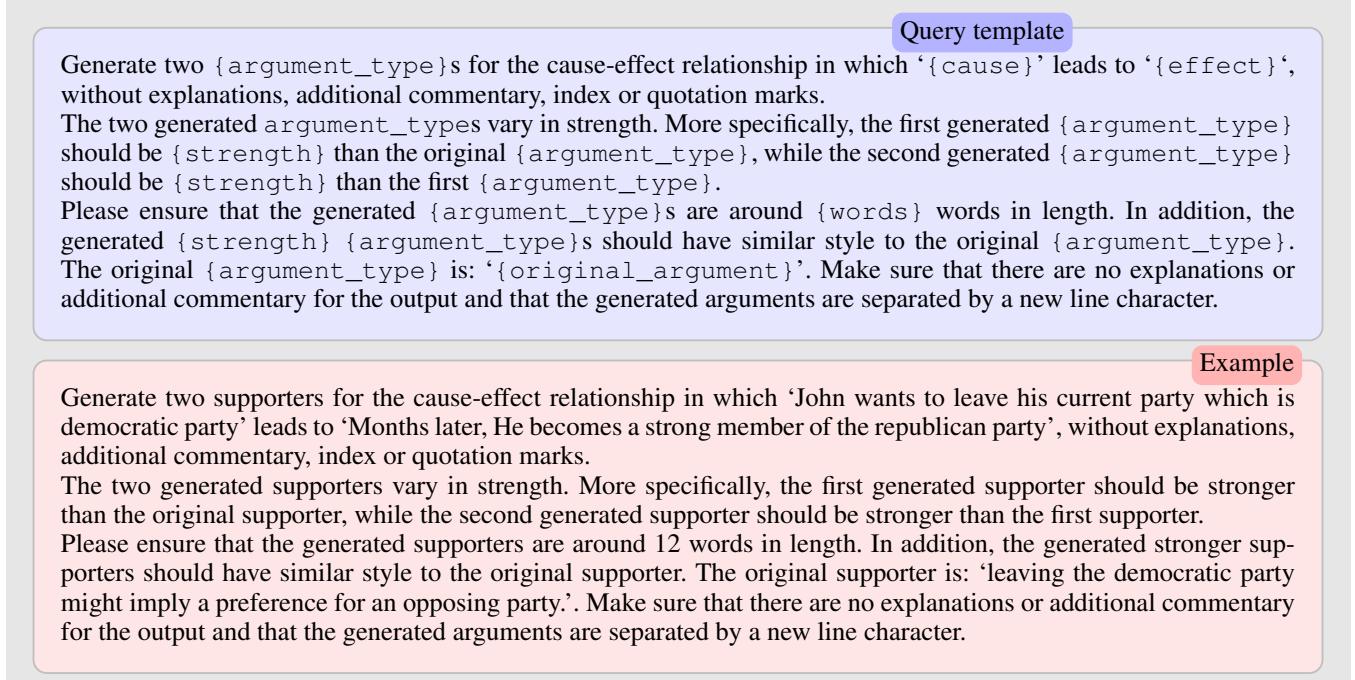


Figure 7: Example prompts for generating fine-grained intermediates with LLMs. The {argument\_type} is selected from {defeater, supporters}, while the {strength} is selected from {stronger, weaker}.

**Ranking.** The prompt we use to rank these fine-grained intermediates is present in Figure 8.

### B.3 Conditional Probability Estimation

```

1  from abc import ABC, abstractmethod
2  import torch
3
4
5  class ConditionalProb(ABC):
6      """
7          An abstract base class for computing conditional probabilities in different models
8          including
9          LLaMA, Mistral, and Gemma.
10         """
11
12     def __init__(self, args):
13         self.args = args
14         self.device = torch.device('cuda' if args.cuda else 'cpu')
15
16         self.base_model = None
17         self.tokenizer = None

```

```

17     self.ignored_id_in_label = None
18     self.initialize_model_and_tokenizers()
19     self.set_ignored_id_in_label()
20
21     self.base_model.eval()
22     self.base_model.to(self.device)
23
24     @abstractmethod
25     def initialize_model_and_tokenizers(self):
26         """
27             Abstract method that must be implemented by all subclasses to set up the model and
28             tokenizers.
29         """
30         pass
31
32     @abstractmethod
33     def set_ignored_id_in_label(self):
34         pass
35
36     @torch.no_grad()
37     def calculate_conditional_probability(self, input_text, output_text):
38         # Before everything start, double-check.
39         assert (self.base_model is not None and self.tokenizer is not None and self.
40         ignored_id_in_label is not None), \
41             "Make sure the base_model, tokenizers, and ignored_id_in_label well set. "
42
43         print("input_text: {} \noutput_text: {}".format(input_text, output_text))
44
45         # Process the input and output text
46         input_text = input_text.strip()
47         output_text = output_text.strip()
48         input_text = input_text + " " # Add a space at the end
49         combined_text = input_text + output_text
50
51         # Combine the input and output text
52         combined_inputs = self.tokenizer(combined_text, return_tensors="pt").to(self.
53         device)
54
55         # Create labels, mask the input text part
56         labels = combined_inputs['input_ids'].clone()
57         labels[labels == self.tokenizer.pad_token_id] = self.ignored_id_in_label # -100
58         is ignored in loss computation
59         labels[:, :len(self.tokenizer.encode(input_text.strip()))] = self.
60         ignored_id_in_label # Remove the last space by strip()
61
62         # Compute the loss
63         loss = self.base_model(**combined_inputs, labels=labels).loss
64
65         # Compute the probability of the output text
66         output_length = len(self.tokenizer.encode(output_text)) - 1 # -1 to remove the
67         first special token
68         probability = torch.exp(-loss * output_length)
69         ret_dict = {"input_txt": input_text, "output_text": output_text, "conditional_prob":
70         probability}
71         return ret_dict

```

Please note that the `base_model` should be `*ForCausalLM` (`GemmaForCausalLM`, `AutoModelForCausalLM`, and `LlamaForCausalLM`), which is for autoregressive language modelling. This series of models predicts the next token in the sequence given all previous tokens. In other words, the model attends only to the leftward context.

**Other formulae.** Apart from the conditional probability discussed in Section 5, alternative approaches exist for estimating the correlation degree between two events.

The average conditional probability is defined as

$$P_{\text{avg}}(x, y) = \frac{\sum_{i=1}^{|y|} p(y_i|x, y_{<i})}{|y|} \quad (10)$$

Holtzman et al. (2021) introduce domain conditional pointwise mutual information (PMI) to measure the correlation between  $x$  and  $y$ .

$$\text{PMI}_{\text{DC}}(x, y, \text{domain}) = \frac{p(y|x, \text{domain})}{p(y|\text{domain})} \quad (11)$$

However, both formulations involve scaling—either by the sentence length of  $y$  or the sequential probability of  $y$ . Consequently, these approaches do not alter the conclusion regarding the ranking order of intermediates discussed in Section 5.1.

## C Further Discussion on Proposed Metrics

In this section, we first present more discussion for the novel intra-clustering metrics in Appendix C.1, which covers the implication of the polarity changes and more case studies. Additionally, to better understand the difference between these proposed metrics, we explain these metrics with examples in Appendix C.2.

### C.1 Intra-Group Clustering

**Implication of Polarity Changes.** Polarity changes in a sequence often indicate transitions between different states, representing cluster changes. By quantifying these polarity changes as distances, IGC accurately captures these cluster changes. Namely, in the context of sequence clustering, counting polarity changes shifts the focus to transitions rather than mere index differences. For example, in a sequence of customer interactions, a transition from browsing items to adding to the shopping cart has a greater impact on cluster formulation.

Besides, polarity change provides an intuitive measure for evaluating the quality of sequence clustering. A sequence with fewer internal polarity changes is more cohesive, as there are no interruptions within different snippets of the sequences. Conversely, frequent polarity changes suggest that the sequences are more intertwined, indicating that the clusters are not distinctly separated but rather mixed together. It reflects overlapping or intertwined behavioral patterns of these snippets with the sequence.

In summary, with polarity changes, we can better understand the clustering quality, leading to more meaningful insights from the sequence data.

**Case study examples** We use the following example ■■●■■●●●●■● to detail the calculation process of IGC. Based on the clustering distance definition, the distance matrix is

0	0	1	1	1	2	2	2	2	3
0	0	1	1	1	2	2	2	2	3
1	1	0	1	1	1	1	1	2	2
1	1	1	0	0	1	1	1	1	2
1	1	1	0	0	1	1	1	1	2
2	2	1	1	1	0	0	0	1	1
2	2	1	1	1	0	0	0	1	1
2	2	1	1	1	0	0	0	1	1
2	2	2	1	1	1	1	1	0	1
3	3	2	2	2	1	1	1	1	0

The silhouette score for each element in the sequence individually is  $\left[ \frac{(1+2+2+2+3)/5-(0+1+1+2)/4}{\max(((1+2+2+2+3)/5,(0+1+1+2)/4)}, \frac{(1+1+1+1+2)/5-(1+1+1+2)/4}{\max((1+1+1+1+2)/5,(1+1+1+2)/4)}, \frac{(1+1+1+1+2)/5-(1+1+0+1)/4}{\max((1+1+1+1+2)/5,(1+1+0+1)/4)}, \frac{(2+2+1+1+1)/5-(1+0+0+1)/4}{\max((2+2+1+1+1)/5,(1+0+0+1)/4)}, \frac{(2+2+1+1+1)/5-(1+0+0+1)/4}{\max((2+2+1+1+1)/5,(1+0+0+1)/4)}, \frac{(2+1+1+1+1)/5-(2+2+1+1)/4}{\max((2+1+1+1+1)/5,(2+2+1+1)/4)}, \frac{(2+1+1+1+1)/5-(2+2+1+1)/4}{\max((2+1+1+1+1)/5,(2+2+1+1)/4)}, \frac{(3+3+2+2+1)/5-(2+1+1+1)/4}{\max((3+3+2+2+1)/5,(2+1+1+1)/4)} \right] = [0.5, 0.5, -0.04, 0.375, 0.375, 0.643, 0.643, 0.643, -0.2, -0.432]$ , and the final IGC value is 0.387.

**Optimal Cases** An optimal case for IGC is that ■■■■■●●●●●. Following the calculation rule, the distance matrix is:

0	0	0	0	0	1	1	1	1	1
0	0	0	0	0	1	1	1	1	1
0	0	0	0	0	1	1	1	1	1
0	0	0	0	0	1	1	1	1	1
0	0	0	0	0	1	1	1	1	1
1	1	1	1	1	0	0	0	0	0
1	1	1	1	1	0	0	0	0	0
1	1	1	1	1	0	0	0	0	0
1	1	1	1	1	0	0	0	0	0
1	1	1	1	1	0	0	0	0	0

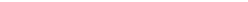
**Edge cases.** An edge case for the IGC is . In this case, the distance matrix is:

In this case, if we calculate the silhouette score for all elements using  $s(i) = \frac{b(i) - a(i)}{\max(a(i), b(i))}$ , the silhouette scores for elements in the sequence individually are [1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 0.0]. For the last element, the silhouette score is 0, which means this element is on the border of two clusters. However, please note that this element ■ is also the only element of its type in the sequence. Motivated by this case, we update the silhouette score calculation as:

$$s(i) = \begin{cases} 1 & \text{if } i \text{ is alone its cluster,} \\ \frac{b(i)-a(i)}{\max(a(i), b(i))} & \text{otherwise.} \end{cases} \quad (12)$$

which considers the edge case when there is only one element inside certain group. With this updated formula, the silhouette scores for all elements are [1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0], which follows our intuition that the elements are perfectly clustered. Similarly, in the dual case , the distance matrix is

The silhouette scores for all elements are [1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0, 1.0].

However, when the sole member of a group appears in the middle inside another group, such as , now the distance matrix becomes

0	0	0	0	1	1	1	1	1
0	0	0	0	1	1	1	1	1
0	0	0	0	1	1	1	1	1
0	0	0	0	1	1	1	1	1
1	1	1	1	0	1	1	1	1
1	1	1	1	1	0	0	0	0
1	1	1	1	1	0	0	0	0
1	1	1	1	1	0	0	0	0
1	1	1	1	1	0	0	0	0
1	1	1	1	1	0	0	0	0

The silhouette scores for elements in the sequence individually are [0.38, 0.38, 0.38, 0.38, 1.0, 0.5, 0.5, 0.5, 0.5, 0.5].

## C.2 Illustration of Proposed Metrics with Examples

We illustrate the proposed metrics with the following cases:

- *Optimal case*: The optimal case is  $\boxed{5} \ \boxed{4} \ \boxed{3} \ \boxed{2} \ \boxed{1} \ \oplus \ \circled{2} \ \circled{3} \ \circled{4} \ \circled{5}$ , where the ranking order matches the order in the generation phase perfectly. In this case, all the values of the metrics are 1.0, which is the desired property for proper evaluation metrics.
  - *Cases to show intensity ranking concordance for intensity discerning*: In this sequence:  $\boxed{5} \ \boxed{4} \ \boxed{3} \ \boxed{2} \ \oplus \ \boxed{1} \ \boxed{1} \ \oplus \ \circled{2} \ \circled{3} \ \circled{4} \ \circled{5}$ , similar as the optimal case, but a slight difference between  $\boxed{1}$  and  $\oplus 1$ . This difference doesn't change the intensity ranking concordance within the supporter and the defeater group. Namely,  $\tau\text{-A}$  and  $\tau\text{-D}$  keep the same. However, this difference changes the intensity ranking concordance for the entire intermediate set, i.e.,  $\tau\text{-all}$ .

Sequence	Intensity ranking concordance			Cross-group position	Intra-group clustering
	$\tau\text{-}\mathcal{A} \uparrow$	$\tau\text{-}\mathcal{D} \uparrow$	$\tau\text{-all} \uparrow$		
<i>Optimal case</i>					
-5 -4 -3 -2 -1 +1 +2 +3 +4 +5	1.0	1.0	1.0	1.0	1.0
<i>Cases to show changes captured by intensity ranking concordance.</i>					
-5 -4 -3 -2 -1 +1 +2 +3 +4 +5	1.000	1.000	1.000	1.000	1.000
-5 -4 -3 -2 +1 -1 +2 +3 +4 +5	1.000	1.000	0.867	0.960	0.694
<i>Cases to show the changes captured by cross-group position agreement.</i>					
-5 -4 -2 +1 +2 -1 -3 +3 +4 +5	1.000	-0.200	0.289	0.840	0.510
-5 -4 -3 -2 +1 +2 +3 +4 -1 +5	1.000	1.000	0.467	0.840	0.502
<i>Cases to show the changes captured by intra-group clustering.</i>					
-5 -4 +1 -2 -1 -3 +2 +3 +4 +5	1.000	-0.200	0.244	0.880	0.543
+4 +3 -1 +2 +1 +5 -2 -3 -4 -5	-0.600	0.200	0.378	0.120	0.543

Table 4: Case studies illustrating different aspects captured by the proposed metrics: intensity ranking concordance, cross-group position agreement, and intra-group clustering.

- *Cases to show the changes captured by cross-group position agreement for polarity differentiation:* In the first sequence:  , two supporters ( and  ) are ranked before two defeaters ( and  ). In this case, the number of cross-group position disagreements is  $2 \times 2 = 4$ . In the second sequence:  , four supporters (, , , and  ) are ranked before one defeater (), resulting in  $4 \times 1 = 4$  cross-group position disagreements. We observe that both sequences achieve the same CGP value of 0.840, verifying the efficacy of our proposed CGP metric.
  - *Cases to show the changes captured by intra-group clustering for cluster formulation:* In the first sequence  and the second sequence  . Although these two sequences differ significantly, they follow the same sequence clustering pattern. Specifically, the first sequence follows the pattern  , while the second sequence follows the dual clustering pattern  . This dualarity is verified by the identical IGC metric values of 0.543 for both sequences.

## D More Results

## D.1 Visualizations of Causal Epistemic Consistency of All Models

In this subsection, we present the visualizations of causal epistemic consistency of all the studied LLMs in Figure 9. Each sub-figure within the figure represents a specific model, showing how each LLMs performs regarding causal epistemic consistency. The result indicates that larger models tend to exhibit more stable and consistent differentiation of fine-grained intermediates.

## D.2 More Results with Conjunction Words

We present the full results of LLMs with different conjunction words in Table 5.

Prompt template

Given a defeasible cause-effect pair and ten arguments with varying strength, please give a ranking of the arguments based on whether they strengthen or weaken the argumentative strength of the cause-effect pair. Note that the ten arguments consist of five supporting arguments and five defeating arguments. The ranking should be in the order from the argument that weakens the argumentative strength of the pair the most to the argument that strengthens the argumentative strength the most.

In addition, please ensure that the result only contains indices referring to each argument, separated by a single space and without any additional explanation or comments.

The cause is '{cause}' and the effect is '{effect}'.

The ten arguments are:

1. {argument\_1}
2. {argument\_2}
3. {argument\_3}
4. {argument\_4}
5. {argument\_5}
6. {argument\_6}
7. {argument\_7}
8. {argument\_8}
9. {argument\_9}
10. {argument\_10}

Example

Given a defeasible cause-effect pair and ten arguments with varying strength, please give a ranking of the arguments based on whether they strengthen or weaken the force of reasons of the cause-effect pair. Note that the ten arguments consist of five supporting arguments and five defeating arguments. The ranking should be in the order from the argument that weakens the argumentative strength of the pair the most to the argument that strengthens the argumentative strength the most.

In addition, please ensure that the result only contains indices referring to each argument, separated by a single space and without any addition explanation or comments.

The cause is 'John wants to leave his current party which is democratic party' and the effect is 'Months later, He becomes a strong member of the republican party'.

The ten arguments are:

1. John is appointed to a nonpartisan governmental position.
2. John decides to become an independent politician.
3. John changes his mind and runs on the Democratic ticket.
4. leaving the democratic party might imply a preference for an opposing party.
5. abandoning the democratic party strongly indicates a shift towards republican ideals and membership.
6. leaving one party could indicate a desire to join another.
7. John changes his position to remain an independent voter.
8. John changes his mind and votes for Democratic candidates.
9. departing the democratic party suggests a likelihood of aligning with the republican opposition.
10. deciding to leave might show interest in an alternative political group.

Figure 8: Example prompts for ranking fine-grained intermediates, guiding LLMs to order arguments based on their influence on the cause-effect relationship.

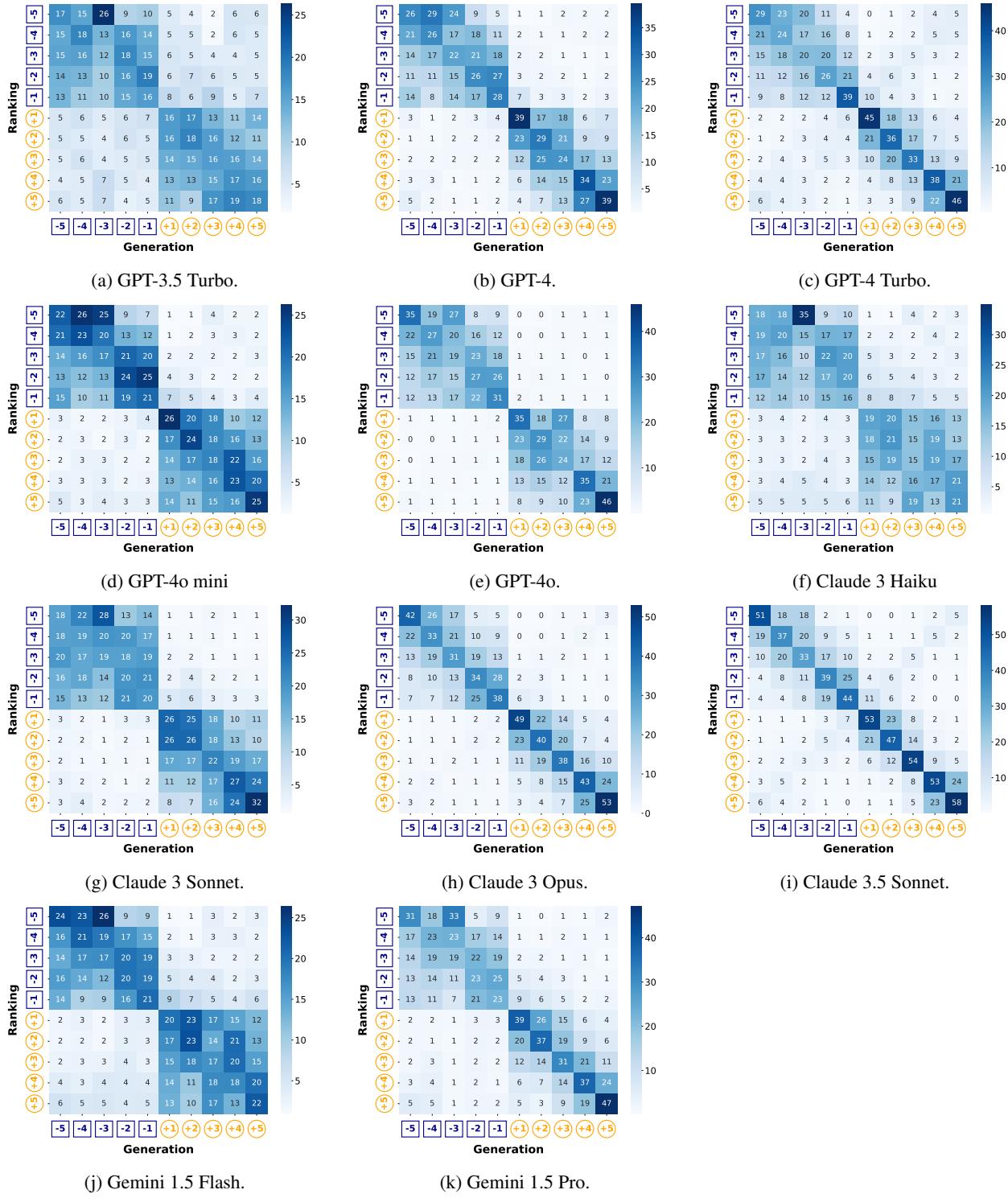


Figure 9: Visualization of causal epistemic consistency in different closed-source LLMs, highlighting their performance in maintaining consistency across generated intermediates.

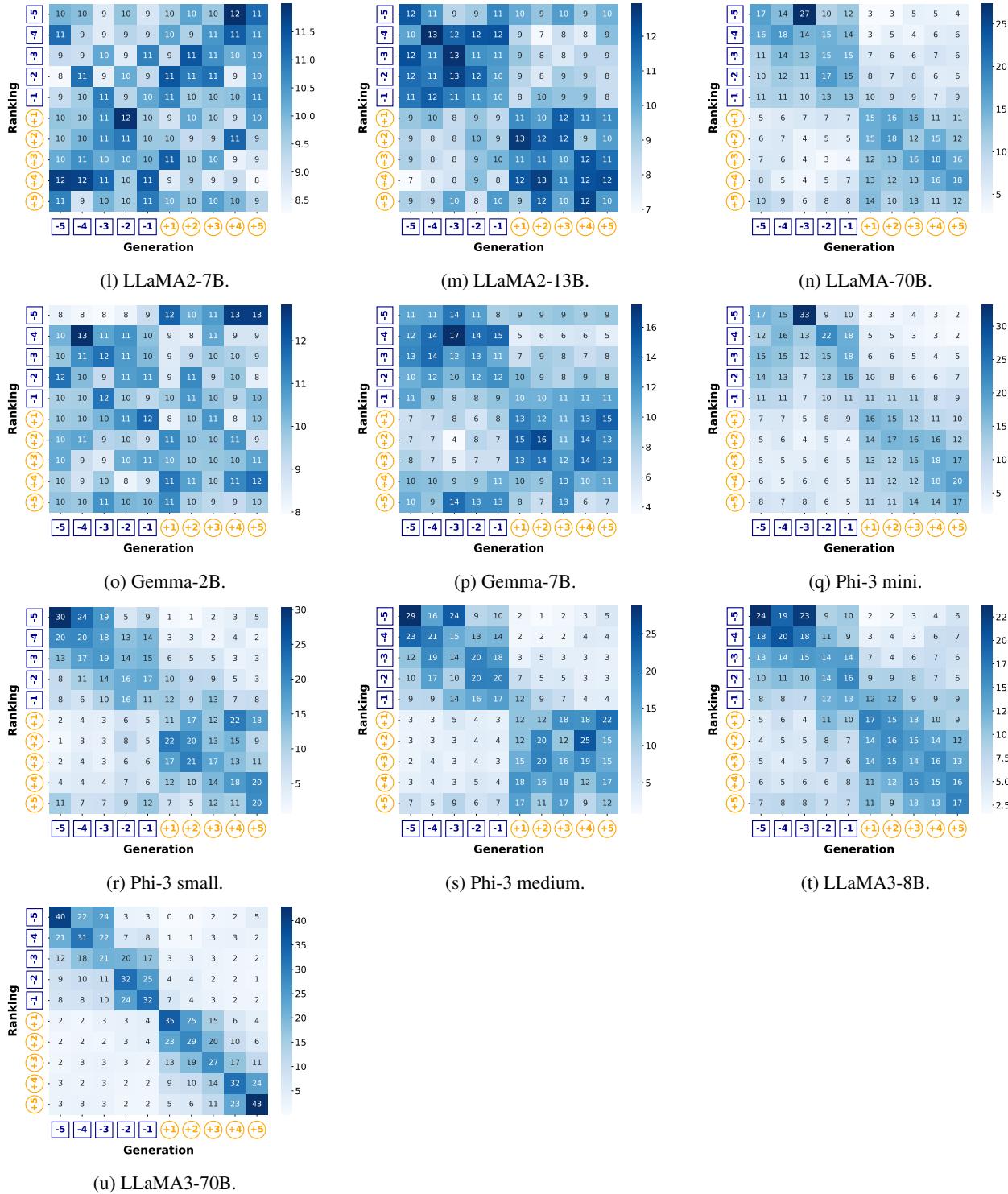


Figure 9: Continued visualization of causal epistemic consistency in different open-source LLMs, providing a comparative analysis against closed-source counterparts.

Aspect	Intensity ranking concordance			Cross-group position	Intra-group clustering
	$\tau\text{-}\mathcal{A} \uparrow$	$\tau\text{-}\mathcal{D} \uparrow$	$\tau\text{-all} \uparrow$	CGP $\uparrow$	IGC $\uparrow$
<i>LLaMA2-7B</i>					
prompting	-0.017 ± 0.403	0.007 ± 0.400	-0.001 ± 0.249	0.475 ± 0.199	0.474 ± 0.090
“so”	0.134 ± 0.432	0.122 ± 0.436	0.255 ± 0.305	0.678 ± 0.227	0.557 ± 0.199
“because”	0.105 ± 0.429	0.073 ± 0.423	0.149 ± 0.309	0.599 ± 0.229	0.514 ± 0.155
“since”	0.107 ± 0.436	0.067 ± 0.427	0.154 ± 0.308	0.604 ± 0.228	0.515 ± 0.160
“as”	0.102 ± 0.436	0.062 ± 0.432	0.148 ± 0.315	0.600 ± 0.233	0.520 ± 0.163
“therefore”	0.139 ± 0.445	0.140 ± 0.437	0.279 ± 0.301	0.695 ± 0.227	0.574 ± 0.211
“thus”	0.126 ± 0.446	0.136 ± 0.426	0.278 ± 0.299	0.698 ± 0.229	0.575 ± 0.210
“hence”	0.138 ± 0.440	0.135 ± 0.426	0.285 ± 0.299	0.702 ± 0.229	0.582 ± 0.214
<i>LLaMA2-13B</i>					
prompting	-0.000 ± 0.411	0.026 ± 0.417	0.072 ± 0.256	0.560 ± 0.197	0.480 ± 0.109
“so”	0.132 ± 0.423	0.128 ± 0.413	0.283 ± 0.281	0.703 ± 0.221	0.567 ± 0.206
“because”	0.114 ± 0.430	0.078 ± 0.427	0.193 ± 0.298	0.635 ± 0.223	0.524 ± 0.168
“since”	0.117 ± 0.429	0.087 ± 0.433	0.199 ± 0.299	0.639 ± 0.225	0.530 ± 0.174
“as”	0.107 ± 0.432	0.091 ± 0.423	0.185 ± 0.299	0.627 ± 0.222	0.519 ± 0.164
“therefore”	0.137 ± 0.427	0.133 ± 0.422	0.303 ± 0.282	0.719 ± 0.221	0.582 ± 0.217
“thus”	0.123 ± 0.427	0.135 ± 0.420	0.305 ± 0.283	0.723 ± 0.219	0.589 ± 0.220
“hence”	0.134 ± 0.423	0.143 ± 0.421	0.309 ± 0.280	0.722 ± 0.219	0.587 ± 0.219
<i>LLaMA2-70B</i>					
prompting	0.012 ± 0.409	0.010 ± 0.434	0.234 ± 0.349	0.707 ± 0.271	0.629 ± 0.215
“so”	0.097 ± 0.424	0.107 ± 0.415	0.231 ± 0.314	0.667 ± 0.241	0.561 ± 0.210
“because”	0.072 ± 0.429	0.045 ± 0.429	0.115 ± 0.323	0.580 ± 0.237	0.512 ± 0.160
“since”	0.080 ± 0.429	0.058 ± 0.425	0.132 ± 0.318	0.591 ± 0.240	0.518 ± 0.165
“as”	0.074 ± 0.434	0.046 ± 0.428	0.128 ± 0.319	0.591 ± 0.238	0.519 ± 0.166
“therefore”	0.090 ± 0.430	0.107 ± 0.409	0.250 ± 0.306	0.685 ± 0.236	0.571 ± 0.215
“thus”	0.102 ± 0.430	0.122 ± 0.409	0.252 ± 0.311	0.682 ± 0.242	0.573 ± 0.216
“hence”	0.102 ± 0.431	0.120 ± 0.410	0.255 ± 0.308	0.685 ± 0.237	0.569 ± 0.213
<i>Gemma-2B</i>					
prompting	-0.021 ± 0.412	0.001 ± 0.410	-0.002 ± 0.245	0.502 ± 0.190	0.468 ± 0.083
“so”	0.106 ± 0.424	0.103 ± 0.440	0.192 ± 0.334	0.631 ± 0.255	0.553 ± 0.204
“because”	0.076 ± 0.420	0.050 ± 0.445	0.107 ± 0.334	0.571 ± 0.252	0.525 ± 0.179
“since”	0.090 ± 0.425	0.063 ± 0.445	0.138 ± 0.332	0.594 ± 0.252	0.532 ± 0.187
“as”	0.093 ± 0.422	0.070 ± 0.455	0.135 ± 0.330	0.589 ± 0.245	0.522 ± 0.175
“therefore”	0.102 ± 0.431	0.089 ± 0.440	0.198 ± 0.340	0.640 ± 0.259	0.564 ± 0.217
“thus”	0.093 ± 0.424	0.095 ± 0.441	0.194 ± 0.340	0.637 ± 0.260	0.563 ± 0.215
“hence”	0.101 ± 0.426	0.096 ± 0.438	0.199 ± 0.339	0.639 ± 0.258	0.562 ± 0.213
<i>Gemma-7B</i>					
prompting	-0.006 ± 0.392	0.016 ± 0.389	0.085 ± 0.256	0.575 ± 0.203	0.484 ± 0.122
“so”	0.095 ± 0.441	0.175 ± 0.431	0.287 ± 0.312	0.704 ± 0.240	0.592 ± 0.229
“because”	0.066 ± 0.430	0.133 ± 0.425	0.220 ± 0.310	0.658 ± 0.239	0.553 ± 0.200
“since”	0.066 ± 0.419	0.147 ± 0.428	0.218 ± 0.311	0.653 ± 0.236	0.547 ± 0.199
“as”	0.062 ± 0.426	0.146 ± 0.426	0.213 ± 0.313	0.650 ± 0.235	0.544 ± 0.195
“therefore”	0.097 ± 0.439	0.177 ± 0.432	0.290 ± 0.309	0.706 ± 0.237	0.586 ± 0.225
“thus”	0.077 ± 0.438	0.189 ± 0.426	0.290 ± 0.307	0.708 ± 0.240	0.596 ± 0.233
“hence”	0.072 ± 0.432	0.177 ± 0.429	0.292 ± 0.307	0.713 ± 0.239	0.598 ± 0.233
<i>Phi3-3.8B</i>					
prompting	0.135 ± 0.431	0.012 ± 0.393	0.300 ± 0.336	0.740 ± 0.275	0.659 ± 0.222

“so”	0.122 ± 0.435	0.108 ± 0.408	0.221 ± 0.283	0.653 ± 0.216	0.535 ± 0.175
“because”	0.074 ± 0.432	0.031 ± 0.428	0.113 ± 0.297	0.581 ± 0.222	0.503 ± 0.140
“since”	0.074 ± 0.429	0.051 ± 0.416	0.130 ± 0.291	0.592 ± 0.217	0.501 ± 0.139
“as”	0.066 ± 0.421	0.036 ± 0.424	0.114 ± 0.293	0.582 ± 0.217	0.496 ± 0.131
“therefore”	0.108 ± 0.434	0.117 ± 0.411	0.223 ± 0.290	0.656 ± 0.222	0.537 ± 0.180
“thus”	0.128 ± 0.436	0.121 ± 0.409	0.234 ± 0.285	0.661 ± 0.220	0.537 ± 0.182
“hence”	0.124 ± 0.430	0.118 ± 0.413	0.242 ± 0.286	0.670 ± 0.223	0.547 ± 0.189
<i>Phi3-7B</i>					
prompting	0.092 ± 0.443	0.204 ± 0.422	0.347 ± 0.348	0.753 ± 0.254	0.672 ± 0.220
“so”	0.101 ± 0.417	0.150 ± 0.420	0.243 ± 0.288	0.669 ± 0.217	0.538 ± 0.178
“because”	0.030 ± 0.411	0.028 ± 0.426	0.040 ± 0.310	0.525 ± 0.226	0.490 ± 0.121
“since”	0.060 ± 0.417	0.054 ± 0.433	0.068 ± 0.303	0.538 ± 0.220	0.487 ± 0.117
“as”	0.024 ± 0.418	0.041 ± 0.421	0.053 ± 0.304	0.534 ± 0.224	0.490 ± 0.120
“therefore”	0.111 ± 0.425	0.145 ± 0.421	0.230 ± 0.290	0.655 ± 0.220	0.534 ± 0.176
“thus”	0.125 ± 0.409	0.155 ± 0.421	0.253 ± 0.285	0.672 ± 0.217	0.542 ± 0.182
“hence”	0.123 ± 0.408	0.153 ± 0.416	0.260 ± 0.283	0.679 ± 0.215	0.544 ± 0.184
<i>Phi3-14B</i>					
prompting	-0.056 ± 0.441	0.154 ± 0.406	0.356 ± 0.367	0.801 ± 0.286	0.801 ± 0.230
“so”	0.150 ± 0.423	0.130 ± 0.403	0.286 ± 0.292	0.701 ± 0.226	0.576 ± 0.216
“because”	0.096 ± 0.425	0.059 ± 0.412	0.120 ± 0.308	0.577 ± 0.234	0.509 ± 0.151
“since”	0.106 ± 0.419	0.069 ± 0.429	0.142 ± 0.304	0.592 ± 0.229	0.509 ± 0.153
“as”	0.105 ± 0.429	0.053 ± 0.424	0.124 ± 0.304	0.580 ± 0.229	0.506 ± 0.147
“therefore”	0.135 ± 0.430	0.148 ± 0.409	0.293 ± 0.298	0.707 ± 0.226	0.577 ± 0.216
“thus”	0.130 ± 0.426	0.149 ± 0.408	0.300 ± 0.290	0.714 ± 0.226	0.585 ± 0.218
“hence”	0.134 ± 0.419	0.146 ± 0.417	0.303 ± 0.291	0.717 ± 0.226	0.586 ± 0.220
<i>LLaMA3-8B</i>					
prompting	0.030 ± 0.444	0.139 ± 0.436	0.273 ± 0.387	0.712 ± 0.285	0.639 ± 0.217
“so”	0.136 ± 0.432	0.139 ± 0.416	0.270 ± 0.310	0.688 ± 0.236	0.573 ± 0.212
“because”	0.105 ± 0.428	0.103 ± 0.435	0.179 ± 0.325	0.619 ± 0.241	0.534 ± 0.175
“since”	0.106 ± 0.441	0.111 ± 0.429	0.198 ± 0.330	0.635 ± 0.242	0.544 ± 0.179
“as”	0.097 ± 0.436	0.101 ± 0.434	0.186 ± 0.325	0.628 ± 0.239	0.533 ± 0.172
“therefore”	0.128 ± 0.441	0.137 ± 0.420	0.280 ± 0.319	0.699 ± 0.239	0.586 ± 0.217
“thus”	0.114 ± 0.432	0.144 ± 0.415	0.286 ± 0.315	0.706 ± 0.237	0.591 ± 0.223
“hence”	0.123 ± 0.438	0.139 ± 0.416	0.285 ± 0.315	0.704 ± 0.237	0.590 ± 0.224
<i>LLaMA3-70B</i>					
prompting	0.357 ± 0.469	0.343 ± 0.419	0.586 ± 0.415	0.887 ± 0.274	0.923 ± 0.177
“so”	0.150 ± 0.433	0.127 ± 0.416	0.302 ± 0.303	0.717 ± 0.227	0.588 ± 0.217
“because”	0.089 ± 0.430	0.085 ± 0.427	0.176 ± 0.320	0.623 ± 0.232	0.523 ± 0.170
“since”	0.099 ± 0.429	0.090 ± 0.421	0.193 ± 0.314	0.636 ± 0.236	0.535 ± 0.181
“as”	0.102 ± 0.435	0.084 ± 0.414	0.187 ± 0.319	0.631 ± 0.236	0.533 ± 0.179
“therefore”	0.155 ± 0.433	0.136 ± 0.427	0.301 ± 0.311	0.713 ± 0.235	0.593 ± 0.222
“thus”	0.130 ± 0.434	0.130 ± 0.423	0.300 ± 0.313	0.718 ± 0.237	0.598 ± 0.225
“hence”	0.133 ± 0.434	0.114 ± 0.423	0.296 ± 0.313	0.717 ± 0.238	0.600 ± 0.226

Table 5: Comparative results of different conjunction words on model performance, emphasizing their influence on maintaining causal epistemic consistency.