## Recent Empirical Studies on Return Predictability

WANG, Yanchu

Shanghai University of Finance and Economics

October 2024

### Motivation

- Forecasting stock returns (risk premium) is of great interests to both academics and practitioners.
- Economic theory indicates that expected returns should be time-varying and predictable.
- However, empirical findings fail to provide such evidence, especially for out-of-sample benefits.
- Welch and Goyal (2008) conclude that numerous economic variables with in-sample predictability fail to deliver out-of-sample gains.
- The failure may be due to:
  - 1. Model uncertainty and instability (Rapach, Strauss, and Zhou, 2010).
  - 2. Regime uncertainty and parameter uncertainty (Zhu and Zhu, 2013).
  - 3. State variable uncertainty (Binsbergen and Koijen, 2010). □

# Rapach, Strauss, and Zhou (2010)

- Previous findings.
- Combination methods.
- Forecast evaluation.
- Empirical Results.
- Macroeconomic links.
- Conclusion

## Previous Findings.

- Return predictability is a long-history topic in finance.
- A set of variables are considered to be helpful in forecasting returns:
  - 1. Firm-level valuation ratios: such as dividend-price, earning price, book-to-market etc.
  - 2. Economic activity indicators: such as interest rate, inflation rate, term and default spread etc.
  - 3. Other market data: consumption-wealth ratio, stock market volatility etc.
- Most existing studies focus on in-sample tests and conclude that there is significant evidence of return predictability.
- But it remains controversial, see the review paper of Spiegel (2008).

#### Combination Forecasts

- Consider two predictive variables: dividend yield and term spread.
- Previous literature shows that both variables can predict stock returns.
- But each variable alone may capture different components of economic conditions, and thus may give a false signal during certain periods.
- If these two variables are correlated, then a combination of them should be less volatile and provide better performance.
- We may extend the idea to numerous factors.

#### Combination Forecasts

- The combination forecasts are linked to macroeconomics.
- Fama and French (1989) and Cochrane (1999, 2007) argue that heightened risk aversion during economic recession require a higher risk premium.
- The combination forecasts reach local maxima very near NBER-dated business-cycle troughs.
- The forecasting power becomes stronger when economy is bad.
- The instability of individual predictive factors is related to instability in real economy.

## Predictive Regression Model

• A standard predictive regression model:

$$r_{t+1} = \alpha_i + \beta_i x_{i,t} + \varepsilon_{t+1},$$

where  $r_{t+1}$  is the return on a stock market index in excess of the risk-free rate, and  $x_{i,t}$  is a predictive variable.

- The out-of-sample forecasts are generated using a recursive estimation window.
- The full sample T is divided into a in-sample portion with m observations, and out-of-sample portion with q observations. T=m+q.

## Predictive Regression Model

• The first forecast is given by

$$\widehat{r}_{i,m+1} = \widehat{\alpha}_{i,m} + \widehat{\beta}_{i,m} x_{i,m},$$

where  $\widehat{\alpha}_{i,m}$  and  $\widehat{\beta}_{i,m}$  are the OLS estimates of  $\alpha_i$  and  $\beta_i$  generated by regressing  $\{r_t\}_{t=2}^m$  on a constant and  $\{x_{i,t}\}_{t=1}^{m-1}$ .

• The next forecast is given by

$$\widehat{r}_{i,m+2} = \widehat{\alpha}_{i,m+1} + \widehat{\beta}_{i,m+1} x_{i,m+1},$$

where  $\widehat{\alpha}_{i,m+1}$  and  $\widehat{\beta}_{i,m+1}$  are the OLS estimates of  $\alpha_i$  and  $\beta_i$  generated by regressing  $\{r_t\}_{t=2}^{m+1}$  on a constant and  $\{x_{i,t}\}_{t=1}^m$ .

- ullet Continue the procedure, we finally generate q forecasts based on  $x_{i,t}$ .
- We generate return forecasts using 15 individual factors (with details later).
- The historical average benchmark:  $\overline{r}_{t+1} = \sum_{j=1}^{t} r_j$ .
- If  $x_{i,t}$  contains useful information, then  $\hat{r}_{t+1}$  should perform better than  $\bar{r}_{t+1}$ .

### Forecast Combinations

- Bates and Granger (1969) point out that combination of individual factors can outperform individual factors.
- Forecast combination has recently received attention in macroeconomic forecasting literature (Stock and Watson, 1999, 2003, 2004).
- The combination forecasts of  $r_{t+1}$  is given by

$$\widehat{r}_{c,t+1} = \sum_{i=1}^{N} \omega_{i,t} \widehat{r}_{i,t+1},$$

where N=15, and  $\{\omega_{i,t}\}_{i=1}^{N}$  are the *ex ante* combining weights formed at time t.

- The first  $q_0$  observations from the out-of-sample period are used as the initial holdout period for estimating  $\omega_{i,t}$ .
- Thus we have  $q q_0$  combining forecasts in total.

### Forecast Combinations

- How to estimate  $\omega_{i,t}$ ?
- The mean combination forecast:  $\omega_{i,t} = 1/N$ .
- In practice, a trimmed mean combination forecast:

$$\omega_{i,t}=0$$
,

with the smallest and largest values, and

$$\omega_{i,t} = 1/(N-2),$$

with the remaining individual forecast.

### Forecast Combinations

 The discount mean square prediction error (DMSPE) combining forecast based on Stock and Watson (2004):

$$\omega_{i,t} = \phi_{i,t}^{-1} / \sum_{j=1}^{N} \phi_{j,t}^{-1},$$

where

$$\phi_{i,t} = \sum_{s=m}^{t-1} \theta^{t-1-s} (r_{s+1} - \widehat{r}_{i,s+1})^2.$$

- The DMSPE method assigns greater weights to individual forecasts with lower MSPE values.
- When  $\theta < 1$ , greater weight is attached to the recent forecast accuracy.
- $oldsymbol{ heta} heta = 1.0$  or 0.9 in empirical analysis.

ullet Out-of-sample  $R_{OS}^2$  based on Campbell and Thompson (2008)

$$R_{OS}^2 = 1 - \frac{\sum_{k=q_0+1}^q (r_{m+k} - \widehat{r}_{m+k})^2}{\sum_{k=q_0+1}^q (r_{m+k} - \overline{r}_{m+k})^2}.$$

- $R_{OS}^2$  compares the specified forecast performance with the historical average forecasts.
- If  $R_{OS}^2 > 0$ , then  $\hat{r}_{t+1}$  is better than  $\bar{r}_{t+1}$ .

- Even if  $R_{OS}^2 > 0$ , we don't know its significance.
- In order to test that, we follow Clark and West (2007) and first define

$$f_{t+1} = (r_{t+1} - \overline{r}_{t+1})^2 - [(r_{t+1} - \widehat{r}_{t+1})^2 - (\overline{r}_{t+1} - \widehat{r}_{t+1})^2].$$

- We the regress  $\{f_{s+1}\}_{s=m+q_0}^{T-1}$  on a constant and calculate the t-statistic.
- This is called MSPE-adjusted statistic and provide a one-sided (upper-tail) test.

- Even if  $R_{OS}^2$  is significantly positive, its values are usually small for predictive regression models.
- This raises the issue of economic significance.
- Let's consider the utility gain for a mean-variance investor who uses predictive returns to construct his optimal portfolio between stocks and risk-free bonds.
- It can be proved that the optimal weight for stocks is

$$w_t = (\frac{1}{\gamma})(\frac{r_{t+1}}{\sigma_{t+1}}).$$

• To be realistic, let  $w_t$  lie between 0% and 150%.

• If the investor use historical average forecast, then at time t, he need to decide the weight applied for t+1

$$w_{0,t}=(\frac{1}{\gamma})(\frac{\overline{r}_{t+1}}{\widehat{\sigma}_{t+1}^2}),$$

where  $\widehat{\sigma}_{t+1}^2$  is the rolling-window estimate of the variance of stock returns.

Over the out-of-sample period, the realized average utility level is

$$\widehat{\mathbf{v}}_0 = \widehat{\mu}_0 - 0.5 \gamma \widehat{\sigma}_0^2$$

where  $\widehat{\mu}_0$  and  $\widehat{\sigma}_0^2$  are the sample mean and variance of the portfolio constructed using the weights over the out-of-sample period.

YW (SUFE) Return Predictability 15

 We then compute the utility gain with individual factor or combined factor, j:

$$w_{j,t} = (\frac{1}{\gamma})(\frac{\widehat{r}_{t+1}}{\widehat{\sigma}_{t+1}^2}).$$

• The utility gain is

$$\widehat{\mathbf{v}}_j = \widehat{\mu}_j - 0.5 \gamma \widehat{\sigma}_j^2.$$

- The certainty equivalent return (CER) is the difference between  $\widehat{v}_j$  and  $\widehat{v}_0$ .
- We choose  $\gamma = 3$ .

#### Data

- Following Welch and Goyal (2008), the paper considers 15 variable (quarterly) for 1947:1 2005:4:
  - 1. Dividend-price ratio (log): D/P
  - 2. Dividend yield (log): D/Y
  - 3. Earnings-price ratio (log): E/P
  - 4. Dividend-payout ratio (log): D/E
  - 5. Stock variance: sum of squared daily returns on the S&P 500 index
  - 6. Book-to-market ratio: B/M
  - 7. Net equity expansion: twelve-month sum of net issues to total end-of-year market cap
  - 8. Treasury bill rate

#### Data

- 9. Long-term yield
  - 10. Long-term return
  - 11. Term spread: difference between long-term yield and the Treasury bill rate
  - 12. Default yield spread: difference between BAA- and AAA-corporate bond yield
  - 13. Default return spread: difference between long-term corporate bond and long-term government bond returns
  - 14. Inflation
  - 15. Investment-to-capital ratio
- Consider three different out-of-sample periods: 1965:1-2005:4, 1976:1-2005:4, and 2000:1-2005:4.

### Forecasting Results

- Cumulative square prediction error for individual factors vs. historical average benchmark (Figure 1).
- Cumulative square prediction error for combining forecasts vs. historical average benchmark (Figure 2).
- Detailed results (Table 1).

# Robustness Checks (Selected)

- Factor stabilization:
  - 1. Correlation between individual factors (Table 3)
  - 2. Combining forecasts reduce forecast variability (Figure 3).
  - 3. "Kitchen sink" Model

$$r_{t+1} = \alpha + \beta_1 x_{1,t} + ... + \beta_N x_{N,t} + \varepsilon_{t+1}.$$

It performs much worse than the combination method!

 It can be shown that the mean combination is a restricted forecast from a multiple regression model.

### Links to Real Economy

- Equity premium forecasts and NBER-dated business-cycle phases (Figure 6).
- Correlation of equity premium forecasts and GDP growth (Table 4).
- Forecasting gains during "good" and "bad" growth periods (Table 5).

### Conclusions

- Forecast combining method provides convincing evidence of out-of-sample predictability.
- It is successful since it is a compromise:
  - 1. Individual forecasts are too volatile.
  - 2. The historical average is too smooth.
- The result shows that existing asset pricing models relying on one or a few state variables will have difficulty in accurately tracking the expected return over time.