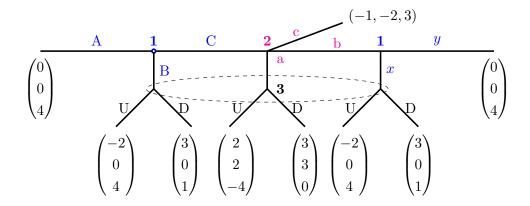
- 1. Determine whether the following statements are True or False and EXPLAIN. Most marks are for your explanations. (5 points each)
  - (a) Players make optimal choice at every information set in a subgame perfect Nash equilibrium.
  - (b) Provided consumers' preferences satisfy Local non-satiation, only relative prices matters in the economy.
  - (c) A Nash equilibrium is normal-form perfect if and only if no players play dominated strategies.
  - (d) The First-price sealed bid auction and the Dutch auction yield the same expected revenue if and only if all bidders are risk neutral.
- 2. For the game given below:

Player 1

	$b_1$	$b_2$	$b_3$	$b_4$
$A_1$	(0, 6)	(3, 1)	(7, 0)	(3, 7)
$A_2$	(5, 0)	(-5, 1)	(0, 7)	(1, 5)
$A_3$	(0, 6)	(10, 2)	(0, 0)	(2, -8)
$A_4$	(7, 3)	(0, 0)	(5, 1)	(2, 2)

- (a) Does any player have any dominated strategies? What are they? (5 points)
- (b) Find all pure strategy NE of the game. (5 points)
- (c) Does the game have any mixed strategy NE? If yes, please also give the mixed strategy NE. (10 points)
- 3. The two divisions of a large corporation, 1 and 2 decide simultaneously whether to develop a new product. Both divisions can get a benefit of 1 if at least one division develops the new product. A division's cost of development is  $c_i$ . While the benefit is common knowledge, each division's cost  $c_i$  is known only to itself. However, it is common knowledge that,  $c_1$  is drawn from a uniform distribution on [0,2] while  $c_2$  is drawn from a uniform distribution on  $[0,\frac{3}{2}]$ . Identify the Bayesian Nash equilibria of this game. (20 points)
- 4. An exchange economy consists of two consumers. Consumer A is endowed with 90 units of good x and 10 units of good y, while B is endowed with 10 units of good x and 90 units of good y. Their utility functions are, respectively,  $U_A(x,y) = \sqrt{(x-20)(y-10)}$ , and  $U_B(x,y) = \ln(x-10) + \ln(y-20)$ .
  - (a) Find the two consumer's demand functions; (5 points)
  - (b) Find the excess demand functions, and show the Walras' law holds; (5 points)
  - (c) Determine the competitive equilibrium. (10 points)
- 5. For the extensive form game below:



- (a) Write down the strategic form and identify all pure strategy NE; (5 points)
- (b) Identify all sequential equilibria; (10 points)
- (c) Identify all normal-form perfect equilibria of the game. (5 points)