

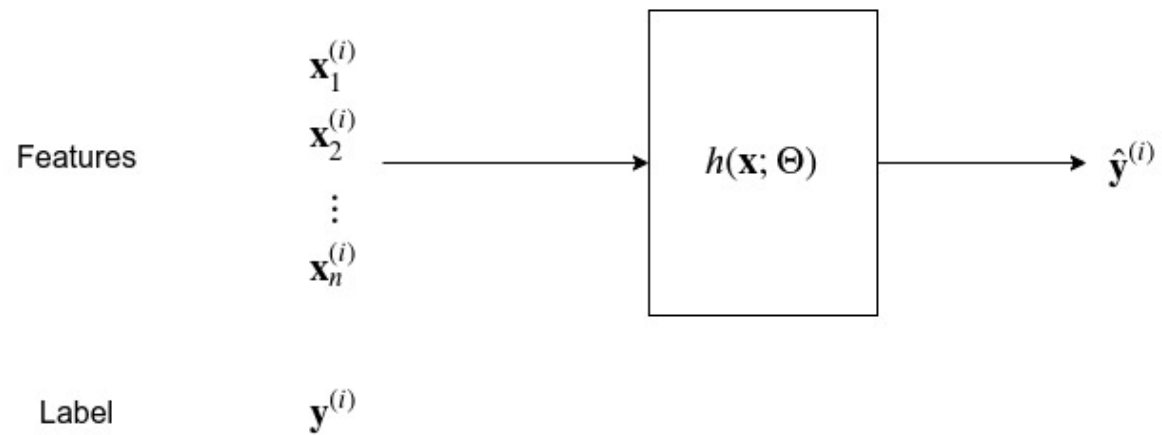
Notation

Training

Example

Model

Prediction

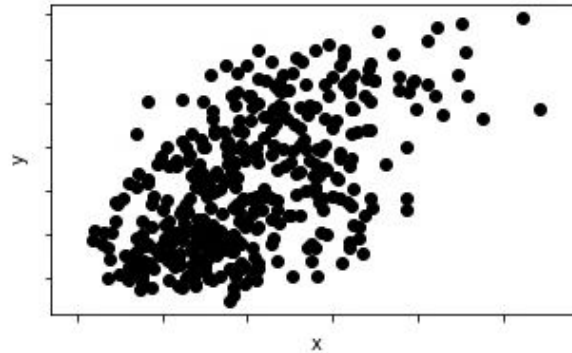


- Training

The key task of Machine Learning is finding the "best" values for parameters Θ .

The process of using training examples \mathbf{X} to find Θ

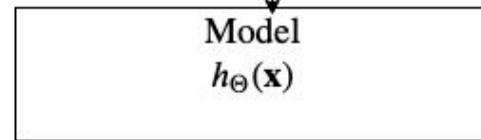
- is called *fitting* the model
- is solved as an optimization problem (to be described)



$\langle \mathbf{X}, \mathbf{y} \rangle$

Training examples

$\mathbf{X} : m \times n$
 $\mathbf{y} : n \times 1$



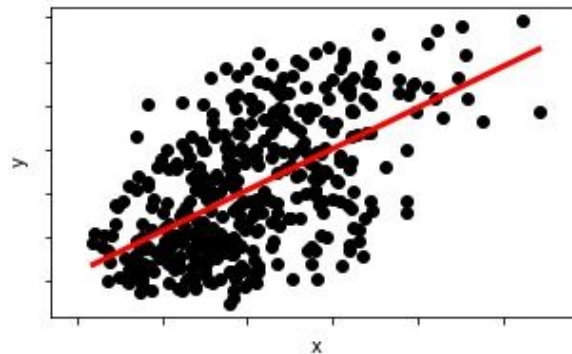
Fitting, training

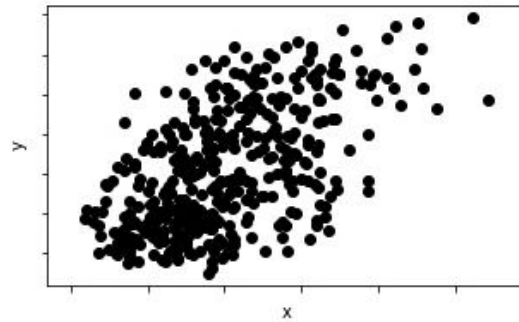
Fit



Θ

$\Theta : n \times 1$





$\langle \mathbf{X}, \mathbf{y} \rangle$

Training examples

$\mathbf{X} : m \times n$
 $\mathbf{y} : n \times 1$

Model

$$h_{\Theta}(\mathbf{x}) = \Theta_0 * \mathbf{x}_0 + \Theta_1 * \mathbf{x}_1$$

$$= \Theta^T \cdot \mathbf{x}$$

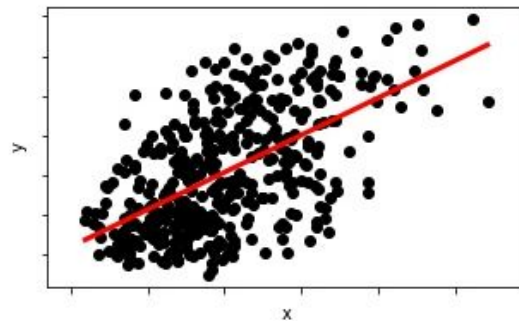
Fitting, training

$\Theta = [\Theta_0, \Theta_1] = [\text{intercept}, \text{slope}]$

$\Theta : (n + 1) \times 1$

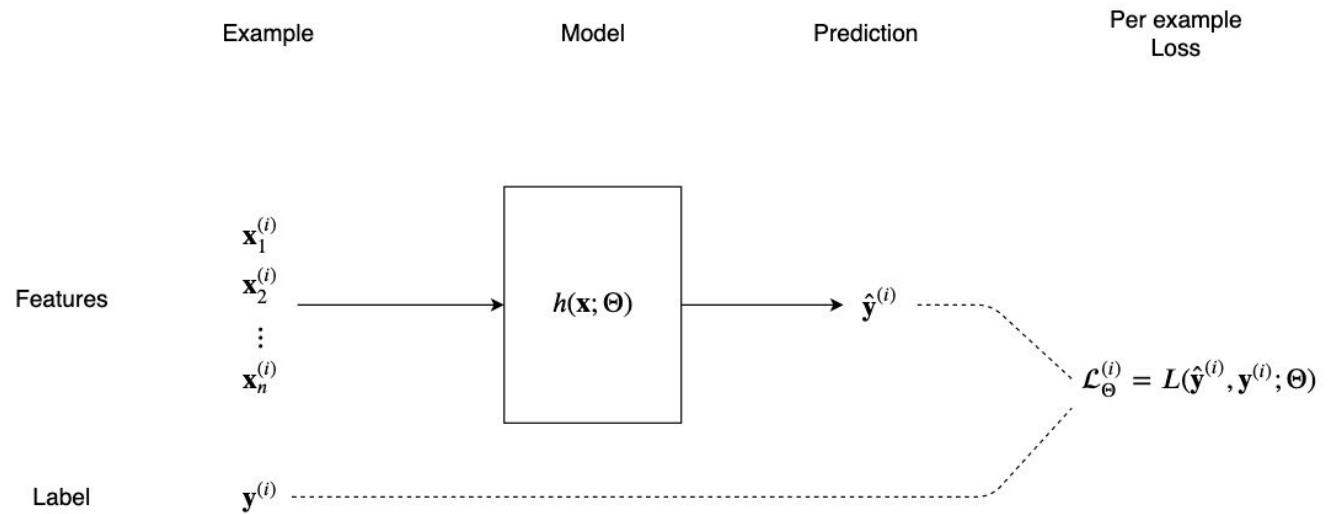
$\mathbf{x}^{(i)} = [1, \mathbf{x}_1^{(i)}, \dots, \mathbf{x}_n] : (n + 1) \times 1$

Fit 



Training, optimization

Training Example



The Loss for the entire training set is simply the average (across examples) of the Loss for the example

$$\mathcal{L}_{\Theta} = \frac{1}{m} \sum_{i=1}^m \mathcal{L}_{\Theta}^{(i)}$$

The best (optimal) Θ is the one that minimizes the Average (across training examples) Loss

$$\Theta = \underset{\Theta}{\operatorname{argmin}} \mathcal{L}_{\Theta}$$

K Nearest Neighbors

KNN algorithm

Test example

\mathbf{x}

Training
examples

$\mathbf{x}^{(1)}$

$\mathbf{x}^{(2)}$

\vdots

$\mathbf{x}^{(m)}$

similarity($\mathbf{x}, \mathbf{x}^{(1)}$)

similarity($\mathbf{x}, \mathbf{x}^{(2)}$)

\vdots

similarity($\mathbf{x}, \mathbf{x}^{(m)}$)

similarity($\mathbf{x}, \mathbf{x}^{(i_1)}$)

similarity($\mathbf{x}, \mathbf{x}^{(i_2)}$)

\vdots

similarity($\mathbf{x}, \mathbf{x}^{(i_m)}$)

Targets ordered
in decreasing order of
similarity of $\mathbf{x}^{(i)}$ to \mathbf{x}

$\mathbf{y}^{(i_1)}$

$\mathbf{y}^{(i_2)}$

\vdots

$\mathbf{y}^{(i_m)}$

Compute similarity of
 \mathbf{x}
to each
 $\mathbf{x}^{(i)}$

Sort $\mathbf{x}^{(i)}$
in decreasing order of
similarity to \mathbf{x}

Prediction: $\hat{\mathbf{y}} = \text{most frequent}(\mathbf{y}^{(i_1)}, \dots, \mathbf{y}^{(i_k)})$

Here's an illustration of KNN in action:

- training example

$$\mathbf{x}^{(i)} = [\mathbf{x}_1, \mathbf{x}_2], \mathbf{y}^{(i)} \in \{0, 1\}$$

is plotted as a colored dot, with the color corresponding to $\mathbf{y}^{(i)}$

- we form many test (non-training) examples by creating arbitrary pairs of $\mathbf{x}_1, \mathbf{x}_2$ values in a grid
 - predict for each, fill the grid with a color corresponding to the predicted class

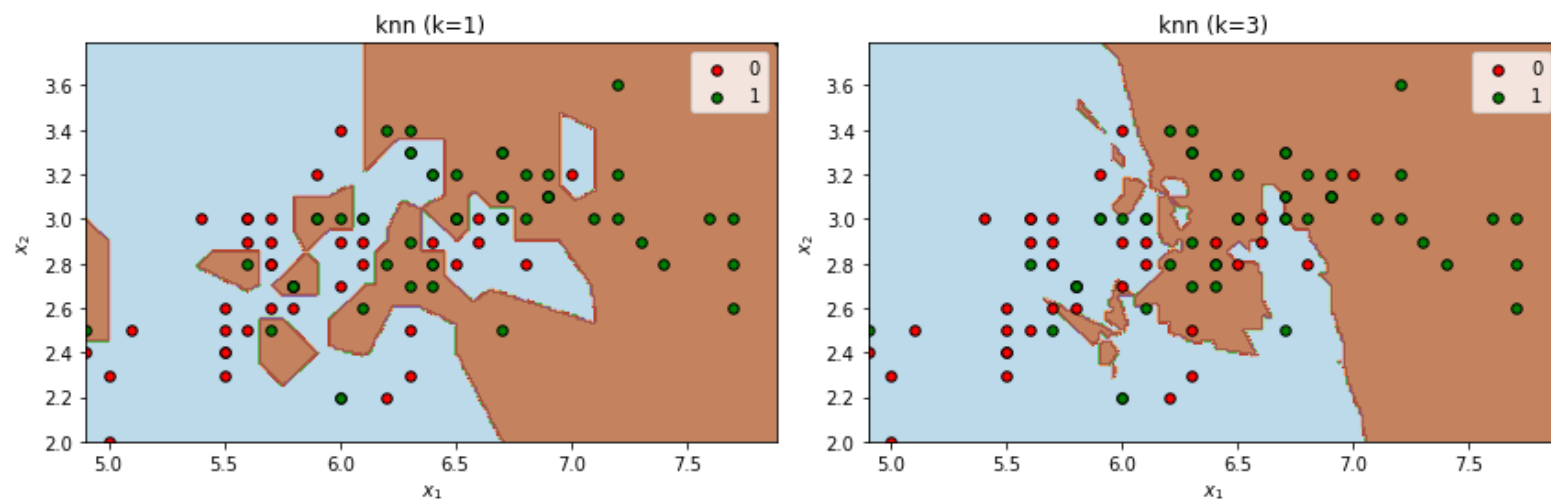
The line separating colors (classes) is called the *separating* or *decision* boundary.

```
In [4]: from sklearn.neighbors import KNeighborsClassifier

classifiers = [ ("knn (k=1)", KNeighborsClassifier(1)),
                  ("knn (k=3)", KNeighborsClassifier(5))
                ]
svmh = svm_helper.SVM_Helper()
_ = svmh.create_kernel_data(classifiers=classifiers)
fig, axs = svmh.plot_kernel_vs_transform(show_margins=False)
plt.close()
```

In [5]: fig

Out[5]:



Useful tools to help with Markdown

A couple of great tools

- [Detexify](http://detexify.kirelabs.org/classify.html) (<http://detexify.kirelabs.org/classify.html>),
 - hand-drawn symbols convert to TeX !
- [Mathpix](https://mathpix.com/) (<https://mathpix.com/>),
 - Screen-shot to markdown !

In [6]: `print("Done")`

Done