

## Analysis of my encoding

### What Are the Constraints in the SMT-LIB2 Encoding Expressing?

The encoding has the following key components:

**Input Constraints:** These enforce the preconditions that both  $x$  and  $y$  must be greater than 0, `assume(x > 0)` and `assume(y > 0)` statements in the original program.

**Program Semantics:** The program changes the array  $A$  in two steps. First, it sets  $A[x]$  to  $y$ . Then, it checks if  $x$  is equal to  $y$ . If they are equal, it sets  $A[y]$  to  $x$ . If not, it sets  $A[x]$  to  $y$  again. In the SMT encoding, these changes are done step by step using the store operation, which updates the array. The final result is a new version of the array that shows what it looks like after the program finishes.

**Formula F:** The goal is to prove that after executing the program, the formula  $2 * \text{read}(A, x) = 2 * y \wedge 2 * \text{read}(A, x) > 0$  holds. This is encoded as a logical conjunction, with `read(A, x)` interpreted as selecting the value at index  $x$  from the „final“ array.

### How Do You Conclude Validity of the Formula F with Respect to p from Your Encoding, Using Z3?

To show that the formula  $F$  is always true after the program runs, we check if  $F$  holds for all values of  $x$  and  $y$  that meet the input conditions. Since Z3 is a tool that looks for examples where something *can* happen, we ask it the opposite of what we want: we tell Z3 to try and find a case where the input conditions and the program behavior are correct, but  $F$  is false.

If Z3 can't find such a case, it means there's no way for  $F$  to be false when the inputs and program logic are followed. In that situation, Z3 returns unsat, which tells us that  $F$  is always true under those conditions.

In our case, Z3 returns unsat, so we've confirmed that  $F$  is always valid after the program runs. This shows that our encoding is correct and the formula is logically guaranteed.