

t-wise Coverage by Uniform Sampling

Jeho Oh

jeho@cs.utexas.edu University of Texas at Austin Austin, Texas, USA Paul Gazzillo paul.gazzillo@ucf.edu University of Central Florida Orlando, Florida, USA

Don Batory batory@cs.utexas.edu University of Texas at Austin Austin, Texas, USA

ABSTRACT

Efficiently testing large configuration spaces of *Software Product Lines* (SPLs) needs a sampling algorithm that is both scalable and provides good *t*-wise coverage. The 2019 SPLC Sampling Challenge provides large real-world feature models and asks for a *t*-wise sampling algorithm that can work for those models.

We evaluated t-wise coverage by $uniform\ sampling\ (\mathbb{US})$ the configurations of one of the provided feature models. \mathbb{US} means that every (legal) configuration is equally likely to be selected. \mathbb{US} yields statistically representative samples of a configuration space and can be used as a baseline to compare other sampling algorithms.

We used existing algorithm called Smarch to uniformly sample SPL configurations. While uniform sampling alone was not enough to produce 100% 1-wise and 2-wise coverage, we used standard probabilistic analysis to explain our experimental results and to conjecture how uniform sampling may enhance the scalability of existing *t*-wise sampling algorithms.

CCS CONCEPTS

• Software and its engineering \rightarrow Software product lines; • Theory of computation \rightarrow Automated reasoning.

KEYWORDS

software product lines, t-wise coverage, uniform sampling.

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1 INTRODUCTION

Software Product Lines (SPLs) are highly configurable. Building blocks of SPL products are features that are increments of product functionality. Each product of an SPL is defined by a unique set of features called a configuration. A feature model declares each feature and constraints among features, so that a user can identify legal configurations with desired feature combinations [4]. As the number of features increase, the size of the configuration space, which is the set of all possible configurations, grows exponentially.

Permission to make digital or hard copies of all or part of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage and that copies bear this notice and the full citation on the first page. Copyrights for components of this work owned by others than ACM must be honored. Abstracting with credit is permitted. To copy otherwise, or republish, to post on servers or to redistribute to lists, requires prior specific permission and/or a fee. Request permissions from permissions@acm.org.

SPLC '19, September 9–13, 2019, Paris, France © 2019 Association for Computing Machinery. ACM ISBN 978-1-4503-7138-4/19/09...\$15.00 https://doi.org/10.1145/3336294.3342359 Smarch [8] is a US algorithm for SPLs based on a #SAT solver. Let ϕ be the propositional formula of a feature model [3]. A #SAT solver can count the number of configurations in ϕ 's configuration space, namely $|\phi|$. (Each solution to ϕ is a configuration, and each configuration is a solution to ϕ). A #SAT solver extends a satisfiability solver by associating the number of solutions with each truth assignment [5]. Smarch uses sharpSAT [15], a state-of-the-art #SAT

A large configuration space could have over a trillion (> 10^{12}) configurations and is a challenge for testing, as testing every configuration is infeasible. Instead, prior work produced a small set of configurations to test selected features and their interactions. The aim is to get a 'high' *t*-wise coverage, ideally meaning 100% of *all* combinations of *t* features are covered by at least one configuration of the set. Achieving 100% can be infeasible for large spaces.\(^12 Common values for *t* include feature-wise (*t*=1), pair-wise (*t*=2), and three-wise coverage (*t*=3).

Different approaches start with a feature model and derive samples for *t*-wise coverage [1, 2, 6, 9, 10]. However, they do not scale well for many features and complex constraints, which limited their applicability to the real-world SPLs. Thus, the proposed Challenge [16] provides large real-world feature models and asks for a sampling algorithm that can generate configuration sets with good *t*-wise coverage for those models.

We explore *t*-wise coverage using *uniform sampling* (\mathbb{US}) in this paper. \mathbb{US} ensures that all configurations in a configuration space have equal probability of being selected, yielding a *statistically representative sample* of the space. \mathbb{US} can be used as a baseline against which other sampling algorithms can compare as a benchmark [13].

Despite its utility, $\mathbb{U}\mathbb{S}$ for large SPLs was considered infeasible until recently [11, 13]. Prior work tried different methods to make sampling as random as possible, but none achieved $\mathbb{U}\mathbb{S}$ for large SPLs. We use a recently developed algorithm called Smarch [8], the first to perform $\mathbb{U}\mathbb{S}$ of configuration spaces of size 10^{245} . Smarch utilizes a #SAT solver, which counts the number of solutions to a propositional formula [15]. We believe we are the first to explore t-wise coverage of $\mathbb{U}\mathbb{S}$ with probabilistic analyses to explain its coverage results.

Our contributions to the 2019 SPLC Sampling Challengeare:

- Demonstration of *t*-wise coverage that can be achieved by US; and
- Probabilistic analysis of configuration spaces that predicts the t-wise coverage by US and that may be useful for developing a practical t-wise sampling algorithm.

2 SMARCH: A US ALGORITHM

assignment [5]. Smarch uses sharpSAT [15], a state-of-the-art #SAT solver.

1 Section 4 shows that uniform sampling alone will not provide 100% coverage unless

the sample set is approximately the size of the configuration space.

Here is how Smarch achieves \mathbb{US} : A uniform random number generator can select an integer r in the range $[1..|\phi|]$. Smarch creates a one-to-one mapping that converts r into a unique configuration, so that \mathbb{US} of range $[1..|\phi|]$ leads to \mathbb{US} of configurations.

Smarch recursively partitions ϕ by a fixed order of variables to create a one-to-one mapping. A variable $v \in \phi$ partitions ϕ into disjoint spaces $(\phi \land \neg v)$ and $(\phi \land v)$. #SAT can compute the number of solutions for each space, i.e., $|\phi \land \neg v|$ and $|\phi \land v|$ respectively.

Then, for a random number $r \in [1..|\phi|]$, if $r \le |\phi \land \neg v|$ the $(\phi \land \neg v)$ space is selected for recursive partitioning, otherwise $(\phi \land v)$ is selected and $|\phi \land \neg v|$ is subtracted from r to adjust the search in $(\phi \land v)$. This process is repeated for the next variable in ϕ , until all variables are considered and a unique configuration has been determined.

Documenting scalability of Smarch and #SAT is beyond the scope of this paper – and is the subject of on-going work. Evidence in [8] reports Smarch is able to \mathbb{US} configuration spaces of size $O(10^{248})$ whereas the nearest \mathbb{US} competitor's largest space is $O(10^{13})$.

3 EVALUATION

3.1 Experimental Set-Up

Among the feature models provided in the Challenge, we used 'FinancialServices01' version '2018-05-09'. This feature model was given in FeatureIDE format [14], so we used the functionality of FeatureIDE to generate its propositional formula as a dimacs file. This file has 771 variables and 7,241 clauses. The size of the configuration space was determined to be $9.7 \cdot 10^{14}$, computed in a mere 46 milliseconds by sharpSAT [15].

We evaluated *t*-wise coverage for t=1 and t=2 and did the following to find valid combinations:

- (1) We derived a list of feature selections. With 771 features, there are $771 \cdot 2 = 1,542$ possible selections since we consider both a feature and its negation;
- (2) We derived all possible 1-wise and 2-wise combinations from this list. 1-wise yields $\binom{1542}{1} = 1542$ combinations and 2-wise yields $\binom{1542}{2} = 1,188,111$; and
- (3) We filtered out invalid combinations using a SAT solver. If a combination is valid, the conjunction of the combination and the feature model should be satisfiable. For example, for a feature f, a 2-wise combination (f,¬f) is invalid as these selections conflict with each other.

For 1-wise, 1,518 valid combinations were found (some features were mandatory). For 2-wise, 914,537 valid combinations were found.

We used Smarch to produce a \mathbb{US} set \mathbb{S}_n of n configurations.We have no idea what fraction of the valid combinations (computed above) are covered by \mathbb{S}_n . So we varied n to observe the results of increasing larger sets, using $n=\{5,10,20,30,40,50,100,200,300,400,500,1000,1518\}$. Then, for each set \mathbb{S}_n , we measured \mathbb{S}_n ?

- Time taken to sample n configurations, measured by the Linux 'time' tool;
- Time taken to sample a configuration, measured for each sample by Smarch;
- Maximum memory used during sampling, measured by the Linux '/usr/bin/time -v' command; and

t-wise coverage for t=1 and t=2, measured as the percentage of t-wise combinations covered in S_n.

We conducted our evaluation on an Intel i7-6700@3.4Ghz Ubuntu 16.04 machine with 16GB of RAM. All the code and data for the evaluation are available at: https://github.com/jeho-oh/Smarch_t_wise.

3.2 Experimental Results

Fig. 1a shows the total sampling time and Fig. 1b the time per sample. The X-axis is the number of samples (*n*) and the Y-axis is the time in seconds. We observed:

- Total sampling time increases linearly with *n*; and
- For all n, the average sampling time for a configuration was approximately 7 seconds, with standard deviation of 1 second. For all samples, the maximum sampling time was 10.1 seconds and the minimum was 3.5 seconds.
- The number of samples taken did not affect the time to sample a configuration.

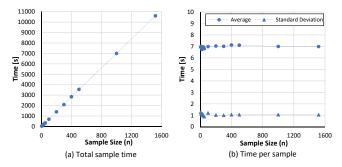


Figure 1: Sampling time.

Fig. 2 shows the maximum memory usage of Smarch, where the X-axis is the number of samples (n) and the Y-axis is the memory size in megabytes. We observed:

- Maximum memory usage was stable, between 16.8MB and 17.1MB for all n; and
- Sampling more configurations did not increase the maximum memory usage.

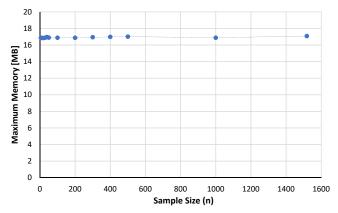


Figure 2: Maximum memory usage.

Fig. 3 shows the *t*-wise coverage result, where the X-axis is the number of samples (*n*) and Y-axis is the percentage of the coverage.

²The Challenge [16] explicitly requests sampling time and memory measurements.

Plots with different color indicates the results for different t. We observed:

- For all values of n, coverage for t=1 was higher than t=2;
- For \$\mathbb{S}_5\$, more than half of the feature combinations were covered for t=1 and over 35% for t=2;
- For both *t*=1 and *t*=2, larger *n* yielded better coverage. With 1,518 samples, coverage for *t*=1 was 61.7% and *t*=2 was 47.6%;
- The difference in coverage between n=5 and n=1,518 was surprisingly small. For t=1, the difference was 6.4%. For t=2, the difference was 9.4%; and
- Although samples are expected to be statistically representative of the configuration space, their *t*-wise coverages seemed low. Both coverages improved imperceptibly for *n*≥200. Why this is so is explained in the next section.

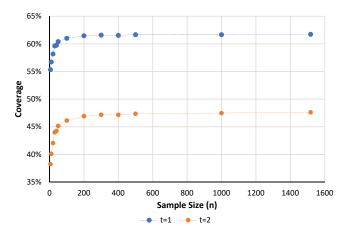


Figure 3: t-wise coverage.

We conclude that although $\overline{\mathbb{US}}$ is feasible with Smarch, $\overline{\mathbb{US}}$ alone is not enough to produce a 100% *t*-wise coverage.

4 ANALYSIS

US allows us to apply standard statistical analysis to explain our experimental results [7].

Let c denote a valid t-wise combination for a given t. Let v_c denote the fraction of all valid configurations that have c in the configuration space. Since every configuration has an equal probability of being selected by \mathbb{US} , the probability that a sample will have c is v_c .

 v_c can vary widely for different c because constraints among features may make certain combinations less frequent than others. A mandatory feature has v_c =1 because it appears in all configurations. A feature with no constraints has v_c =0.5; it can be freely enabled and disabled, making it appear in half of the valid configurations.

 v_c can be computed by a #SAT solver. Let ϕ be the propositional formula of an SPL's feature model. Let ϕ_c be the propositional formula of the conjunction of c's features. We can use a #SAT solver to compute v_c as:

$$v_c = \frac{|\phi_c|}{|\phi|} \tag{1}$$

The probability p(c, n) that at least one of n samples includes combination c is:

$$p(c,n) = 1 - (1 - v_c)^n \tag{2}$$

where the more samples taken, the higher the probability we encounter combination c. The value of p(c,n) largely depends on how often this combination appears in the configuration space, i.e., ν_c . In our experiments of the previous section, we discovered:

- 61.5% of all 1-wise combinations have a ratio v_c >0.9. Even with the minimum number of samples we used in the evaluation (n=5), these combinations have more than 0.99 probability of being encountered in n=5 samples; and
- 38.8% of the 1-wise combinations have a ratio of v_c <0.0001. Even with the maximum number of samples we used in the evaluation (n=1815), they have less than 0.15 probability of being encountered in n=1815 samples.

We can use p(c,n) to predict t-wise coverage. Let \mathbb{C}_t denote the set of all valid t-wise combinations, where $|\mathbb{C}_t|$ is the number of combinations in \mathbb{C}_t . The estimated t-wise coverage $E(\mathbb{C}_t,n)$ for a given t,n is:

$$E(\mathbb{C}_t, n) = \frac{1}{|\mathbb{C}_t|} \sum_{c \in \mathbb{C}_t} p(c, n) = \frac{1}{|\mathbb{C}_t|} \sum_{c \in \mathbb{C}_t} (1 - (1 - \nu_c)^n)$$
 (3)

Fig. 4 uses (blue) X markers to plot $E(\mathbb{C}_1, n)$ and (brown) X markers for $E(\mathbb{C}_2, n)$ with our experimental results (\bullet for t=1 and \bullet for t=2) overlaid. Eqn. (3) accurately predicts the results of our experiments and also explains why the coverage of t=1 is higher than that for t=2: there are many 2-way feature combinations (c_{ij}) that are much less likely than any 1-way combination (c_k), meaning $v_{c_k} \gg v_{c_{ij}}$.

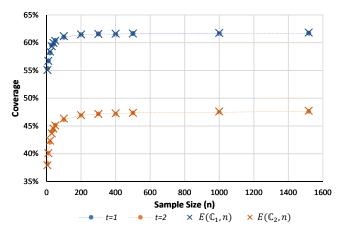


Figure 4: t-wise coverage estimation.

It is interesting to explore the relationship between coverage and larger sample set sizes which are infeasible to explore experimentally. Fig. 5 shows the estimated *t*-wise coverage for n up to 10^{14} , which is approximately 10% of the configuration space (ie., 9.7×10^{14}). We observed:

 With 10¹⁴ samples, more than 99.99% of 1-wise and 2-wise combinations are expected to be covered. Of course, this is almost enumeration; and Many combinations will be covered with a small number of samples, over 30% of 2-way combinations are not likely to be covered even with 10⁷ samples(!).

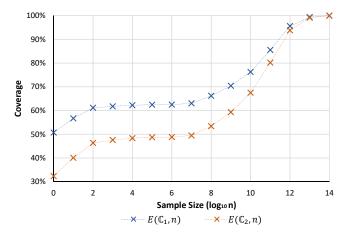


Figure 5: t-wise coverage estimation for large n.

We could accurately predict these results because Smarch can uniform sample from a configuration space and standard probabilistic analyses rely on US [7].

Our analysis suggests possible enhancements to existing t-wise approaches. Once v_c values are known, we can determine which combinations can be covered by a small number of USs. Then, for combinations that are unlikely to be found by US, we may either: 1) constrict the configuration space with constraints to (recursively) sample configuration sub-space of interest [12] or 2) use existing approaches that do not rely on US. As sampling with many features limits the scalability of existing approaches, US may improve sampling scalability by reducing the features to consider. An equally important issue is to define a reasonable t-wise coverage (percentage) for large configuration spaces (other than 100%) for practitioners to use.

5 CONCLUSIONS AND FUTURE WORK

As \mathbb{US} of configurations was considered infeasible, probabilistic analyses of a configuration space based on \mathbb{US} was unexplored or considered unexplorable. We used a recently developed algorithm, Smarch [8], to \mathbb{US} configurations of a configuration space. We also derived probabilistic models to explain Smarch results. We showed:

- US alone is not enough to produce 100% t-wise coverage; and
- Distribution of ν_c can be used to predict the *t*-wise coverage of US.

Our work opens new possibilities on analyzing an SPL configuration space and deriving samples for testing. As \mathbb{US} produces statistically representative samples of a configuration space, it may be possible to utilize the information from samples to improve the efficiency of existing approaches. As a future work, we plan to:

- Analyze other systems to validate and expand our insights on probabilistic analyses;
- Derive an algorithm utilizing \mathbb{US} for *t*-wise coverage; and
- Enhance the performance of the Smarch algorithm.

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