### HARD TO CRACK (VJTI)

# TEAM NOTEBOOK (ICPC PUNE)

```
//ret.resize(v1.size()+v2.size()-1); //as if first ka size a,second ka b, so degree of ret=a-1+b-1=a+b-2,so size of ret=a+b-1
```

### Mo's Algorithm:

```
const int N=2e5+5;
const int M=1e6+5:
struct data
       int l;int r;int idx;long long store ans;};
int n, q, blocksz=1000;
int a[N];
data queries[N];
long long freq[M];
long long ans=0;
bool comp(data &d1, data &d2)
       int blocka=d1.l/blocksz;
       int blockb=d2.l/blocksz;
       if(blocka < blockb)
              return true;
       else if(blocka==blockb)
              return (d1.r < d2.r)^(blocka\%2);
       else
              return false;
bool comp2(data &d1, data &d2)
       return d1.idx<d2.idx;
void update(long long k, int sign) //Sign 1 = Add, -1
= Remove
       if(sign==1)
              ans-=freq[k]*freq[k]*k;
```

### **Game Theory:**

- 1. If nim-sum is non-zero, player starting first wins.
- 2. Mex: smallest non-negative number not present in a set.
- 3. Grundy=0 means game lost.
- 4. Grundy=mex of all possible next states.
- 5. Sprague-Grundy theorem:

If a game consists of sub games (nim with multiple piles)

Calculate grundy number of each sub game (each pile)

Take xor of all grundy numbers:

If non-zero, player starting first wins.

Pattern Matching:

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```
freq[k]++;
           ans+=freq[k]*freq[k]*k;
    else
           ans-=freq[k]*freq[k]*k;
           freq[k]--;
           ans+=freq[k]*freq[k]*k;
d calcmo()
    int moleft=1;
    int moright=0;
    for(int i=1;i \le q;i++)
           int r=queries[i].r;
           int l=queries[i].l;
           while(moright<r)
                  moright++;
                   update(a[moright], 1);
           while(moright>r)
                   update(a[moright], -1);
                   moright--;
           while(moleft<l)
                   update(a[moleft], -1);
                  moleft++;
           while(moleft>l)
                  moleft--;
                   update(a[moleft], 1);
```

```
suffixes[i].rank[1] = ((i+1) < n)? (txt[i+1] -
'a'): -1;
  sort(suffixes, suffixes+n, cmp);
  int ind[n];
  for (int k = 4; k < 2*n; k = k*2)
     int rank = 0;
     int prev rank = suffixes[0].rank[0];
     suffixes[0].rank[0] = rank;
     ind[suffixes[0].index] = 0;
     for (int i = 1; i < n; i++)
       if (suffixes[i].rank[0] == prev rank &&
            suffixes[i].rank[1] ==
suffixes[i-1].rank[1])
          prev rank = suffixes[i].rank[0];
          suffixes[i].rank[0] = rank;
       else
          prev rank = suffixes[i].rank[0];
          suffixes[i].rank[0] = ++rank;
       ind[suffixes[i].index] = i;
     for (int i = 0; i < n; i++)
       int nextindex = suffixes[i].index + k/2;
       suffixes[i].rank[1] = (nextindex < n)?
suffixes[ind[nextindex]].rank[0]: -1;
     sort(suffixes, suffixes+n, cmp);
```

FFT:	21	queries[i].store_ans=ans;	// Store indexes of all sorted suffixes in the
Mo's Algorithm:	1	}	suffix array
HLD:	3	}	int *suffixArr = new int[n];
Articulation Point (cut-vertices):	6	for(int $i=1$ ; $i \le q$ ; $i++$ )	for (int $i = 0$ ; $i < n$ ; $i++$ )
Bridges:	8	101(1111 1–1,1×–q,1++)	suffixArr[i] = suffixes[i].index; return suffixArr;
	o	cin>>queries[i].l>>queries[i].r;	}
Euler path/circuit: path->every edge exactly	8	queries[i].idx=i;	,
once		}	void search(char *pat, char *txt, int *suffArr, int
Hierholzer's algorithm for directed graph:	8	sort(queries+1, queries+q+1, comp);	$  n \rangle$
Bipartite graph:	10	calcmo();	{
Max flow Algorithm(V^3):	10	sort(queries+1, queries+q+1, comp2);	int m = strlen(pat);
Min cost max flow:	13	for(int i=1;i<=q;i++)	int 1 = 0, r = n-1;
Maximum Bipartite Matching:	17	cout< <queries[i].store_ans<<endl;< td=""><td>while (l &lt;= r)</td></queries[i].store_ans<<endl;<>	while (l <= r)
Coometury	10	*/	int mid = $1 + (r - 1)/2$ ;
Geometry:	19	HLD:	int ring = 1 + (1 - 1)/2, int res = strncmp(pat, txt+suffArr[mid], m);
Orientation:	21	HLD.	if (res $== 0$ )
Line intersection:	21	//just call init(),then updateUp or queryUp,always	{
Circle intersection area:	22	remember to clear adjacency adj[N], and g[N]	cout << "Pattern found at index " <<
Convex Hull:(nlogn)	22	//,init() doesn't do it for u,subtree query for v	suffArr[mid];
Point in a polygon:	24	[in[v],out[v]] in array rin	return;
Game Theory:	25	//1 based indexing for everything	}
D (4 )	2.5	Il n; //number of nodes	if (res < 0) r = mid - 1;
Pattern Matching:	25	vector <pair<ll,ll> &gt; adj[N]; //adjacency list of form</pair<ll,ll>	else $l = mid + 1$ ;
Suffix Arrays:(remaining to read)	25	<pre>(v,cost of edges) Il treeSize[N]; //subtree size</pre>	cout << "Pattern not found";
KMP Algorithm:	27	Il cost[N]; //cost of a node->if nodes have a cost then	}
Advanced Techniques:	2	cost[i]=givenCost[i],if edges have cost then	,
Catalan numbers:	2	cost[i]=givenCost(edge(parent[i],i))	KMP Algorithm:
	2	//with some value to root(-inf for maximisation and	ll arr[200005],arr2[200005];
Centroid Decomposition:	2	vice versa could be kept)	ll n,w;
Persistent Segment Tree(kth number):	3	ll depth[N]; //depth of a node	ll lps[200005];
2-sat:	5	ll dp[N][20];	void computeLps();
Sos Dp:	7	world dfg(   ourr    prov   = 1    donth   = 0    cost   = 1)	ll kmp()
Parallel binary Search(Algorithm):	8	void dfs(ll curr,ll prev1=-1,ll depth1=0,ll cost1=-1) //to initaialise dp,cost,depth	ll i=1,j=1; //i is pointing to main,j is pointing
Closest Pair of Points(Nlog^2N):	9	{	to pattern
			to pattern

Python Syntax:	1
Big integer c++:	1
2D bit (point update and query):	1
2D bit Submatrix Update:	1
Convex Hull trick Offline:	1
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### **Techniques:**

- 1. For counting problems, try counting number of incorrect ways instead of correct ways.
- 2. Prune Infeasible/Inferior Search Space Early
- 3. Utilize Symmetries
- 4. Try solving the problem backwards
- 5.Binary Search the answer
- 6. Meet in the middle (Solve left half, Solve right half, combine)
- 7. Greedy
- 8. DP
- 9. Analyse complexity carefully
- 10. Reduce the problem to some standard problem
- 11. Add m when doing modular arithmetic.
- 12. Carefully analyse reasoning behind adding small details in the Q.
- 13. Use exponential search in case of unbounded search.

### STL DS:

```
stack<type> name
empty(),size(),pop(),top(),push(x)

queue<type> name
empty(),size(),pop(),front(),back(),push(x)
```

```
depth[curr]=depth1;
  dp[curr][0]=prev1;
  treeSize[curr]=1;
  cost[curr]=cost1;
  for(pair<ll,ll> x:adj[curr])
     if(x.first!=prev1)
       dfs(x.first,curr,depth1+1,x.second);
       treeSize[curr]+=treeSize[x.first];
ll t=0; //euler tour,and hld time
vector\langle ll \rangle g[N];
1l sz[N],in[N],nxt[N],out[N],rin[N]; //nxt means
name of head node of the chain this node belongs to
void dfs sz(int v=1,int prev1=-1)
  sz[v] = 1;
  for(auto &u: g[v])
    if(u!=prev1){
    dfs sz(u,v);
    sz[v] += sz[u];
    if(sz[u] > sz[g[v][0]])
       swap(u, g[v][0]);
void dfs hld(int v=1,int prev1=-1)
  in[v] = ++t;
  rin[in[v]] = v;
  for(auto u: g[v])
    if(u!=prev1){
```

```
computeLps();
  ll len1=0; //length matched uptil now
  11 res=0:
  while(i \le n)
     if(arr[i]==arr2[i])
       i++;
       j++;
       if(j==(w+1))
         j=lps[j-1]+1;
         res++;
else
       if(i!=1)
         j=lps[j-1]+1;
       else
         i++;
         j=1;
  return res;
void computeLps()
  lps[1]=0;
  11 i=2;
  Il len1=0; //best longest proper prefix which is
also a suffix upto prev Val
  while(i<=w)
```

```
priority_queue <type> name
empty(),size(),pop(),top(),push(x)

deque<type> name
pop_front(),pop_back(),push_front(),push_back(),s
ize(),at(index),front()
,back()

set/multiset/map/multimap<type>name
begin(),end(),size(),empty(),insert(val),erase(itr or
val),find(val),
lower_bound(val),upper_bound(val)
(lower bound includes val, upper bound does not)
pair<type,type> name (first and second)
```

### **STL Algorithms:**

- 1.sort(first\_iterator, last\_iterator) To sort the given vector.
- 2. reverse(first\_iterator, last\_iterator) To reverse a vector.
- 3. \*max\_element (first\_iterator, last\_iterator) To find the maximum element of a vector.
- 4. \*min\_element (first\_iterator, last\_iterator) To find the minimum element of a vector.
- 5.lower\_bound(first\_iterator, last\_iterator, x) returns an iterator pointing to the first element in the range [first,last) which has a value not less than 'x'.
- 6.upper\_bound(first\_iterator, last\_iterator, x) returns an iterator pointing to the first element in the range [first,last) which has a value greater than 'x'.

```
nxt[u] = (u == g[v][0] ? nxt[v] : u);
     dfs hld(u,v);
  out[v] = t;
void init()
  nxt[1]=1;
  t=0:
  memset(dp,-1,sizeof(dp));
  //change this according to cost
  dfs(1);
  /*dont change this*/
  dfs sz();
  dfs hld():
  /*dont change this*/
  for(11i=1;i<20;i++)
     for(11 j=1; j \le n; j++)
       if(dp[i][i-1]!=-1)
          dp[i][i]=dp[dp[i][i-1]][i-1];
  /*update part
  memset(tr,-1,sizeof(tr));
  for(11 i=1; i \le n; i++)
     update(i,cost[rin[i]],1,n);
  */
ll queryUp(ll a,ll b) //a is always down wala node
```

```
if(arr2[i]==arr2[len1+1])
       len1++;
       lps[i]=len1;
       i++;
    else
       if(len1!=0)
         len1=lps[len1];
       else
         len1=0;
         lps[i]=len1;
         i++;
       }}}
Advanced Techniques:
Catalan numbers:
1, 1, 2, 5, 14, 42, 132, 429, 1430,......
C(n) = (1/(n+1)) * choose(2n, n);
C(n+1) = Summation(i = 0 to n) [C(i) * C(n-i)]
Centroid Decomposition:
int subtree[N], parentcentroid[N];
set\leqint\geq g[N];
ll nodes=0;
void dfs(int k, int par)
       nodes++;
       subtree[k]=1;
```

7.next\_permutation(first\_iterator, last\_iterator) – This modified the vector to its next permutation.

8.prev\_permutation(first\_iterator, last\_iterator) – This modified the vector to its previous permutation

9. random shuffle(arr.begin(), arr.end());

### **Number Theory:**

- 1. To calculate sum of factors of a number, we can find the number of prime factors and their exponents. N = ae1 \* be2 \* ce3 ...Then sum =  $(1 + a + a^2....)(1 + b + b^2...)...$ Number of factors=(a+1)\*(b+1)...
- 2.Every even integer greater than 2 can be expressed as the sum of 2 primes.
- 3. For rootn prime method, check for 2, 3 then: for  $(i=5; i*i \le n; i=i+6)$  n%i and n%(i+2)
- 4. Number of divisors will be prime only if  $N=p^x$  where p is prime.
- 5. fib(n+m)=fib(n)fib(m+1)+fib(n-1)fib(m)
- 6. A number is Fibonacci if and only if one or both of (5\*n2 + 4) or (5\*n2 4) is a perfect square
- 7. every positive Every positive integer can be written uniquely as a sum of distinct non-neighbouring Fibonacci numbers.
- 8. Matrix multiplication

```
if(b==-1)
    return -1;
  ll curr=a;
  ll res=-1:
  while(nxt[curr]!=nxt[b])
    res=max(res,query(in[nxt[curr]],in[curr],1,n));
    curr=dp[nxt[curr]][0];
  res=max(res,query(in[b],in[curr],1,n));
  //if wanted to do a upto b, but excluding
b, comment above, and uncomment below, and make
sure that segment tree handles l>r case, with inf for
min...
 // res=max(res,query(in[b]+1,in[curr],1,n));
  return res;
void updateUp(ll a,ll b,ll val) //a is always down
wala node
  ll curr=a:
  while(nxt[curr]!=nxt[b])
    updateRange(in[nxt[curr]],in[curr],val);
    curr=dp[nxt[curr]][0];
  updateRange(in[b],in[curr],val);
  //if wanted to do a upto b, but excluding
b, comment above, and uncomment below
  //updateRange(in[b]+1,in[curr],val);
Articulation Point (cut-vertices):
void APUtil(LL u, bool visited[], LL disc[],
```

```
for(auto it:g[k])
               if(it==par)
                      continue;
               dfs(it, k);
               subtree[k]+=subtree[it];
int centroid(int k, int par)
       for(auto it:g[k])
               if(it==par)
                      continue:
               if(subtree[it]>(nodes>>1))
                      return centroid(it, k);
       return k;
void decompose(int k, int par)
       nodes=0;
       dfs(k, k);
       int node=centroid(k, k);
       parentcentroid[node]=par;
       for(auto it:g[node])
               g[it].erase(node);
               decompose(it, node);
//call decompose (1,-1)
Persistent Segment Tree(kth number):
ll n,arr[100005];
struct node
```

```
mul[i][j] += a[i][k]*b[k][j];
9. Root n under mod p exists only if
   n^{(p-1)/2} % p = 1
10..divisibility by 4: last 2 digits divisible by 4
11. divisibility by 8: last 3 digits divisible by 8
12. Divisibility by 3,9: sum of digs divisible by 3,9
13. Divisibility by 11: alternate (+ve,-ve) digit sum
is divisible by 11
14. Divisibility by 12: divisible by 3 and 4
15. Divisibility by 13: alternating sum in blocks of
3 (L to R) div 13
16. Integral solution of ax+by=c exists if gcd(a,b)
divides c
Extended Euclid's Algorithm:
    1. LL gcde(LL a,LL b,LL *x,LL *y)
   2.
         if (a == 0)
    4.
    5.
            x = 0, x_v = 1
    6.
            return b;
   7.
   8.
         LL x1, y1;
```

LL gcd = gcde(b%a, a, &x1, &y1);

x = y1 - (b/a) x1;

y = x1;

10.

11.

```
LL low[], LL parent[], bool
ap[])
  static LL time = 0;
  LL children = 0;
  visited[u] = true;
  disc[u] = low[u] = ++time;
  list<LL>::iterator i;
  for (i = adj[u].begin(); i!= adj[u].end(); ++i)
    LL v = *i:
    if (!visited[v])
       children++;
       parent[v] = u;
       APUtil(v, visited, disc, low, parent, ap);
       if (parent[u] == NIL && children > 1)
         ap[u] = true;
       if (parent[u] != NIL && low[v] >= disc[u])
         ap[u] = true;
    else if (v != parent[u])
       low[u] = min(low[u], disc[v]);
void AP()
  bool *visited = new bool[V];
  LL *disc = new LL[V];
  LL *low = new LL[V];
  LL *parent = new LL[V];
  bool *ap = new bool[V];
  for (LL i = 0; i < V; i++)
    parent[i] = NIL;
    visited[i] = false;
    ap[i] = false;
```

```
node *left, *right;
       11 cnt=0;
       node(node *left,node *right,ll cnt)
               this->left=left;
               this->right=right;
                this->cnt=cnt;
       //since insert return a ptr to child
       node* insert(ll 1,ll r,ll pos);
//base pointer pointing to null tree
node *null=new node(NULL,NULL,0);
//in this all leaf nodes ka left and right points to
base pointer
node* node:: insert(ll l,ll r,ll pos)
       //pos in range
       if(pos \ge 1 \&\& pos \le r)
               if(l==r)
                        return new
node(null,null,this->cnt+1);
               11 \text{ m}=(1+r)>>1;
               return new
node(this->left->insert(1,m,pos),this->right->inse
rt(m+1,r,pos),this->cnt+1);
       //if out of range, we can use previous
version tree node
       return this;
ll query(node *a,node *b,ll l,ll r,ll w)
       if(l==r)
```

```
12. return gcd;
    13. }
To find inverse of a wrt m:
gcde(a,m,&x,&y);
x is the inverse of a.
Segmented Sieve for primes
    1. void segsieve(LL l,LL r)
    2.
    3.
         LL limit = \underline{floor}(\underline{sqrt}(r))+1;
         vector<LL> prime;
    4.
         sieve(limit, prime);
    5.
   6.
            limit=r-l+1;
   7.
            bool mark[limit+1];
   8.
            memset(mark, true, sizeof(mark));
           //True= is prime
   9.
            for (int i = 0; i < prime.size(); i++)
    10.
               int loLim = floor(l/prime[i]) *
    11.
       prime[i];
               if (loLim < 1)
    12.
    13.
                 loLim += prime[i];
    14.
    15.
               for (int j=loLim; j<=r; j+=prime[i])
    16.
                 mark[j-1] = false;
    17.
    18. }
Matrix Exponentiation
LL power(LL F[3][3], LL n)
  LL M[3][3] = \{\{1,1,1\}, \{1,0,0\}, \{0,1,0\}\};
  if (n==1)
     return F[0][0] + F[0][1];
  power(F, n/2);
  multiply(F, F);
  if (n\%2!=0)
     multiply(F, M);
```

```
for (LL i = 0; i < V; i++)
    if (visited[i] == false)
       APUtil(i, visited, disc, low, parent, ap);
  for (LL i = 0; i < V; i++)
    if (ap[i] == true)
       cout << i << " ";
Bridges:
Replaceboth condition for articulation point with
if (low[v] > disc[u])
Euler path/circuit: path->every edge exactly once
```

Euler path in undirected graph:

All vertices have even degree except or 2 have odd degrees, and vertex with non zero degree in same component.

Euler Circuit in undirected graph:

All vertices have even degree and vertex with non zero degree in same component.

Euler circuit in directed graph:

All no zero degree vertices are a part of a single strongly connected component and indegree and outdegree of all vertices is same.

Euler path in directed graph:

At most one vertex has (out-degree) – (in-degree) = 1, at most one vertex has (in-degree) – (out-degree) = 1, every other vertex has equal in-degree and out-degree, and all of its vertices with nonzero degree belong to a single connected component of the underlying undirected graph.

### Hierholzer's algorithm for directed graph:

```
return 1;
       11 \text{ m}=(1+r)>>1;
       ll cnt1=(b->left->cnt-a->left->cnt);
       if(cnt1 \ge w)
       return query(a->left,b->left,l,m,w);
       return
query(a->right,b->right,m+1,r,w-cnt1);
null->left=null->right=null;
root[0]=null;
for(11 i=1; i \le n; i++)
  root[i] = (root[i-1]) - sinsert(1, cnt/N) (of segment)
tree),arr[i]);
ll res=query(root[1-1],root[r],1,cnt/N(of segment
tree),k);
2-sat:
struct TwoSAT
       static const int MAXV=2e5+5;(2*number
of variables)
       int n, cnt; //n is number of
vertices(2*number of variables)
       vector<int> g[MAXV], rg[MAXV];
//g=forward, rg=backward
       bool vis[MAXV];
       int order[MAXV], comp[MAXV];
       void init(int curn)
               n=curn;
               for(int i=0;i< n;i++)
```

```
return F[0][0] + F[0][1];
LL findNthTerm(LL n)
  LL F[3][3] = \{\{1,1,1\}, \{1,0,0\}, \{0,1,0\}\};
  return power(F, n-2);
Euler's totient:
Number of integers coprime to n less than n
LL phi(LL n)
  LL result = n;
  for (LL p=2; p*p<=n; ++p)
     if (n \% p == 0)
       while (n \% p == 0)
          n = p;
       result -= result / p;
  if (n > 1)
     result -= result / n:
  return result;
Largest power of p that divides n!:
// Returns largest power of p that divides n!
int largestPower(int n, int p)
  // Initialize result
  int x = 0;
  // Calculate x = n/p + n/(p^2) + n/(p^3) + ...
```

```
void printCircuit(vector< vector<int> > adj)
  unordered map<int,int> edge count;
  for (int i=0; i<adj.size(); i++)
    edge count[i] = adi[i].size();
  if (!adj.size())
    return;
  stack<int> curr path;
  vector<int> circuit:
  curr path.push(0);
  int curr v = 0;
  while (!curr path.empty())
    if (edge count[curr v])
       curr path.push(curr v);
       int next v = adj[curr v].back();
       edge count[curr v]--;
       adj[curr v].pop back();
       curr v = next v;
    else
       circuit.push back(curr v);
       curr v = curr path.top();
       curr path.pop();
  for (int i=circuit.size()-1; i>=0; i--)
    cout << circuit[i];
    if (i)
      cout<<" -> ":
```

```
g[i].clear();
               rg[i].clear();
void add(int u, int v)
       g[u].push back(v);
       rg[v].push back(u);
void dfs1(int u)
       vis[u] = true;
       for(auto it:g[u])
               if(!vis[it])
                       dfs1(it);
       order[cnt++] = u;
void dfs2(int u, int c)
       comp[u] = c;
       for(auto it:rg[u])
               if(comp[it]==-1)
                       dfs2(it, c);
int solve(vector<int> &ans)
       cnt=0;
       memset(vis, 0, sizeof(vis));
       for(int i=0;i< n;i++)
               if(!vis[i])
                       dfs1(i);
       memset(comp, -1, sizeof(comp));
       int grp=0;
       for(int i=n-1; i>=0; i--)
               int u=order[i];
               if(comp[u] == -1)
                       dfs2(u, grp++);
```

```
while (n)
                                                       Bipartite graph:
                                                       Coloring possible with 2 colors.
                                                                                                                                for(int i=0;i< n;i+=2)
                                                                                                                                        if(comp[i]==comp[i^1])
     n \neq p;
                                                       Max flow Algorithm(V^3):
                                                                                                                                                return 0;
     x += n;
                                                                                                                                ans.clear();
                                                                                                                                for(int i=0;i< n;i+=2)
                                                       //To obtain the actual flow values, look at all edges
  return x;
                                                       with capacity > 0
                                                       //Zero capacity edges are residual edges
                                                                                                                                        int choose = (comp[i] >
nCr (with lucas Theorem):(nCr%p)
                                                       struct edge
                                                                                                                 comp[i^1]) ? i : (i^1);
                                                                                                                                        ans.push back(choose);
P ->prime,complexity->O(p^2logn)
                                                               int from, to, cap, flow, index;
    1. LL ncrp(LL n, LL r, LL p)
                                                               edge(int from, int to, int cap, int flow, int
                                                                                                                                return 1;
   2.
                                                       index):
   3.
         LL C[r+1];
                                                                      from(from), to(to), cap(cap),
                                                                                                                 }sat;
   4.
         \underline{\text{memset}}(C, 0, \underline{\text{sizeof}}(C));
                                                       flow(flow), index(index) {}
         C[0] = 1:
                                                                                                                 /*use 0 based indexing of variables
   5.
         for (LL i = 1: i \le n: i++)
                                                       //to check flow just dont consider the edges with 0
                                                                                                                 sat.init(number of vertices) where number of
   6.
   7.
                                                       capcities, as when dding (a->b with capaacity c, we
                                                                                                                 vertices=2*number of variables
   8.
            for (LL j = min(i, r); j > 0; j--)
                                                       add b->a with capacity 0)
                                                                                                                 variable no.i at 2*i,and 2*i+1,always keep p at
                                                       //and it could have negative flow which we ignore
                                                                                                                 2*i,~p at 2*i+1,as ans will be value of p,and not
   9.
              C[j] = (C[j] + C[j-1])\%p;
    10.
                                                                                                                 ~p
*/
                                                       for(11 i=1;i \le 2*n;i++)
    11.
         return C[r];
   12. }
    13. LL nerpl(LL n,LL r, LL p)
                                                          for(auto&edge:obj.g[i])
                                                                                                                 Sos Dp:
    14. {
    15. if (r==0)
                                                            if((edge.to!=0) && (edge.to!=(2*n+1)) &&
                                                                                                                 const 11 K=22:
          return 1;
                                                       (edge.cap!=0)
                                                                                                                 \lim_{K \to \infty} dp[(1 \le K) + 5][K]; //dp[mask][i] represents the
    17. int ni = n\%p, ri = r\%p;
                                                                                                                 f(x) for all x -subset of mask(ie some operations
    18. return (ncrpl(n/p, r/p, p) *
                                                                                                                 over all subset of mask ,eg:sum(arr[x]))
   19.
              ncrp(ni, ri, p)) % p;
                                                               ans[i][edge.to-n]+=edge.flow;
                                                                                                                      //changes in first i elements only
                                                               ans[i][i]-=edge.flow;
   20. }
                                                                                                                 //initialise dp
                                                            }}}*/
                                                       struct PushRelabel
                                                                                                                 //memset(dp,0,sizeof(dp));
                                                                                                                 //dp[mask][0]=f(mask)->no changes
                                                               int n;
                                                               vector<vector<edge>> g;
                                                                                                                 for(11 i=1; i \le n; i++)
                                                               vector<long long> excess;
                                                               vector<int> height, active, count;
                                                                                                                   dp[arr[i]][0]=arr[i];
```

### **Chinese Remainder Theorem:**

The Chinese remainder theorem is a theorem of number theory, which states that if one knows the remainders of the <u>Euclidean division</u> of an <u>integer</u> n by several integers, then one can determine uniquely the remainder of the division of n by the product of these integers, under the condition that the <u>divisors</u> are <u>pairwise coprime</u>.

```
1. LL crt(LL num[], LL rem[], LL k)
2.
3.
     LL prod = 1;
4.
     for (int i = 0; i < k; i++)
5.
        prod *= num[i];
     LL result = 0;
6.
     for (int i = 0; i < k; i++)
8.
9.
        LL pp = prod / num[i];
10.
        LL inv,y;
11.
        gcde(pp,num[i],&inv,&y);
12.
        result += rem[i] * inv * pp;
13.
14.
     return result % prod;
15. }
```

For combining wrt a large number, use it 2 numbers at a time.

### Wilson's theorem(doubt):

```
((p-1)!)%p=-1
```

### Number of solutions to a linear eqn:(doubt):

```
LL countSol(LL coeff[], LL start, LL end, LL rhs) {

// Base case
if (rhs == 0)
return 1;
```

```
queue<int> Q;
       PushRelabel(int n): //number of nodes
              n(n), g(n), excess(n), height(n),
active(n), count(2*n) {}
       void addEdge(int from, int to, int cap)
//direction dependent
              g[from].push back(edge(from, to,
cap, 0, g[to].size()));
              if(from==to)
                      g[from].back().index++;
              g[to].push back(edge(to, from, 0, 0,
g[from].size()-1));
       void enqueue(int v)
              if(!active[v] && excess[v] > 0)
                      active[v]=true;
                      Q.push(v);
       void push(edge &e)
              int amt=(int)min(excess[e.from],
(long long)e.cap - e.flow);
              if(height[e.from]<=height[e.to] ||
amt==0)
                      return:
              e.flow += amt;
              g[e.to][e.index].flow -= amt;
              excess[e.to] += amt;
              excess[e.from] -= amt;
              enqueue(e.to);
       void relabel(int v)
              count[height[v]]--;
```

```
}
//for optimised approach use i&1,(i+1)&1
for(ll i=1;i<=K;i++)
{
    for(ll mask=0;mask<(1<<(K));mask++)
    {
        if(mask&(1<<(K-i)))
        {
             //instead of +,anything like &,or
        sth..could be there

dp[mask][i]=dp[mask][i-1]+dp[mask^(1<<(K-i))
][i-1];
        }
        else
        {
            dp[mask][i]=dp[mask][i-1];
        }
        else
        {
            dp[mask][i]=dp[mask][i-1];
        }
    }
}</pre>
```

### **Parallel binary Search(Algorithm):**

Q. There are N member states and M sectors. Each sector is owned by a member state. There are Q queries, each of which denote the amount of meteor shower in a [L, R] range of sectors on that day. The ith member state wants to collect reqd[i] meteors over all its sectors. For every member state, what is the minimum number of days it would have to wait to collect atleast the required amount of meteors?

```
LL result = 0; // Initialize count of solutions
                                                                     int d=2*n;
                                                                     for(auto &it:g[v])
                                                                                                             for all logQ/or any like 30 steps:
  // One by subtract all smaller or equal
                                                                                                                clear range tree and linked list check
coefficiants and recur
                                                                            if(it.cap-it.flow>0)
  for (LL i=start; i<=end; i++)
                                                                                    d=min(d,
                                                                                                                for all member states i:
   if (coeff[i] \le rhs)
                                                      height[it.to]+1);
                                                                                                                  if L[i] != R[i]:
     result += countSol(coeff, i, end, rhs-coeff[i]);
                                                                     height[v]=d;
                                                                                                                     mid = (L[i] + R[i]) / 2
  return result;
                                                                    count[height[v]]++;
                                                                                                                     insert i in check[mid]
                                                                     enqueue(v);
                                                                                                                for all queries q:
Sum of GP:
                                                             void gap(int k)
                                                                                                                  apply(q)
long long gp(LL r, LL p,LL m){
if(p==0)
                                                                     for(int v=0; v< n; v++)
                                                                                                                  for all member states m in check[q]:
return 1;
                                                                                                                     if m has requirements fulfilled:
if(p==1)
                                                                            if(height[v]<k)
return 1;
                                                                                    continue:
                                                                                                                       R[m] = q
LL ans=0;
                                                                            count[height[v]]--;
if(p\%2==1){
                                                                            height[v]=max(height[v],
ans=Mpow(r,p-1,m);
                                                      n+1);
                                                                                                                    else:
ans=(ans+((1+r)*gp(Mpow(r,2,m),(p-1)/2,m))%m)
                                                                            count[height[v]]++;
                                                                                                                       L[m] = q + 1
%m;
                                                                            enqueue(v);
else{
  ans=((1+r)*gp(Mpow(r,2,m),p/2,m))%m;
                                                             void discharge(int v)
                                                                                                             Closest Pair of Points(Nlog^2N):
                                                                    for(int i=0; excess[v]>0 &&
return ans;
                                                      i<g[v].size(); i++)
                                                                                                             struct Point
                                                                            push(g[v][i]);
                                                                     if(excess[v]>0)
                                                                                                                     int x, y;
Ternary Search (max of unimodal function):
                                                                            if(count[height[v]]==1)
                                                                                                                     Point operator -(Point p)
double ts(double start, double end)
                                                                                    gap(height[v]);
                                                                            else
                                                                                                                            return \{x-p.x, y-p.y\};
  double l = start, r = end;
                                                                                    relabel(v);
  for(int i=0; i<200; i++) {
                                                                                                                     int dist()
   double 11 = (1*2+r)/3;
                                                             long long max flow(int source, int dest)
```

```
double 12 = (1+2*r)/3;
                                                                                                                              return x*x + y*y;
   //cout<<11<<" "<<12<<endl;
                                                                      count[0] = n-1;
   if(func(11) > func(12)) r = 12; else 1 = 11;
                                                                      count[n] = 1;
                                                                                                               bool by x(Point &a, Point &b)
                                                                      height[source] = n;
  return func(r);
                                                                      active[source] = active[dest] = 1;
                                                                                                                       return a.x < b.x;
                                                                      for(auto &it:g[source])
                                                                             excess[source]+=it.cap;
                                                                                                               bool by y(Point &a, Point &b)
Data Structures:
                                                                             push(it);
                                                                                                                       return a.y < b.y;
Segment tree(point update to val, and range
                                                                      while(!Q.empty())
Sum):
                                                                                                               int n, ans=1e18;
                                                                             int v=Q.front();
                                                                                                               int a[N], pref[N];
//just do memset(tr,0,sizeof(tr))
                                                                             Q.pop();
                                                                                                               Point pt[N];
11 tr[4*N];
                                                                             active[v]=false;
void update(ll indx,ll val,ll ogL,ll ogR,ll si=1)
                                                                                                               int solve(int L, int R)
                                                                             discharge(v);
  if((indx < ogL) \text{ or } (indx > ogR))
                                                                      long long max flow=0;
                                                                                                                       if(L==R)
     return:
                                                                      for(auto &e:g[source])
                                                                                                                              return 1e18;
  if(ogL = ogR)
                                                                             max flow+=e.flow;
                                                                                                                       int M=(L+R)/2;
                                                                      return max flow;
                                                                                                                       sort(pt+L, pt+R+1, by x);
     tr[si]=val;
                                                                                                                       int d=min(solve(L, M), solve(M+1, R));
     return;
                                                                                                                       int midx=pt[L+(R-L+1)/2].x;
                                                       PushRelabel obj(2*n+2); //obj(number of nodes)
                                                                                                                       vector<Point> v;
  11 \text{ mid=}(ogL+ogR)>>1;
                                                       obj.addEdge(src,dest,capacity)
                                                                                                                       for(int i=L;i \le R;i++)
  update(indx,val,ogL,mid,si<<1);
                                                       Il flow=obj.max flow(0,2*n+1); (src,dest)
  update(indx,val,mid+1,ogR,(si<<1)|1);
                                                                                                                               if(Point\{pt[i].x-midx, 0\}.dist() < d)
  tr[si]=tr[si << 1]+tr[(si << 1)|1];
                                                       Min cost max flow:
                                                                                                                                      v.push back(pt[i]);
ll query(ll l, ll r, ll ogL, ll ogR, ll si=1)
                                                       //uncomment depending on cost type
                                                       //typedef long long int ct
  if(1>r)
                                                       //typedef double ct
                                                                                                                       sort(v.begin(), v.end(), by y);
     return 0;
                                                       //typedef int ct
                                                                                                                       for(int i=0;i<v.size();i++)
  if((r < ogL) \text{ or } (l > ogR))
                                                       //typedef long double ct
     return 0;
                                                                                                                               for(int j=i+1;j < v.size();j++)
  if((ogL>=1) && (ogR<=r))
                                                       //also DO: 11 MAXDIST=1e9; (or more if u
                                                      want, depending on max possible cost)
                                                                                                                                      if(Point{0,
     return tr[si];
                                                                                                               v[i].y-v[j].y.dist()>d)
```

```
break:
  11 \text{ mid} = (ogL + ogR) >> 1;
                                                        //Works for negative costs, but does not work for
                                                                                                                                           d=min(d, (v[i]-v[i]).dist());
                                                        negative cycles
  return
                                                        //Complexity: O(min(E^2 *V log V, E logV * flow))
query(1,r,ogL,mid,(si << 1))+query(1,r,mid+1,ogR,(si))
                                                        struct edge
i << 1)|1);
                                                                                                                           return d;
                                                                int to, flow, cap;
                                                                                                                   //pt[i]=\{x,y\} //initialise like this
Lazy Segment tree( range addition, range sum):
                                                                                                                   //int res=solve(1,n);
                                                                ct cost;
                                                                int rev;
11 \text{ tr}[4*N], \text{lazy}[4*N];
//initilialise both with 0
                                                        struct MinCostMaxFlow
                                                                                                                   Python Syntax:
void push(ll ogL,ll ogR,ll si)
                                                                int nodes:
                                                                                                                   1) from fractions import gcd # gcd(a,b)
                                                                vector<int> curflow, prevedge, prevnode, q;
                                                                                                                   2) raw input() # returns string , int()
  if(ogL!=ogR)
                                                                vector<ct> pot,prio;
                                                                                                                   3) map(int,raw input(),split()) # for full int array
                                                                vector<br/>bool> inqueue;
                                                                                                                   4) sorted(A)
     lazy[si << 1] += lazy[si];
     lazy[(si << 1)|1] += lazy[si];
                                                                vector<vector<edge>> graph;
                                                                                                                   5) Fast I/O
                                                                MinCostMaxFlow() {}
                                                                                                                   from sys import stdin, stdout
                                                                MinCostMaxFlow(int n): nodes(n), prio(n,
                                                                                                                           stdin.readline() # in place of raw input()
  tr[si]+=lazy[si]*(ogL-ogR+1); //for minimum
                                                        0), curflow(n, 0), //number of nodes
or max ,do tr[si]+=lazy[si]
                                                                                                                           stdout.write(str())
                                                                prevedge(n, 0), prevnode(n, 0), q(n, 0), pot(n, 0)
                                                                                                                   6) List functions, let A be list
  lazy[si]=0;
                                                        0), inqueue(n, 0), graph(n) \{\}
                                                                                                                           A.count('apple') # returns count
void update(ll l,ll r,ll val,ll ogL,ll ogR,ll si=1)
                                                                void addEdge(int source, int to, int capacity,
                                                                                                                           A.reverse(), len(A)
                                                        ct cost) //direction dependent
                                                                                                                           A.sort()
                                                                                                                           A.pop(), A.append()
  if(lazy[si])
                                                                                                                           del A[1:r] # deletes from (1,r) inclusive
                                                                        edge a = \{to, 0, capacity, cost, 
     push(ogL,ogR,si);
                                                        (int)graph[to].size()};
                                                                                                                   7) Sets
                                                                        edge b = \{\text{source}, 0, 0, -\text{cost}, \}
                                                                                                                           A=\{1,2,3,2\} # will remove duplicates
                                                                                                                           A=set('vinit') # A will contain
  if((r < ogL) \text{ or } (l > ogR))
                                                        (int)graph[source].size()};
                                                                        graph[source].push back(a);
                                                                                                                   {'v','i','n','t'}
     return:
  if((ogL>=1) && (ogR<=r))
                                                                        graph[to].push back(b);
                                                                                                                           a-b,a|b,a&b
                                                                                                                   8) dictionary
     lazy[si]+=val;
                                                                void bellman ford(int source, vector<ct>
                                                                                                                           A = \{ (a':23, b':34) \}
                                                                                                                           list(A) # will contain list of keys
     push(ogL,ogR,si);
                                                        &dist)
                                                                                                                   A = ['a', 'b']
     return;
                                                                        fill(dist.begin(), dist.end(),
                                                                                                                           A.get(key name) # returns None if not
  11 \text{ mid} = (ogL + ogR) >> 1;
                                                        MAXDIST);
                                                                                                                   found
  update(l,r,val,ogL,mid,si<<1);
                                                                        dist[source] = 0;
                                                                                                                           # don't use A[key name]
```

```
update(l,r,val,mid+1,ogR,(si << 1)|1);
                                                                                                                 9) from collections import deque
                                                                       int qt=0;
  tr[si]=tr[si << 1]+tr[(si << 1)|1];
                                                                       q[qt++] = source;
                                                                                                                         A=deque(list name)
                                                                       for(int qh=0;(qh-qt)%nodes!=0;qh++)
                                                                                                                         append(),popleft()
ll query(ll l, ll r, ll ogL, ll ogR, ll si=1)
                                                                                                                 10) import bisect
                                                                               int u = q[qh\%nodes];
                                                                                                                         A = [1,3,4,5,5,5,6] \#  must be sorted
                                                                                                                         bisect.bisect(A,5) # returns index after all
  if(lazy[si])
                                                                               inqueue[u] = false;
                                                                               for(auto &e : graph[u])
                                                                                                                 5's, i.e 6
     push(ogL,ogR,si);
                                                                                                                         bisect.bisect left(A,5) #lower bound
                                                                                      if(e.flow \ge e.cap)
                                                                                                                 index, i.e 3
  if((r < ogL) \text{ or } (l > ogR))
                                                                                              continue;
                                                                                                                 11)
                                                                                                                 from operator import itemgetter, attrgetter
     return 0:
                                                                                      int v = e.to:
  if((ogL>=1) && (ogR<=r))
                                                                                      ct newDist = dist[u] +
                                                                                                                 class node:
                                                                                                                    def init (self, L, R):
                                                       e.cost;
                                                                                      if(dist[v] > newDist)
                                                                                                                      self.L = L
     return tr[si];
                                                                                                                      self R = R
                                                                                              dist[v] =
  11 \text{ mid} = (ogL + ogR) >> 1;
                                                                                                                    def repr (self):
                                                       newDist:
                                                                                                                      return repr((self.L, self.R))
  return
query(1,r,ogL,mid,(si << 1))+query(1,r,mid+1,ogR,(si))
                                                                                              if(!inqueue[v])
                                                                                                                 A=sorted(A, key=attrgetter('L'))
i << 1)|1);
                                                                                                                 12)bin(ans).count("1") #counts number of set bits
                                                       inqueue[v] = true;
                                                                                                                 in binary representation of ans
                                                                                                                 13)2d array input
Lazy Segment tree( range update to val, range
                                                                                                      q[qt++
sum):
                                                       % nodes = v;
                                                                                                                 arr=[[] for i in xrange(100005)]
                                                                                                                 for i in xrange(n):
                                                                                                                      arr[i]= map(int, raw input().split())
11 tr[4*N],lazy[4*N];
//initialialise tr with 0, and lazy with -1(or anything
                                                                                                                 14)initialising and creating 2d array
like -inf, which will never come in update)
                                                                                                                 dp=[[0]*K \text{ for i in range}(N)]
void push(ll ogL,ll ogR,ll si)
                                                                                                                 1d array: a=[0]*N
                                                               pair<int, ct> minCostFlow(int source, int
                                                                                                                 15)array of map
                                                       dest, int maxflow) //max flow,min cost (pass
                                                                                                                 arr3=list( {} for i in xrange(1005) )
  if(ogL!=ogR)
                                                       maxflow as 1e9,or depending on largest possible
                                                                                                                 if x in arr3[i]:
                                                       max flow)
     lazy[si << 1] = lazy[si];
                                                                                                                      arr3[i][x] += 1
     lazy[(si << 1)|1] = lazy[si];
                                                                                                                    else:
                                                                       bellman ford(source, pot);
                                                                                                                      arr3[i][x]=1
                                                                       int flow = 0;
  tr[si]=lazy[si]*(ogL-ogR+1);
                                                                                                                 16)
                                                                       ct flow cost = 0;
  lazy[si]=-1;
                                                                                                                 Dict functions:clear(),get(key),pop(key),
                                                                       while(flow < maxflow)
void update(ll l,ll r,ll val,ll ogL,ll ogR,ll si=1)
```

```
priority queue<pair<ct, int>,
                                                                                                                   Big integer c++:
                                                        vector<pair<ct, int>>, greater<pair<ct, int>>> q;
  if(lazy[si]!=-1)
                                                                                g.push({0, source});
                                                                                                                   #include <boost/multiprecision/cpp int.hpp>
     push(ogL,ogR,si);
                                                                                fill(prio.begin(), prio.end(),
                                                                                                                   using namespace boost::multiprecision;
                                                        MAXDIST);
  if((r < ogL) \text{ or } (l > ogR))
                                                                                prio[source] = 0;
                                                                                                                   //arbitrary precision
                                                                                curflow[source] = INT MAX;
                                                                                                                   cpp int u = 1;
     return:
  if((ogL>=1) && (ogR<=r))
                                                                                while(!q.empty())
                                                                                                                   //fixed precision
                                                                                                                   int128 t v = 1;
     lazy[si]=val;
                                                                                        ct d = q.top().first;
     if(lazy[si]!=-1)
                                                                                        int u = q.top().second;
     push(ogL,ogR,si);
                                                                                        q.pop();
     return;
                                                                                        if(d != prio[u])
                                                                                                                   2D bit (point update and query):
                                                                                                continue;
  11 \text{ mid} = (ogL + ogR) >> 1;
                                                                                        for(int
                                                                                                                   //initialise bit to 0
  update(l,r,val,ogL,mid,si<<1);
                                                                                                                   //memset(bit,0,sizeof(bit));
                                                        i=0;i\leq graph[u].size();i++)
  update(1,r,val,mid+1,ogR,(si << 1)|1);
                                                                                                                   //1 based indexing
  tr[si]=tr[si << 1]+tr[(si << 1)|1];
                                                                                                edge
                                                                                                                   //query - prefix sum
                                                                                                                   //2d array ->1 based indexing
                                                        &e=graph[u][i];
ll query(ll l, ll r, ll ogL, ll ogR, ll si=1)
                                                                                                                   11 bit[N][N];
                                                                                                int v = e.to:
                                                                                                if(e.flow >=
                                                                                                                   void update(ll x,ll y,ll val,ll n,ll m)
  if(lazy[si]!=-1)
                                                        e.cap)
                                                                                                                      for(ll i=x;i<=n;i+=i&-i)// (instead of n,m u can
                                                                                                                   do < N \text{ where } N > max(n,m)
     push(ogL,ogR,si);
                                                        continue;
                                                                                                ct newPrio =
  if((r < ogL) \text{ or } (l > ogR))
                                                        prio[u] + e.cost + pot[u] - pot[v];
                                                                                                                         for(ll j=y;j \le m;j+=j\&-j)
     return 0;
                                                                                                if(prio[v] >
  if((ogL>=1) && (ogR<=r))
                                                        newPrio)
                                                                                                                           bit[i][j]+=val;
     return tr[si];
                                                                                                        prio[v]
                                                        = newPrio;
  ll mid=(ogL+ogR)>>1;
                                                                                                                   ll query(ll x, ll y)
  return
                                                        q.push({newPrio, v});
query(l,r,ogL,mid,(si<<1))+query(l,r,mid+1,ogR,(s
i << 1)|1);
                                                        prevnode[v] = u;
                                                                                                                      11 res=0;
                                                                                                                      for(11 i=x;i>=1;i==i\&-i)
                                                        prevedge[v] = i;
                                                                                                                        for(11 \text{ j=y;j} >= 1;j==j\&-j)
```

#### Policy based DS:(to read) $\operatorname{curflow}[v] = \min(\operatorname{curflow}[u], \operatorname{e.cap} - \operatorname{e.flow});$ #include <ext/pb ds/assoc container.hpp> #include <ext/pb ds/tree policy.hpp> using namespace gnu pbds; typedef tree<int, null type, less<int>, rb tree tag, if(prio[dest] == MAXDIST) tree order statistics node update> pbds; break: insert(val),erase(),order of key(),find by order() for(int i=0;i<nodes;i++) pot[i]+=prio[i]; int df = min(curflow[dest], **Graph Theory** maxflow - flow): **Bellman-Ford(for negative edges):** flow += df; for(int void BellmanFord(struct Graph\* graph, LL src) v=dest;v!=source;v=prevnode[v]) LL V = graph > V; edge &e = LL E = graph -> E; graph[prevnode[v]][prevedge[v]]; LL dist[V]; e.flow += df;for (LL i = 0; i < V; i++) graph[v][e.rev].flow -= dist[i] = INT MAX;df; dist[src] = 0; flow cost += df \*for (LL i = 1; $i \le V-1$ ; i++) e.cost; for (LL j = 0; j < E; j++) return {flow, flow cost}; LL u = graph -> edge[i].src;LL v = graph -> edge[i].dest;LL weight = graph->edge[i].weight; //MinCostMaxFlow obj(2\*n+2); if (dist[u] != INT MAX && dist[u] + //obj.addEdge(i,j+n,1,sqrt((y[j]-y[i])\*(y[j]-y[i])+(x[j]weight < dist[v]) -x[i]\*(x[i]-x[i]));dist[v] = dist[u] + weight;//pair<int,ct> flow=obj.minCostFlow(0,2\*n+1,1e9); rest same as prev }//to check for negative weight cycle, repeat above **Maximum Bipartite Matching:** \\ // if shorter path is found, cycle exists bool bpm(bool bpGraph[M][N], int u, bool seen[],

int matchR[])

```
res+=bit[i][i];
  return res;
//(upper left,bottom right) x is row,y is column
ll subMatrixSum(ll x1,ll y1,ll x2,ll y2)
  return
query(x2,y2)-query(x1-1,y2)-query(x2,y1-1)+qu
ery(x1-1,y1-1);
2D bit Submatrix Update:
#define N 505
//N>max(n,m)
11 bit[4][N][N];
//initialise bit to 0
//lets say array given,two ways->first for each
element call updateSubMatrix(i,j,i,j),
//or calculate sum[i][j],and treat matrix as
0's(baadmei bas add kar dena)
void update(ll node,ll x,ll y,ll v)
  for(11 i=x; i< N; i+=i&-i)
     for(11 \text{ j=y;j} < N; j+=j\&-j)
       bit[node][i][i]+=v;
ll query(ll node,ll x,ll y)
  11 ans=0;
  for(11 i=x; i>=1; i==i&-i)
```

```
// Try every job one by one
Prim's Algorithm for MST
void primMST()
                                                       for (int v = 0; v < N; v++)
                                                                                                                 for(ll j=y; j>=1; j==j&-j)
                                                                                                                   ans+=bit[node][i][i];
                                                          // If applicant u is interested in job v and v is
priority queue<pair<LL,LL>,greater<pair<LL,LL
                                                          // not visited
                                                                                                              return ans;
                                                          if (bpGraph[u][v] && !seen[v])
>>> pq;
  LL src = 0;
                                                                                                            //top left,bottom right
  vector<LL> key(V, INF);
                                                            seen[v] = true; // Mark v as visited
                                                                                                            void updateSubMatrix(ll x1,ll y1,ll x2,ll y2,ll
  vector < LL > parent(V, -1);
                                                            // If job 'v' is not assigned to an applicant OR
                                                                                                            val)
  vector<bool> inMST(V, false);
                                                            // previously assigned applicant for job v
  pq.push(make pair(0, src));
                                                     (which is matchR[v])
                                                                                                              update(0,x1,y1,val);
  key[src] = 0;
                                                            // has an alternate job available.
                                                                                                              update(0,x1,y2+1,-val);
                                                            // Since v is marked as visited in the above
  while (!pq.empty())
                                                                                                               update(0,x2+1,y1,-val);
                                                     line, matchR[v]
                                                                                                              update(0,x2+1,y2+1,va1);
    LL u = pq.top().second;
                                                            // in the following recursive call will not get
     pq.pop();
                                                     job 'v' again
                                                                                                              update(1,x1,y1,val*(1-y1));
     inMST[u] = true; // Include vertex in MST
                                                            if (matchR[v] < 0 \parallel bpm(bpGraph,
                                                                                                              update(1,x1,y2+1,va1*y2);
     list< pair<LL, LL>>::iterator i;
                                                     matchR[v], seen, matchR))
                                                                                                              update(1,x2+1,y1,va1*(y1-1));
     for (i = adj[u].begin(); i!= adj[u].end(); ++i)
                                                                                                              update(1,x2+1,y2+1,-val*y2);
                                                               matchR[v] = u;
       LL v = (*i).first;
                                                               return true;
                                                                                                              update(2,x1,v1,val*(1-x1));
       LL weight = (*i).second;
                                                                                                              update(2,x1,y2+1,(x1-1)*val);
       if (inMST[v] == false \&\& kev[v] > weight)
                                                                                                              update(2,x2+1,y1,va1*x2);
                                                                                                              update(2,x2+1,y2+1,-x2*val);
         kev[v] = weight;
                                                       return false;
         pq.push(make pair(key[v], v));
                                                                                                              update(3,x1,y1,(x1-1)*(y1-1)*val);
         parent[v] = u;
                                                                                                              update(3,x1,y2+1,-y2*(x1-1)*val);
                                                     int maxBPM(bool bpGraph[M][N])
                                                                                                              update(3,x2+1,y1,-x2*(y1-1)*val);
     }}}
                                                                                                              update(3,x2+1,y2+1,x2*y2*val);
                                                     // The value of matchR[i] is the applicant number
Strongly Connected Components (Kasuraja's
                                                     // assigned to job i
                                                       int matchR[N];
Algo):
                                                       memset(matchR, -1, sizeof(matchR));
                                                                                                            ll queryPoint(ll x,ll y)
//topological sort where for each edge a->b,a
comes before b
                                                       int result = 0; // Count of jobs assigned to
                                                                                                              return query(0,x,y)*x*y + query(1,x,y)*x
stack<ll> st;
                                                     applicants
                                                                                                              + query(2,x,y)*y+query(3,x,y);
ll sccCnt=0; //for scc
                                                       for (int u = 0; u < M; u++)
//uncomment if want topological sort too
```

```
//vector<ll> topo;
void dfs(ll curr)
  visited[curr]=true;
  for(ll x:adi[curr])
     if(!visited[x])
       dfs(x);
  st.push(curr);
void dfs2(ll curr)
  //uncomment if want topological sort too
  //topo.push back(curr);
  visited[curr]=true;
  scc[curr]=sccCnt;
  for(ll x:adjr[curr])
     if(!visited[x])
       dfs2(x);
void SCC(ll n)
  //uncomment if want topological sort too
  //topo.clear()
  memset(visited,false,sizeof(visited));
  for(11 i=1; i \le n; i++)
     if(!visited[i])
       dfs(i);
  sccCnt=0;
  memset(visited,false,sizeof(visited));
  while(!st.empty())
     11 curr=st.top();
```

```
// Mark all jobs as not seen for next applicant.
bool seen[N];
memset(seen, 0, sizeof(seen));

// Find if the applicant 'u' can get a job
if (bpm(bpGraph, u, seen, matchR))
    result++;
}
return result;
}
```

### **Geometry:**

1. Area of a regular polygon(equal sides):

$$area = \frac{s^2n}{4\tan\left(\frac{180}{n}\right)}$$

```
2. Angle between (m1, b1) and (m2, b2):
```

```
\arctan ((m2 - m1) / (m1 \cdot m2 + 1))
```

- 3. Triangle: Area =  $a \cdot b \cdot \sin \gamma / 2$
- Area =  $|x1 \cdot y2 + x2 \cdot y3 + x3 \cdot y1 y1 \cdot x2 y2 \cdot x3 y3 \cdot x1|/2$
- Heron's formula:

```
ll querySubMatrix(ll x1,ll y1,ll x2,ll y2)
  return queryPoint(x2,y2)-queryPoint(x1-1,y2)
  -queryPoint(x2,y1-1)+queryPoint(x1-1,y1-1);
Convex Hull trick Offline:
// convex hull, minimum
struct LineContainer{
vector<ll> M, B;
int ptr;
bool bad(int a,int b,int c) {
// use deterministic computation with long long
if sufficient
 return (long
double)(B[c]-B[a])*(M[a]-M[b])<(long
double)(B[b]-B[a])*(M[a]-M[c]);
// insert with non-increasing m
//m is slope,b is c in eqn y=mx+c
void insert(ll m, ll b) {
 M.push back(m);
 B.push back(b);
```

while  $(M.size() \ge 3 \&\& bad(M.size()-3,$ 

M.size()-2, M.size()-1)) {

M.erase(M.end()-2);

B.erase(B.end()-2);

return M[i]\*x + B[i];

ll get(int i, ll x){

```
st.pop();
    if(!visited[curr])
       sccCnt++;
       dfs2(curr);
     }}}
Others:
String Hashing:
struct Hashs
       vector<int> hashs;
       vector<int> pows;
       int P;
       int MOD;
       Hashs() {}
       Hashs(string &s, int P, int MOD): P(P),
MOD(MOD)
              int n = s.size();
              pows.resize(n+1, 0);
              hashs.resize(n+1, 0);
              pows[0] = 1;
              for(int i=n-1;i>=0;i--)
                     hashs[i]=(1LL * hashs[i+1]
* P + s[i] - 'a' + 1) \% MOD;
                     pows[n-i]=(1LL *
pows[n-i-1] * P) % MOD;
              pows[n] = (1LL * pows[n-1] *
P)%MOD;
       int get hash(int l, int r)
```

```
Let s = (a + b + c) / 2; then Area = s \cdot (s - a) \cdot (s - a)
b) \cdot (s - c)
4. Circle: (x - xc)^2 + (v - vc)^2 = r^2
5. Polygon area (vertex coordinates):
|x1 \cdot y2 + x2 \cdot y3 + ... + xn \cdot y1 - y1 \cdot x2 - y2 \cdot x3 -
... - yn \cdot x1 | / 2
6 Sine Rule: \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} = 2R
7. Cosine Rule: a^2 = b^2 + c^2 - 2bc \cos A
8. Half-Angle Rule: \sin \frac{A}{2} = \sqrt{\frac{(s-b)(s-c)}{bc}}:
\cos \frac{A}{2} = \sqrt{\frac{s(s-a)}{bc}} \tan \frac{A}{2} = \sqrt{\frac{(s-b)(s-c)}{s(s-a)}}
9. Circumradius: R = \frac{abc}{4(area)}
10 In-radius
r = 4R\sin\frac{A}{2}\sin\frac{B}{2}\sin\frac{C}{2} = (s-a)\tan\frac{A}{2}
11 Area:
\Delta = rs = \frac{1}{2}bc\sin A = 2R^2\sin A\sin B\sin C = \frac{abc}{4R} = \sqrt{s(s-a)(s-b)(s-c)}
12.Medians: m_a = \frac{1}{2}\sqrt{2b^2 + 2c^2 - a^2} and similar
expressions for other medians.
```

13.Area of a quadrilateral ABCD with AB = a; BC = b; CD = c DA = d  $A + C = 2\alpha$  is given by  $\Delta = \sqrt{(s-a)(s-b)(s-c)(s-d) - abcd\cos^2\alpha}$ 

Its diagonals are given by  $AC=\sqrt{\frac{(ac+bd)(ad+bc)}{(ab+cd)}}$ ;  $BD=\sqrt{\frac{(ac+bd)(ab+cd)}{(ad+bc)}}$ 

```
// query with non-decreasing x
ll query(ll x) {
 ptr=min((int)M.size()-1,ptr);
 while (ptr<M.size()-1 &&
get(ptr+1,x) < get(ptr,x)
  ptr++;
 return get(ptr,x);
LineContainer obj;
//usage if want maximum,then if y=mx+c
,convert it to equation y'=-mx-c, and then do the
below, only at last res=-obj.query(xi)
//lets say lines (m1,x1),(m2,x2)...,sort these in
decreasing order of m, and then do
obj.insert(mi,xi)
//if query x1,x2,x3..xn,sort increasing order,and
then query->obj.query(xi)
```

### **Convex Hull Trick Online Set:**

```
//Convex hull,maximum
bool Q;
struct Line {
    mutable ll k, m, p;
    bool operator<(const Line& o) const {
        return Q ? p < o.p : k < o.k;
    }
};
struct LineContainer : multiset<Line> {
    ll div(ll a, ll b) {
        return a / b - ((a ^ b) < 0 && a % b);
}
bool isect(iterator x, iterator y) {
    if (y == end()) { x->p = inf; return false; }
    if (x->k == y->k) x->p = x->m > y->m ? inf
```

```
int ans = hashs[1] + MOD -
(1LL*hashs[r+1]*pows[r-l+1])%MOD;
               ans%=MOD;
               return ans;
//Hashs obj;
//obj=Hashs(s1,P1,mod1));
//obj.get hash(l,r)
FFT:
//put this #define compulsarily, change int main()
to int32 t main()
#define int long long
const int N = 8e5+5;
typedef complex<double> base;
const double PI = acos(-1.01);
const int Maxb = 19;
const int Maxp = 450;
const int MOD=13313;
vector<int> rev;
vector<br/>base> omega;
void calc rev(int n, int log n) //Call this before
FFT
      omega.assign(n, 0);
       rev.assign(n, 0);
       for(int i=0;i< n;i++)
              rev[i]=0;
               for(int j=0;j < log n; j++)
                      if((i>>j)&1)
                             rev[i] |=
1 << (log n-j-1);
```

```
14. If two chords AB, CD of a circle intersect at a
point O (which may lie inside or outside the circle),
then AO.OB = CO.OD
Orientation:
LL orientation(PoLL p1, PoLL p2, PoLL p3)
  LL \text{ val} = (p2.y - p1.y) * (p3.x - p2.x) -
        (p2.x - p1.x) * (p3.y - p2.y);
  if (val == 0) return 0; // colinear
  return (val > 0)? 1: 2; // clock or counterclock
wise
Line intersection:
bool on Segment (PoLL p, PoLL q, PoLL r)
  if (q.x \le max(p.x, r.x) \&\& q.x \ge min(p.x, r.x)
&&
```

 $q.y \le max(p.y, r.y) && q.y >= min(p.y, r.y)$ 

bool doIntersect(PoLL p1, PoLL q1, PoLL p2, PoLL

if (o1 == 0 && onSegment(p1, p2, q1)) return

LL o1 = orientation(p1, q1, p2); LL o2 = orientation(p1, q1, q2);

LL o3 = orientation(p2, q2, p1);

LL o4 = orientation(p2, q2, q1); if (o1 != o2 && o3 != o4)

return true;

return true;

return false;

q2)

true;

## else x->p = div(y->m - x->m, x->k - y->k);return x->p>=y->p; void add(ll k, ll m) { auto $z = insert(\{k, m, 0\}), y = z++, x = y;$ while (isect(y, z)) z = erase(z); if (x != begin() && isect(--x, y)) isect(x, y =erase(y)); while ((y = x) != begin() && (--x)->p >=y - pisect(x, erase(y)); ll query(ll x) { // cout<<endl<<jk<<endl; assert(!empty()); Q = 1; auto $l = *lower bound(\{0,0,x\}); Q =$ 0; cout<<l.k<<" h "<<l.m<<endl: return 1.k \* x + 1.m; **}**; LineContainer obj; //usage if want minimum,then if y=mx+c ,convert it to equation y'=-mx-c,and then do the below, only at last res=-obj.query(xi) //adding line y=mx+c->obj.add(m,c) //querying-> obj.query(x)

: -inf:

```
if (o2 == 0 \&\& onSegment(p1, q2, q1)) return
                                                      true;
void fft(vector<base> &A, int n, bool invert)
                                                        if (o3 == 0 \&\& onSegment(p2, p1, q2)) return
                                                      true;
       for(int i=0;i< n;i++)
                                                        if (o4 == 0 \&\& onSegment(p2, q1, q2)) return
                                                      true;
               if(i<rev[i])</pre>
                      swap(A[i], A[rev[i]]);
                                                        return false;}
       for(int len=2;len<=n;len<<=1)
                                                      Circle intersection area:
               double ang=2*PI/len *
                                                      int areaOfIntersection(x0, y0, r0, x1, y1, r1){
(invert?-1:+1);
                                                      var rr0 = r0*r0;
               int half=(len>>1);
                                                      var rr1 = r1*r1:
               base curomega(cos(ang), sin(ang));
                                                      var c = Math.sqrt((x1-x0)*(x1-x0)+(y1-y0)*(y1-x0)
               omega[0]=base(1, 0);
                                                      y0));
               for(int i=1;i<half;i++)
                                                      var phi = (Math.acos((rr0+(c*c)-rr1)/(2*r0*c)))*2;
                                                      var theta = (Math.acos((rr1+(c*c)-rr0)/(2*r1*c)))*2;
                                                      var area 1 = 0.5*theta*rr1 - 0.5*rr1*Math.sin(theta);
omega[i]=omega[i-1]*curomega;
                                                      var area2 = 0.5*phi*rr0 - 0.5*rr0*Math.sin(phi);
               for(int i=0;i< n;i+=len)
                                                      return area1 + area2;
                      base t;
                      int pu = i,
                              pv = i + half
                                                      Convex Hull:(nlogn)
                                                      Point nextToTop(stack<Point> &S)
                              pu end = i+half,
                              pw = 0:
                      for(; pu!=pu end; pu++,
                                                        Point p = S.top();
pv++, pw++)
                                                        S.pop();
                                                        Point res = S.top();
                              t=A[pv] *
                                                        S.push(p);
omega[pw];
                                                        return res;
                              A[pv] = A[pu] - t;
                              A[pu] += t;
                                                      int distSq(Point p1, Point p2)
                                                        return (p1.x - p2.x)*(p1.x - p2.x) +
                                                            (p1.y - p2.y)*(p1.y - p2.y);
       if(invert)
              for(int i=0;i< n;i++)
                                                      int compare(const void *vp1, const void *vp2)
```

```
A[i]/=n;
                                                        Point p1 = (Point *)vp1;
void multiply(int n, vector < base > & A,
                                                        Point p2 = (Point *)vp2;
vector<br/>base> &B, vector<int> &C)
                                                        int o = orientation(p0, *p1, *p2);
                                                        if (o == 0)
                                                         return (distSq(p0, *p2) >= distSq(p0, *p1))? -1:
       fft(A, n, false);
       fft(B, n, false);
                                                      1;
       for(int i=0;i< n;i++)
                                                        return (o == 2)? -1: 1;
               A[i] *= B[i];
                                                      void convexHull(Point points[], int n)
       fft(A, n, true);
       for(int i=0;i< n;i++)
                                                        int ymin = points[0].y, min = 0;
                                                        for (int i = 1; i < n; i++)
               C[i] = (int)(A[i].real() + 0.5);
               C[i] \% = MOD;
                                                         int y = points[i].y;
                                                         if ((y < ymin) || (ymin == y &&
void Solve(int n, vector<int> &coeffA,
                                                            points[i].x < points[min].x)
vector<int> &coeffB, vector<int> &result, bool
                                                           ymin = points[i].y, min = i;
big1, bool big2) //Call 4 times: 00, 01, 10, 11
                                                        swap(points[0], points[min]);
       vector<base> A(n), B(n);
                                                        p0 = points[0];
       for(int i=0;i< n;i++)
                                                        qsort(&points[1], n-1, sizeof(Point), compare);
                                                        int m = 1:
               A[i]=big1?coeffA[i]/Maxp:
                                                        for (int i=1; i < n; i++)
coeffA[i]%Maxp;
                                                          // Keep removing i while angle of i and i+1 is
               B[i]=0;
                                                      same
       for(int i=0;i< n;i++)
                                                           while (i < n-1 &\& orientation(p0, points[i],
                                                                             points[i+1] == 0
               B[i]=big2?coeffB[i]/Maxp:
                                                            i++;
                                                           points[m] = points[i];
coeffB[i]%Maxp;
                                                          m++;
       vector\leqint\geq C(n);
       multiply(n, A, B, C);
                                                        if (m < 3) return;
                                                        stack<Point>S;
       for(int i=0;i< n;i++)
                                                        S.push(points[0]);
               int add=C[i];
                                                        S.push(points[1]);
               if(big1)
                                                        S.push(points[2]);
```

```
add*=Maxp;
                                                        for (int i = 3; i < m; i++)
               if(big2)
                       add*=Maxp;
                                                          while (orientation(nextToTop(S), S.top(),
                                                      points[i]) != 2)
               add%=MOD;
               result[i]+=add;
                                                            S.pop();
               result[i]%=MOD;
                                                          S.push(points[i]);
                                                        while (!S.empty())
void do FFT(vector<int> &A, vector<int> &B,
vector<int> &result)
                                                           Point p = S.top();
                                                           cout << "(" << p.x << ", " << p.y <<")" << endl;
       int n=1, bits=0;
                                                           S.pop();
       while(n \le 2*A.size() \parallel n \le 2*B.size())
               n < < = 1, bits++;
       result.assign(n, 0);
       calc rev(n, bits);
       vector<int> tempA(A.begin(), A.end());
                                                      Point in a polygon:
       vector<int> tempB(B.begin(), B.end());
                                                      bool isInside(Point polygon[], int n, Point p)
       tempA.resize(n);
       tempB.resize(n);
       for(int i=0; i<2; i++)
                                                         if (n < 3) return false;
                                                         Point extreme = {INF, p.y};
                                                         int count = 0, i = 0;
               for(int j=0; j<2; j++)
                                                         do
                       Solve(n, tempA, tempB,
                                                           int next = (i+1)%n;
result, i, j);
                                                           if (doIntersect(polygon[i], polygon[next], p,
                                                      extreme))
//vector<int>v1;
                                                              if (orientation(polygon[i], p, polygon[next])
//v1.resize(n+1);
                                                      == 0)
// fill(v1.begin(),v1.end(),0);
                                                                return on Segment(polygon[i], p,
//if x^2+3*x then v1[2]=1,v1[1]=3
                                                      polygon[next]);
//vector<int> res:
//do FFT(v1,v2,res);
                                                              count++;
//res.resize(2*n+1) //so agar x size ka tha ,then x to
2*n tak sab 0
                                                           i = next:
                                                         \} while (i != 0);
```

return count&1; // Same as (count%2 == 1) }	
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