| Question Number | Answer | | Mark |
|--------------------|--|-----|------|
| 18(a) | Use of $T^2 = KR^3$ | (1) | |
| | $K \text{ for Earth} = 2.96 \times 10^{-19} (\text{s}^2 \text{ m}^{-3})$ | (1) | |
| | $K \text{ for Mars} = 2.97 \times 10^{-1} \text{ (s}^2 \text{ m}^{-3}\text{)}$ | (1) | 3 |
| | Example of calculation | | |
| | $K = \frac{T^2}{R^3} = \frac{(3.16 \times 10^7 \text{s})^2}{(1.50 \times 10^{11} \text{ m})^3} = 2.959 \times 10^{-19} \text{ s}^2 \text{ m}^{-3}$ | | |
| | $K = \frac{T^2}{R^3} = \frac{(5.93 \times 10^7 \text{s})^2}{(2.28 \times 10^{11} \text{ m})^3} = 2.967 \times 10^{-19} \text{ s}^2 \text{ m}^{-3}$ | | |
| 18(b) | Either Use of $F = \frac{GMm}{r^2}$ with $F = \frac{mv^2}{r}$ | (1) | |
| | | | |
| | Re-arrangement with $v = \frac{2\pi r}{T}$ to identify K as $\frac{(2\pi)^2}{GM}$ | (1) | |
| | $K = 2.97 \times 10^{-19} \text{ (s}^2 \text{ m}^{-3}\text{)}$ | (1) | |
| | Or | (1) | |
| | Use of $F = \frac{GMm}{r^2}$ with $F = m\omega^2 r$ | (1) | |
| | Re-arrangement with $\omega = \frac{2\pi}{T}$ to identify K as $\frac{(2\pi)^2}{GM}$ | (1) | |
| | $K = 2.97 \times 10^{-19} (\text{s}^2 \text{m}^{-3})$ | (1) | 3 |
| | Example of calculation | | |
| | $\frac{GMm}{r^2} = m\omega^2 r$ | | |
| | $\frac{GM}{r^2} = \left(\frac{2\pi}{T}\right)^2 r$ | | |
| | $T^2 = \frac{(2\pi)^2}{GM} r^3$ | | |
| | $K = \left(\frac{4\pi^2}{6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2} \times 1.99 \times 10^{30} \text{ kg}}\right) = 2.97 \times 10^{-1} \text{ s}^2 \text{m}^{-3}$ | | |

18(c) Use of
$$T^2 = KR^3$$
 (1)

 $T = 43 \text{ hours}$ (1)

Example of calculation

$$\left(\frac{T_I}{T_G}\right)^2 = \left(\frac{R_I}{R_G}\right)^3$$
 $T = \sqrt{\left(\frac{4.22 \times 10^8 \text{ m}}{1.07 \times 10^9 \text{ m}}\right)^3 \times (172 \text{ hour})^2} = 42.6 \text{ hours}$

Total for question 18