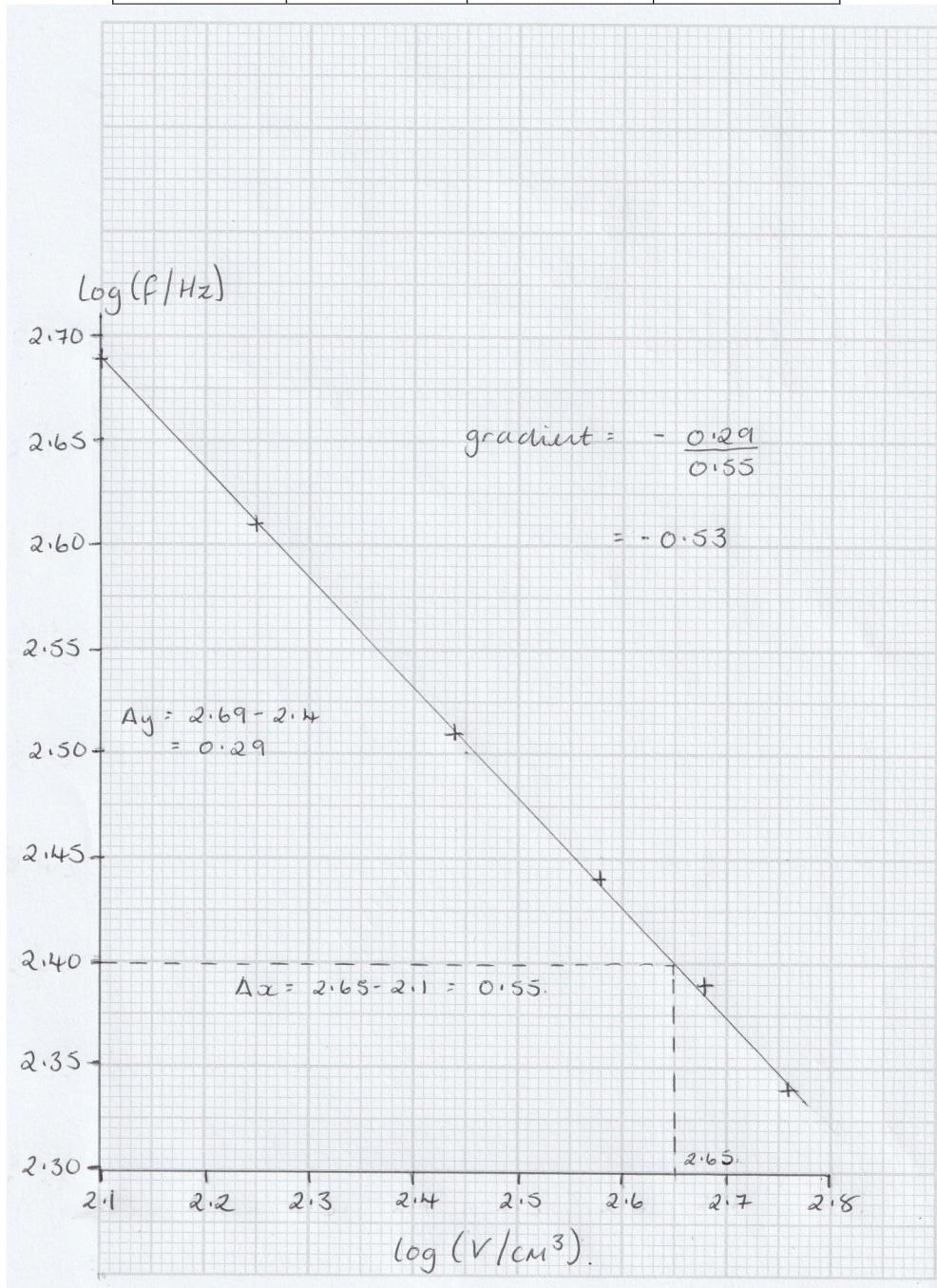
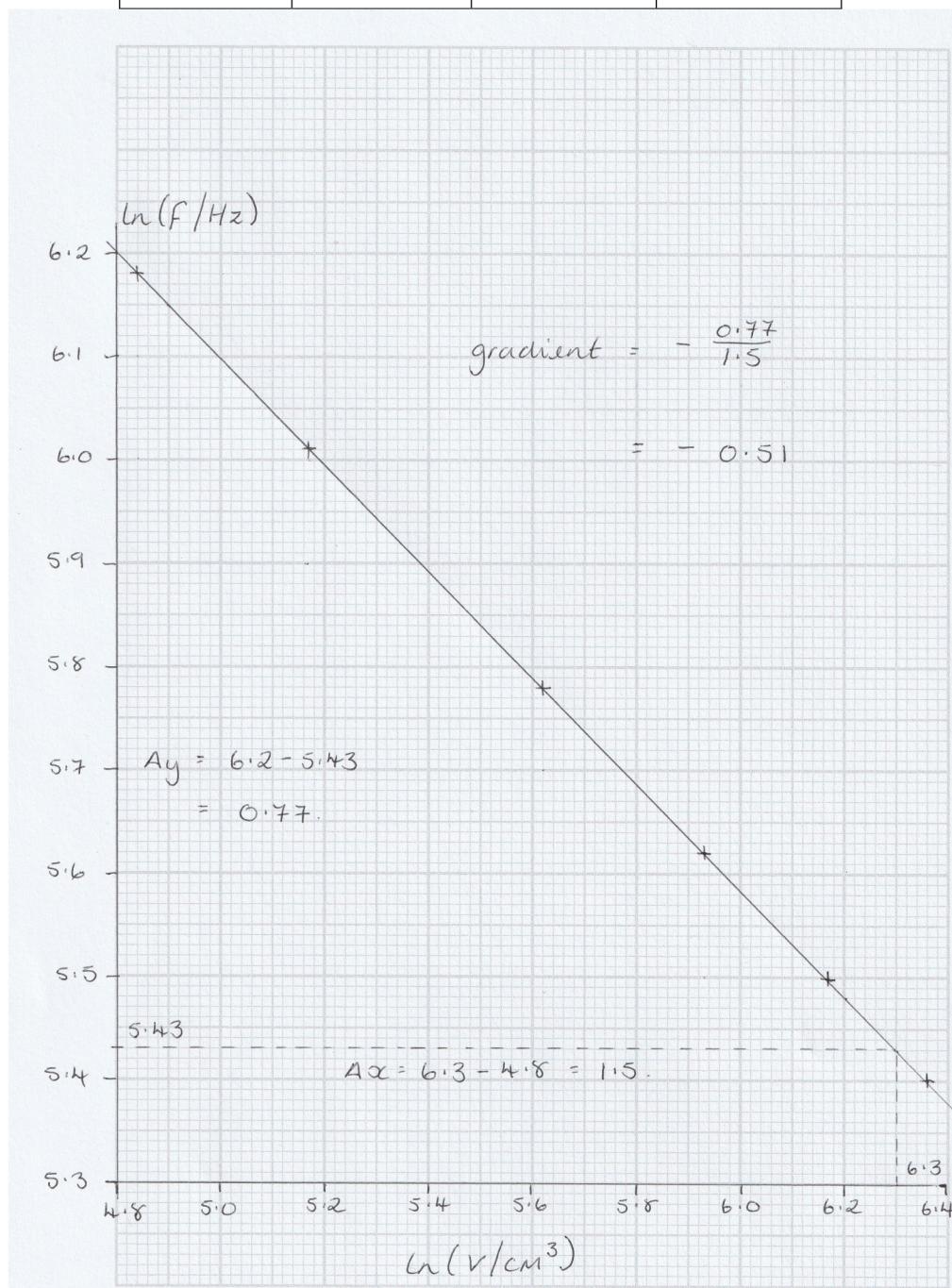


$V / \text{cm}^3$	$f / \text{Hz}$	$\log (V / \text{cm}^3)$	$\log (f / \text{Hz})$
576	221	2.76	2.34
476	244	2.68	2.39
376	275	2.58	2.44
276	323	2.44	2.51
176	408	2.25	2.61
126	485	2.10	2.69



$V / \text{cm}^3$	$f / \text{Hz}$	$\ln(V / \text{cm}^3)$	$\ln(f / \text{Hz})$
576	221	6.36	5.40
476	244	6.17	5.50
376	275	5.93	5.62
276	323	5.62	5.78
176	408	5.17	6.01
126	485	4.84	6.18



Question Number	Answer	Mark
4 (a)(i)	<p>Any <b>TWO</b> from:</p> <p>Ensure the metre rule is vertical using a set square valid methods</p> <p>Accept alternative (1)</p> <p>Ensure the end of the rod is close to the metre rule <b>Or</b> use a set square to read off the values (1)</p> <p>Take readings perpendicular to the scale (to avoid parallax) (1)</p>	<b>2</b>
4 (a)(ii)	<p>The uncertainty of a single reading is half the resolution of the metre rule, (which is 0.5 mm) (1)</p> <p>As the two readings are subtracted, the uncertainties are added (1)</p>	<b>2</b>
4 (b)(i)	<p>Micrometer screw gauge (with a resolution of 0.01mm) (Accept digital caliper) (1)</p> <p>As this would produce an uncertainty of 0.25% which is small (1)</p>	<b>2</b>
4 (b)(ii)	<p>One <b>PAIR</b> from:</p> <p>Repeat at different orientations <b>and</b> calculate a mean (1)</p> <p>To reduce the effect of <u>random errors</u> (1)</p> <p>Check (and correct) for zero error (1)</p> <p>To eliminate <u>systematic error</u> (1)</p>	<b>2</b>
4 (b)(iii)	<p>Mean value of <math>d = \underline{2.35}</math> (mm) (1)</p> <p>Calculation from half range shown to give uncertainty of 0.02 (mm) (1)</p> <p><u>Example of calculation</u></p> <p>Mean <math>d = (2.35 + 2.37 + 2.34 + 2.34 + 2.33) \text{ mm} / 5 = 11.74 \text{ mm} / 5</math>  <math>= 2.348 \text{ mm} = 2.35 \text{ mm}</math></p> <p>Uncertainty <math>= (2.37 - 2.33) \text{ mm} / 2 = 0.04 \text{ mm} / 2 = 0.02 \text{ mm}</math></p>	<b>2</b>
4 (c)	<p>Use of <math>G = (32mglx^2) / (\pi yd^4)</math> shown (1)</p> <p>Correct value of <math>G</math> given to 2 or 3 s.f. e.c.f. (b)(iii) (1)</p> <p>Bald answer scores 0</p> <p>Accept value of <math>1.5 \times 10^{11} (\text{N m}^{-2})</math> if <math>d = 2 \text{ mm}</math> used</p> <p><u>Example of calculation</u></p> $G = \frac{32 \times 0.1\text{kg} \times 9.81 \text{ N kg}^{-1} \times 0.589 \text{ m} \times (0.103 \text{ m})^2}{3.14159 \times 0.026 \text{ m} \times (2.35 \times 10^{-3} \text{ m})^4}$ $= 0.196 \text{ N m}^3 / 2.49 \times 10^{-12} \text{ m}^5$ $= 7.87 \times 10^{10} (\text{N m}^{-2})$ $= 7.9 \times 10^{10} (\text{N m}^{-2})$	<b>2</b>

4 (d)	Use of $2 \times \%U$ in $x$ <b>Or</b> $4 \times \%U$ in $d$ shown	(1)		
	Calculation of correct value of $\%U$ in $G$	e.c.f. (b)(iii)		
	Correct value of relevant limits from $\%U$	e.c.f. (c)		
	Valid conclusion based on comparison of relevant limits with data	(1)		
<u>Example of calculation</u>				
$\begin{aligned}\%U &= (0.1 / 58.9) \times 100 + 2 \times (0.1 / 10.3) \times 100 + (1 / 26) \times 100 \\ &\quad + 4 \times (0.02 / 2.35) \times 100 \\ &= 0.17\% + 2 \times 0.97\% + 3.85\% + 4 \times 0.85\% \\ &= 0.17\% + 1.94\% + 3.85\% + 3.40\% \\ &= 9.36\% = 9.4\%\end{aligned}$ <p>Upper limit = <math>78.7 \times 10^9 \text{ N m}^2 \times (1+0.094) = 86.1 \times 10^9 \text{ N m}^2</math></p> <p>Lower limit = <math>78.7 \times 10^9 \text{ N m}^2 \times (1 - 0.094) = 71.3 \times 10^9 \text{ N m}^2</math></p> <p>As both values fall within this range, the student cannot determine which type of steel the rod is made from.</p>				
<b>Or</b>				
<p>Use of uncertainties to calculate maximum or minimum shown</p> <p>Calculation of correct value of upper limit</p> <p>Calculation of correct value of lower limit</p> <p>Valid conclusion based on comparison of relevant limit with data</p>				
<u>Example of calculation</u>				
<p>Upper limit <math>G = \frac{32 \times 0.1 \text{ kg} \times 9.81 \text{ N kg}^{-1} \times (0.589+0.001) \text{ m} \times ((0.103+0.001) \text{ m})^2}{3.14159 \times (0.026-0.01) \text{ m} \times ((2.35-0.02) \times 10^{-3} \text{ m})^4}</math></p> $\begin{aligned}&= 0.200 \text{ N m}^3 / 2.31 \times 10^{-12} \text{ m}^5 \\ &= 8.68 \times 10^{10} (\text{N m}^{-2})\end{aligned}$ <p>Lower limit <math>G = \frac{32 \times 0.1 \text{ kg} \times 9.81 \text{ N kg}^{-1} \times (0.589-0.001) \text{ m} \times ((0.103-0.001) \text{ m})^2}{3.14159 \times (0.026+0.01) \text{ m} \times ((2.35+0.02) \times 10^{-3} \text{ m})^4}</math></p> $\begin{aligned}&= 0.192 \text{ N m}^3 / 2.68 \times 10^{-12} \text{ m}^5 \\ &= 7.16 \times 10^{10} (\text{N m}^{-2})\end{aligned}$ <p>As both values fall within this range, the student cannot determine which type of steel the rod is made from.</p>				
<b>Or</b>				
<p>Use of <math>2 \times \%U</math> in <math>x</math> <b>Or</b> <math>4 \times \%U</math> in <math>d</math> shown</p> <p>Calculation of correct value of <math>\%U</math> in <math>G</math></p> <p>Correct calculation of relevant <math>\%D</math> shown</p> <p>Valid conclusion based on comparison of relevant <math>\%D</math> with <math>\%U</math></p>				
<u>Example of calculation</u>				
$\begin{aligned}\%U &= (0.1 / 58.9) \times 100 + 2 \times (0.1 / 10.3) \times 100 + (1 / 26) \times 100 \\ &\quad + 4 \times (0.02 / 2.35) \times 100\end{aligned}$				

$$= 0.17\% + 2 \times 0.97\% + 3.85\% + 4 \times 0.85\%$$

$$= 0.17\% + 1.94\% + 3.85\% + 3.40\%$$

$$= 9.36\% = 9.4\%$$

$$\%D \text{ for structural steel} = (78.7 - 79.3)/79.3 \times 100 = 0.76 \%$$

$$\%D \text{ for carbon steel} = (78.7 - 77)/77 \times 100 = 2.3\%$$

As % D for both structural and carbon steel are less than the %U, the student cannot determine which type of steel the rod is made from.

**Total for question**

**16**