12 The 'escape velocity' is the minimum speed needed for an object to escape from the gravitational field of a planet.

An object travelling at the escape velocity has a kinetic energy equal to the magnitude of its gravitational potential energy at the surface of the planet.

(a) Show that the escape velocity v for a planet of mass M and radius r is given by the expression

$$v = \sqrt{\frac{2GM}{r}}$$

**(2)** 

(b) (i) Show that the escape velocity for a mass at the Earth's surface is about  $1.1 \times 10^4 \, \text{m s}^{-1}$ .

mass of Earth = 
$$5.98 \times 10^{24}$$
 kg radius of Earth =  $6.36 \times 10^6$  m

(2)

(ii)	When the Earth formed,	a l	large	proportion	of the	gas i	n the	Earth's	atmosp	here
	was hydrogen.									

Explain why hydrogen gas is no longer a large proportion of the gas in the Earth's atmosphere. No further calculation is necessary.

at 20 °C, 
$$\sqrt{\langle c^2 \rangle} = 1900 \,\mathrm{m \, s^{-1}}$$
 for hydrogen

	(2)

(Total for Question 12 = 6 marks)