4 A student measured a metal nut of the type shown below.



- (a) The student measured the diameter d of the hole in the centre of the metal nut.
  - (i) She made one measurement in cm using Vernier calipers and one measurement in mm using digital calipers. The photographs show the measurements.





Explain why the digital calipers would be a better choice of instrument for this measurement.

You should include calculations in your answer.



(2)

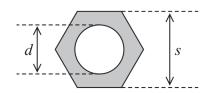
(iii) The student recorded the following measurements.

Determine the mean value of d and its uncertainty in mm.

(3)

Mean value of  $d = mm \pm mm$ 

(b) The student was given a different size metal nut. She measured the distances shown.



She calculated the shaded area A of the metal using the formula

$$A = \frac{\sqrt{3}}{2} \ s^2 - \frac{\pi}{4} d^2$$

 $s = 16.83 \, \text{mm} \pm 0.02 \, \text{mm}$ 

$$d = 8.55 \,\mathrm{mm} \pm 0.04 \,\mathrm{mm}$$

$$A = 1.88 \, \text{cm}^2$$

Show that the uncertainty in A is about  $0.01 \,\mathrm{cm}^2$ .

**(4)** 

(c) The student measured	the mass m	and the	thickness x	of the meta	l nut.
m = 10.3  g + 0.1  g					

$$m = 10.3 \text{ g} \pm 0.1 \text{ g}$$
  
 $x = 7.92 \text{ mm} \pm 0.03 \text{ mm}$   
 $A = 1.88 \text{ cm}^2 \pm 0.01 \text{ cm}^2$ 

(i) Determine the density  $\rho$  of the metal from which the nut is made.

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(ii) The density of steel ranges from  $7.85\,\mathrm{g\,cm^{-3}}$  to  $8.03\,\mathrm{g\,cm^{-3}}$ .

Deduce whether the metal nut could be made from steel.	
	(3)

(2)