

Question Number	Answer	Mark
16(a)	<p><b>Either</b> (1)</p> <p>Use of <math>F = \frac{GMm}{r^2}</math> with <math>F = m\omega^2 r</math> (1)</p> <p>Use of <math>\omega = \frac{2\pi}{T}</math> (1)</p> <p><math>T = 5800 \text{ s}</math></p> <p><b>Or</b></p> <p>Use of <math>F = \frac{GMm}{r^2}</math> with <math>F = \frac{mv^2}{r}</math> (1)</p> <p>Use of <math>v = \frac{2\pi r}{T}</math> (1)</p> <p><math>T = 5800 \text{ s}</math> (1)</p> <p><u>Example of calculation</u></p> $\frac{GMm}{r^2} = m\omega^2 r$ $\therefore \omega = \sqrt{\frac{GM}{r^3}}$ $\therefore \omega = \sqrt{\frac{6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2} \times 6.0 \times 10^{24} \text{ kg}}{(6.4 \times 10^6 \text{ m} + 5.5 \times 10^5 \text{ m})^3}} = 1.09 \times 10^{-3} \text{ rad s}^{-1}$ $T = \frac{2\pi \text{ rad}}{1.09 \times 10^{-3} \text{ rad s}^{-1}} = 5755 \text{ s}$	3
16(b)	<p><b>Either</b></p> <p>(<math>F = \frac{GMm}{r^2}</math>, so) the (gravitational) force is greater for a low Earth orbit (1)</p> <p><math>F = m \left( \frac{2\pi}{T} \right)^2 r</math> (1)</p> <p>So if <math>F</math> increases when <math>r</math> decreases, then <math>T</math> must decrease (1)</p> <p>(MP3 dependent upon MP1 or MP2)</p> <p><b>Or</b></p> <p>(<math>\frac{2\pi}{T} = \sqrt{\frac{GM}{r^3}}</math>, so) <math>T^2 = \frac{4\pi^2 r^3}{GM}</math> (1)</p> <p><math>G</math> and <math>M</math> are constant, so <math>T \propto \sqrt{r^3}</math> (1)</p> <p>So when <math>r</math> is smaller, <math>T</math> is smaller. (1)</p> <p>(MP3 dependent upon MP1 or MP2)</p> <p>[Accept converse argument]</p>	3

<p><b>16(c)</b></p>	<p>Use of <math>V_{\text{grav}} = (-) \frac{GM}{r}</math> (1)</p> <p>Use of <math>\Delta E_k = GMm \left( \frac{1}{r_1} - \frac{1}{r_2} \right)</math> (1)</p> <p><math>\Delta E_k = 1.1 \times 10^9 \text{ J}</math> (1)</p> <p>(Do not credit use of <math>\Delta E_{\text{grav}} = mg\Delta h</math>, as <math>g</math> is not constant)</p> <p><u>Example of calculation</u></p> <p><math>\Delta E_k = 6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2} \times 6.0 \times 10^{24} \text{ kg} \times 227 \text{ kg} \left( \frac{1}{6.4 \times 10^6 \text{ m}} - \frac{1}{(6.4 \times 10^6 + 5.5 \times 10^5) \text{ m}} \right)</math></p> <p><math>\therefore \Delta E_k = 1.12 \times 10^9 \text{ J}</math></p>	<p><b>3</b></p>
	<p><b>Total for question 16</b></p>	<p><b>9</b></p>