Inference for numerical data

Subhalaxmi Rout

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North Carolina births

In 2004, the state of North Carolina released a large data set containing information on births recorded in this state. This data set is useful to researchers studying the relation between habits and practices of expectant mothers and the birth of their children. We will work with a random sample of observations from this data set.

Exploratory analysis

Load the nc data set into our workspace.

load("more/nc.RData")

We have observations on 13 different variables, some categorical and some numerical. The meaning of each variable is as follows.

variable	description
fage	father's age in years.
mage	mother's age in years.
mature	maturity status of mother.
weeks	length of pregnancy in weeks.
premie	whether the birth was classified as
	premature (premie) or full-term.
visits	number of hospital visits during
	pregnancy.
marital	whether mother is married or not
	married at birth.
gained	weight gained by mother during
	pregnancy in pounds.
weight	weight of the baby at birth in pounds.
lowbirthweight	whether baby was classified as low
	birthweight (low) or not (not low).
gender	gender of the baby, female or male.
habit	status of the mother as a nonsmoker or
	a smoker.
whitemom	whether mom is white or not white.

1. What are the cases in this data set? How many cases are there in our sample?

Answer

A case is a single birth in the state of North Caroline. There are total 1000 cases in this dataset.

```
dim(nc)
```

```
## [1] 1000 13
```

As a first step in the analysis, we should consider summaries of the data. This can be done using the summary command:

summary(nc)

```
##
         fage
                           mage
                                             mature
                                                            weeks
                                                                                premie
##
            :14.00
                             :13
                                    mature mom :133
                                                               :20.00
                                                                         full term:846
    Min.
                     Min.
                                                        Min.
                                    younger mom:867
    1st Qu.:25.00
                     1st Qu.:22
                                                        1st Qu.:37.00
                                                                                   :152
                                                                         premie
##
    Median :30.00
                     Median:27
                                                        Median :39.00
                                                                         NA's
                                                                                   :
            :30.26
                                                               :38.33
##
    Mean
                     Mean
                             :27
                                                        Mean
##
    3rd Qu.:35.00
                     3rd Qu.:32
                                                        3rd Qu.:40.00
##
    Max.
            :55.00
                     Max.
                             :50
                                                        Max.
                                                               :45.00
##
    NA's
            :171
                                                        NA's
                                                               :2
                                             gained
##
        visits
                            marital
                                                              weight
##
    Min.
            : 0.0
                    married
                                 :386
                                        Min.
                                                : 0.00
                                                          Min.
                                                                  : 1.000
##
    1st Qu.:10.0
                    not married:613
                                        1st Qu.:20.00
                                                          1st Qu.: 6.380
                                        Median :30.00
##
    Median:12.0
                    NA's
                                 : 1
                                                          Median: 7.310
##
    Mean
            :12.1
                                        Mean
                                                :30.33
                                                          Mean
                                                                  : 7.101
##
    3rd Qu.:15.0
                                        3rd Qu.:38.00
                                                          3rd Qu.: 8.060
##
    Max.
            :30.0
                                                :85.00
                                                                 :11.750
                                        Max.
                                                          Max.
##
    NA's
            :9
                                        NA's
                                                :27
##
    lowbirthweight
                        gender
                                         habit
                                                          whitemom
##
    low
            :111
                    female:503
                                   nonsmoker:873
                                                    not white:284
##
    not low:889
                    male :497
                                             :126
                                                              :714
                                   smoker
                                                    white
##
                                   NA's
                                                    NA's
##
##
##
##
```

As you review the variable summaries, consider which variables are categorical and which are numerical. For numerical variables, are there outliers? If you aren't sure or want to take a closer look at the data, make a graph.

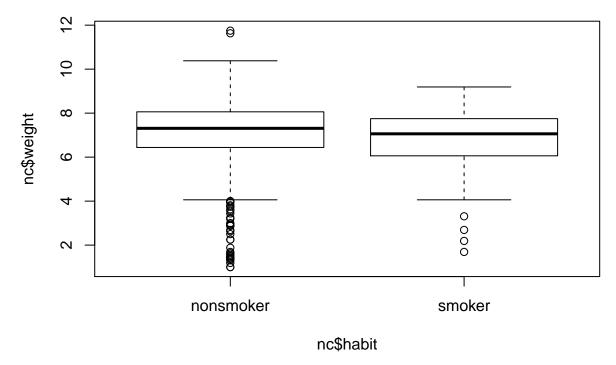
Consider the possible relationship between a mother's smoking habit and the weight of her baby. Plotting the data is a useful first step because it helps us quickly visualize trends, identify strong associations, and develop research questions.

2. Make a side-by-side boxplot of habit and weight. What does the plot highlight about the relationship between these two variables?

Answer

The boxplot shows that the median birth weight of newborns of mothers who is non-smoker is higher than the newborns mothers who is smoker.

boxplot(nc\$weight ~ nc\$habit)



The box plots show how the medians of the two distributions compare, but we can also compare the means of the distributions using the following function to split the weight variable into the habit groups, then take the mean of each using the mean function.

There is an observed difference, but is this difference statistically significant? In order to answer this question we will conduct a hypothesis test \cdot .

Inference

3. Check if the conditions necessary for inference are satisfied. Note that you will need to obtain sample sizes to check the conditions. You can compute the group size using the same by command above but replacing mean with length.

Answer

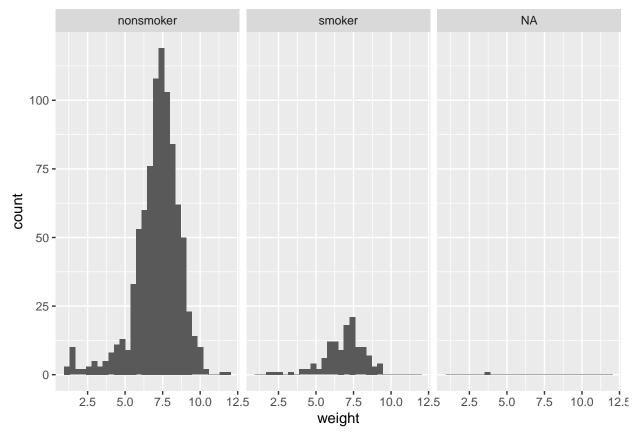
```
by(nc$weight, nc$habit, length)

## nc$habit: nonsmoker
## [1] 873
```

```
## nc$habit: smoker
## [1] 126

library(ggplot2)
ggplot(nc,aes(x=weight)) + geom_histogram() + facet_grid(~nc$habit)
```

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



samples are approximately normally distributed in both group. The sample size in each group is > 30. The sample is definately less than 10% birth in North Carolina. Observations in each group seems independent. So from this we can say this is a normal distribution.

4. Write the hypotheses for testing if the average weights of babies born to smoking and non-smoking mothers are different.

Answer

H0: average weights of babies born to smoking and non-smoking mother are same HA: average weights of babies born to smoking and non-smoking mother are not same

Next, we introduce a new function, inference, that we will use for conducting hypothesis tests and constructing confidence intervals.

```
DATA606::inference(y = nc$weight, x = nc$habit, est = "mean", type = "ht", null = 0, alternative = "twosided", method = "theoretical")
```

```
## Response variable: numerical, Explanatory variable: categorical
## Difference between two means
## Summary statistics:
## n_nonsmoker = 873, mean_nonsmoker = 7.1443, sd_nonsmoker = 1.5187
## n_smoker = 126, mean_smoker = 6.8287, sd_smoker = 1.3862
## Observed difference between means (nonsmoker-smoker) = 0.3155
##
## HO: mu_nonsmoker - mu_smoker = 0
## HA: mu_nonsmoker - mu_smoker != 0
## Standard error = 0.134
## Test statistic: Z = 2.359
## p-value = 0.0184
               9
\infty
9
                                 0
                                 0
                                 0
\alpha
                                 0
                                                       -0.32
                                                                      0
                                                                                0.32
          nonsmoker
                             smoker
```

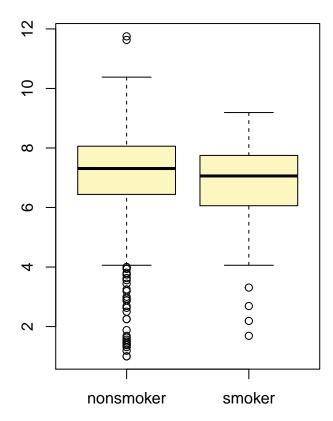
Let's pause for a moment to go through the arguments of this custom function. The first argument is y, which is the response variable that we are interested in: nc\$weight. The second argument is the explanatory variable, x, which is the variable that splits the data into two groups, smokers and non-smokers: nc\$habit. The third argument, est, is the parameter we're interested in: "mean" (other options are "median", or "proportion".) Next we decide on the type of inference we want: a hypothesis test ("ht") or a confidence interval ("ci"). When performing a hypothesis test, we also need to supply the null value, which in this case is 0, since the null hypothesis sets the two population means equal to each other. The alternative hypothesis can be "less", "greater", or "twosided". Lastly, the method of inference can be "theoretical" or "simulation" based.

nc\$habit

5. Change the type argument to "ci" to construct and record a confidence interval for the difference between the weights of babies born to smoking and non-smoking mothers.

Answer

```
## Response variable: numerical, Explanatory variable: categorical
## Difference between two means
## Summary statistics:
## n_nonsmoker = 873, mean_nonsmoker = 7.1443, sd_nonsmoker = 1.5187
## n_smoker = 126, mean_smoker = 6.8287, sd_smoker = 1.3862
```



nc\$habit

```
## Observed difference between means (nonsmoker-smoker) = 0.3155
##
## Standard error = 0.1338
## 95 % Confidence interval = ( 0.0534 , 0.5777 )
```

By default the function reports an interval for $(\mu_{nonsmoker} - \mu_{smoker})$. We can easily change this order by using the order argument:

Response variable: numerical, Explanatory variable: categorical

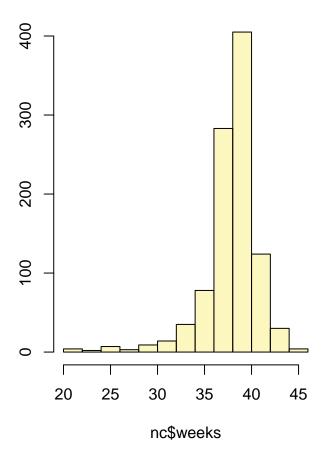
```
## Difference between two means
## Summary statistics:
## n_smoker = 126, mean_smoker = 6.8287, sd_smoker = 1.3862
## n_nonsmoker = 873, mean_nonsmoker = 7.1443, sd_nonsmoker = 1.5187
                                 8
10
\infty
9
               0
               0
               0
^{\circ}
            smoker
                            nonsmoker
                    nc$habit
## Observed difference between means (smoker-nonsmoker) = -0.3155
```

```
## ## Standard error = 0.1338
## 95 % Confidence interval = ( -0.5777 , -0.0534 )
```

On your own

• Calculate a 95% confidence interval for the average length of pregnancies (weeks) and interpret it in context. Note that since you're doing inference on a single population parameter, there is no explanatory variable, so you can omit the x variable from the function.

Answer



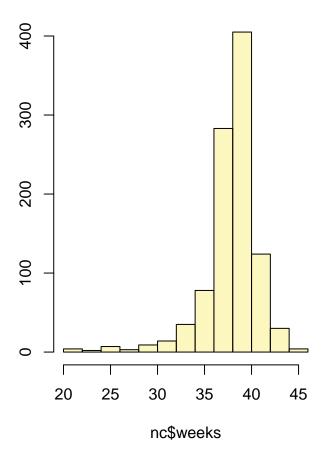
```
## mean = 38.3347 ; sd = 2.9316 ; n = 998
## Standard error = 0.0928
## 95 % Confidence interval = ( 38.1528 , 38.5165 )
```

95~% Confidence interval is (38.1528 , 38.5165)

• Calculate a new confidence interval for the same parameter at the 90% confidence level. You can change the confidence level by adding a new argument to the function: conflevel = 0.90.

Answer

Single mean
Summary statistics:



```
## mean = 38.3347 ; sd = 2.9316 ; n = 998
## Standard error = 0.0928
## 90 % Confidence interval = ( 38.182 , 38.4873 )
```

• Conduct a hypothesis test evaluating whether the average weight gained by younger mothers is different than the average weight gained by mature mothers.

Answer

H0: There is no difference between average weight gained by mature mothers and younger mothers. HA: There is difference between average weight gained by mature mothes and younger mothers.

```
## Response variable: numerical, Explanatory variable: categorical
## Difference between two means
## Summary statistics:
## n_mature mom = 133, mean_mature mom = 7.1256, sd_mature mom = 1.6591
## n_younger mom = 867, mean_younger mom = 7.0972, sd_younger mom = 1.4855
## Observed difference between means (mature mom-younger mom) = 0.0283
##
## HO: mu_mature mom - mu_younger mom = 0
## HA: mu_mature mom - mu_younger mom != 0
## Standard error = 0.152
```

Since the confidence interval (-4.2896, 0.7502). Based on above data, we accept reject the null hypothesis and we are saying that there is no difference in birth weight of babies born to younger and mature mothers.

nc\$mature

• Now, a non-inference task: Determine the age cutoff for younger and mature mothers. Use a method of your choice, and explain how your method works.

Answer

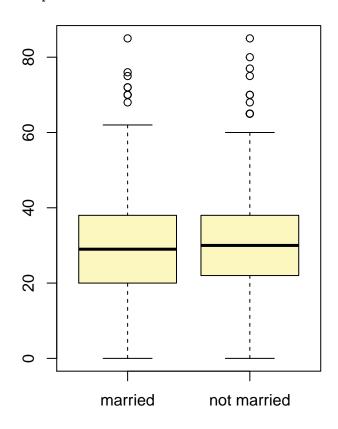
From the above analysis, we can see the age for younger mother is between 13 to 34. The age for mature mother in between 35 to 50. Here I have used by() to calculate age consideration for mature and younger mother.

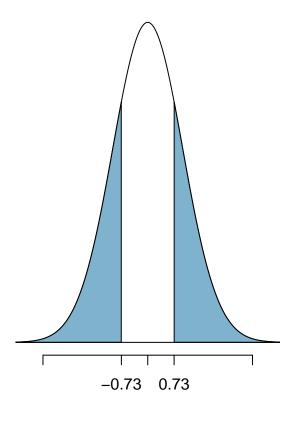
• Pick a pair of numerical and categorical variables and come up with a research question evaluating the relationship between these variables. Formulate the question in a way that it can be answered using a hypothesis test and/or a confidence interval. Answer your question using the inference function, report the statistical results, and also provide an explanation in plain language.

Answer

Hypothesis test: H0: There is no difference in the mean of the weight gained during pregnancy of between married and unmarried mothers. HA:There is difference in the mean of the weight gained during pregnancy of between married and unmarried mothers

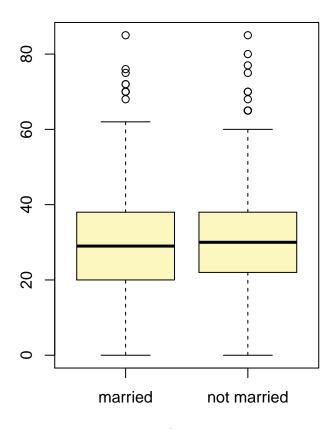
```
## Response variable: numerical, Explanatory variable: categorical
## Difference between two means
## Summary statistics:
## n_married = 370, mean_married = 29.873, sd_married = 15.2721
## n_not married = 603, mean_not married = 30.6036, sd_not married = 13.5757
## Observed difference between means (married-not married) = -0.7307
## HO: mu_married - mu_not married = 0
## HA: mu_married - mu_not married != 0
## Standard error = 0.967
## Test statistic: Z = -0.755
## p-value = 0.4502
```





nc\$marital

```
## Response variable: numerical, Explanatory variable: categorical
## Difference between two means
## Summary statistics:
## n_married = 370, mean_married = 29.873, sd_married = 15.2721
## n_not married = 603, mean_not married = 30.6036, sd_not married = 13.5757
```



nc\$marital

```
## Observed difference between means (married-not married) = -0.7307 ## ## Standard error = 0.9675 ## 95 % Confidence interval = ( -2.6269 , 1.1655 )
```

From the above data, we cannot reject the hypothesis. There is no evidence based on statistical data to show that theer is difference betweem the weight gained by married and unmarried mothers during pregnancy.