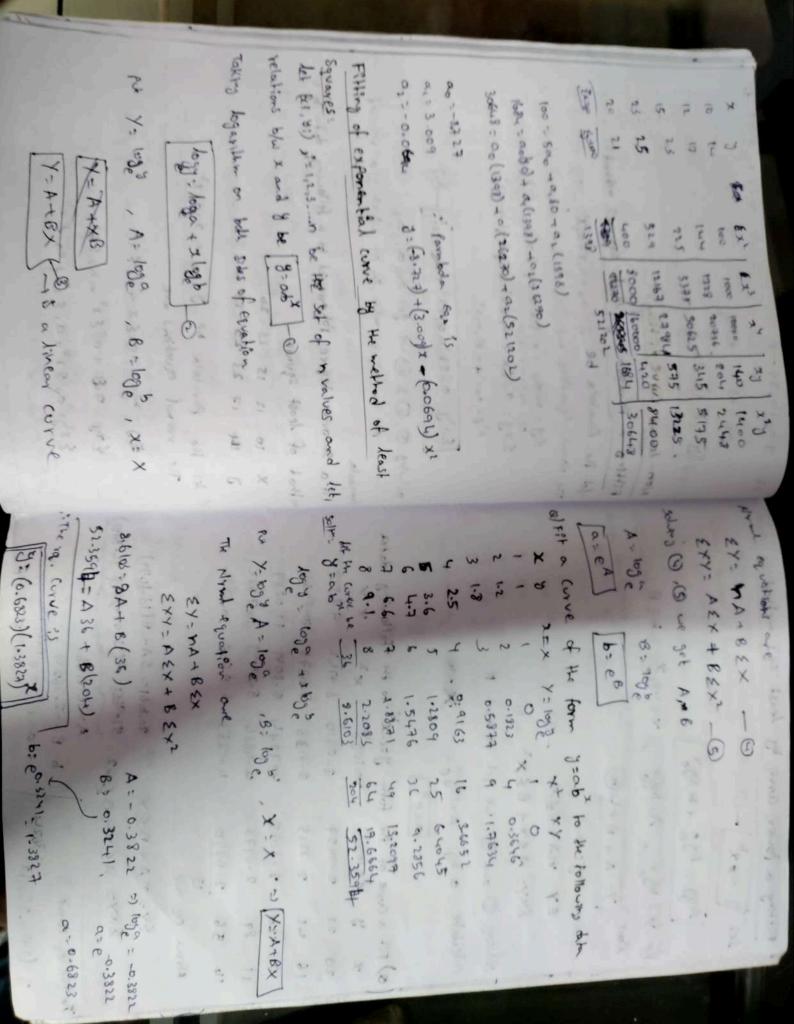
Chapter-5 Function Approximation Tools in Engineering curved - fitting: least eaks curve fitting procedures: with and experimental data , the data is plotted or graph Phaser and a straight live is drawn to the Mothed Points. This is "He usual method to Fit a mattenation equation to Experimental data. The method of bows , least squares & the most systematic procedure to fit a. some of unique curve to the given data points. its application is wide in practical computations 7 121 let the set of data points be: (x:, y:), P: 42, ... m suppose the curve y=f(x) is fitted to this database let the observed value at x= xi is y; and the corresponding value on the curve is f(x;), let ei is he error of approximation at I shi Hen we have e: - y: - f(2?) 491 consider s = [pr-f(x)] = (b2-f(2)) + - [b-f(x)] : ei + ei + ... . em The method of least sq. consists of minimising s. Fifting a straight line: let y = ao + aix is a straight live to be fitted to the given 5: [7,-(aota,2)) + [2-(aota,2)]+ :--+[9,-aota,2,]-(3)

Chapter-5 Function Approximation Tools in Engineering corved - fifting: least sals curve fitting procedures: with and experimental data , the data is plotted on graph Phaper and a straight live is frawn to the Atted Points. This is the usual nethod to fit a material equation to Experimental data. The method of less squares & the most systematic procedure to fit a 7 Finally He unique curve to the given data foints. its application! orea is b. is wide in Practical Computations 24 balt ( let the set of data points be-(x:, y:), 8:1,2,...m (s, 8,2) fel suppose the curve y=f(x) is fitted to this databas. Let the observed value at x=x; is y; and the corresponding value on He curve is f(xi), let ei is the error of approximation at H NO (3,61%) X=Xi Hen we have ( 186,300) e: - y: - f(a:) (onsider S = [71-f(x1)] = (32-f(22)) + - [3-f(x-)]2 10-1 491 : e1 + e2 + -- tem - (2) 7 Hire We welled of least sq. consists of minimising s. for cashin to Fifting a straight line: let y=ao+a,x ?s a straight line to be fitted to the given 0= 76 (10) (1. (8-1)) 5: [y,-(aota,x)) + [y2-(aota,x2)] + :--+[y\_-aota,xm)]-()

LET THE required the equation be diagotal X The would equation of st. line are a) Fit a straight like for the following data 29- 2ao+ Eatx. solving the above equations we get required stilling -) The rormal equations are Eg: 500+018x -03 J : 00 + 01.7 \$2-72 27-36 85-200 100 1554543 433 3 9 9 9 8 8 F F 9 X Ex3. 200 x 300 5x2 English of the state of the XX to to come and the X310 + \$ 01 EX APP & 24 64 36 81 30 36 というとなっとなけるとかっといる 1-00 tain 15 = 001 + 0121 JABA 5 mollip by x We thou of deast squares.

X (0 12 15 23 20

J (44 17 23 25 2) Fit a second degree Potymontal to a following data by a Non- dread Coave & fitting 36 = 9 anta 12 - 35 The News equalibres are solving @, @ L @ we get ao, a, daz Fitters or parabola by deast squares method: let the Parabola be 3 = a + a, x + a, x - 0 let the Parabola be 3=00 tan 2+00 x but so to last appear in a milital sive required The versel equations are 8-8-(0:5)x Exi: 00 Ext a 'Ext a Ext - (5) 00 - 18 A 21-37 123 - mas Haisx tar Ext Esy: ad + a, E12 + a, End ... (A) - 4x3 20 + 5x3,0 - (3 00 - (2 x3 られかかられるいとよるかのでより XID - X + a + X - OIX

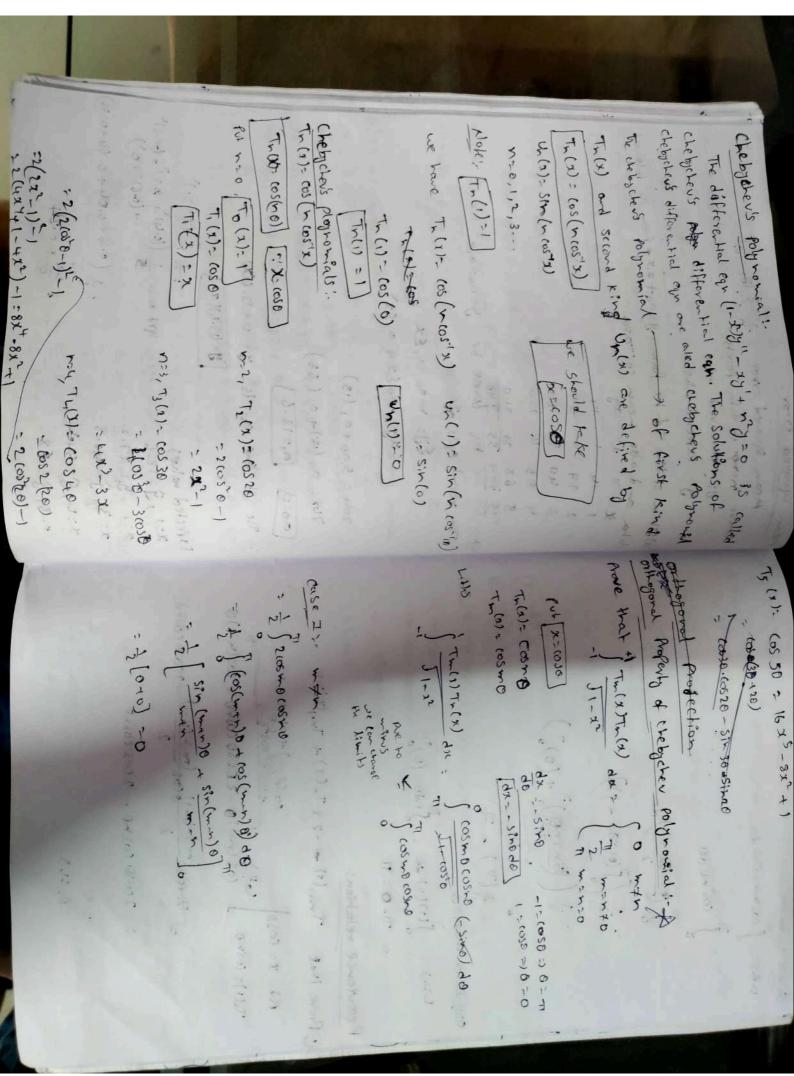


To Herez worse is J = (2728.8539)x Alrus eg as a) Fit a conve of the form years to the following data

x y x=1032. y=1058 x2 x5

20 21 2-9957 3-0910 8-9942 9-2517 10 120 2-3025 14 56 2-6390 Calculate a by A=1090 \*\* solving @ and @ we get A and B 16 41 2.7725 By y 100 A 1000 X 1000 X b= B Law Y: A+ Bx for Net Down to ]-0 Fitting a power curve by least sq's method s. EY: WATBEX. -@ Logy: loge + 6 loge 1×30+434 -4x3 X38+Au=K3 Exy - 4 2x + 8 2 x 1 - (1) 4.486 6.304 11.0237 E570:11 1005:9 1284.7 3-7135 7-6873 10-2963 4-0253 6-9648 10-6234 b=8--2-3624 a-eA= e10.21+6 一次以本 大田本 一次 アンコ トマタイ・マスラ A=10.2146 51.963: A(13.1074)+12 34.848 20.1061- 5AT B(13.1079) ストライナストング 27298- 353CI data and also ream sq. surar.

1 14 1 14
2 17 4 54
3 40 9 120
4 55 16 220 g: observed value 5 68 20 300 St. He FET LOWEVE BE YOUR ON A. X. offit a state of the form grantax - from the following wear squared error : Expected values .. The statement of is The wormand eg's affe 8.04-5. 8:2 2:4:2 -3. 3. -4.2 x=1,9=13.6 apid 9,=13.6 Mean squared expor = + \(\frac{1}{2}(\pi\_1 - \beta\_1)\) ++45 - B (+-+ 204 = 500+01 (15) 1:5, J. 68 THE = 00 (15) + 01 (55) Ey: mao ta, Ex 5x3. 005x+015x2 Me on Spy on on : 1 (6.4) + (0.6) + (0.3) + (-0. y= 0 + 13.60W 8-(3.6)(2) 1.00 000 00 1 1. X 000 7 1 = (xx - 5x) To Care = 1 (0.16+0.04+0.64+0.34) からった中 Creptores Galler or 197



(as no do

これいい

(1.4.5) Th (x) = nx | hc | x | (1.4.12)

- 1.(x) = -sin (n(05'x))

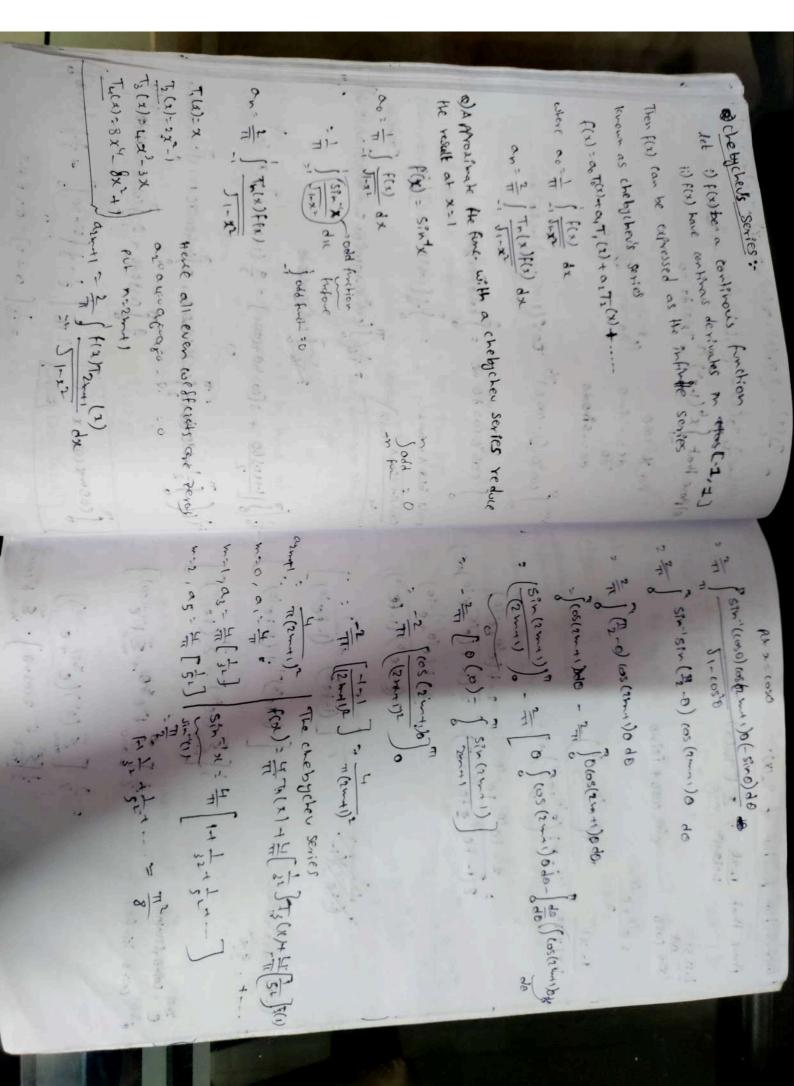
- 1.(x) = -sin (n(05'x))

- 1.(x) = -sin (n(05'x))

- 1.(x) = -n(050 (05 n0 + n) (05(n0 - 0))

- 1.(050x)

メチュスニメナン: 上[13(1)一日、(1)] ナンナ[12(1)十16(2)] OF spress He Polymontal chebychus phyromial 7,0021 了(何): 423-32 =) 33: 3(1) 43(万(江)) 7(1): 2321 3) 2= 72(1)+ 706) Prove that i) 7,(0): (1) i) That = cos(prios'x) T. (2): 103 (m (05 12)) 1 to 500 : 101 12 Tra-50): (05-47) · (05 ×77 10)-100 (pm) (05 (0)) - 下しい 中で(火) x3+2x--x+1111 he hard of (a) to (b) +0 (1) Tule) > (1) Tour (1) Tour (1) Tour (1) (a): (a) ((m+1) 2) すいいていかいらな) = (05 (MT+ 7) COS NTI COS TI + SIN NTI SINTI (1050 (1050) COS (8105 1050) (-5250) do al home that \x6(1-x) "\2 \tag{x} \dx =0 cossA= b105 A-5105 1 16 ( 5 = 108.80 46+ + 1 (cos80 cos60 de + 3 ) (cos40 cos80 de + 3) (cos20 cos0 + 16 ( [1+10560 + 3[10540+10520] + 9 (1+10520) (10520 do) ( os my logua : o AX = -58 = 0 J cos 60 cos 80 do = [ (cos o) τω \$ 2 do dx -- Sinodo 75(1) + 37, (x) + 70(x) + 75 (x) - 7(x) +276(x) 16 ( 2 x 3 (singo) - 28 x (singo) To States Bode - 16 ( ( cos so ratios 0+ 600 so ( 0580 ) ( ) 2) . ( Joen ( 500) = ) 4[(0530+3(050) 4(@522+5(050) 3 (cost ode + 3 (cost e costo de) = 16 0+0] =0= R.H.S Cos80de



en-coshe -isinfo) e - condisintel . Prove that with no trans herevation function of This 1-x+
1-x+ (ei0+ei0)++1 2 [(1-tere) (1-tere)] 2-te10-te-10+12) = 2-t(e10+e-10) eio\_ coso + isino 1 [ 2 (4) (2,00) - 2 1,50,00 - 2 1,20,00 -2 [ strews + strews) 1 (fe's) - 5 (te'd) = 1 (1-te-0)-1+ (1-te-0)-1 2 (6-te16) (1-60-10)) 2-+(eio+e-io) F(1) = x (1) = 1 (0) = 0

a) de termine the 5th degree marchausers polynomial machanins polynomial. (i): f(o): 100-0 (1): 1+(1-0) 0 + x (-1) 1 x (0) (1-1) 1 cemelined at x=0 for given function f(x): (osx. Toy lors polynomials (function approx. by toy loss f" a) - strat => f"(0) = 0 Given Centered of 200 Note: If c=0 then it is called not defree 1" - =( 0)" } (= x201 - -(K)" } is called the toy not degree Taylor refynomial for fly) + 8-15 FIG + (1,-1)5(0)

(05x-1-x2+x4

a) october the dispress that follow in x

at x=1 for given further in x

The size of the dispress that the follow series is

The size of the dispress that the follow series is

The size of the dispress that the follow series is 1,(1), = - = - (1), 1 = -1 からなったからい。1 sell-The Taylors espansion of FOX, T) at Point 1,2 is fr = 1m1120. Taylor Series expansion of f(1,1) about the foint (0,6) 10 5 21 C. O 100. If 35. S. (1.1) + (- 10) 1 = x20 - 10) ((0,0); f(1,2)+ [0-1)fx(1,2) + (+1)fx(1,2) | + 2; [6-1)fx(1,2) + 2(x4)(3-2) 1 2 (2-5) (2-6) (3-6) (3-6) (3-6) (3-6) (3-6) (3-6) (3-6) (3-6) (3-6) (3-6) (3-6) (a-b) and (a-b) of (a-b) and (a-a) taylor's sories for further of two variables. is known as Taylor series (a) Taylors expansion (or) maclaurants sevies expansion & a special expansion a) We Taylor some to estand flant) = of the th of Taylor series when the expansion is whome ortgin ine (0,0). find- x2+xy+y2+ fin1=1+2+4 +57 fr: of = 27+2 = fo(1,1) = 5 中心一下一日本日二日十二十 ((4.18) - f(0,6) + [(2-0) fy(0,0) + (3-6) fy(0,0)] + 1 (4-0) fxx610 +1(2-0)(8-からりてはからしてもしましている) 3 Full (1-1) (1-1) + 3 k-1/6-2) Fxyy (1,1)

 $f_{2x} = \frac{\partial^2 f}{\partial x^2} = \frac{\partial}{\partial x} \left( \frac{\partial f}{\partial x} \right)^2 = \frac{\partial}{\partial x} \left( \frac{\partial f}{\partial x} \right)^2 = 2 \Rightarrow f_{2x}(1/2) = 2$  $f_{yy} = \frac{3^2 f}{3^2 y} = \frac{36}{34} \left(\frac{3 f}{3 y}\right) = \frac{3}{32} \left(\frac{23}{42}\right) = 1 = 3 f_{xy}(1/2) = 1$ 13/310-10 -10.012 -16.01x for = シュナーラー(引力): シャンコーン = for (ハン) = 2 from = 3x3 3x (2)=0. It loves more than 2. He good is o for = 3t - 3 (2) = 0 . The try by series of f(213)= 7++ [11-1)4+(12)5)++ [11-1)-12 1+(1-2)-2 12(x-1)(y-2)(y) of the sends to company set when 276-97 relies to " by the color proces of mount good relient sold (48) 600 (48) fo 273609) 1 3.1 - 19-9) to (6/10) 1/2 (6/10 (34) (40) 5 - (50) 16 0) 15 + H(0) 100 + (0) 100 (10) 100 + (5) 200 45. 1 (1) wet (4) to - (4) col (000 45 + 000 (00) 200 3 COMPANY FORMS CHEKER SOS