

/*To find the roots of the equation $f(x) = 0$ by successive approximations, we write it in the form $x = p(x)$. The roots of $f(x) = 0$ are the same as the points of intersection of the straight line $y = x$ and the curve representing $y = p(x)$. Let $X = X_0$ be an initial approximation of the desired root, then the first approximation x_1 is given by $X_1 = p(X_0)$. Now, treating x_1 as the initial value, the second approximation is $X_2 = p(X_1)$. Proceeding in this way the n th approximation is given by $X_n = p(X_{n-1})$. The equation $X_{k+1} = 1.2/\log(x_k)$ is used to find the roots of the equation $x\log(x) = 1.2$.

In this method we use X_0 as initial value to find X_1 using $X_1 = 1.2/\log(X_0)$, then X_2 is calculated using $X_2 = 1.2/\log(X_1)$ and the process goes on.....

Finally we find the value of X for which $x = 1.2/\log(x)$, and that is the point of convergence of the equation $f(x) = x\log(x) - 1.2$.

*/

```
#include <stdio.h>
#include <stdlib.h>
#include <math.h>
```

```
void log_eq(double guess); //Function prototypes
```

```
int main(int argc, char **argv)
{
    if(argc != 2)
    {
        fprintf(stderr, "USAGE: %s <guess>\n", argv[0]);
        exit (0);
    }
    double guess;

    guess = atof(argv[1]);
    log_eq(guess); //Invoking the function
    exit (0);
}
```

```
// $X_{k+1} = 1.2/\log(X_k)$ 
```

```
void log_eq(double guess)
```

```
{
    double x, root; //x is  $x_k$ 
    int i = 1; //To record number of iterations

    printf("F(x) =  $x\log(x) - 1.2$ \n");
    x = guess;

    //Loop infinitely
    while(1)
    {
        //printf("Checking: %lf\n", x);
        root = 1.2/log10(x); //Substitute the values into the equation Here  $X_{k+1}$  is root And  $X_k$  is x
        if(root == x) //If loop converges, then break out of the loop
        {
            printf("After %d iteration root %lf found.\n", i, root);
            break;
        }
        //If the loop goes infinitely, break after 100000 iterations
        if(i > 100000)
        {
            printf("Root of F(x) might be around %lf\n", root);
            exit (0);
        }
        x = root; //Update  $X_k$ 
        i++;
    }
    return;
}
```