

/*To find the roots of the equation $f(x) = 0$ by successive approximations, we write it in the form $x = p(x)$. The roots of $f(x) = 0$ are the same as the points of intersection of the straight line $y = x$ and the curve representing $y = p(x)$.

Let $X = X_0$ be an initial approximation of the desired root, then the first approximation x_1 is given by $X_1 = p(X_0)$. Now, treating x_1 as the initial value, the second approximation is $X_2 = p(X_1)$. Proceeding in this way the n th approximation is given by $X_n = p(X_{n-1})$

The equation $X_{k+1} = (1 + \cos(X_k))/3$ is used to find the roots of the equation $F(x) = 1 + \cos(x) - 3x$.

In this method we use X_0 as initial value to find X_1 using $X_1 = (1 + \cos(X_0))/3$, then X_2 is calculated using $X_2 = (1 + \cos(x))/3$ and the process goes on.....

Finally we find the value of X for which $x = (1 + \cos(x))/3$, and that is the point of convergence of the equation $F(x) = 1 + \cos(x) - 3x$.

*/

```
#include <stdio.h>
```

```
#include <stdlib.h>
```

```
#include <math.h>
```

```
void cos_eq(double guess);
```

```
int main(int argc, char **argv)
```

```
{
    if(argc != 2)
    {
        printf("USAGE: %s <guess>\n", argv[0]);
        exit (0);
    }
    float guess;
```

```
    guess = atof(argv[1]);
    cos_eq(guess);
```

```
    exit (0);
}
```

```
//Xk+1 = (1 + cos(Xk))/3
```

```
void cos_eq(double guess)
```

```
{
    int i = 1; //To record the number of iterations
    double root, x; //x is Xk and root is Xk+1
    x = guess; //Initializing Xk with guess

    printf("F(x) = 1 + cos(x) - 3x.\n");
    //Loop infinitely
    while(1)
    {
        //printf("checking: %f\n", x);
        root = (1 + cos(x))/3; //Substitute the values in the equation
        if(root == x) //If the Root converges, then break out
        {
            printf("After %d iterations root %f found\n", i, root/100000000);
            break;
        }
        //If loop goes infinitely, then break after 100000 iterations
        if(i > 100000)
        {
            printf("Root of F(x) might be around %lf\n", root);
            exit (0);
        }
        x = root;
        i++;
    }
    return;
}
```