

1. If a qubit is in the state $\begin{bmatrix} 1 \\ 0 \end{bmatrix}$, what is the result of applying the Hadamard gate to it?

- a. $\begin{bmatrix} + \\ \end{bmatrix}$
- b. $\begin{bmatrix} - \\ \end{bmatrix}$
- c. $\begin{bmatrix} - & + \\ \end{bmatrix}$
- d. $\begin{bmatrix} - \\ + \\ \end{bmatrix}$
- e. $\begin{bmatrix} 0 \\ 0 \\ \end{bmatrix}$

2. Is the tensor product of $\begin{bmatrix} 0 \\ 1 \end{bmatrix}$ and $\begin{bmatrix} 0 \\ 1 \end{bmatrix}$ the same as the tensor product of $\begin{bmatrix} 0 \\ 1 \end{bmatrix}$ and $\begin{bmatrix} 1 \\ 0 \end{bmatrix}$?

- a. Yes, because the qubits are the same.
- b. No, because the qubits are different.
- c. No, because the qubits are in a different state.
- d. Yes, because even though the qubits are different, they will give the same result.
- e. No, because this is an entangled state and the tensor product cannot be used here.

3. What is the tensor product of these two qubit states $\begin{bmatrix} \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \end{bmatrix}$ and $\begin{bmatrix} \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \end{bmatrix}$?

- a. $\frac{1}{\sqrt{2}} \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$
- b. $\frac{1}{2} \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$
- c. $\frac{1}{4} \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$
- d. $\begin{bmatrix} 1 \\ 0 \\ 1 \\ 0 \end{bmatrix}$

- e. These two states are entangled, so we cannot represent them using tensor products.

4. What is the probability of measuring $|01\rangle$ in this quantum system: $\begin{bmatrix} \frac{\sqrt{3}}{2} \\ 0 \\ \frac{1}{2} \\ 0 \end{bmatrix}$?

- a. $\frac{\sqrt{3}}{2}$
- b. $\frac{3}{4}$
- c. 0
- d. $\frac{1}{2}$
- e. $\frac{3}{4}$

5. What is the probability of measuring $|00\rangle$ in this quantum system:

$$\sqrt{\frac{1}{3}}|00\rangle + \sqrt{\frac{1}{6}}|01\rangle + \sqrt{\frac{1}{3}}|10\rangle + \sqrt{\frac{1}{6}}|11\rangle?$$

- a. $\sqrt{\frac{1}{3}}$
- b. $\frac{1}{3}$
- c. $\sqrt{\frac{1}{6}}$
- d. $\frac{1}{6}$
- e. $\frac{2}{3}$

6. What is the tensor product of these two qubit states: $\begin{bmatrix} \sqrt{\frac{2}{3}} \\ \sqrt{\frac{1}{3}} \end{bmatrix}$ and $\begin{bmatrix} \sqrt{\frac{1}{3}} \\ \sqrt{\frac{2}{3}} \end{bmatrix}$?

a.
$$\begin{bmatrix} \sqrt{\frac{2}{3}} \\ \frac{2}{3} \\ \frac{1}{3} \\ \frac{2}{3} \\ \frac{1}{3} \end{bmatrix}$$

b.
$$\begin{bmatrix} \sqrt{\frac{\sqrt{2}}{3}} \\ \frac{1}{3} \\ \frac{2}{3} \\ \frac{2}{3} \\ \frac{\sqrt{2}}{3} \end{bmatrix}$$

c.
$$\begin{bmatrix} \sqrt{\frac{2}{9}} \\ \frac{4}{9} \\ \frac{1}{9} \\ \frac{2}{9} \\ \frac{2}{9} \end{bmatrix}$$

d.
$$\begin{bmatrix} \frac{\sqrt{2}}{3} \\ \frac{2}{3} \\ \frac{2}{3} \\ \frac{1}{3} \\ \frac{2}{3} \\ \frac{\sqrt{2}}{3} \end{bmatrix}$$

e. These two states are entangled, so we cannot represent them using tensor products.

7. Given the quantum state $\begin{bmatrix} 0 \\ \frac{1}{\sqrt{2}} \\ 0 \\ -\frac{1}{\sqrt{2}} \end{bmatrix}$, if we apply the X gate to the second qubit, what is the new state?

a. $\begin{bmatrix} \frac{1}{\sqrt{2}} \\ 0 \\ \frac{-1}{\sqrt{2}} \\ 0 \end{bmatrix}$

b. $\begin{bmatrix} \frac{1}{\sqrt{2}} \\ 0 \\ 0 \\ \frac{-1}{\sqrt{2}} \end{bmatrix}$

c. $\begin{bmatrix} \frac{1}{\sqrt{2}} \\ 0 \\ 0 \\ \frac{1}{\sqrt{2}} \end{bmatrix}$

d. $\begin{bmatrix} 0 \\ 0 \\ -1 \\ 0 \end{bmatrix}$

e. $\begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \end{bmatrix}$

8. Consider the quantum state $|101\rangle$. If we apply the CNOT gate to the first (leftmost) qubit (control) and the second (middle) qubit (target), what is the resulting state?

a. $|101\rangle$

b. $|111\rangle$

c. $|100\rangle$

d. $|001\rangle$

e. $|110\rangle$

9. If a collection of qubits are in the state below, how many qubits are there?

[illegible]

- c. 5