

1. The recurrence relation is as follows

$$T(b, n, k) = \begin{cases} 0 & \text{if } n=0 \text{ or } b < 0 \\ 1 & \text{if } b=0 \\ \sum_{i=0}^k T(b-i, n-1, k) & \text{if } b \geq i \end{cases}$$

2. The base cases are -

If number of stacks (n) is 0 or number of robots(b) less than 0, there are no ways to arrange, hence return 0

If the number of robots (b) is 0, return 1, which is an empty set.

3. Time complexity = $O(b \cdot n \cdot k)$, Space Complexity = $O(b, n, k)$

4. Pseudocode for iterative approach -

Input: b,n,k

Algorithm waysToDistribute:

Create a matrix with zeroes of size $b \times n$

mat=[]

for i = 0 to n do

 mat[i][0]=1

end

for i = 1 to n do

 For j = 1 to b do

 if k ==1 then

 mat[i][j] = mat[i-1][j-1]

 end

 else if j == k then

 mat[i][j] = mat[i+j-1][j]

 end

 else if j>=k then

 mat[i][j] = mat[i+j-2][j-1] - mat[i-2][j-2]

 end

 end

end

return mat[n][b]

5. Time complexity for iterative = $O(b \cdot n \cdot k)$, Space is size of matrix, $O(b \cdot n)$