

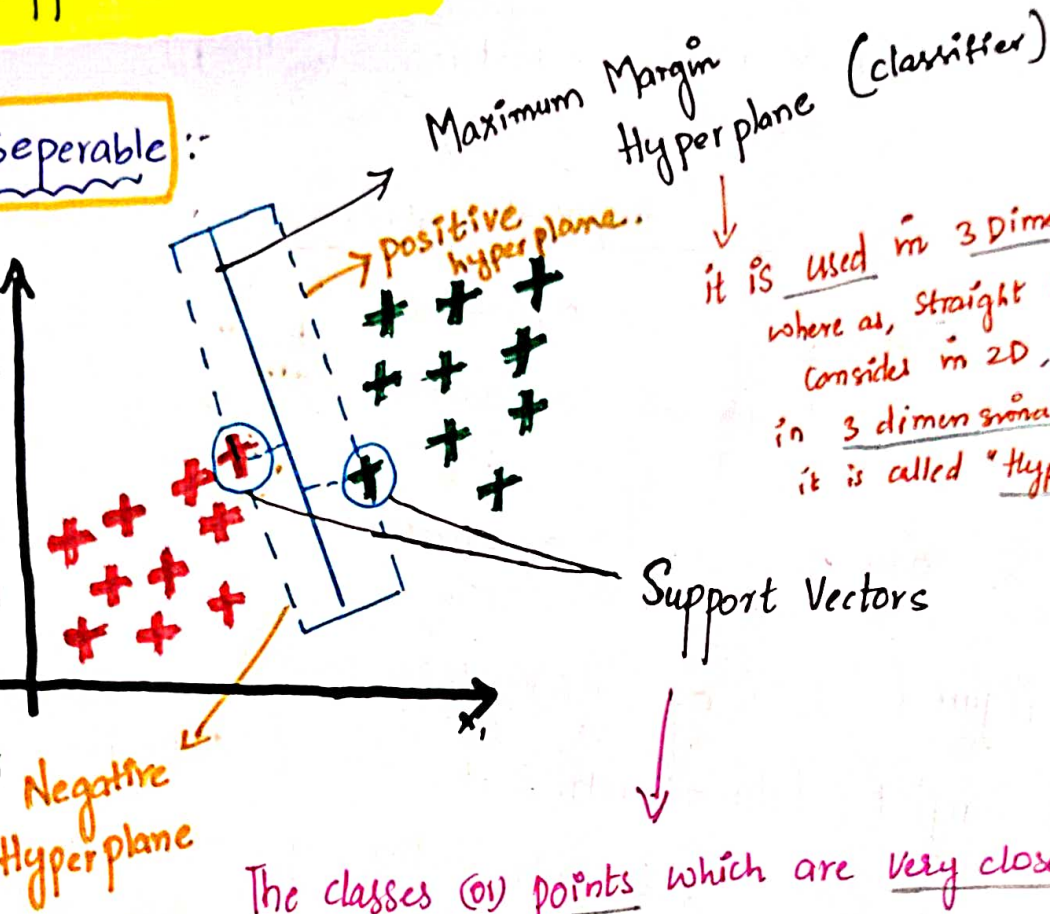
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# SVM (Support Vector Machines)

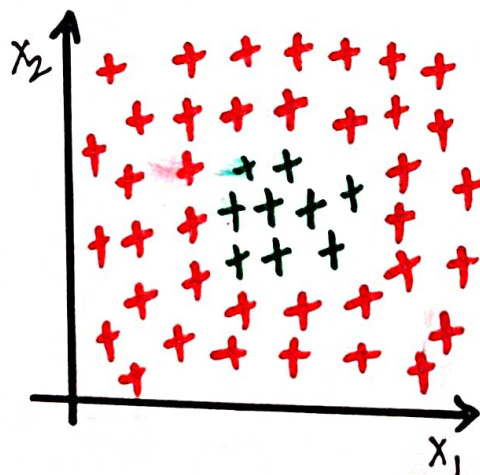
## \* Linear Seperable :-

seperating  
The classes  
by using a  
straight line  
is called "Linear  
SVM"

it identify  
Best fit line by  
"Maximum  
margin classifier"



## \* Non-linear seperable (or) Kernel SVM

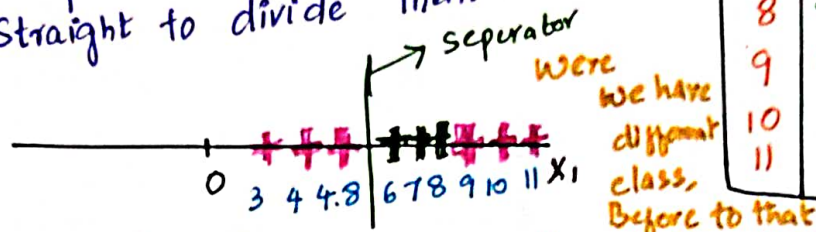


\* In This situation, we use  
"Non-linear SVM"  
(or) Kernel SVM

# Non-linear

Ex:- Mapping to a higher Dimension

# These points are not linearly separable. we can't draw a straight line to divide them.



x	y
3	Pink
4	Pink
4.8	Pink
6	green
7	green
8	green
9	Pink
10	Pink
11	Pink

\* Earlier, it is degree of 1  
Now, we convert it into "quadratic Equation" and we separate the data, By writing single condition

So, we convert Every Data point to

$$f = x - 5$$

Why  $f = (x-5)$ ?

Because, we identify "separator".

Ex: 9 → separator  
if it is 9,  $f = 9 - 9$

$$\begin{aligned} f &= 3 - 5 = -2 \\ f &= 4 - 5 = -1 \\ f &= 4.8 - 5 = -0.2 \end{aligned}$$

$$\begin{aligned} f &= 6 - 5 = 1 \\ f &= 7 - 5 = 2 \\ f &= 8 - 5 = 3 \end{aligned}$$

$$\begin{aligned} f &= 9 - 5 = 4 \\ f &= 10 - 5 = 5 \\ f &= 11 - 5 = 6 \end{aligned}$$



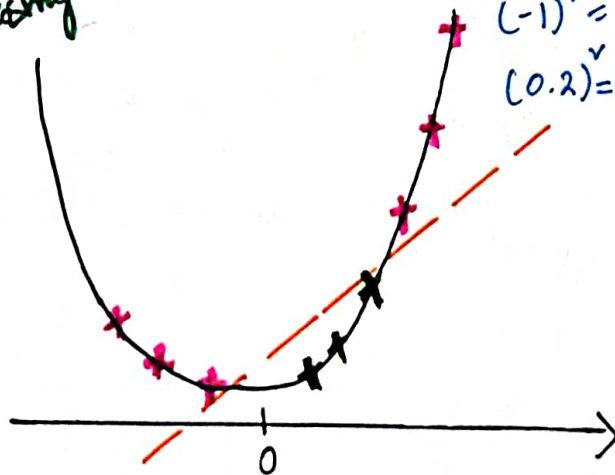
Next, we square the data points.

$$f = (x - 5)^2$$

Here, we are increasing "Higher" dimension.

$$\begin{aligned} (-2)^2 &= 4 \\ (-1)^2 &= 1 \\ (0.2)^2 &= 0.04 \end{aligned}$$

$$\begin{aligned} 1^2 &= 1 \\ 2^2 &= 4 \\ 3^2 &= 9 \end{aligned} \quad \begin{aligned} 4^2 &= 16 \\ 5^2 &= 25 \\ 6^2 &= 36 \end{aligned}$$



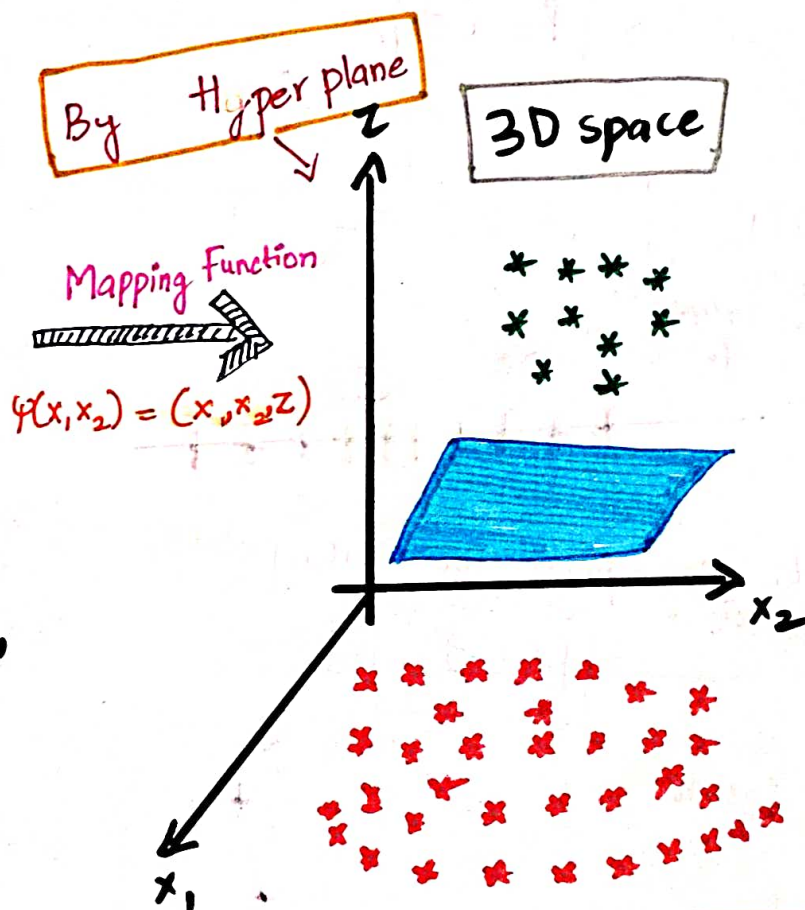
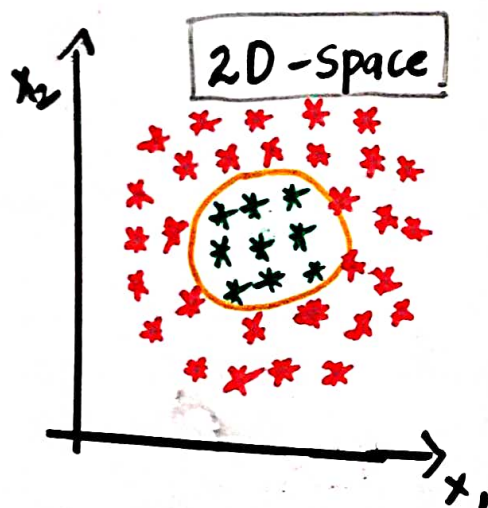
Now, we can separate them by "Linear" line



By Table

x	y	x-5	(x-5) <sup>2</sup>
3	Pink	-2	4
4	Pink	-1	1
4.8	Pink	-0.2	0.04
6	green	1	1
7	green	2	4
8	green	3	9
9	Pink	4	16
10	Pink	5	25
11	Pink	6	36

⇒ SVM-Kernal :-



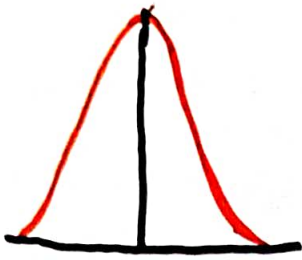
Mapping Function  
 $\varphi(x_1, x_2) = (x_1, x_2, z)$

\* Mapping to higher dimensional space can be Highly Compute  
intensive. More RAM needed.

# \* Types of Kernel functions

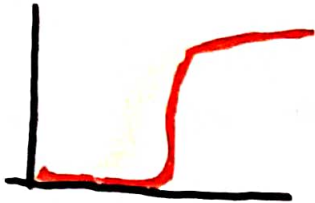
Radial Basis function

∴ Shape of Kernel: R.B.F



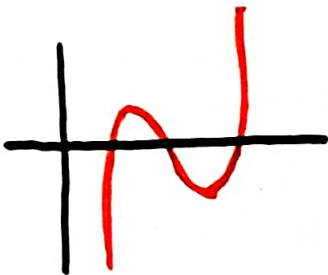
Gaussian RBF Kernel

$$k(\vec{x}, \vec{l}) = e^{-\frac{\|\vec{x} - \vec{l}\|^2}{2\sigma^2}}$$



Sigmoid Kernel

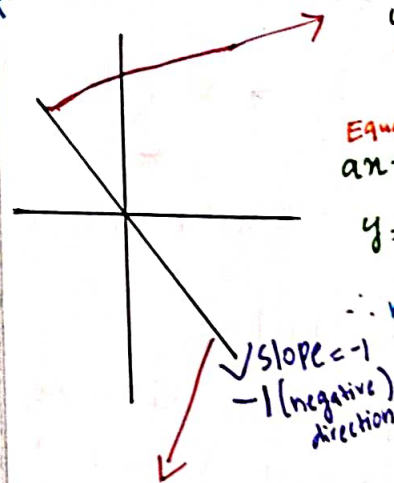
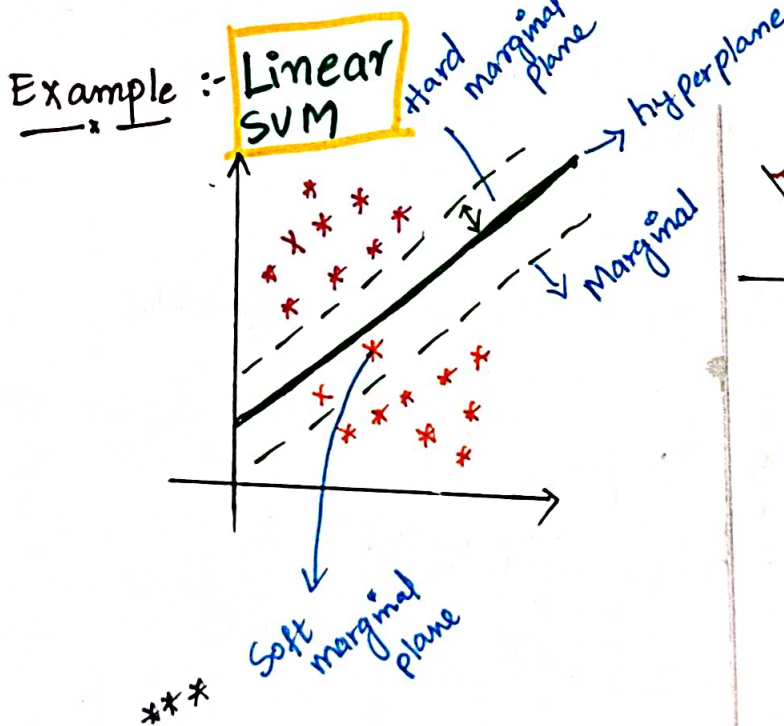
$$k(x, y) = \tanh(\gamma \cdot x^T y + r)$$



Polynomial Kernel

$$k(x, y) = (\gamma \cdot x^T y + r)^d, \gamma > 0$$

apply Higher The "degree"



$$y = mx + c$$

slope ↑ intercept ↑

Equation For straight line  
 $ax + by + c = 0$  } same

$$y = -\frac{c}{b} - \frac{a}{b}x$$

∴  $m = -\frac{a}{b}, c = -\frac{c}{b}$

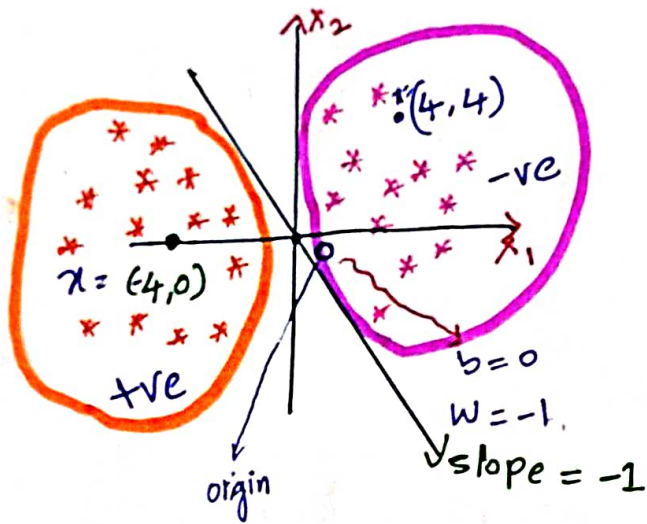
$$y = mx + c$$

written as

$$y = w_1x + w_2x + w_3x + \dots + c$$

$$y = W^T x + b$$

→ Transpose



Equation :-  $y = W^T x + b$

$$y = \begin{bmatrix} -1 \\ 0 \end{bmatrix} \begin{bmatrix} 4 \\ 0 \end{bmatrix}$$

By multiplication

$$= 4 \Rightarrow (+ve) \text{ value.}$$

Any point under the line is Positive value.

New Data point (4,4)

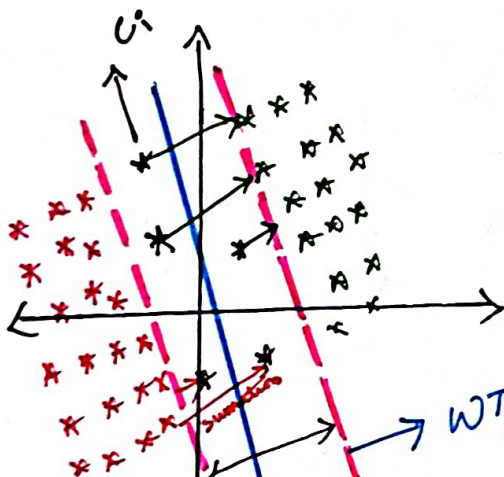
$$y = W^T x + b$$

$$y = \begin{bmatrix} -1 \\ 0 \end{bmatrix} \begin{bmatrix} 4 \\ 4 \end{bmatrix}$$

$$= -4 + 0 = -4$$

Any point above the line is negative value.

⇒ Marginal plane



$$W^T x_2 + b = -1[k]$$

$$W^T x + b = 0$$

$$W^T x_1 + b = +1[k]$$

Our Aim should increase distance, to Perform model well Maximize

$$W^T x_1 + b = +1$$

$$W^T x_2 + b = -1$$

$$\underline{W^T(x_1 - x_2) = 2} \quad (\text{difference between above \& below plane})$$

Vectors + magnitude

$$\downarrow$$

$$W$$

$$\downarrow$$

$$\|W\|$$

$$\frac{W^T(x_1 - x_2)}{\|W\|} = \frac{2}{\|W\|}$$



Maximize  $(w, b)$   $\frac{2}{\|w\|}$  <sup>Maximize Cost function</sup> (Marginal plane will be bigger)

Such that,

$$y_i \begin{cases} +1 & w^T x + b \geq 1 \\ -1 & w^T x + b \leq -1 \end{cases}$$

$y_i * (w^T x_i + b) \geq 1$

↓  
For Correct point

Condition

$(w^T x + b)$  greater than  $= 1 = +1$   
 $(w^T x + b)$  lesser than  $= -1 = -1$

Maximize  $(w, b) = \frac{2}{\|w\|} \Rightarrow$  Both are Equal  $\Rightarrow$  Minimize  $(w, b) = \frac{\|w\|}{2}$

for [SVM] Parameter changes.

Min  $(w, b) \frac{\|w\|}{2} + c_i \sum_{i=1}^n \{ \}$

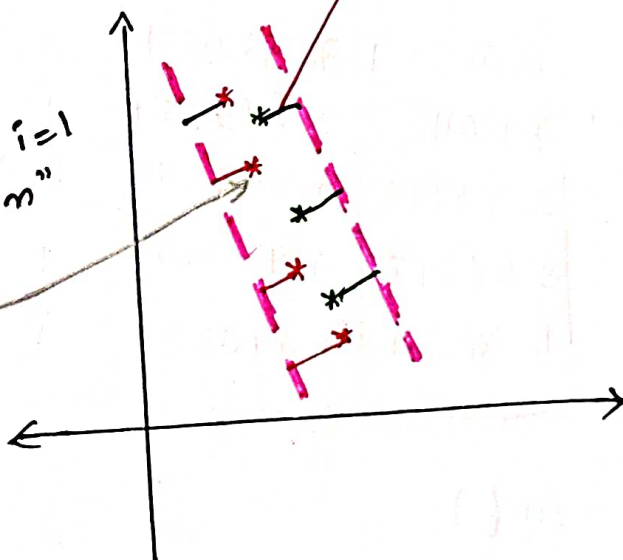
"Hypertuning Parameter"

Eta (Summation of the distance of the wrong data points)

How many wrong prediction (or) Errors, we can Have

Sumation  $i=1$  to "n"

Errors



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29/9/2019

## CODE :-

Data :-

The data shown here simulates a medical study in which infected with a virus were given various doses of two medicines and then checked 2 weeks later to see if they were still infected. Given this data, Our goal is to create a

classification model than predict (given two dosage measurements if they mouse will still be infected with virus).

# load data, with import libraries.

```
# df = pd.read_csv("mouse_viral_study.csv")
```

```
# df.head()
```

Out :

med_1_mL	Med_2_mL	Virus_Present
6.508231	8.532531	0
4.126116	3.073459	1
6.427870	6.369758	0
3.672953	4.905215	1
1.580321	2.440562	1

```
# df.info()
```

Out : Range Index 400 entries 0 to 399

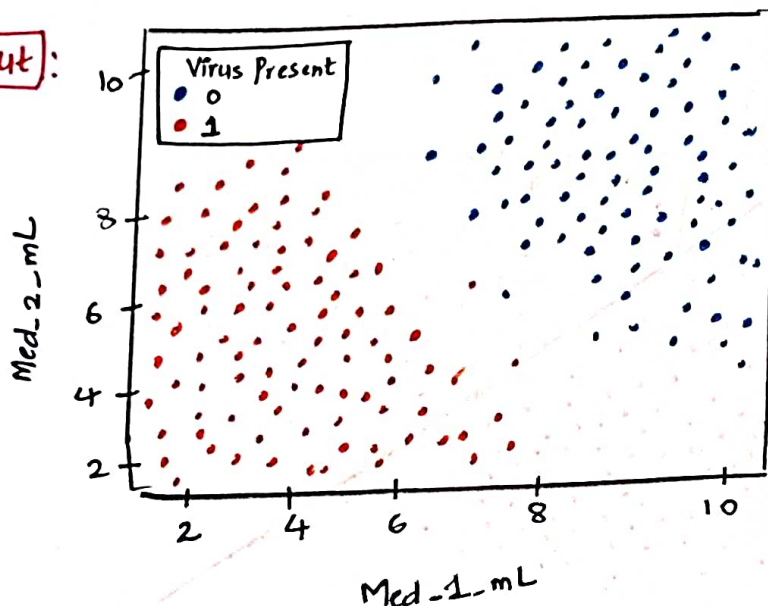
0	Med_1_mL	400 non null	Float64
1	Med_2_mL	400 non null	Float64
2	Virus_Present	400 non null	int64

## EDA

```
# sns.scatterplot (x = "Med-1-mL", y = "Med-2-mL", hue = "Virus Present", data = df)
```

```
# plt.show()
```

Out:



## X & Y

```
# x = df.drop("Virus Present", axis=1)
```

```
# y = df["Virus Present"]
```

## MODELLING

```
from sklearn.svm import SVC
```

```
# model = SVC(kernel = "linear")
```

```
# model.fit(x, y)
```

```
Out: SVC(kernel = "linear")
```

30/4/22  
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## Seperating Hyper plane

```
#sns.scatterplot(x = "Med_1-mL", y = "Med_2-mL", hue = "Virus Pres.",  
                palette = "seismic", data = df)
```

# we want to somehow automatically create a separating hyperplane  
(a line in 2D)

```
# x = np.linspace(0, 10, 100)
```

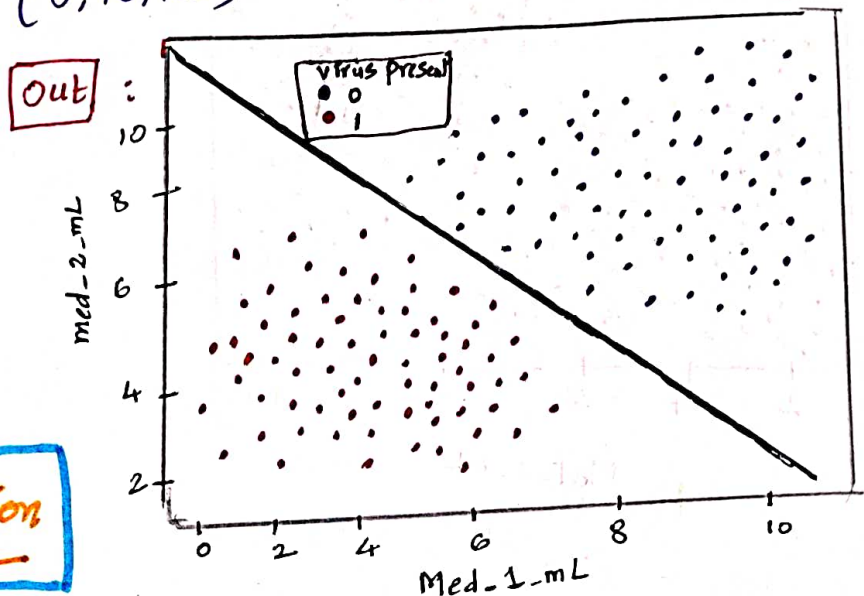
```
# m = -1
```

```
# b = 11
```

```
# y = m*x + b
```

```
# plt.plot(x, y, "k")
```

# user defined function



```
# def plot_svm_boundary(model, x, y):
```

```
    x = x.values
```

```
    y = y.values
```

# scatter plot

```
plt.scatter(x[:, 0], x[:, 1], c = y, s = 30,  
           cmap = "seismic")
```

# plot the decision function.

```
ax = plt.gca()
```

```
xlim = ax.get_xlim()
```

```
ylim = ax.get_ylim()
```

# Creating grid to Evaluate model.

$xx = \text{np.linspace}(x\text{lim}[0], x\text{lim}[1], 30)$

$yy = \text{np.linspace}(y\text{lim}[0], y\text{lim}[1], 30)$

$YY, XX = \text{np.meshgrid}(yy, xx)$

$xy = \text{np.vstack}([xx.\text{ravel}(), YY.\text{ravel}()]).T$

$Z = \text{model.decision\_function}(xy).\text{reshape}(xx.\text{shape})$

# plot decision boundary and margins.

$\text{ax.contour}(XX, YY, Z, \text{colors} = "k", \text{Levels} = [-1, 0, 1])$   
 $\alpha = 0.5, \text{line styles} = ["--", "-", "--"]$

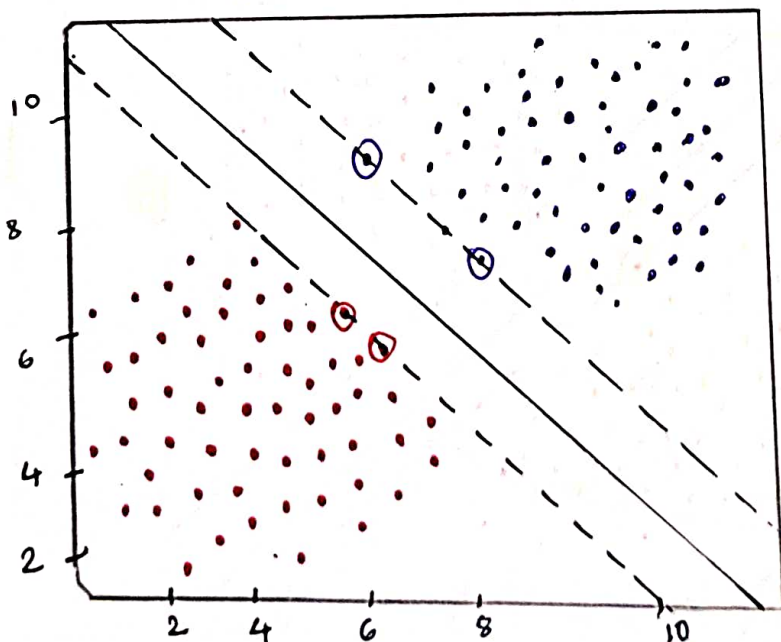
# plot support vectors.

$\text{ax.scatter}(\text{model.support\_vectors}[:, 0], \text{model.support\_vectors}[:, 1], s = 100, \text{linewidth} = 1, \text{facecolors} = "none", \text{edge colors} = "k")$

$\text{plt.show}()$

# plot\_svm\_boundary(model, x, y)

Out:



# Our goal with SVM is to create the best separating hyperplane with Maximum margin classifier.

# In 2 dimensions, The hyperplane is simply a line.  
In 3 dimensional  $\rightarrow$  plane

## Hyper Parameters

# C :- Regularization parameter.

# The strength of the regularization is inversely proportional to 'C'. Must be strictly positive. The penalty is a

Squared L2 penalty.  $C \uparrow$  (Less Sensitivity).

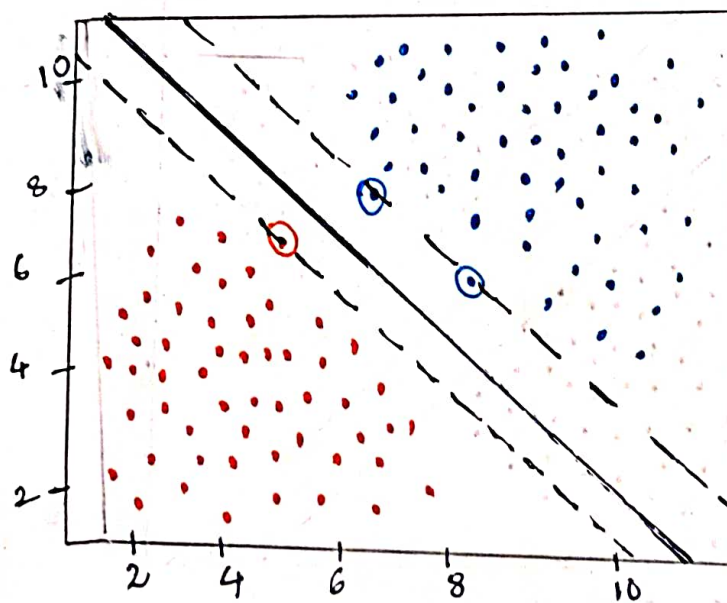
\*  $C \downarrow$  (# lower The "C" value - in correct answer  
# Higher The "C" value - Lesser The missclassification

# model = SVC (kernel = "Linear", C = 1000)

# model.fit(x, y)

# plot\_svm\_boundary(model, x, y)

Out :-



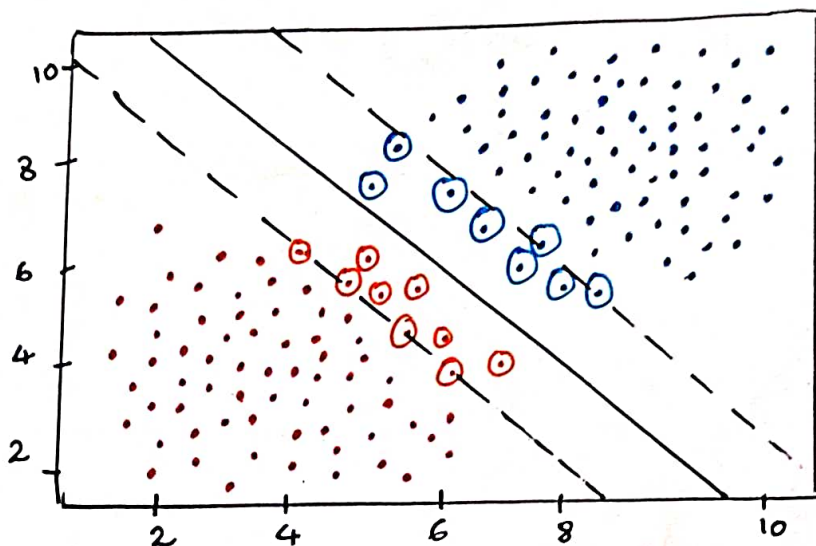


```
# model = SVC (kernel = "linear", C = 0.05)
```

```
# model.fit(x,y)
```

```
# plot_svm(model, x,y)  
boundary
```

out :



# Kernel

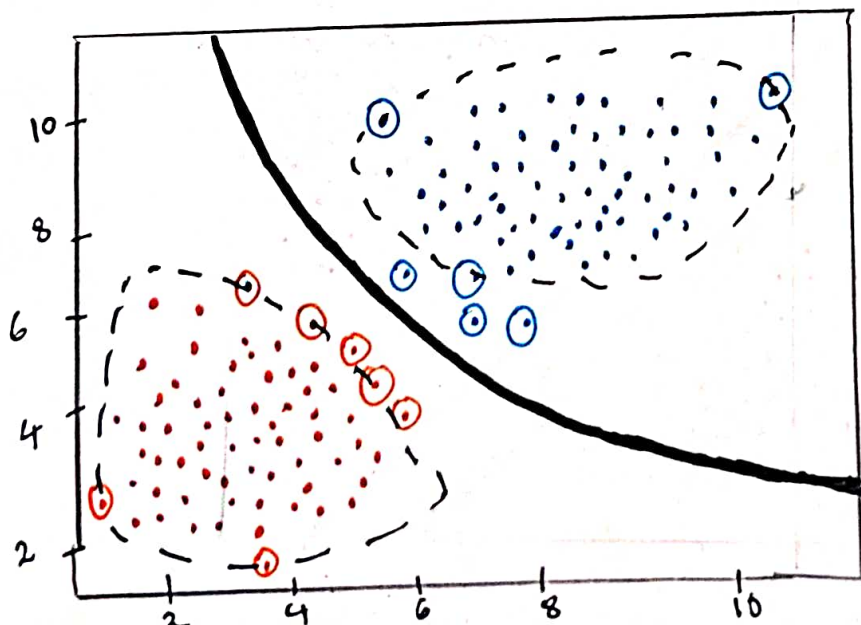
1. RBF

```
# model = SVM (kernel = "rbf", C = 1)
```

```
# model.fit(x,y)
```

```
# plot_svm_boundary (model, x,y)
```

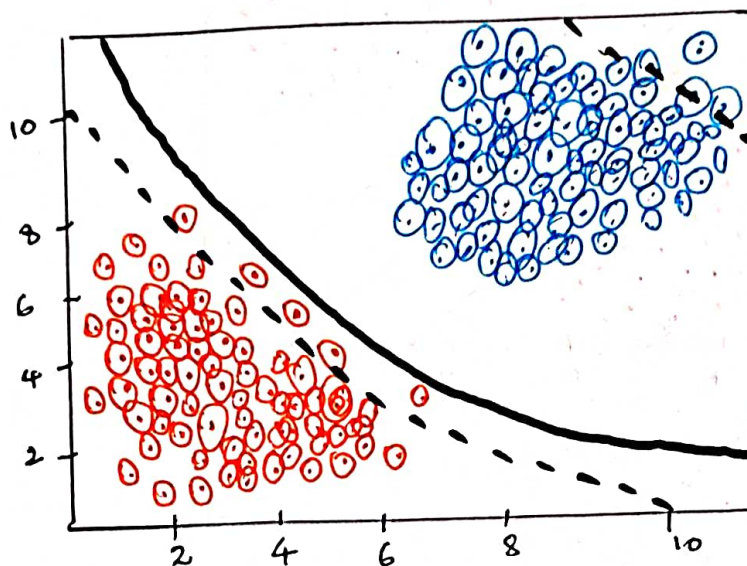
out :



## 2. Sigmoid

```
# model = SVC(kernel = "sigmoid")  
# model.fit(x,y)  
# plot_svm_boundary(model, x,y)
```

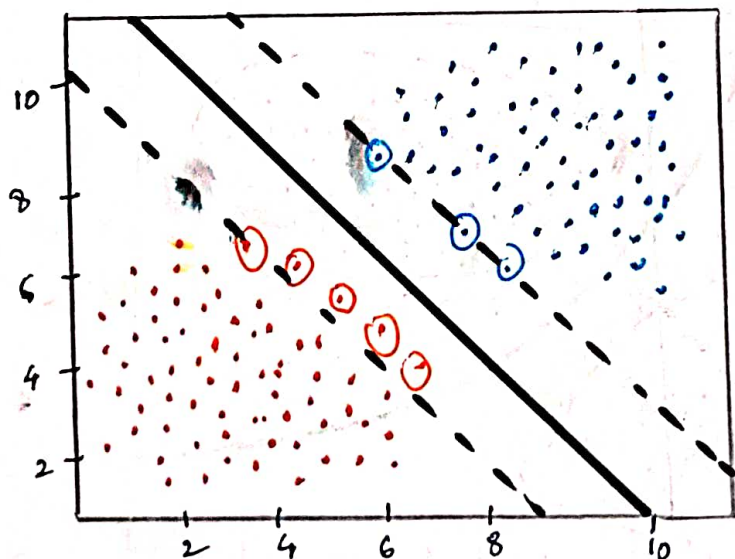
Out:



## 3. Polynomial

```
# model = SVC(kernel = "poly", C=1, degree=1)  
# model.fit(x,y)  
# plot_svm_boundary(model, x,y)
```

Out:



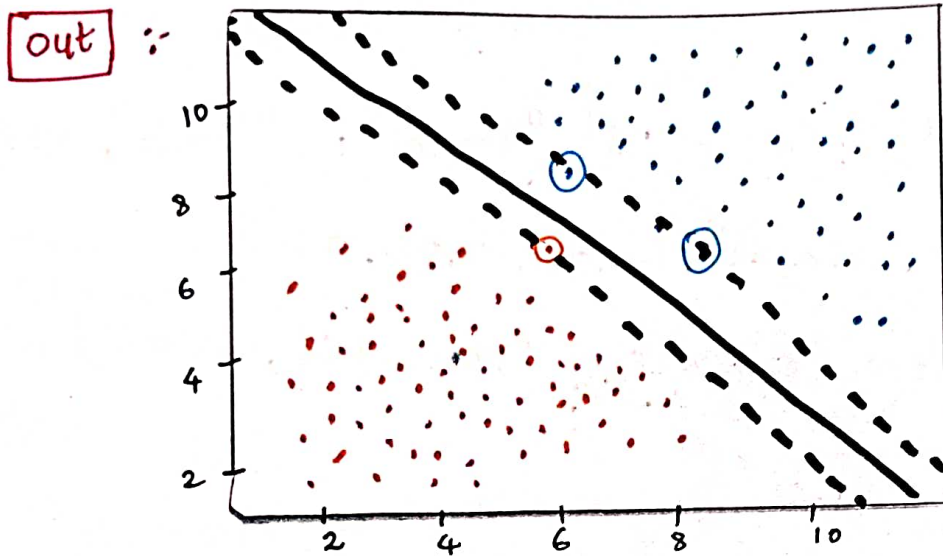
"Linear"  
Both are same.

```
# model = SVC (kernel = "Poly" , c = 1 , degree = 2)
```

"Quadratic" curve.

```
# model . fit (x,y)
```

```
# plot - svm - boundary (model , x,y)
```



# gamma

gamma :- { scale , auto } or float

# Default = "scale" Kernel Coefficient for "rbf", "poly" & "sigmoid"

"gamma = scale"  $\Rightarrow \frac{1}{\text{num. of feature}} \times x. \text{Var}(C)$

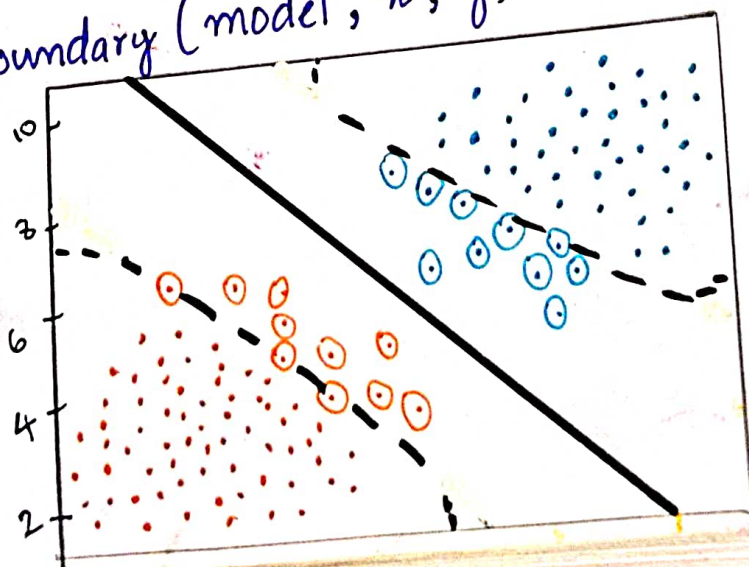
"gamma = auto"  $\Rightarrow \frac{1}{n - \text{features}}$

```
# model = SVC (kernel = "rbf" , c = 1 , gamma = 0.01)
```

```
# model . fit (x,y)
```

```
# plot - svm - boundary (model , x , y)
```

out :





## Hyper parameter Tuning

```
from sklearn.model_selection import GridSearchCV
```

```
# estimator = SVC()
```

```
# param_grid = {"c": [0, 0.01, 0.1], "kernel": ["linear", "rbf"],  
               , "gamma": [0.01, 0.02, 0.1]}
```

```
# grid = GridSearchCV(estimator, param_grid, cv=5)
```

```
# grid.fit(x, y)
```

```
[out]: GridSearchCV(cv=5, estimator=SVC(), param_grid=  
        {"c": [0, 0.01, 0.1], "kernel": ["linear", "rbf"],  
         "gamma": [0.01, 0.02, 0.1]})
```

```
# grid.best_params_
```

```
[out]: {"c": 0.01, "gamma": 0.01, "kernel": "rbf"}
```

```
# grid.best_score_
```

```
[out]: 1.0
```

↓  
If we don't write  
gamma,

kernel = "linear"

gives best prediction  
and accuracy.

Only for this problem

## train test Split

```
from sklearn.model_selection import train_test_split  
# x_train, x_test, y_train, y_test = train_test_split(x, y,  
test_size = 0.25, random_state = 29)
```

## Scaling

```
from sklearn.preprocessing import StandardScaler
```

```
# sc = StandardScaler()
```

```
# x_train = sc.fit_transform(x_train)
```

```
# x_test = sc.fit_transform(x_test)
```

## model

```
# model = SVC(Kernel = "rbf", C = 0.01, gamma = 0.01)
```

```
# model.fit(x_train, y_train)
```

```
out SVC [C = 0.01, gamma = 0.01, kernel = "Linear"]
```

## Prediction

```
# y_pred_train = model.predict(x_train)
```

```
# y_pred_test = model.predict(x_test)
```

accuracy

from sklearn.metrics import accuracy\_score

# accuracy\_score (y-test, ypred-test)

Out: 1.0

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5:00 pm.

Que:- What is "model selection"?

Ans:- Identify The best Algorithm with best Hyperparameters  
By applying hyperparameter "tunning"