Dynamic Analysis of a Series RLC Circuit

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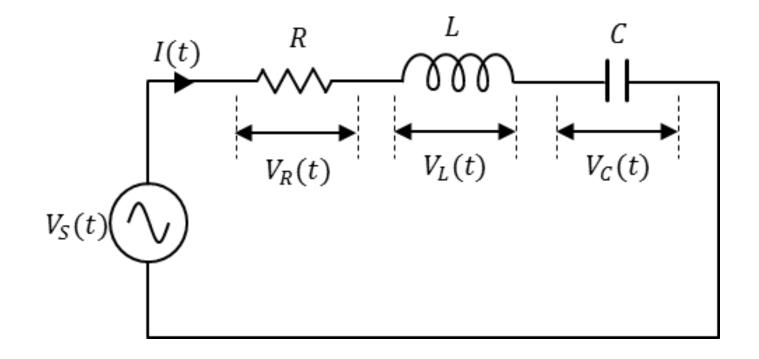
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- Series RLC Circuit, Damped Oscillation, Frequency response

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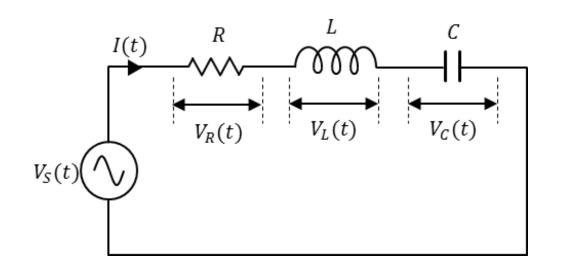
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설계 목적



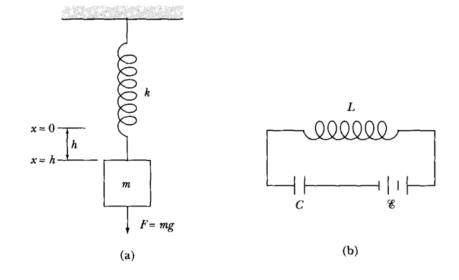
직렬 RLC 회로에서 V_C 분석 단순화 및 시각화 1. 감쇠비, Q 등 parameter 분석 후 damped oscillation 구분 2. 시간에 따른 V_C 그래프와 주파수 응답 plot

기본 이론 - 직렬 RLC 회로



직렬 RLC 회로에 Kirchhoff's law 적용

$$L\ddot{q}+R\dot{q}+rac{1}{C}q=V_{
m in}(t), \quad V_C=rac{q}{C}$$
 $\ddot{y}+2\zeta\omega_0\,\dot{y}+\omega_0^2y=(입력/상수)$



cf) damped oscillation model

 TABLE 3-1
 Analogous Mechanical and Electrical Quantities

Mechanical		Electrical	
x	Displacement	q	Charge
ż	Velocity	$\dot{q} = I$	Current
m	Mass	L	Inductance
b	Damping resistance	R	Resistance
1/k	Mechanical compliance	\boldsymbol{c}	Capacitance
\boldsymbol{F}	Amplitude of impressed force	${\cal E}$	Amplitude of impressed emf

$$L\ddot{q}+R\dot{q}+rac{1}{C}q=V_{
m in}(t), \quad V_C=rac{q}{C}$$

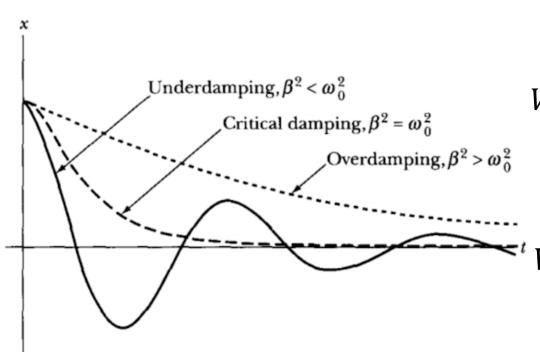
1) 직류 전원일 때 (V_{in} 은 상수)

표준형:
$$\ddot{y}+2\zeta\omega_0\,\dot{y}+\omega_0^2y=(입력/상수)$$

$$\omega_0 = \frac{1}{\sqrt{LC}}$$
 $\zeta = \frac{R}{2}\sqrt{\frac{L}{C}}$ $Q = \frac{1}{2\zeta} = \frac{1}{R}\sqrt{\frac{L}{C}}$ (에너지 저장 효율, 공진 특성, 대역폭과 반비례 관계)

미분 방정식: $s^2 + 2\zeta\omega_0 s + \omega_0^2 = 0$

$$s_{1,2} = \begin{cases} -\zeta \omega_0 \pm j \omega_d, & (\zeta < 1, Underdamping) \\ -\omega_0 \ (중군), & (\zeta = 1, Critical\ damping) \\ -\omega_0 \ (\zeta \pm \sqrt{\zeta^2 - 1}, & (\zeta > 1, Overdamping) \end{cases}$$



$$V_C(0) = 0$$
 (방전) $V_C(\infty) = V_{in}$ (충전)

- Underdamping

$$V_C(t) = V_{\rm in} \left[1 - \frac{1}{\sqrt{1 - \zeta^2}} e^{-\zeta \omega_0 t} \sin(\omega_d t + \arccos \zeta) \right]$$

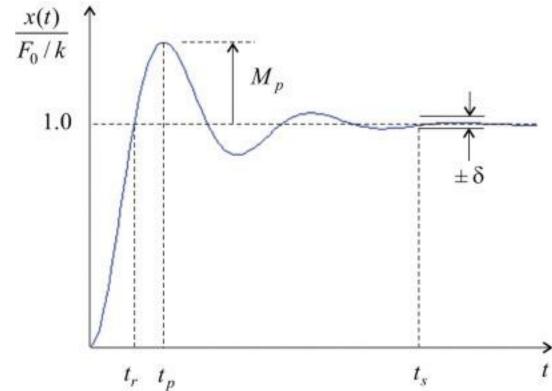
- Critical damping

$$V_C(t) = V_{\text{in}}[1 - \{1 + \omega_0 t\}e^{-\omega_0 t}]$$

- Overdamping

$$V_C(t) = V_{\text{in}} \left[1 - \frac{s_2 e^{s_1 t} - s_1 e^{s_2 t}}{s_2 - s_1} \right]$$

Underdamped Oscillation의 특성 지표



- T_s : 정착 시간 응답 곡선이 수렴하는 값의 오차 범위에 들어가는 데 걸리는 시간

$$T_s = -\frac{1}{\zeta \omega_n} \ln \delta \sqrt{1 - \zeta^2} = \frac{4}{\zeta \omega_n}$$
, $\delta = 0.02$

- M_D: 최대 오버 슈트

🚺 응답 곡선 최대 봉우리에서 1을 뺀 값

$$M_p = \exp\left(-\frac{\pi\zeta}{\sqrt{1-\zeta^2}}\right)$$

$$L\ddot{q}+R\dot{q}+rac{1}{C}q=V_{
m in}(t), \quad V_C=rac{q}{C}$$

2) 교류 전원일 때 (V_{in} 은 AC+DC)

표준형:
$$\ddot{y} + 2\zeta\omega_0\dot{y} + \omega_0^2y = V_{in}\sin(\omega t)$$
, $y(t) = V_C(t)$

$$\omega_0 = \frac{1}{\sqrt{LC}}$$
 $\zeta = \frac{R}{2} \sqrt{\frac{L}{C}}$ $Q = \frac{1}{2\zeta} = \frac{1}{R} \sqrt{\frac{L}{C}}$

$$V_C(t) = V_C^{(h)}(t) + V_C^{(p)}(t)$$

 $V_C^{(h)}(t)$ 는 자유응답, complementary function과 유사 (앞서 구함) $V_C^{(p)}(t)$ 는 강제응답, particular solution과 유사

$$V_C(t) = V_C^{(h)}(t) + V_C^{(p)}(t)$$

 $V_{C}^{(p)}(t)$ 는 전달 함수를 이용해 쉽게 구할 수 있음 -> 전달함수는 steady-state 상황에서 페이저 변환을 이용해 계산

임피던스:
$$Z_R=R,\ Z_L=j\omega L,\ Z_C=rac{1}{j\omega C}$$

전달함수: $H(j\omega)=rac{V_C}{V_{in}}=rac{Z_C}{Z_{tot}}=rac{1}{1-j\omega RC-\omega^2 LC}$

$$|H(j\omega)| = \frac{1}{\sqrt{(1-\omega LC)^2 - (\omega RC)^2}} \quad \angle H(j\omega) = \phi = \arctan\left(-\frac{\omega RC}{1-\omega^2 LC}\right)$$

$$\rightarrow V_C^{(p)}(t) = |H(j\omega)|V_{in}\sin(\omega t + \phi)$$

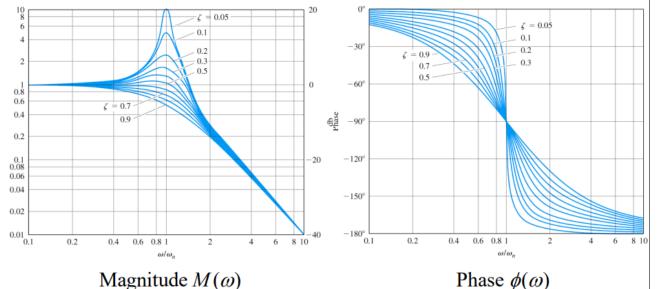
기본 이론 - 주파수 응답

주파수 응답: 신호 주파수의 변화에 따른 회로 동작의 변화, 교류 전원 인가시 필요

전달함수:
$$H(j\omega) = \frac{V_C}{V_{in}} = \frac{Z_C}{Z_{tot}} = \frac{1}{1 - j\omega RC - \omega^2 LC}$$

$$|H(j\omega)| = \frac{1}{\sqrt{(1-\omega LC)^2 - (\omega RC)^2}} \qquad \angle H(j\omega) = \phi = \arctan\left(-\frac{\omega RC}{1-\omega^2 LC}\right)$$

• Frequency response of $G(s) = \frac{1}{(s/\omega_n)^2 + 2\zeta(s/\omega_n) + 1}$



Q가 커질수록 공진주파수 근처에서 진폭 응답 뾰족해짐 위상 응답 기울기 가팔라짐

코드 설명

- 1. DC 입력
 - 핵심 parameter 정의
 - ODE solver와 analytic solution 통해 Vc 계산
 - 출력할 그래프 세부 설정
 - 각각의 oscillation에 대한 출력값 설정
 - 메인 함수를 통해 앞서 정의한 함수 불러오고, plotting
- 2. AC 입력
 - 파라미터, 전달함수, 정의
 - ODE solver 통해 Vc 계산
 - 메인 함수 통해 plotting

코드 설명 - DC 입력

```
import numpy as np
import matplotlib.pyplot as plt
import ipywidgets as widgets
from ipywidgets import link
from IPython.display import display, clear_output, Math
from math import sqrt, pi
from scipy.integrate import solve_ivp
# --- core formulas ---
def omega0(L, C): return 1.0/np.sqrt(L*C)
def zeta(R. L. C): return (R/2.0)*np.sqrt(C/L)
def compute_poles(R, L, C):
    w0, z = omega0(L, C), zeta(R, L, C)
    if z < 1.0:
        wd = w0*np.sqrt(1.0 - z*z)
        return complex(-z*w0, +wd), complex(-z*w0, -wd)
    # z >= 1: real poles
    root = np.sqrt(max(0.0, z*z - 1.0))
    s1 = -w0*(z - root)
    s2 = -w0*(z + root)
    return complex(s1, 0.0), complex(s2, 0.0)
```

```
근을 구함
```

```
def H_jw(R, L, C, w):
   Zc = 1.0/(1j*w*C)
   return Zc / (R + 1j*w*L + Zc) # Vc/Vin
```

ODE solver 통해 Vc 파형 얻음

주어진 꼴을 이용해 Vc 계산

실근, 허근일 때 나눠

전달함수 계산

```
# --- simulations ---
# Simulate RLC step response using ODE solver
def simulate_step_Vc_only(R, L, C, V_step, t_end, n=3000):
    if t_end <= 0: return np.array([]), np.array([])</pre>
    def f(t, x):
        q, i = x
        return [i, (V \text{ step } - R*i - q/C)/L]
    t = np.linspace(0, t_end, n)
    sol = solve_{ivp}(f, [0, t_{end}], [0.0, 0.0], t_{eval=t, max_step=t_{end/max}(n, 1)}
    if not sol.success: return t, np.full_like(t, np.nan)
    return t, sol.y[0] / C # Vc = q/C
```

```
# Analytic solution for RLC step response
def analytic_Vc(Vin, R, L, C, t):
    w0, z = omega0(L, C), zeta(R, L, C)
    if z < 1.0:
        wd = w0*np.sqrt(1.0 - z*z)
        A = 1.0/np.sqrt(1.0 - z*z)
        phi = np.arccos(z)
        return Vin*(1 - A*np.exp(-z*w0*t)*np.sin(wd*t + phi))
    elif abs(z-1.0) \le 1e-12:
        return Vin*(1 - (1 + w0*t)*np.exp(-w0*t))
    else:
        s1 = -w0*(z - np.sqrt(z*z - 1.0))
        s2 = -w0*(z + np.sqrt(z*z - 1.0))
       return Vin*(1 - ((s2*np.exp(s1*t) - s1*np.exp(s2*t))/(s2 - s1)))
```

```
# --- plotting ranges ---
# choose time samples based on t_end
def choose_time_samples(t_end):
    return 1500 if t_end < 5e-3 else 3000 if t_end < 5e-2 else 5000 if t_end < 0.2 else 8000
# choose frequency sweep based on w0 and z
def choose_freq_sweep(w0, z):
    span = 100.0 if (z < 0.5) else 40.0 if (z < 1.0) else 20.0
    wmin = max(1e-3, w0/span); wmax = w0*span
    Nf = 1200 if span >= 40 else 800
    return np.logspace(np.log10(wmin), np.log10(wmax), Nf)
# --- formatting float number ---
def _fmt(x, precision=6):
    s = np.format_float_positional(float(x), precision=precision, trim='-')
    if s.startswith('-0') and round(float(x), precision) == 0.0:
        s = '0'
    return s
```

코드 설명 - DC 입력

```
# Display numeric formulas
def show_numeric_formulas(R, L, C, Vin, s1, s2):
   w0 = omega0(L, C)
   z = zeta(R, L, C)
   def tex(s):
       display(Math(s))
                                Zeta 값 기준으로 damping 구분
   # UNDERDAMPED: 7 < 1 \
   if z < 1.0:
       wd = abs(s1.imag)
                                               # damped natural freq
                                               # amplitude scale in step response
       A = 1.0/np.sqrt(1.0 - z*z)
       phi = np.arccos(z)
                                               # phase shift
       0 = 1.0/(2.0*z)
                                               # quality factor
       Mp = np.exp(-np.pi*z/np.sqrt(1.0 - z*z)) # overshoot fraction
       Ts = 4.0/(z*w0)
                                               # ~ settling time
       # 상태 + 핵심 파라미터
       tex(
           r"\textbf{UNDERDAMPED }(\zeta<1)"</pre>
           + r"\quad \zeta=" + _fmt(z)
           + r",\ \omega_0=" + _fmt(w0) + r"\ \text{rad/s}"
          + r",\ Q=" + _fmt(Q)
       # 시간 응답 Vc(t)
       tex(
           r"V_C(t)=" + _fmt(Vin)
          + r"\Big[1-"
           + _fmt(A)
           + r" e^{-("+ _fmt(z*w0) + r")t}"
           + r"\sin(" + _fmt(wd) + r"t+" + _fmt(phi) + r")\Big]"
       # 핵심 성능 지표
       tex(
           r"M p \approx "
           + f"{Mp*100:.2f}"
                                              Underdamping 상황에서
           + r"\% \quad,\quad "
                                              성능 지표 계산 후 출력
           + r"T s \approx "
           + _fmt(Ts)
           + r"\ \text{s}"
```

```
# CRITICALLY DAMPED: \zeta = 1 \rightarrow  중복 실근, 진동 없이 가장 빠르게 감쇠
elif abs(z - 1.0) < 0.02: # zeta가 1에 매우 근접한 경우
    tau = 1.0/w0 # dominant time constant
   tex(
        r"\textbf{CRITICALLY DAMPED }(\zeta=1)"
       + r"\quad \zeta=" + fmt(z)
       + r",\ \omega_0=" + _fmt(w0) + r"\ \text{rad/s}"
       + r",\ \tau=" + fmt(tau) + r"\ \text{s}"
   tex(
                                                           Critical damping
        r"V_C(t)=" + fmt(Vin)
                                                           상황에서 Vc 출력
       + r"\Big[1-(1+" + _fmt(w0)
       + r"t)e^{-(" + _fmt(w0) + r")t}\Big]"
   tex(r"\text{no overshoot, fastest return}")
# OVERDAMPED: \zeta > 1 \rightarrow \text{ 서로 다른 두 실근, 진동 없이 느리게 감쇠}
else:
    s1r, s2r = s1.real, s2.real
   tau slow = 1.0/abs(min(s1r, s2r, key=lambda x: abs(x)))
   tex(
        r"\textbf{0VERDAMPED }(\zeta>1)"
       + r"\quad \zeta=" + _fmt(z)
       + r",\ \omega_0=" + _fmt(w0) + r"\ \text{rad/s}"
       + r",\ \tau_{\text{slow}}\approx " + _fmt(tau_slow) + r"\ \text{s}"
   tex(
        r"V C(t)=" + fmt(Vin)
                                                            Overdamping
       + r"\left[1-\frac{(" + _fmt(s2r) + r")e^{("
                                                            상황에서 Vc 출력
       + _fmt(s1r) + r")t}-(" + _fmt(s1r)
       + r")e^{(" + _fmt(s2r)
       + r")t}{" + _fmt(s2r - s1r) + r"}\right]"
   tex(r"\text{no oscillation, slow tail}")
```

코드 설명 - DC 입력

```
# --- 인력 UI ---
# R (0hm)
R_slider = widgets.FloatSlider(
                                             R.L.C는 슬라이더로 입력받아
   description='R (\Omega)',
                                             그래프에 실시간 반영
   min=0.1, max=100.0, step=0.1,
   value=10.0,
   readout=True.
   continuous update=True, # 드래그 중에도 업데이트
   layout=widgets.Layout(width='250px')
# L (H) - 슬라이더
L slider = widgets.FloatLogSlider(
   description='L (H)',
   base=10.
   min=-6, # 1e-6 H
   max=-1, # 1e-1 H
   step=0.1,
   value=1e-3.
   readout=True.
   layout=widgets.Layout(width='250px')
# C (F) - 슬라이더
C_slider = widgets.FloatLogSlider(
   description='C (F)',
   base=10.
   min=-9, # 1e-9 F
   max=-4. # 1e-4 F
   step=0.1,
   value=1e-5.
   readout=True,
   layout=widgets.Layout(width='250px')
                                         VIN과 t end는 값으로 입력 받음
VIN_in = widgets.FloatText(value=1.0, description='Vin_step [V]', layout=widgets.Layout(width='170px'))
TEND_in = widgets.FloatText(value=5e-3, description='t_end [s]', layout=widgets.Layout(width='150px'))
       = widgets.Output()
```

```
def main(_=None):
    with out:
        clear output()
                                            Main 함수에서 앞서 정의한
       R = R slider.value
                                            함수 호출하고, 그래프 plot
       L = L slider.value
       C = C slider.value
       Vin, t_end = VIN_in.value, TEND_in.value
       if L<=0 or C<=0 or R<0 or t end<=0:
           print("Invalid parameters: require L>0, C>0, R>=0, t_end>0."); return
       # (1) numeric formulas (with substituted values)
       s1, s2 = compute poles(R, L, C)
       show numeric formulas(R, L, C, Vin, s1, s2)
       # (2) time response: numeric vs analytic
       n_time = choose_time_samples(t_end)
       t, Vc_num = simulate_step_Vc_only(R, L, C, Vin, t_end, n_time)
       Vc_ana = analytic_Vc(Vin, R, L, C, t)
       fig1, ax1 = plt.subplots(figsize=(6.6,3.2))
       ax1.plot(t, Vc_num, label='Numeric (solve_ivp)')
       ax1.plot(t, Vc_ana, '--', label='Analytic')
       ax1.set_title("Step response: Vc(t)")
       ax1.set_xlabel("t [s]"); ax1.set_ylabel("Vc [V]")
       ax1.grid(True, ls=':'); ax1.legend(); plt.tight_layout(); plt.show()
for w in [R slider, L slider, C slider,
         VIN in, TEND in]:
   w.observe(main, names='value')
display(widgets.VBox([
   widgets.HTML("<h4>DC Step - R,L,C,Vin_step,t_end (compact)</h4>"),
   widgets.HBox([R_slider, L_slider,C_slider,
                 VIN in, TEND in]),
    out
1))
```

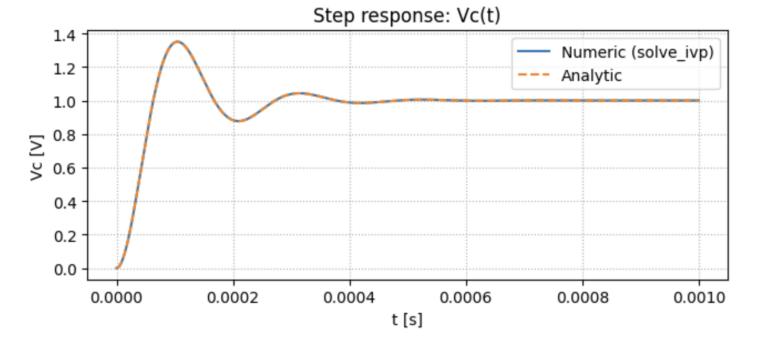
실행 결과 - DC 입력

DC Step — R,L,C,Vin_step,t_end (compact)

R (Ω) 20.00 L (H) 0.00100 C (F) 0.00000100 Vin_step [V] 1 t_end [s] 0.001 \diamondsuit UNDERDAMPED ($\zeta < 1$) $\zeta = 0.316228$, $\omega_0 = 31622.776602 \, \mathrm{rad/s}, \, Q = 1.581139$

 $V_C(t) = 1 \Big[1 - 1.054093 e^{-(10000)t} \sin(30000t + 1.249046) \Big]$

 $M_p pprox 35.09\% \quad , \quad T_s pprox 0.0004 ext{ s}$



실행 결과 - DC 입력

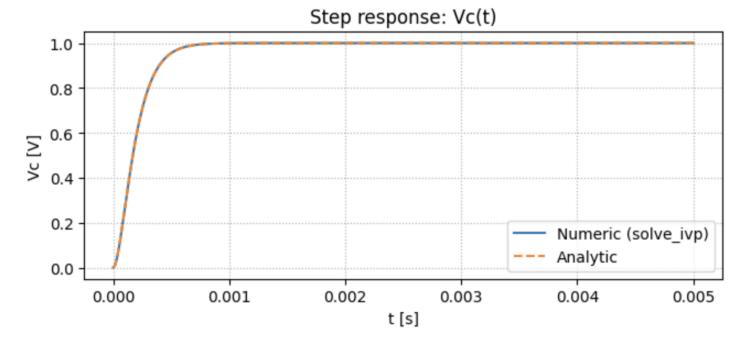
DC Step — R,L,C,Vin_step,t_end (compact)

R (Ω) 20.30 L (H) 0.00100 C (F) 0.0000100 Vin_step [V] 1 t_end [s] 0.005

CRITICALLY DAMPED ($\zeta = 1$) $\zeta = 1.015, \ \omega_0 = 10000 \ \mathrm{rad/s}, \ \tau = 0.0001 \ \mathrm{s}$

$$V_C(t) = 1 \Big[1 - (1 + 10000t) e^{-(10000)t} \Big]^{rac{1}{2}}$$

no overshoot, fastest return



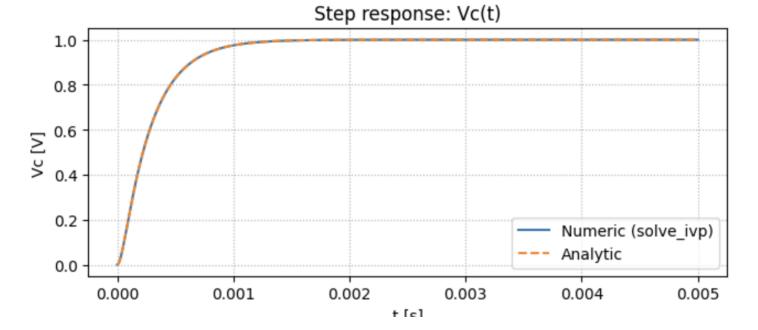
실행 결과 - DC 입력

DC Step — R,L,C,Vin_step,t_end (compact)

R (Ω) 29.80 L (H) 0.00100 C (F) 0.0000100 Vin_step [V] 1 t_end [s] 0.005

$$egin{aligned} \mathbf{OVERDAMPED} \ (\zeta > 1) \quad \zeta = 1.49, \ \omega_0 = 10000 \ \mathrm{rad/s}, \ au_\mathrm{slow} pprox 0.000259 \ \mathrm{s} \ V_C(t) = 1 \left[1 - rac{(-25945.813687)e^{(-3854.186313)t} - (-3854.186313)e^{(-25945.813687)t}}{-22091.627373}
ight] \end{aligned}$$

no oscillation, slow tail



코드 설명 - AC 입력

```
def show_ac_summary(R, L, C, Vac, w_drive):
   # 시스템 파라미터
   w0 = omega0(L, C)
   z = zeta(R, L, C)
   # 전달함수 H(j\omega) = Vc/Vin
   H_{drive} = H_{jw}(R, L, C, w_{drive})
   mag
           = np.abs(H drive)
                                     # |H|
   phi = np.angle(H_drive) # [rad]
   def tex(s):
       display(Math(s))
   # 요약 텍스트
   tex(
       r"V_C^{\text{(steady)}}(t) \approx "
       + _fmt(mag * Vac)
       + r"\,\sin\!\big("
                                         AC 입력시 파라미터,
       + fmt(w drive)
                                         전달함수 정의 후 출력
       + r"t + "
       + fmt(phi)
       + r"\big)"
    tex(
       r''|H| = " + _fmt(mag)
       + r",\quad"
       r"\angle H = " + fmt(phi)
       + r"\ \mathrm{rad}"
       + r"\ (" + _fmt(phi * 180/np.pi) + r"^\circ)"
```

```
def simulate_ac_Vc(R, L, C, Vac, w_drive, t_end, n=3000):
     dq/dt = i
     di/dt = (Vin(t) - R i - q/C)/L
     Vin(t) = Vac * sin(w_drive * t)
   def f(t, x):
       q, i = x
       Vin_t = Vac * np.sin(w_drive * t)
       dqdt = i
       didt = (Vin_t - R*i - q/C)/L
       return [dqdt, didt]
   # 시간축
   t = np.linspace(0, t_end, n)
   q0 = 0.0 \# => Vc(0)=0
   i0 = 0.0
   sol = solve_ivp(
       f,
       [0, t end],
                                  ODE solver 이용해
       [q0, i0],
                                  Vc 파형 얻음
       t_eval=t,
       max_step=t_end/max(n, 1)
   if not sol.success:
       return t, np.full_like(t, np.nan), np.full_like(t, np.nan)
   q = sol.y[0]
   Vc = q / C
   Vin_t = Vac * np.sin(w_drive * t)
   return t, Vc, Vin_t
```

코드 설명 - AC 입력

(위젯 관련 코드 생략)

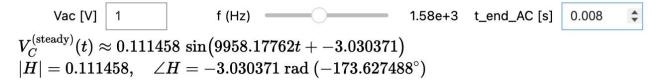
```
# --- (3) AC 전용 main 함수 ---
                           Main 함수에서 정의한 함수
def main ac( =None):
   with out_ac:
                           불러오고 graph plot
       clear_output()
       # --- RLC / AC 파라미터 읽기 ---
       R = R slider.value
      L = L slider.value
       C = C slider.value
       Vac = VAC_in.value
                                 # [V] 사인파 진폭
      f_drive = FREQ_slider.value # [Hz] 구동 주파수
       w_drive = 2.0 * np.pi * f_drive # [rad/s]
       t_end_ac = TAC_in.value # [s] 시뮬레이션 길이
       # --- 유효성 검사 ---
       if L \le 0 or C \le 0 or R < 0:
          print("Invalid RLC: need L>0, C>0, R>=0.")
           return
       if t end ac <= 0 or f drive < 0:
          print("Invalid AC params: need t end>0 and f>=0.")
           return
       # --- 적당한 샘플 수 정하기
       n time ac = choose time samples(t end ac)
       # --- 정상상태(해석적) 표현을 먼저 보여주기
       show_ac_summary(R, L, C, Vac, w_drive)
       # --- 실제(수치) 시뮬레이션: 과도 + 정상상태 포함
       t_ac, Vc_ac, Vin_ac = simulate_ac_Vc(
          R, L, C,
          Vac,
           w drive,
          t_end_ac,
           n_time_ac
```

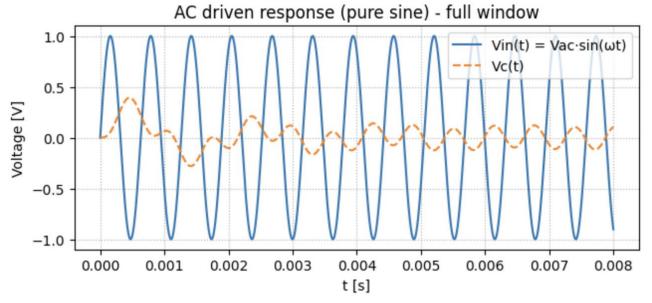
```
# (1) 전체 시간 파형: Vin vs Vc
fig full, ax full = plt.subplots(figsize=(6.6, 3.2))
ax_full.plot(t_ac, Vin_ac, label='Vin(t) = Vac·sin(ωt)')
ax_full.plot(t_ac, Vc_ac, '--', label='Vc(t)')
ax full.set title("AC driven response (pure sine) - full window")
ax_full.set_xlabel("t [s]")
ax full.set ylabel("Voltage [V]")
                                                                   파형 graph plot
ax_full.grid(True, ls=':')
ax_full.legend()
plt.tight layout()
plt.show()
# (2) 주파수 응답 크기 (Bode magnitude)
w0 = omega0(L, C)
z = zeta(R, L, C)
ws = choose_freq_sweep(w0, z)
                                  # log-spaced ω range
Hs = H_jw(R, L, C, ws)
mag_db = 20*np.log10(np.abs(Hs) + 1e-30)
fig_mag, ax_mag = plt.subplots(figsize=(6.4, 3.2))
ax_mag.semilogx(ws, mag_db)
ax mag.axvline(w0, alpha=0.35, ls='--', label='ω0')
ax_mag.set_title("Frequency response: |Vc/Vin| [dB]")
                                                              주파수 응답 (크기, 위상) plot
ax mag.set xlabel("ω [rad/s]")
ax mag.set_ylabel("20 log10 |H(j\omega)| [dB]")
                                                # (3) 주파수 응답 위상 (Phase)
ax_mag.grid(True, which='both', ls=':')
ax_mag.legend()
                                                phi = np.unwrap(np.angle(Hs))
                                                                                    # [rad]
                                                fig_phase, ax_phase = plt.subplots(figsize=(6.4, 3.2))
plt.tight_layout()
                                                ax_phase.semilogx(ws, np.degrees(phi))
plt.show()
                                                ax phase.axvline(w0, alpha=0.35, ls='--', label='\omega0 (\sim -90°)')
                                                ax_phase.set_title("Phase response: ∠H(jω)")
                                                ax_phase.set_xlabel("ω [rad/s]")
                                                ax phase.set ylabel("phase [deq]")
                                                ax_phase.grid(True, which='both', ls=':')
                                                ax_phase.legend()
                                                plt.tight_layout()
                                                plt.show()
```

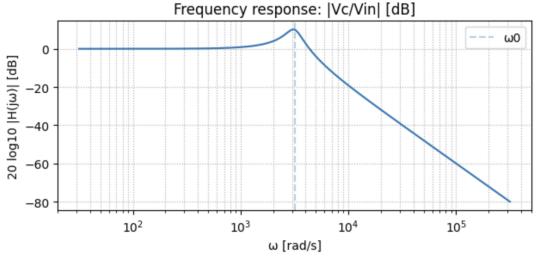
실행 결과 - AC 입력

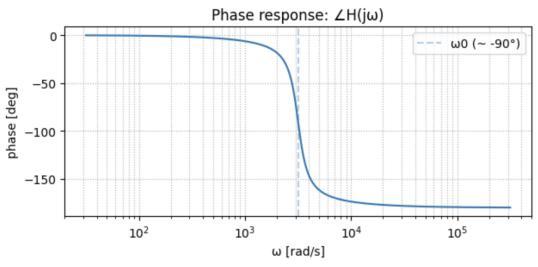
R=10 Ω , L=10mH, C=10uF, ω_0 =3162.27766 rad/s, Q=3.162278

AC drive settings





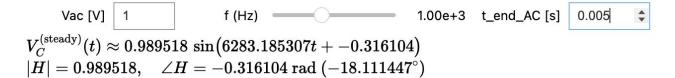




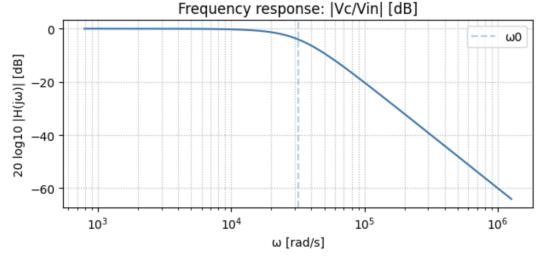
실행 결과 - AC 입력

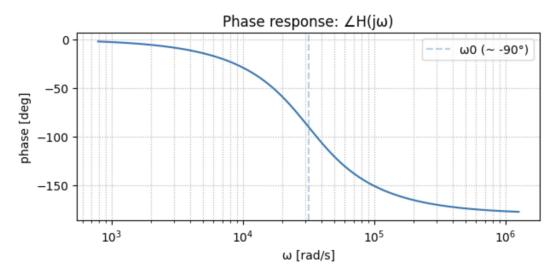
R=50 Ω , L=1mH, C=0.1uF, ω_0 =31622.776602 rad/s, Q=0.632456

AC drive settings



AC driven response (pure sine) - full window 1.0 0.5 Vin(t) = Vac·sin(ωt) -0.5 -1.0 0.000 0.001 0.002 0.003 0.004 0.005





결론

- 직렬 RLC 회로의 소자 값과 입력 전압을 입력했을 때 간단하게 Vc 값을 파악하고 Oscillation 종류를 구분할 수 있음

- 파형 그래프와 주파수 응답 그래프를 확인하고, Q 값에 따른 주파수 응답 변화를 쉽게 관찰할 수 있음

- 활용: oscillation 종류와 성능 지표를 입력하면 그에 맟는 회로를 구성하는 코드를 설계해 공학적인 도구로서 발전

참고문헌

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- Irwin & Nelms, *Basic Engineering Circuit Analysis*, 12th ed., Wiley, 2021, pp. 532-558.
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