

## STATS

### LESSON 1 (RANDOM VARIABLE)

**Random Variable** - a variable (typically represented as  $x$ ) that has a single numerical value, determined by chance, for each outcome of a procedure.

#### TYPES OF RANDOM VARIABLE

1. Discrete Random Variable
  - It is a collection of values that is finite or countable.
2. Continuous Random Variable
  - It has infinitely many values, and the collection of values is not countable.

#### EXAMPLE #1 TWO COINS ARE TOSSED

Step 1: Sample Outcome

COIN 1    COIN 2

H          H          HH = 2

            T          HT = 1

T          H          TH = 1

            T          TT = 0

Step 2: Sample Space (total outcome)

$$2 \cdot 2 = 4$$

Step 3: P. D. T (Probability Distribution Table)

Z	0	1	2
P(z)	$\frac{1}{4}$	$\frac{1}{2}$	$\frac{1}{4}$

- let z be the random variable representing the number of heads that occurs. Find the value of the random variable Z with its corresponding probabilities.

**EXAMPLE #2 TWO FAIR DICE ARE THROWN SIMULTANEOUSLY**

Step 1: Sample Outcome

2	3	4	5	6	7
3	4	5	6	7	8
4	5	6	7	8	9
5	6	7	8	9	10
6	7	8	9	10	11
7	8	9	10	11	12

Step 2: Sample Space

$$6 \bullet 6 = 36$$

Step 3: PDT

X	P(x)
2	1/36
3	1/18
4	1/12
5	1/9
6	5/36
7	1/6
8	5/36
9	1/9
10	1/12
11	1/18
12	1/36

<b>X</b>	<b>0</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>
<b>P(x)</b>	<b>. 11</b>	<b>. 19</b>	<b>. 28</b>	<b>. 15</b>	<b>. 12</b>	<b>. 004</b>	<b>. 006</b>

1.  $P(3) = 0.15$
2.  $P(x > 2) = 0.39$
3.  $P(x < 4) = 0.73$
4.  $P(1 < x < 4) = 0.43$

if x is a random variable with x elements, then

- a. They probability of each value is between 0 and 1  
 $0 < P(x) < 1$
- b. They sum of all probabilities is 1

## WEEK #2

Expected Value, Theoretical Mean, Mean of D. R. V ~ ARE ALL SAME

$$M = E(x) =$$

Step 1:

Step 4:

Step 5:

x	P(x)	$x \cdot P(x)$	$x'^2$	$x'^2 \cdot P(x)$
0	$\frac{1}{4}$	0	0	0
1	$\frac{1}{2}$	$\frac{1}{2}$	1	$\frac{1}{2}$
2	$\frac{1}{4}$	$\frac{1}{2}$	4	1

Step 2:  $M = 1$

Step 6:  $= 1 \frac{1}{2} = \frac{3}{2}$

Step 3:  $M'^2 = 1$

Step 7:  $\text{Var}(x) = 0'^2 = S_6 - S_3$

$$3/2 - 1 = 1/2$$

$$\text{Step 8: std}(x) = \sqrt{\text{Var}(x)} = \sqrt{S^2}$$

$$= \sqrt{1/2} = \sqrt{1/\sqrt{2}} = 1/\sqrt{2} \circ \sqrt{2}/\sqrt{2}$$

$$= \sqrt{2}/2$$

### **LESSON 3: NORMAL DISTRIBUTION**

Formula:  $z = (x - m) / (\sigma)$

$z =$  standard deviation

$x =$  raw score/normal score

$M =$  population mean

$\sigma =$  population standard

### **EXAMPLE 1**

Step 1: Given & Unknown

$z = ?$

$x = 88$

$M = 81$

$\sigma = 6$

Step 2: Find z score

$$z = (88 - 81) / 6$$

$$z = 1.17$$

Step 3: Find the probability

$$\text{Probability} = P(z > 1.17) = 0.1210$$

#### ***LESSON 4: Mean & Variance***

$M_x$  = mean of sample means

$M$  = population mean

$\sigma^2_x$  = variance of the sample means

$\sigma^2$  = population variance

$n$  = sample size

$\sigma_x$  = sample standard deviation of the sample means

$\sigma$  = population standard

$N-n/N-1$  = Finite Population Correction Factor (PPCF)

#### ***LESSON 5: Sampling Distribution of Large Sample size***

Formula:  $z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}}$

$\bar{x}$  : sample mean

$\mu$  : population mean

$\sigma$  : population standard deviation

$n$  : sample size

#### **EXAMPLE 1**

### Step #1: Given & Unknown

$$z = \bar{x} - \mu / \sigma / \sqrt{n}$$

$$\bar{x} : 7$$

$$\mu : 6$$

$$\sigma : 3.2$$

$$n : 5$$

$$P(\bar{x} < 7) = ?$$

### Step #2: Find z

$$z = 7 - 6 / 3.2 / \sqrt{5}$$

$$= 2.32$$

### Step #3: Find $P(\bar{x} < 7)$

$$P(z < 2.32) = 0.9898$$

## ***LESSON 6: Margin of error and Length of Confidence interval***

$$\bar{x} - t_{\alpha/2} (s / \sqrt{n}) < \mu < \bar{x} + t_{\alpha/2} (s / \sqrt{n})$$

$\bar{x}$ : sample mean

$t_{\alpha/2}$ : t-value for two tailed

s: sample standard deviation

n: sample size

**Confidence level** (CL) of an interval estimate of a parameter is the probability that the interval estimate will contain the parameter, assuming that a large number of samples are selected and that the estimation process on the same parameter is repeated (Bluman, 2014)

**The margin of error**, also called the maximum error of the estimate, is the maximum likely difference between the point estimate of a parameter and the actual value of the parameter.

## REFERENCE

<https://www.scribd.com/presentation/395633175/C1-Lesson-1-Exploring-Random-Variables>

<https://study.com/skill/learn/how-to-calculate-the-variance-of-a-discrete-random-variable-explanation.html>