

**Determine two coterminal angles (one positive and one negative) for each given angle:**  $\theta = -\frac{\pi}{3}$  radians

To find positive coterminal angles add  $360^\circ$  or  $2\pi$  to the given angle.

To find negative coterminal angles subtract  $360^\circ$  or  $2\pi$  to the given angle.

Positive coterminal angle:  $\theta = -\frac{\pi}{3} + 2\pi = \frac{5\pi}{3}$

Negative coterminal angle:  $\theta = -\frac{\pi}{3} - 2\pi = -\frac{7\pi}{3}$

**Converting between radians and degree for  $50^\circ$  and  $2\pi$ .**

To convert between radians and degree you need to know if the given value is either a degree or a radian. If there is a  $^\circ$  then it is a degree else, it's radian.

Then for degree to radians you will multiply the given degree with  $\frac{\pi}{180}$ .

Then for radians to degree you will multiply the given degree with  $\frac{180}{\pi}$ .

Given:  $50^\circ$

1.  $50^\circ \times \frac{\pi}{180} =$

2.  $= \frac{50\pi}{180}$

3.  $= \frac{5\pi}{18}$

Given:  $2\pi$

$$1. 2\pi * \frac{180}{\pi} =$$

$$2. \frac{2\pi}{1} * \frac{180}{\pi} = \frac{360\pi}{\pi}$$

$$3. = 360^\circ$$

### Complementary Angles

When 2 positive angles add up to either  $90^\circ$  or  $180^\circ$ .

Given angle,  $\theta = 45^\circ$ :

$$1. \theta_c = 90^\circ - 45^\circ = 45^\circ$$

$$2. \theta_s = 180^\circ - 45^\circ = 135^\circ$$

### Degree, Minutes, Second Form

A way to denote fraction parts, ex.  $25^\circ 12' 12''$ .

Given **DMS**:  $12^\circ 23' 12''$

**DMS to Radians**

$$1. 12 + \frac{23}{60} + \frac{12}{3600} = 12.38666$$

Given **Radian**:  $12.625$  Radians

**Radians to DMS**

$$1. 12.625 \text{ Radians [Multiple } .625 \text{ by } 60]$$

$$2. 0.625 \cdot 60 = 37.5$$

$$3. 12^\circ 37.5' \text{ [Multiple } .5 \text{ by } 60]$$

$$4. 0.5 \cdot 60 = 30$$

$$5. = 12^\circ 37' 30''$$

### Finding Arc Length

A circle has a radius of  $27$  inches. Find the length of the arc intercepted by a central angle of  $160^\circ$ .

$$r = 27 \text{ in}$$

Now convert degree to radians, as  $\theta$  **HAS** to be a RADIAN.

$$1. 160^\circ \times \frac{\pi}{180} = \frac{160\pi}{180}$$

$$2. = \frac{8\pi}{9}$$

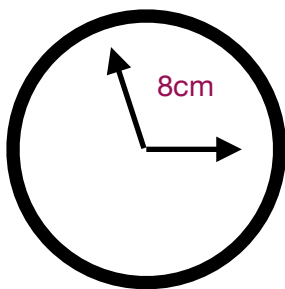
$$3. 27\left(\frac{8\pi}{9}\right) = 75.3982\dots$$

$$4. = 75.398 \text{ inch}$$

### Linear and Angular Speed.

$$LS = \frac{r\theta}{t} \text{ \& } AS = \frac{s}{rt}$$

The second hand of a clock is **8-cm** long. Find the linear speed of the tip of this second hand as it passes around the clock face.



It's a circle so we can imply  $r = 2\pi$ .

The arm is the minute-arm so  $t = 60$ .

$$LS = \frac{8(2\pi)}{60} = 0.8377\dots$$

$$LS = 0.838 \text{ cm/min.}$$

The circular blade on a saw rotates at **2,400 revolutions per minute** (2,400 rpm).

Given  $\theta = 2,400$ , Given  $t = 1$ , implied  $r = 2\pi$

$$1. 2400(2\pi) = 4800\pi$$

$$2. \frac{4800\pi}{1} = 15079.6447... \text{ rads/min}$$

If  $r = 4$  we can solve for LS.

$$1. \frac{4(4800\pi)}{1} = 19200\pi = 60318.579 \text{ in/mins.}$$